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Abstract: Clifford algebra of a quadratic space  $(V; q)$  is the quotient of the tensor algebra of  $V$  by the two-sided ideal  $I(V; q)$ , generated by  $fx - q(x):1 \leq x \leq \dim V$ . In [Sus77], A.A. Suslin defined a sequence of matrices whose size doubles at each step. Using Suslin construction, for  $v, w \in \mathbb{R}^{n+1}$  we get a matrix of size  $2n \times 2n$ . Moreover, each Suslin matrix  $S$  has a conjugate Suslin matrix  $S^c$  such that  $SS^c = S^cS = (v:wT)I_{2n}$ . In [Chi15], V.R. Chintala showed that Suslin matrices can be used to construct Clifford algebra of  $H(\mathbb{R}^n)$  with the quadratic form determined by the bilinear form  $b(v;w) = v:wT$ . Suslin identities are used to define standard involution on the Clifford algebra. As an application of Suslin matrices, we obtain a proof of the following exceptional isomorphism [Chi15],  $Spin_4(\mathbb{R}) \cong SL_2(\mathbb{R}) \times SL_2(\mathbb{R})$ ,  $Spin_6(\mathbb{R}) \cong SL_4(\mathbb{R})$ . Suslin matrices are defined in an inductive way. We tried to generalize the idea of Suslin matrices to a more general set up of central simple algebras. For that, a new set was defined called Suslin set with certain properties that are satisfied by Suslin matrices. We looked at algebras that are isomorphic to  $M_{2n}(F)$ . Let  $A$  be an algebra isomorphic to  $M_{2n}(F)$  by the map  $\phi$ . Then, by taking inverse image of Suslin matrices under  $\phi$ , we indeed obtain a Suslin set. We hope that Suslin sets could be useful to understand Suslin matrices.


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