

Q1. Complete kinetic energy & velocities of an electron in terms of neutron for which De Broglie wavelength are equal to 1Å .

$$\lambda = \frac{h}{mv}$$

Given that de Broglie wavelength are equal for both

$$\frac{h}{m_e v_e} = \frac{h}{m_n v_n}$$

$$\frac{m_n}{m_e} = \frac{v_e}{v_n}$$

$$\frac{m_e}{m_n} = \frac{1}{1836.152} \Rightarrow \frac{v_e}{v_n} = 1836.152$$

$$\therefore v_e = v_n \times 1836.152$$

$$KE = \frac{1}{2} m v^2$$

$$\therefore KE = \frac{1}{2} m v_n^2 [1836.152]^2$$

Q2. Find wavelength of a neutron having $KE = 1 \text{ eV}$

$$\lambda = \frac{h}{mv} \quad \therefore (mv)^2 = \frac{h^2}{\lambda^2}$$

$$KE = \frac{h^2}{2m\lambda^2}$$

$$1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$$

$$1.602 \times 10^{-19} \text{ J} = \frac{(6.63 \times 10^{-34} \text{ kg m}^2/\text{s})^2}{2 \times m \times \lambda^2}$$

$$\lambda^2 = \frac{(6.63 \times 10^{-34})^2}{2 \times 1.602 \times 10^{-19}}$$

$$\lambda = 1.2272 \times 10^{-9} \text{ m}$$

Q3. The radius of a typical atom is 1 \AA . To locate the nucleus of an electron within a distance of $5 \times 10^{-12} \text{ m}$ using electromagnetic waves, the wavelength must be of this order. Calculate energy & momentum of a photon with wavelength $\lambda = 5 \times 10^{-12} \text{ m}$. If $\Delta x = 5 \times 10^{-12} \text{ m}$; what is corresponding uncertainty in momentum?

$$\rightarrow \lambda = 5 \times 10^{-12} \text{ m} - \text{given}$$

$$E = \frac{hc}{\lambda} = \frac{6.63 \times 10^{-34} \times 3 \times 10^8}{5 \times 10^{-12}}$$

$$= 3.978 \times 10^{-4} \text{ J}$$

$$p = \frac{h}{\lambda} = \frac{6.63 \times 10^{-34}}{5 \times 10^{-12}} = 1.33 \times 10^{-22} \text{ kg m/s}$$

Uncertainty in momentum

$$\Delta p \cdot \Delta x \geq \frac{h}{4\pi}$$

$$\therefore \Delta p \geq \frac{h}{4\pi \Delta x}$$

$$\therefore \Delta p \geq 1.055 \times 10^{-23} \text{ kg m/s}$$

Q4. Compare wavelength of a cricket ball of mass 500 gm flying with a velocity of 500 km/hr with that of an e^- having energy 100 eV

\rightarrow

$$100 \text{ eV} = \frac{h^2}{2m\lambda^2}$$

27. In two QUBIT'S with wave fun
 $(0.70710) + 0.70711)$ are entangled
 then what is resultant wave
 fun?

→ For entangled wave
 2nd possible state
 i.e. $\Rightarrow 2^2 = 4$

$$\psi = ((0.7072|0\rangle + 0.7072|1\rangle) \\ \times (0.7072|0\rangle + 0.7072|1\rangle))$$

$$\psi = ((0.7072 \times 0.7072)|00\rangle) + \\ (0.7072 \times 0.7072)|01\rangle + \\ (0.7072 \times 0.7072)|10\rangle + \\ (0.7072 \times 0.7072)|11\rangle$$

$$\psi = 2 \times (0.50013184)^2 + (0.50013184)^2$$

$$\psi = 4 \times (0.5013184)^2$$

$$\psi = 1.00052743$$

$$\boxed{\psi \approx 1}$$

Q5. An electron and a 150 gm baseball are travelling with velocity of 250 m/s. If they are measured to an accuracy of 0.025%, calculate & compare uncertainty in position of each.

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$$P_e = m_e \times v_e$$

$$P_b = m_b \times v_b$$

$$\therefore P_e = 9.1 \times 10^{-31} \times 250$$

$$= P_e = 2.275 \times 10^{-28}$$

$$\text{uncertainty in momentum} = 0.025 \times 2.275 \times 10^{-28}$$

$$= 5.693 \times 10^{-32}$$

$$\therefore \Delta x \Delta p \geq \frac{h}{4\pi}$$

$$\Delta x \geq \frac{h}{4\pi \times 5.693 \times 10^{-32}}$$

$$\therefore \Delta x \geq 9.26 \times 10^{-4} \text{ m}$$

$$\lambda_e = \frac{h}{\sqrt{2mE}}$$

$$\lambda_e = \frac{6.63 \times 10^{-34}}{\sqrt{2 \times 9.1 \times 10^{-31} \times 1.602 \times 10^{-19}}}$$

$$\boxed{\lambda_e = 1.2278 \text{ \AA}}$$

wavelength of ball of mass 0.5 kg

$$KE_b = 0.5 \times 0.5 \times (138.8889)^2$$

$$KE_b = 4822.5309 \text{ J}$$

$$\lambda_b = \frac{6.63 \times 10^{-34}}{\sqrt{2 \times 0.5 \times 4822.5309}} = 9.5471 \times 10^{-26} \text{ \AA}$$

$$\frac{\lambda_e}{\lambda_b} = \frac{1.2278 \times 10^{26}}{9.5471}$$

$$\boxed{\lambda_e = \lambda_b \times 1.28 \times 10^{23} \text{ m}}$$