

# Lab Assignment 8

October 20, 2022

**Q1.** Solve the following problem using Newton method. Use stopping criterion:  $\|\nabla F(x^{k+1}) + A^T \mu_{k+1}\| \leq 10^{-3}$ .

a)

$$\begin{aligned} \min F(x) &= \sum_{i=1}^5 x_i \log x_i \\ \text{s.t. } \sum x_i &= 1 \end{aligned}$$

and choose  $x^0 = (1/5, 1/5, 1/5, 1/5, 1/5)$ .

b)

$$\begin{aligned} \min F(x) &= \sum_{i=1}^4 x_i \exp(-x_i) \\ \text{s.t. } x_1 + x_2 + x_3 + x_4 &= 1 \\ x_1 - 2x_2 + 3x_3 - 4x_4 &= 0 \end{aligned}$$

choose  $x^0 = (2/3, 1/3, 0, 0)$ .

**Q2.** Solve the following problem using log barrier method. Choose  $\sigma_0 = 1, R = 10, x^0 \rightarrow$  Strictly feasible point. Stopping criterion  $\frac{m}{\sigma_k} < 10^{-3}$

$$\begin{aligned} \min F(x) &= x_1 + 2x_2 + 5x_3 - 8x_4 + 7x_5 - 11x_6 \\ \text{s.t. } x_1 - x_2 + x_3 &= 0 \\ x_1 - 2x_2 + 2x_3 + x_4 + x_6 &= 3 \\ 2x_3 + x_4 - 5x_5 + x_6 &= -2 \\ x_2 + x_3 + 2x_4 - 3x_5 + 2x_6 &= 1 \\ x_1 + 3x_3 - x_4 + 2x_6 &= 2 \end{aligned}$$