

Set - 4

2. Row-major order - This method stores array row by row. The entire first row is stored in memory, followed by next row & so on.

Column-major order - This method stores array column by column. The entire first column is stored in memory, followed by entire next column & so on.

Example For 2×3 array $A = [1, 2, 3], [4, 5, 6]$

Row major layout $[1, 2, 3, 4, 5, 6]$

Column major layout $[1, 4, 2, 5, 3, 6]$

3. For 2-D array

B = Base address

S = size of element

(i) Get to correct row = $(i \times N)$

(ii) Get to correct element = j

$$\text{Address } A[i][j] = B + (i \times N + j) \times S$$

For 3-D array

(i) Get to correct depth = $k \times D_1 \times D_2$

(ii) Get to correct column with depth = $j \times D_1$

(iii) Get to correct row = i

$$\text{Address } A[i][j][k] = B + [(k \times D_1 \times D_2) + (j \times D_1) + i] \times S$$

| 4. Complexity | Insertion sort | Selection sort |
|---------------|----------------|----------------|
| Best case | $O(n)$ | $O(n^2)$ |
| Average case | $O(n^2)$ | $O(n^2)$ |
| worst case | $O(n^2)$ | $O(n^2)$ |

5. Divide

(i) Divide unsorted array into two halves.
 Recursively calls itself until single sorted element is left in sub-array

(ii) Merge first compares two sub-arrays, then it ~~comp~~ copies the ~~o~~ smaller element into temporary array first & then the larger number.

$[8, 3, 5, 1]$

$[8, 3]$ & $[5, 1]$

$[8]$ & $[3]$ & $[5]$ & $[1]$

compare 8 & 3
 copy 3 then copy 8
 $[3, 8]$

compare 5 & 1
 • copy 1 into temporary array then copy 5
 $[1, 5]$

Merge $[3, 8]$ & $[1, 5]$

compare 3 & 1, copy 1 (Temp $\rightarrow [1]$)
 compare 3 & 5, copy 3 (Temp $\rightarrow [1, 3]$)
 compare 8 & 5, copy 5 (Temp $\rightarrow [1, 3, 5]$)
 copy remaining 8 (Temp $\rightarrow [1, 3, 5, 8]$)

6. Removal of recursion is process of converting a recursive function into iterative on to -

(i) Avoid stack overflow

(ii) Improve performance

Iterative algorithm for factorial

```
int fact(int n){
```

```
    int result = 1;
```

```
    for (int i = n; i > 0; i--){
```

```
        result = result * i; }
```

```
    return result; }
```

8a) Base case - If 1 disk ($n=1$), move directly from source to destination

Recursive case (for n disks)

(i) Move $n-1$ disks from source to temp (using desti as helper)

(ii) Move n^{th} disk from source to desti

(iii) Move $n-1$ disk from temp to desti (using source as helper)

TOH(n , source, desti, temp)

If $n == 1$ then

Move disk 1 from source to desti

Else

// 1. Move $n-1$ from source to temp

TOH($n-1$, source, temp, desti)

// 2. Move largest from source to desti

~~Move~~ Move disk n from source to desti

// 3. Move $n-1$ from temp to dest
TOH($n-1$, temp, dest, source)
END IF

b) Advantages

- (i) Code elegance - provide clean, simple & more readable solution
- (ii) Problem decomposition - Break complex problem to smaller, ~~idea~~ identical sub-problems.

Disadvantages

- (i) Memory usage - It can cause stack overflow error
- (ii) Performance overhead - Function calls are more time taking.

9. Sparse matrix - Matrix which have mostly 0 zeroes as its elements.

2-D array representation

2-D array of size $(k+1) \times 3$

where k = no. of non-zero element

- (i) First row [0] is header, storing original dimension & count [Total rows, total columns, Total non-zeroes]
- (ii) Subsequent k rows ~~each~~ each store a 'triplet' for non-zero element [row, column, value]

Advantages -

- (i) Space efficiency - For 1000×1000 matrix with only 100 non-zero element, the savings are 1,000,000 elements v/s ~~101~~ $101 \times 3 = 303$ elements

Disadvantages -

- (i) Slower access - will take time complexity $O(k)$ instead of $O(1)$
- (ii) Implementation complexity - Algorithms for matrices (add or multiply) becomes much complex as they must iterate through triplet instead using nested loops.