

DAA
Tutorial - 5

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Ans 1

BFS

DFS

- i) Uses queue data structure. Uses stack data structure.
- ii) Stands for breath first. Stands for depth first search.
- iii) Can be used to find single we might traverse through source shortest path in more edges to reach a destination vertex from a source vertex with min. no. of edges from a source vertex.
- iv) Siblings are visited before children are visited before the children.

Applications:

- 1. Shortest path & minimum spanning tree for unweighted graph.
- 2. Peer-to-peer networks. Path finding.
- 3. Social Networking websites. Topological sorting.
- 4. GPS Navigation system. Solving puzzles with only one solution.

Applications:

Ans 2 In BFS we use queue data structure. Queue is used when things don't have to be processed immediately, but have to be processed in FIFO order like

BFS

In DFS stack is used as DFS uses backtracking. For DFS, we retrieve it from root to the farthest node as much as possible, this is the same idea as LIFO (used by stacks).

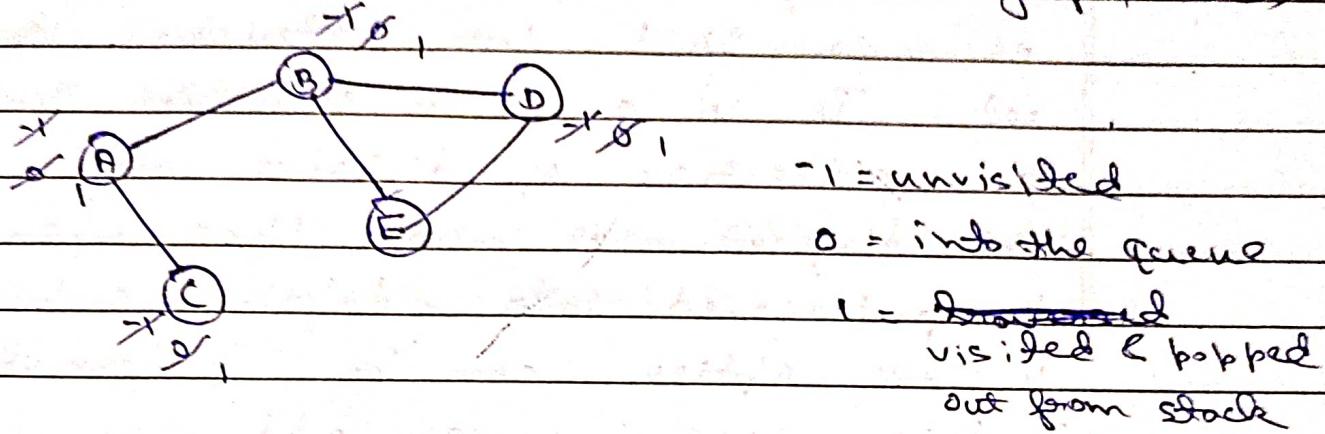
Ans 3 Dense graph is a graph in which the no. of edges is close to the maximal no. of edges.

Sparse graph is a graph in which the no. of edges is close to the minimal no. of edges. It can be disconnected.

Adjacency lists are preferred for sparse graph & adjacency matrix for dense graph.

Ans)

Cycle detection in undirected graph (BFS)



Stack :	E	visited set :	A B C D E
	D		=> B → D → E → B
	B	vertex	A
	A		Present -
			B
			C
			D
			E

Here E finds B (adjacent vertex of E)
with 0.

=> it contains a cycle.

Ans The disjoint set data structure is also known as union-find data structure & merge-set. It is a data structure that contains a collection of disjoint sets.

The disjoint set means that when the set is partitioned into disjoint subsets, various operation can be performed on it. In this case, we can add new sets, we can merge the sets, & we can also find the representation member of a set. It also allows to find out whether the two elements are in the same set or not efficiently.

Operation on disjoint set.

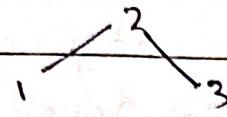
Union

- If S_1 & S_2 are two disjoint sets, the union $S_1 \cup S_2$ is a set of all elements x such that x is in either S_1 or S_2 .
- As the sets should be disjoint $S_1 \cup S_2$ replaces S_1 & S_2 which no longer exists.
- Union is achieved by simply making one of the trees as a subtree of other i.e. set parent field of one of the roots of the trees to other root.

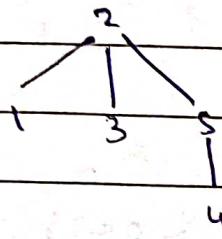
eg

S_1

S_2



$S_1 \cup S_2$



Merge the sets containing X & containing Y into one.

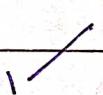
Find

Given an element X, to find the set containing it.

eg

S_1

S_2



$\text{find}(3) \Rightarrow S_1$

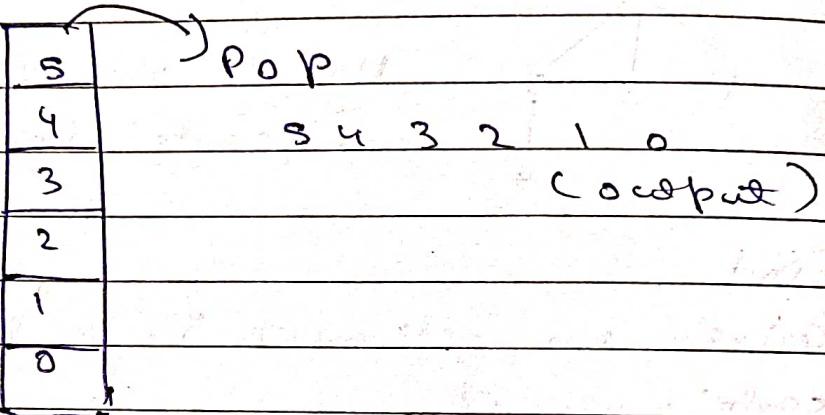
$\text{find}(5) \Rightarrow S_2$

return in which set

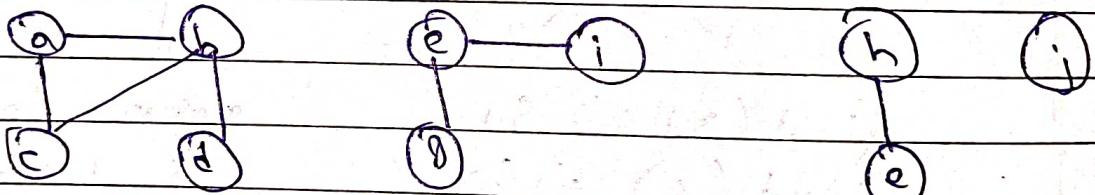
X belongs

Make-Set (X): Create a set containing X

Ans 6 Go to node 5, all its adjacent nodes are already visited so push node 5 in the stack & mark it visited.



Ans 7



$$N = \{a, b, c, d, e, g, h, i, j, l\}$$

$$E = \{(a,b), (a,c), (b,c), (b,d), (e,i), (e,g), (h,l), (j)\}$$

- $\{a\}$ $\{b\}$ $\{c\}$ $\{d\}$ $\{e\}$ $\{f\}$ $\{g\}$ $\{h\}$ $\{i\}$ $\{j\}$ $\{k\}$ $\{l\}$ $\{m\}$
- (a,b) $\{a, b\}$ $\{c, d\}$ $\{e, f\}$ $\{g, h\}$ $\{i, j\}$ $\{k, l\}$ $\{m\}$
 (a,c) $\{a, c\}$ $\{b, d\}$ $\{e, g\}$ $\{f, h\}$ $\{i, k\}$ $\{j, l\}$ $\{m\}$
 (b,c) $\{b, c\}$ $\{a, d\}$ $\{e, f\}$ $\{g, h\}$ $\{i, k\}$ $\{j, l\}$ $\{m\}$
 (b,d) $\{b, d\}$ $\{a, c\}$ $\{e, g\}$ $\{f, h\}$ $\{i, k\}$ $\{j, l\}$ $\{m\}$
 (e,i) $\{e, i\}$ $\{a, d\}$ $\{b, f\}$ $\{c, g\}$ $\{h, k\}$ $\{j, l\}$ $\{m\}$
 (e,g) $\{e, g\}$, $\{a, i\}$ $\{b, h\}$, $\{c, l\}$ $\{d, j\}$
 (h,l) $\{h, l\}$ $\{a, b, c, d\}$ $\{e, i, g\}$
 (j) $\{j\}$ $\{a, b, c, d\}$ $\{e, i, g\}$ $\{h, l\}$ $\{k\}$ $\{m\}$

We have

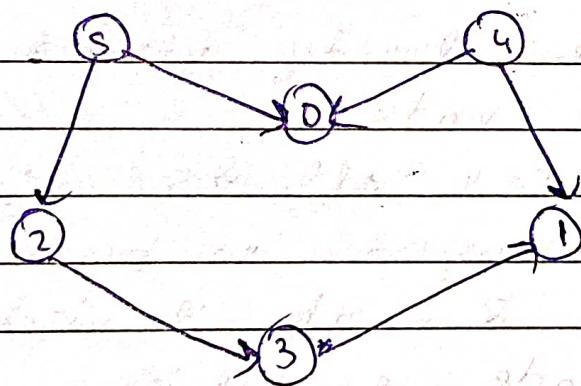
$$\{a, b, c, d\}$$

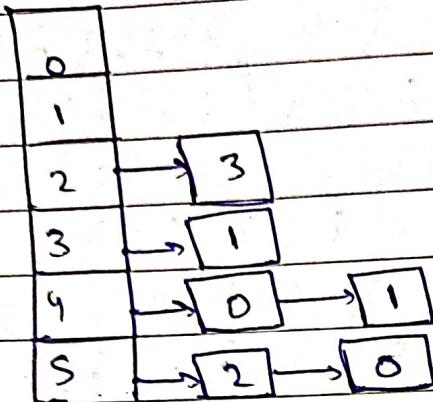
$$\{e, i, g\}$$

$$\{h, l\}$$

$$\{j\}$$

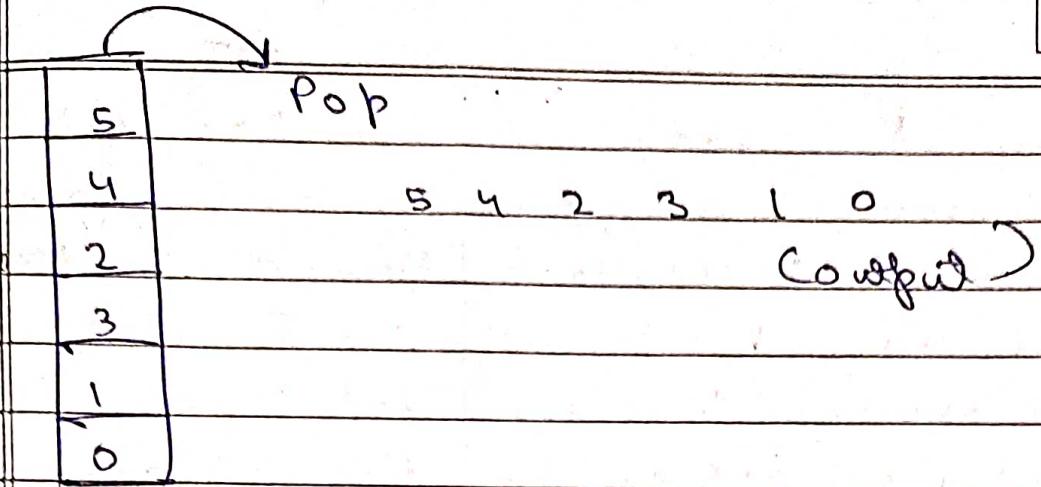
Ans 3





Algo:

- 1) Go to node 0, it has no outgoing edges so push node 0 into the stack & mark it visited.
- 2) Go to node 1, again it has no outgoing edges so push node 1 into the stack & mark it visited.
- 3) Go to node 2, process all the adjacent nodes and mark node 2 visited.
- 4) Node 3 is already visited so continue with next node.
- 5) Go to node 4, all its adjacent nodes are already visited so push node 4 into the stack & mark it visited.
- 6) Go to node 5, all its adjacent nodes are already visited so push node 5 into stack and mark it visited.



Ans Heap is generally preferred for priority queue implementation, because heap provides better performance compared to array or linked list.

Algorithms where priority queue is used -

- 1) Dijkstra's shortest path Algorithm: when the graph is stored in the form of adjacency list or matrix, priority queue can be used to extract minimum efficiently when implementing dijkstra's algorithm.
- 2) Prim's algorithm: To store keys of nodes & extract minimum key node at every step.

Min heap

Max heap

- 1) **Value every pair of the** For every pair of the parent & descendant parent & descendant child node, the parent child node, the parent node always has lower node has greater value value than descended than descended child, child node.
- 2) **The value of nodes** The value of nodes increases as we traverse decreases as we traverse from root to leaf node, from root to leaf node
- 3) **root node has the** The root node has the lowest value. greatest value.

