

## Instructions.

- This is a written assignment.
- Your answers should be precise and clearly written in  $\text{\LaTeX}$ .

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## WECCAK (WEAK-KECCAK)

Consider a variant of KECCAK hash function which we will be called as WECCAK (WEAK-KECCAK). The following is the description of WECCAK.

1. Input to the hash function is a message  $M \in \{0, 1\}^*$ .
2.  $M$  is padded with minimum number of zeros such that bit-length of padded message is a multiple of 184.
3. The padded message is divided into blocks of 184 bits. Let's call them  $M_1, M_2, \dots, M_r$ .
4. A state in WECCAK hash function is a  $5 \times 5 \times 8$  3-dimensional array.
5. Initial state  $S$  contains all zeros.
6. The first message block  $M_1$  is appended with 16 zeros to form  $M'_1$  and is XORed with  $S$ . (This procedure is similar to KECCAK).
7. This state is given as input to a function  $F$  (which will be defined later) and let's call its output as  $O_1$ . The output of  $F$  is also a  $5 \times 5 \times 8$  3-dimensional array.
8. The second message block  $M_2$  is appended with 16 zeros to form  $M'_2$  and is XORed with  $O_1$  and is given as input to  $F$ .
9. This is continued for  $r$  times.
10. The output of WECCAK is the initial 80 bits of  $O_r$ . (This is similar to KECCAK).
11. For more details on KECCAK, refer <https://nvlpubs.nist.gov/nistpubs/FIPS/NIST.FIPS.202.pdf>

Let  $R = \chi \circ \rho \circ \pi \circ \theta$  ( $\theta, \rho, \pi, \chi$  are the same as defined in KECCAK). Please note that now in all operations  $z$  indices are modulo 8.

1. Compute the inverse of  $\chi$  and  $\theta$ .
2. Claim about the security of WECCAK with  $F = R \circ R$ . (Give a preimage, collision and second preimage attack).