

Set-5

3. For $A[i][j]$

B = Base address ($A[0][0]$)

S = size of element

(i) Must skip i rows each containing C element

no. of elements = $i \times C$

(ii) At start of row i , we must be j more elements

no. of elements = $(i \times C) + j$

(iii) Address($A[i][j]$) = $B + [(i \times C) + j] \times S$

4. Linear search - It checks every element in collection, one by one, until target is found or collection ends. It works on both sorted or unsorted array with time complexity is slow i.e. $O(n)$

Binary search - It uses divide & conquer algorithm but it requires data to be sorted

Example

(i) Set two pointers, low & high

(ii) Find middle $mid = (high + low) / 2$
 ~~$mid = low + hi$~~

(iii) If target = middle, return middle

(iv) If target > mid,
set $low = mid + 1$

- (v) If $\text{target} < \text{mid}$,
 set $\text{high} = \text{mid} - 1$
- (vi) Repeat process
- Time complexity = $O(\log n)$

5.

- (i) Select pivot element
- (ii) Array is rearranged so that all elements smaller than pivot are arranged to its left while others at its right
- (iii) Algorithm then recursively applies same process to two sub-arrays.

Real life example - when sorting large list of exam ~~ex~~ scores for national test. If organisation needs to find 90th percentile cutoff (top 10%) quick sort is ideal

6. Algorithm

Function $\text{fib}(n)$

If $n \leq 0$ return 0

If $n == 1$ return 1

$a = 0$

$b = 0$

For $i = 2$ to n

$\text{current} = a + b$

$a = b$

$b = \text{current}$

END For

return b

8. ^{reference to}
a) Comparison with stack usage

(i) Recursion - It uses call stack implicitly. Each time function calls ~~itself~~ itself, new stack frame is pushed onto stack to store local variable. It consumes memory of $O(n)$. If recursion is too deep, it can cause stack overflow error.

(ii) Iterative - It typically uses constant amount of stack space $O(1)$ for its single stack frame. State is managed through local variable within that frame.

b) Recursive program for factorial

If $n = 0$ or $n = 1$ then
return 1

ELSE
Return $n \times \text{factorial}(n)$

END If

END function

9.

MergeSort Function (Divide & conquer)

(i) Divide : if array has more than one element, find middle & split into two halves

(ii) Conquer : recursively call MergeSort on left half

(iii) Conquer : recursively call MergeSort on right half

(iv) Combine : call Merge function to combine two sorted sub-arrays to one sorted array

Merge function (Combine)

- (i) Create two temporary arrays for each sorted half (L & R)
- (ii) Use ~~two~~ two pointers (i for L & j for R) & main pointer of original array
- (iii) Compare $L[i]$ & $R[j]$. Copy smaller element to $A[k]$
- (iv) Increment pointer ~~to~~ (i or j) from copied one & also increment k
- (v) Repeat until one temporary array is empty
- (vi) Copy ~~new~~ remaining element from other temporary array back into A

Significance in Large Dataset Sorting -

- (i) Guaranteed performance - It always runs in $O(n \log n)$ time even in worst case.
- (ii) External sorting - If dataset is too large to fit in RAM. It sorts "chunks" of file in RAM, saves them to disk then merges sorted files on disk
- (iii) Stability - It is stable sort. If two items have same value, they will stay in their original relative order.