AE 10: Probability

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Learning goals

- Introduce probabilities and how we can use them to understand categorical data
- Create a contingency table using pivot_wider() and kable()
- Use a contingency table to explore the relationship between two categorical variables.

Introduction

```
library(tidyverse)
library(knitr)
```

```
sta199 <- read_csv("sta199-fa21-year-major.csv")</pre>
```

For this Application Exercise, we will look at the year in school and majors for students taking STA 199 in Fall 2021. The data set includes the following variables:

- section: STA 199 section
- year: Year in school
- major_category: Major / academic interest.
 - For the purposes of this AE, we'll call this the student's "major".

Definitions

- The **probability** of an event tells us how likely an event is to occur, and it can take values from 0 to 1, inclusive. It can be viewed as
 - the proportion of times the event would occur if it could be observed an infinite number of times.
 - our degree of belief an event will happen.
- An **event** is the basic element to which probability is applied, e.g. the result of an observation or experiment.
 - Example: **A** is the event a student in STA 199 is a sophomore.
- A sample space is the set of all possible outcomes. Each outcome in the sample space is disjoint or mutually exclusive meaning they can't occur simultaneously.
 - Example: The sample space for year is {First-year, Sophomore, Junior, Senior}

Exercise 1

Let's take a look at the majors. Note that we have categorized majors so that each student can only be in one major category.

• What is the sample space for major? You can use code to identify the sample space.

```
sta199 %>%
  distinct(major_category) %>%
  kable
```

major_category
other
pubpol only
stats only
compsci only
undecided
stat + other major
econ only

• Let's make a table that includes the majors, the number of students in each, and the associated probabilities.

```
sta199 %>%
  count(major_category) %>%
  mutate(prop = n/sum(n)) %>%
  kable
```

major_category	n	prop
compsci only	40	0.1619433
econ only	15	0.0607287
other	98	0.3967611
pubpol only	38	0.1538462
stat + other major	36	0.1457490
stats only	10	0.0404858
undecided	10	0.0404858

• What is the probability a randomly selected STA 199 student is a "pubpol only" major?

```
sta199 %>%
  count(major_category) %>%
  mutate(prop = n/sum(n)) %>%
  filter(major_category == "pubpol only")
```

• What is the probability a randomly selected STA 199 student is studying statistics?

• What is the probability a randomly selected STA 199 student is not a "pubpol only" major?

Exercise 2

Now let's make at table looking at the relationship between year and major.

```
sta199 %>%
count(year, major_category)
```

```
## # A tibble: 23 x 3
##
     year
               major_category
                                        n
      <chr>
##
                <chr>
                                    <int>
##
   1 First-year compsci only
                                        8
## 2 First-year econ only
                                        6
## 3 First-year other
                                       39
## 4 First-year pubpol only
                                       22
## 5 First-year stat + other major
                                       26
  6 First-year stats only
                                        7
  7 First-year undecided
                                        5
##
                                        7
## 8 Junior
                compsci only
## 9 Junior
                                        3
                 econ only
## 10 Junior
                 other
                                       12
## # ... with 13 more rows
```

We'll reformat the data into a **contingency table**, a table frequently used to study the association between two categorical variables. In this contingency table, each row will represent a year, each column will represent a major, and each cell is the number of students have a particular combination of year and major.

To make the contingency table, we will use a new function in dplry called pivot_wider(). It will take the data frame produced by count() that is current in a "long" format and reshape it to be in a "wide" format.

We will also use the kable() function in the knitr package to neatly format our new table.

year	compsci only	econ only	other	pubpol only	$ stat + other \\ major $	stats only	undecided
First-year	8	6	39	22	26	7	5
Junior	7	3	12	4	1	0	0
Senior	2	0	5	1	1	0	0
Sophomore	23	6	42	11	8	3	5

- How many students in STA 199 are first-years and in the "econ only" majors category. Answer: 6
- How many students in STA 199 are in the "other" major category? Answer: 98

Exercise 3

For each of the following exercises:

- (1) Calculate the probability using the contingency table above.
- (2) Then write code to check your answer using the sta199 data frame and dplyr functions.
 - What is the probability a randomly selected STA 199 student is a sophomore?

```
## # A tibble: 1 x :
## mean
## <dbl>
## 1 0.397
```

• What is the probability that a randomly selected STA 199 student is a "compsci only" major?

```
## # A tibble: 1 x 1
## mean
## <dbl>
## 1 0.162
```

• What is the probability that a randomly selected STA 199 student is a sophomore **or** a "compsci only" major?

• What is the probability that a randomly selected STA 199 student is a sophomore **and** a "compsci only" major

Resources

- Notes on pivot_wider and pivot_longer
 - Click here for slides
 - Click here for video