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Title:	Integer sequences and monomial ideals
Authors:	Kumar, Chanchal (/jspui/browse?type=author&value=Kumar%2C+Chanchal) Roy, Amit (/jspui/browse?type=author&value=Roy%2C+Amit)
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Abstract:	Let S_n be the set of all permutations of $[n]=\{1, \dots, n\}$ and let W be the subset consisting of permutations $\sigma \in S_n$ avoiding 132 and 312-patterns. The monomial ideal $I_W = \langle x_{\sigma} = \prod_{i=1}^n x_{\sigma(i)} : \sigma \in W \rangle$ in the polynomial ring $R = k[x_1, \dots, x_n]$ over a field k is called a hypercubic ideal in Kumar and Kumar (Proc. Indian Acad. Sci. (Math Sci.) 126(4) (2016) 479–500). The Alexander dual $I[n]W$ of I_W with respect to $n=(n, \dots, n)$ has the minimal cellular resolution supported on the first barycentric subdivision $Bd(\Delta_{n-1})$ of an $n-1$ -simplex Δ_{n-1} . We show that the number of standard monomials of the Artinian quotient $R/I[n]W$ equals the number of rooted-labelled unimodal forests on the vertex set $[n]$. In other words, $\dim_k(R/I[n]W) = \sum_{r=1}^n nr! s(n, r) = \text{Per}([mij]n \times n)$, where $s(n, r)$ is the (signless) Stirling number of the first kind and $\text{Per}([mij]n \times n)$ is the permanent of the matrix $[mij]$ with $m_{ii}=i$ and $m_{ij}=1$ for $i \neq j$. For various subsets S of S_n consisting of permutations avoiding patterns, the corresponding integer sequences $\{\dim_k(R/I[n]S)\}_{n=1}^{\infty}$ are identified.
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