
MLDS 422 - Intro to Python

Lab 5

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Today's Lab Materials

- ▶ Binary Tree and Hash Table
 - ▶ Details

- ▶ Implementation

Binary Tree

- A tree data structure for hierarchical data

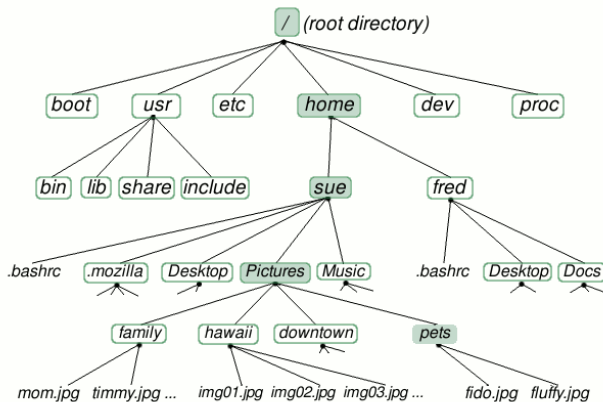


Figure: <https://astikanand.github.io/techblogs/data-structures/binary-tree>

Binary Tree - Terminology

- ▶ **node**: any element of a tree
- ▶ **root**: Topmost node
- ▶ **children**: nodes directly under a node
- ▶ **parent**: node directly above the node or nodes
- ▶ **leaves**: nodes with no children
- ▶ **edge** (link from node to node), **path** (list of links from one node to another)
- ▶ **level** (distance from the root), **height** (distance from the root to leaf)

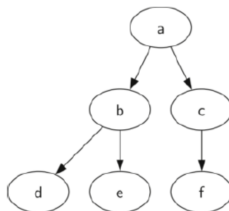
Binary Tree - Methods

- ▶ **BinaryTree()** - create a new instance
- ▶ **get_left_child()** - return the binary tree corresponding to the left child of the current node
- ▶ **get_right_child()** - return the binary tree corresponding to the right child of the current node
- ▶ **set_root_val(val)** - set root node as val
- ▶ **get_root_val()** - return the root node value
- ▶ **insert_left(val)** - create a new binary tree and install it as the left child of the current node
- ▶ **insert_right(val)** - create a new binary tree and install it as the right child of the current node

Implementations - List of Lists

- ▶ Functional programming
- ▶ `my_tree = [root, [left tree], [right tree]]`

```
my_tree = ['a', #root
           ['b', #left subtree
            ['d' [], []],
            ['e' [], []] ],
           ['c', #right subtree
            ['f' [], []],
            [] ]
          ]
```



Implementations - Class BinaryTree

- ▶ Attributes: root value, left subtree, right subtree
- ▶ Method definitions

Hash Table

- ▶ A collection of items that are stored in a way that can be fast to find ($\mathcal{O}(1)$)
- ▶ Label each position of the hash table by an integer
- ▶ Implement a hash table by a list of some size

Hash Function

- ▶ A mapping between an item and its integer label
- ▶ Takes the item as input and returns an integer in the range between 0 and $m - 1$, where m is the predefined size of list

0	1	2	3	4	5	6	7	8	9	10
77	None	None	None	26	93	17	None	None	31	54

Hash Function

- ▶ **perfect hash function:** takes each unique item to unique label
- ▶ Goal:
 - ▶ Minimize the number of collisions (number of items in each unique label)
 - ▶ Easy to compute
 - ▶ Evenly distributes the items in the hash table
 - ▶ Larger hash table (list) than items - memory issues

Hash Function

- hash functions for **character-based items** such as strings.
 - Map string to numbers using **Ordinal** value.
 - Example: "cat"

```
>>> ord('c')
```

```
99
```

```
>>> ord('a')
```

```
97
```

```
>>> ord('t')
```

```
116
```

$$\begin{array}{ccccccc} \text{c} & & \text{a} & & \text{t} & & \\ \downarrow & & \downarrow & & \downarrow & & \\ 99 & + & 97 & + & 116 & = & 312 \\ & & & & & & 312 \% 11 \longrightarrow 4 \end{array}$$

```
def hash(a_string, table_size):  
    sum = 0  
    for pos in range(len(a_string)):  
        sum = sum + ord(a_string[pos])  
  
    return sum % table_size
```

Collision Resolution

- Allow each slot to hold a reference to a chain of items

