

Memo

CS 634

Date: . . .

Q2a

The probability of a signal at the output here is computed as:

Probability that a parallel of two switches work is computed as:

$$= 1 - (1-p)^2$$

Therefore probability that a series work is computed as

$$= p \times (1 - (1-p)^2)$$

$$= p \times (2p - p^2)$$

$$= p^2 (2 - p)$$

Therefore the probability that the whole system works now is computed as

$$= 1 - (1 - p^2)(2 - p)^2$$

$$= 1 - (1 + p^4(2 - p)^2 - 2p^2(2 - p))$$

$$= 2p^2(2 - p) - p^4(2 - p)^2$$

Q2b) = probability that S3 is open and the below series works / p

$$= (1 - p)p^2(2 - p) / (2p^2(2 - p) - p^4(2 - p)^2)$$

$$= (1 - p) / (2 - p^2(2 - p))$$