# notebook dqn

November 9, 2021

```
[1]: %%javascript
    IPython.OutputArea.prototype._should_scroll = function(lines) {
        return false;
    }
```

<IPython.core.display.Javascript object>

Before submitting, make sure you are adhering to the following rules, which helps us grade your assignment. Assignments that do not adhere to these rules will be penalized.

- Make sure your notebook only contains the exercises requested in the notebook, and the written homework (if any) is delivered in class in printed form, i.e. don't submit your written homework as part of the notebook.
- Make sure you are using Python3. This notebook is already set up to use Python3 (top right corner); Do not change this.
- If a method is provided with a specific signature, do not change the signature in any way, or the default values.
- Don't hard-code your solutions to the specific environments which it is being used on, or the specific hyper-parameters which it is being used on; Be as general as possible, which means also using ALL the arguments of the methods your are implementing.
- Clean up your code before submitting, i.e. remove all print statements that you've used to develop and debug (especially if it's going to clog up the interface by printing thousands of lines). Only output whatever is required by the exercise.
- For technical reasons, plots should be contained in their own cell which should run instantly, separate from cells which perform longer computations. This notebook is already formatted in such a way, please make sure this remains the case.
- Make sure your notebook runs completely, from start to end, without raising any unintended errors. After you've made the last edit, Use the option Kernel -> Restart & Run All to rerun the entire notebook. If you end up making ANY edit, re-run everything again. Always assume any edit you make may have broken your code!

# 1 Homework 6: Deep Q-Networks in Pytorch

In this assignment you will implement deep q-learning using Pytorch.

```
[2]: import copy
     import math
     import os
     from collections import namedtuple
     import gym
     import ipywidgets as widgets
     import matplotlib.pyplot as plt
     import more_itertools as mitt
     import numpy as np
     import torch
     import torch.nn as nn
     import torch.nn.functional as F
     import tqdm
     import random
     plt.style.use('ggplot')
     plt.rcParams['figure.figsize'] = [12, 4]
```

**Environments** In this notebook, we will implement DQN and run it on four environments which have a continuous state-space and discrete action-space. There are:

- CartPole: Balance a pole on a moving cart (https://gym.openai.com/envs/CartPole-v1/).
- Mountain Car: Gather momentum to climb a hill (https://gym.openai.com/envs/MountainCar-v0/).
- AcroBot: A two-link robot needs to swing and reach the area above a line (https://gym.openai.com/envs/Acrobot-v1/).
- LunarLander: A spaceship needs to fly and land in the landing spot. (https://gym.openai.com/envs/LunarLander-v2/).

```
[3]: envs = {
    'cartpole': gym.make('CartPole-v1'),
    'mountaincar': gym.make('MountainCar-v0'),
    'acrobot': gym.make('Acrobot-v1'),
    'lunarlander': gym.make('LunarLander-v2'),
}
```

These environments are particularly cool because they all include a graphical visualization which we can use to visualize our learned policies. Run the folling cell and click the buttons to run the visualization with a random policy.

```
[4]: def render(env, policy=None):
    """Graphically render an episode using the given policy

:param env: Gym environment
:param policy: function which maps state to action. If None, the random policy is used.
```

```
if policy is None:
    def policy(state):
        return env.action_space.sample()

state = env.reset()
env.render()

while True:
    action = policy(state)
    state, _, done, _ = env.step(action)
    env.render()

if done:
    break

env.close()
```

```
[5]: # Jupyter UI
     def button_callback(button):
         for b in buttons:
             b.disabled = True
         env = envs[button.description]
         render(env)
         env.close()
         for b in buttons:
             b.disabled = False
     buttons = []
     for env_id in envs.keys():
         button = widgets.Button(description=env_id)
         button.on_click(button_callback)
         buttons.append(button)
     print('Click a button to run a random policy:')
     widgets.HBox(buttons)
```

Click a button to run a random policy:

HBox(children=(Button(description='cartpole', style=ButtonStyle()),

Button(description='mountaincar', style=Bu...

#### 1.1 Misc Utilities

Some are provided, some you should implement

### 1.1.1 Smoothing

In this homework, we'll do some plotting of noisy data, so here is the smoothing function which was also used in the previous homework.

## 1.1.2 Q1 (1 pt): Exponential $\epsilon$ -Greedy Decay

This time we'll switch from using a linear decay to an exponential decay, defined as

$$\epsilon_t = a \exp(bt)$$

where a and b are the parameters of the schedule.

The interface to the scheduler is the same as in the linear case from the previous homework, i.e. it receives the initial value, the final value, and in how many steps to go from initial to final. Your task is to compute parameters a and b to make the scheduler work as expected.

```
[7]: class ExponentialSchedule:
    def __init__(self, value_from, value_to, num_steps):
        """Exponential schedule from `value_from` to `value_to` in `num_steps`_

⇒steps.

$value(t) = a \exp (b t)$

:param value_from: initial value
:param value_to: final value
:param num_steps: number of steps for the exponential schedule
```

```
11 11 11
        self.value_from = value_from
        self.value_to = value_to
        self.num_steps = num_steps
        # YOUR CODE HERE: determine the `a` and `b` parameters such that the
⇒schedule is correct
        self.a = self.value from
        self.b = math.log(self.value_to / self.a) / (self.num_steps - 1)
    def value(self, step) -> float:
        """Return exponentially interpolated value between `value_from` and \Box
 → `value_ to `interpolated value between.
        returns {
             `value_from`, if step == 0 or less
             `value_to`, if step == num_steps - 1 or more
            the exponential interpolation between `value_from` and `value_to`, _
\hookrightarrow if \ 0 \le steps < num\_steps
        }
        :param step: The step at which to compute the interpolation.
        :rtype: float. The interpolated value.
        \# YOUR CODE HERE: implement the schedule rule as described in the
\rightarrow docstring,
        # using attributes `self.a` and `self.b`.
        if step <= 0:</pre>
            return self.value_from
        elif step >= (self.num_steps - 1):
            return self.value_to
        else:
            return self.a * math.exp(self.b * step)
# test code, do not edit
def _test_schedule(schedule, step, value, ndigits=5):
    """Tests that the schedule returns the correct value."""
    v = schedule.value(step)
    if not round(v, ndigits) == round(value, ndigits):
        raise Exception(
            f'For step {step}, the scheduler returned {v} instead of {value}'
        )
```

```
_schedule = ExponentialSchedule(0.1, 0.2, 3)
_test_schedule(_schedule, -1, 0.1)
_test_schedule(_schedule, 0, 0.1)
_test_schedule(_schedule, 1, 0.141421356237309515)
_test_schedule(_schedule, 2, 0.2)
_test_schedule(_schedule, 3, 0.2)
del _schedule
_schedule = ExponentialSchedule(0.5, 0.1, 5)
_test_schedule(_schedule, -1, 0.5)
_test_schedule(_schedule, 0, 0.5)
_test_schedule(_schedule, 1, 0.33437015248821106)
_test_schedule(_schedule, 2, 0.22360679774997905)
_test_schedule(_schedule, 3, 0.14953487812212207)
_test_schedule(_schedule, 4, 0.1)
_test_schedule(_schedule, 5, 0.1)
del _schedule
```

### 1.1.3 Q2 (1 pt): Replay Memory

Now we will implement the Replay Memory, the data-structure where we store previous experiences so that we can re-sample and train on them.

```
[16]: # Batch namedtuple, i.e. a class which contains the given attributes
      Batch = namedtuple(
          'Batch', ('states', 'actions', 'rewards', 'next_states', 'dones')
      )
      class ReplayMemory:
          def __init__(self, max_size, state_size):
              """Replay memory implemented as a circular buffer.
              Experiences will be removed in a FIFO manner after reaching maximum
              buffer size.
              Args:
                  - max_size: Maximum size of the buffer.
                  - state_size: Size of the state-space features for the environment.
              self.max_size = max_size
              self.state size = state size
              # preallocating all the required memory, for speed concerns
              self.states = torch.empty((max_size, state_size))
```

```
self.actions = torch.empty((max_size, 1), dtype=torch.long)
    self.rewards = torch.empty((max_size, 1))
    self.next_states = torch.empty((max_size, state_size))
    self.dones = torch.empty((max_size, 1), dtype=torch.bool)
    # pointer to the current location in the circular buffer
    self.idx = 0
    # indicates number of transitions currently stored in the buffer
    self.size = 0
def add(self, state, action, reward, next state, done):
    """Add a transition to the buffer.
    :param state: 1-D np.ndarray of state-features.
    :param action: integer action.
    :param reward: float reward.
    :param next_state: 1-D np.ndarray of state-features.
    :param done: boolean value indicating the end of an episode.
    HHHH
    # YOUR CODE HERE: store the input values into the appropriate
    # attributes, using the current buffer position `self.idx`
   self.states[self.idx] = torch.from numpy(state)
    self.actions[self.idx] = action
    self.rewards[self.idx] = reward
    self.next states[self.idx] = torch.from numpy(next state)
   self.dones[self.idx] = done
    # DO NOT EDIT
    # circulate the pointer to the next position
    self.idx = (self.idx + 1) % self.max_size
    # update the current buffer size
    self.size = min(self.size + 1, self.max_size)
def sample(self, batch_size) -> Batch:
    """Sample a batch of experiences.
    If the buffer contains less that `batch_size` transitions, sample all
    of them.
    :param batch_size: Number of transitions to sample.
    :rtype: Batch
    HHHH
    # YOUR CODE HERE: randomly sample an appropriate number of
    # transitions *without replacement*. If the buffer contains less than
```

```
# `batch size` transitions, return all of them. The return type must
       # be a `Batch`.
       if batch_size > self.size:
           sample_indices = list(range(self.size))
       else:
           sample_indices = random.sample(list(range(self.max_size)),__
→batch_size)
       batch = Batch(self.states[sample_indices], self.
→actions[sample_indices], self.rewards[sample_indices], self.
→next_states[sample_indices], self.dones[sample_indices])
       return batch
  def populate(self, env, num_steps):
       """Populate this replay memory with `num_steps` from the random policy.
       :param env: Openai Gym environment
       :param num_steps: Number of steps to populate the
       # YOUR CODE HERE: run a random policy for `num_steps` time-steps and
       # populate the replay memory with the resulting transitions.
       # Hint: don't repeat code! Use the self.add() method!
       state = env.reset()
       for i in range(num_steps):
           action = np.random.choice(env.action space.n)
           next_state, reward, done, _ = env.step(action)
           self.add(state, action, reward, next_state, done)
           if done:
               state = env.reset()
           else:
               state = next_state
```

# 1.1.4 Q3 (2 pts): Pytorch DQN module

Pytorch is a numeric computation library akin to numpy, which also features automatic differentiation. This means that the library automatically computes the gradients for many differentiable operations, something we will exploit to train our models without having to program the gradients' code. There are a few caveats: sometimes we have to pay explicit attention to whether the operations we are using are implemented by the library (most are), and there are a number of operations which don't play well with automatic differentiation (most notably, in-place assignments).

This library is a tool, and as many tools you'll have to learn how to use it well. Sometimes not using it well means that your program will crash. Sometimes it means that your program won't crash but won't be computing the correct outputs. And sometimes it means that it will compute the correct things, but is less efficient than it could otherwise be. This library is SUPER popular,

and online resources abound, so take your time to learn the basics. If you're having problems, first try to debug it yourself, also looking up the errors you get online. You can also use Piazza and the office hours to ask for help with problems.

In the next cell, we inherit from the base class torch.nn.Module to implement our DQN module, which takes state-vectors and returns the respective action-values.

```
[11]: class DQN(nn.Module):
          def __init__(self, state_dim, action_dim, *, num_layers=3, hidden_dim=256):
              """Deep Q-Network PyTorch model.
              Args:
                  - state_dim: Dimensionality of states
                  - action dim: Dimensionality of actions
                  - num_layers: Number of total linear layers
                  - hidden_dim: Number of neurons in the hidden layers
              11 11 11
              super().__init__()
              self.state_dim = state_dim
              self.action_dim = action_dim
              self.num_layers = num_layers
              self.hidden_dim = hidden_dim
              # YOUR CODE HERE: define the layers of your model such that
              # * there are `num_layers` nn.Linear modules / layers
              # * all activations except the last should be ReLU activations
                 (this can be achieved either using a nn.ReLU() object or the nn.
       → functional.relu() method)
              # * the last activation can either be missing, or you can use nn.
       \rightarrow Identity()
              layers = []
              layers.append(nn.Linear(self.state_dim, self.hidden_dim))
              layers.append(nn.ReLU())
              for i in range(num layers - 2):
                  layers.append(nn.Linear(self.hidden_dim, self.hidden_dim))
                  layers.append(nn.ReLU())
              layers.append(nn.Linear(self.hidden_dim, self.action_dim))
              self.linear = nn.ModuleList(layers)
          def forward(self, states) -> torch.Tensor:
              """Q function mapping from states to action-values.
              :param states: (*, S) torch. Tensor where * is any number of additional
                      dimensions, and S is the dimensionality of state-space.
              :rtype: (*, A) torch. Tensor where * is the same number of additional
                      dimensions as the `states`, and A is the dimensionality of the
                      action-space. This represents the Q values Q(s, .).
```

```
# YOUR CODE HERE: use the defined layers and activations to compute
        # the action-values tensor associated with the input states.
        for layer in self.linear:
            states = layer(states)
       return states
    # utility methods for cloning and storing models. DO NOT EDIT
   @classmethod
   def custom load(cls, data):
       model = cls(*data['args'], **data['kwargs'])
       model.load_state_dict(data['state_dict'])
       return model
   def custom_dump(self):
       return {
            'args': (self.state_dim, self.action_dim),
            'kwargs': {
                'num_layers': self.num_layers,
                'hidden_dim': self.hidden_dim,
            'state_dict': self.state_dict(),
       }
# test code. do not edit
def _test_dqn_forward(dqn_model, input_shape, output_shape):
    """Tests that the dgn returns the correctly shaped tensors."""
    inputs = torch.torch.randn((input_shape))
   outputs = dqn_model(inputs)
   if not isinstance(outputs, torch.FloatTensor):
       raise Exception(
            f'DQN.forward returned type {type(outputs)} instead of torch.Tensor'
        )
   if outputs.shape != output shape:
        raise Exception(
            f'DQN.forward returned tensor with shape {outputs.shape} instead of,
 →{output_shape}'
        )
   if not outputs.requires_grad:
       raise Exception(
```

```
f'DQN.forward returned tensor which does not require a gradient ⊔
 ⇔(but it should)'
        )
dqn \mod el = DQN(10, 4)
_test_dqn_forward(dqn_model, (64, 10), (64, 4))
_test_dqn_forward(dqn_model, (2, 3, 10), (2, 3, 4))
del dqn_model
dqn_{model} = DQN(64, 16)
_test_dqn_forward(dqn_model, (64, 64), (64, 16))
_test_dqn_forward(dqn_model, (2, 3, 64), (2, 3, 16))
del dqn_model
# testing custom dump / load
dqn1 = DQN(10, 4, num_layers=10, hidden_dim=20)
dqn2 = DQN.custom_load(dqn1.custom_dump())
assert dqn2.state dim == 10
assert dqn2.action_dim == 4
assert dqn2.num layers == 10
assert dqn2.hidden_dim == 20
```

### 1.1.5 Q4 (1 pt): Single batch-update

```
[12]: def train_dqn_batch(optimizer, batch, dqn_model, dqn_target, gamma) -> float:
          """Perform a single batch-update step on the given DQN model.
          :param optimizer: nn.optim.Optimizer instance.
          :param batch: Batch of experiences (class defined earlier).
          :param dqn_model: The DQN model to be trained.
          :param dqn_target: The target DQN model, ~NOT~ to be trained.
          :param gamma: The discount factor.
          :rtype: float The scalar loss associated with this batch.
          # YOUR CODE HERE: compute the values and target values tensors using the
          # given models and the batch of data.
         values = torch.gather(dqn model(batch.states), -1, batch.actions)
         target_values = torch.zeros_like(values, requires_grad=False)
         with torch.no grad():
             target_values = torch.add(batch.rewards, torch.max(dqn_target(batch.
       →next_states), -1).values.unsqueeze(-1) * torch.logical_not(batch.dones).
       →float(), alpha=gamma)
          # DO NOT EDIT FURTHER
```

```
assert (
    values.shape == target_values.shape
), 'Shapes of values tensor and target_values tensor do not match.'

# testing that the value tensor requires a gradient,
# and the target_values tensor does not
assert values.requires_grad, 'values tensor should not require gradients'
assert (
    not target_values.requires_grad
), 'target_values tensor should require gradients'

# computing the scalar MSE loss between computed values and the TD-target
loss = F.mse_loss(values, target_values)

optimizer.zero_grad() # reset all previous gradients
loss.backward() # compute new gradients
optimizer.step() # perform one gradient descent step

return loss.item()
```

### 1.1.6 Q5 (2 pts):

```
[13]: def train_dqn(
          env,
          num_steps,
          *,
         num_saves=5,
          replay_size,
          replay_prepopulate_steps=0,
          batch_size,
          exploration,
          gamma,
      ):
          DQN algorithm.
          Compared to previous training procedures, we will train for a given number
          of time-steps rather than a given number of episodes. The number of
          time-steps will be in the range of millions, which still results in many
          episodes being executed.
          Args:
              - env: The openai Gym environment
              - num_steps: Total number of steps to be used for training
              - num_saves: How many models to save to analyze the training progress.
              - replay_size: Maximum size of the ReplayMemory
```

```
- replay prepopulate steps: Number of steps with which to prepopulate
                                the memory
    - batch_size: Number of experiences in a batch
    - exploration: a ExponentialSchedule
    - gamma: The discount factor
Returns: (saved models, returns)
    - saved_models: Dictionary whose values are trained DQN models
    - returns: Numpy array containing the return of each training episode
    - lengths: Numpy array containing the length of each training episode
    - losses: Numpy array containing the loss of each training batch
# check that environment states are compatible with our DQN representation
assert (
   isinstance(env.observation_space, gym.spaces.Box)
   and len(env.observation_space.shape) == 1
)
# get the state_size from the environment
state_size = env.observation_space.shape[0]
# initialize the DQN and DQN-target models
dqn_model = DQN(state_size, env.action_space.n)
dqn_target = DQN.custom_load(dqn_model.custom_dump())
# initialize the optimizer
optimizer = torch.optim.Adam(dqn_model.parameters())
# initialize the replay memory and prepopulate it
memory = ReplayMemory(replay_size, state_size)
memory.populate(env, replay_prepopulate_steps)
# initiate lists to store returns, lengths and losses
rewards = []
returns = []
lengths = []
losses = []
# initiate structures to store the models at different stages of training
t_saves = np.linspace(0, num_steps, num_saves - 1, endpoint=False)
saved models = {}
i episode = 0 # use this to indicate the index of the current episode
t_episode = 0 # use this to indicate the time-step inside current episode
state = env.reset() # initialize state of first episode
```

```
return_ep = 0.0
   # iterate for a total of `num_steps` steps
   pbar = tqdm.notebook.trange(num_steps)
   for t_total in pbar:
       # use t_total to indicate the time-step from the beginning of training
       # save model
       if t total in t saves:
           model_name = f'{100 * t_total / num_steps:04.1f}'.replace('.', '_')
           saved models[model name] = copy.deepcopy(dgn model)
       # YOUR CODE HERE:
       # * sample an action from the DQN using epsilon-greedy
       # * use the action to advance the environment by one step
       # * store the transition into the replay memory
       eps = exploration.value(t_total)
       if random.random() < eps:</pre>
           action = np.random.choice(env.action_space.n)
       else:
           with torch.no_grad():
               action = int(np.argmax(dqn_model(torch.from_numpy(state).
→float()).numpy()))
       next_state, reward, done, _ = env.step(action)
       memory.add(state, action, reward, next_state, done)
       # YOUR CODE HERE: once every 4 steps,
       # * sample a batch from the replay memory
       # * perform a batch update (use the train_dqn_batch() method!)
       if t total % 4 == 0:
           losses.append(train_dqn_batch(optimizer, memory.sample(batch_size),_
→dqn_model, dqn_target, gamma))
       # YOUR CODE HERE: once every 10_000 steps,
       # * update the target network (use the dqn_model.state_dict() and
       # dqn_target.load_state_dict() methods!)
       if t_total % 10_000 == 0:
           dqn_target.load_state_dict(dqn_model.state_dict())
       if done:
           # YOUR CODE HERE: anything you need to do at the end of an
           # episode, e.g. compute return G, store stuff, reset variables,
           # indices, lists, etc.
```

```
state = env.reset()
           rewards.append(reward)
           lengths.append(t_episode + 1)
           G = 0
           for i in range(len(rewards)-1, -1, -1):
               G = gamma*G + rewards[i]
           returns.append(G)
           pbar.set description(
               f'Episode: {i_episode} | Steps: {t_episode + 1} | Return: {G:5.
\rightarrow2f} | Epsilon: {eps:4.2f}'
           )
           i_episode += 1
           t_episode = 0
           rewards = []
       else:
           # YOUR CODE HERE: anything you need to do within an episode
           state = next state
           t_episode += 1
           rewards.append(reward)
   saved_models['100_0'] = copy.deepcopy(dqn_model)
   return (
       saved_models,
       np.array(returns),
       np.array(lengths),
       np.array(losses),
   )
```

# 1.1.7 Q6 (1 pt): Evaluation of DQN on the 4 environments

CartPole Test your implentation on the cartpole environment. Training will take much longer than in the previous homeworks, so this time you won't have to find good hyper-parameters, or to train multiple runs. This cell should take about 60-90 minutes to run. After training, run the last cell in this notebook to view the policies which were obtained at 0%, 25%, 50%, 75% and 100% of the training.

```
[12]: env = envs['cartpole']
gamma = 0.99

# we train for many time-steps; as usual, you can decrease this during

→development / debugging.

# but make sure to restore it to 1_500_000 before submitting.

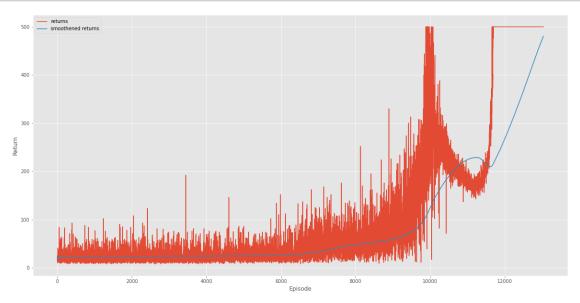
num_steps = 1_500_000
```

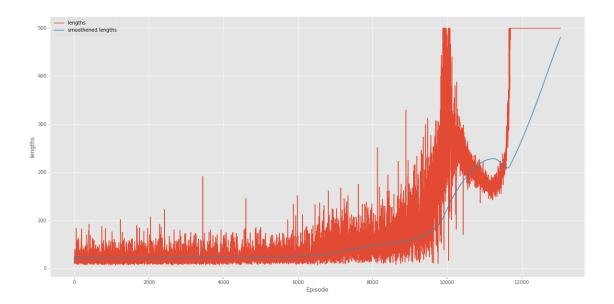
```
num_saves = 5 # save models at 0%, 25%, 50%, 75% and 100% of training
replay_size = 200_000
replay_prepopulate_steps = 50_000
batch_size = 64
exploration = ExponentialSchedule(1.0, 0.05, 1_000_000)
# this should take about 90-120 minutes on a generic 4-core laptop
dqn_models, returns, lengths, losses = train_dqn(
   env.
   num_steps,
   num saves=num saves,
   replay_size=replay_size,
   replay_prepopulate_steps=replay_prepopulate_steps,
   batch_size=batch_size,
    exploration=exploration,
   gamma=gamma,
)
assert len(dqn_models) == num_saves
assert all(isinstance(value, DQN) for value in dqn_models.values())
# saving computed models to disk, so that we can load and visualize them later.
checkpoint = {key: dqn.custom_dump() for key, dqn in dqn_models.items()}
torch.save(checkpoint, f'checkpoint {env.spec.id}.pt')
```

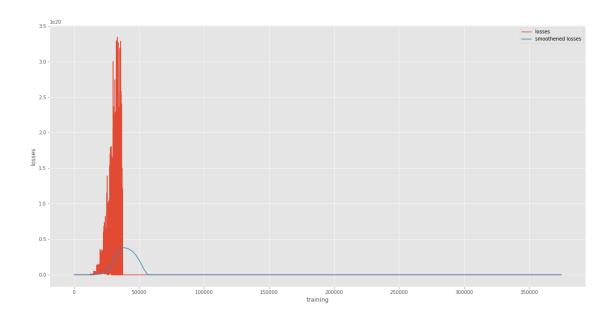
Plot the returns, lengths and losses obtained while running DQN on the cartpole environment.

```
[17]: smooth_returns = rolling_average(returns, window_size=1500)
    episodes = range(len(returns))
    plt.plot(episodes, returns, label="returns")
    plt.plot(episodes, smooth_returns, label="smoothened returns")
    plt.xlabel('Episode')
    plt.ylabel('Return')
```

```
plt.legend(loc='best')
plt.show()
smooth_lengths = rolling_average(lengths, window_size=1500)
plt.plot(episodes, lengths, label="lengths")
plt.plot(episodes, smooth_lengths, label="smoothened lengths")
plt.xlabel('Episode')
plt.ylabel('lengths')
plt.legend(loc='best')
plt.show()
smooth_losses = rolling_average(losses, window_size=20_000)
training = range(len(losses))
plt.plot(training, losses, label="losses")
plt.plot(training, smooth_losses, label="smoothened losses")
plt.xlabel('training')
plt.ylabel('losses')
plt.legend(loc='best')
plt.show()
```







MountainCar Test your implentation on the mountaincar environment. Training will take much longer than in the previous homeworks, so this time you won't have to find good hyper-parameters, or to train multiple runs. This cell should take about 60-90 minutes to run. After training, run the last cell in this notebook to view the policies which were obtained at 0%, 25%, 50%, 75% and 100% of the training.

```
[25]: env = envs['mountaincar']
gamma = 0.99
```

```
# we train for many time-steps; as usual, you can decrease this during_
→ development / debugging.
# but make sure to restore it to 1 500 000 before submitting.
num\_steps = 1_500_000
num saves = 5 # save models at 0%, 25%, 50%, 75% and 100% of training
replay_size = 200_000
replay_prepopulate_steps = 50_000
batch_size = 64
exploration = ExponentialSchedule(1.0, 0.05, 1_000_000)
# this should take about 90-120 minutes on a generic 4-core laptop
dqn_models, returns, lengths, losses = train_dqn(
    env,
   num_steps,
   num_saves=num_saves,
   replay_size=replay_size,
   replay_prepopulate_steps=replay_prepopulate_steps,
   batch size=batch size,
   exploration=exploration,
   gamma=gamma,
)
assert len(dqn_models) == num_saves
assert all(isinstance(value, DQN) for value in dqn_models.values())
# saving computed models to disk, so that we can load and visualize them later.
checkpoint = {key: dqn.custom_dump() for key, dqn in dqn_models.items()}
torch.save(checkpoint, f'checkpoint_{env.spec.id}.pt')
```

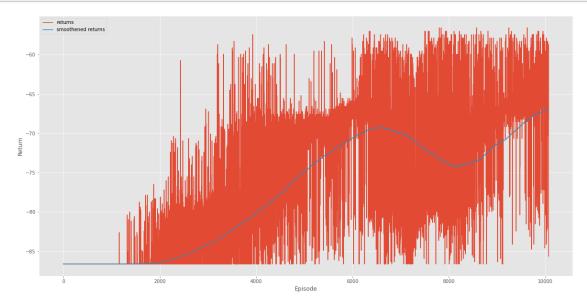
```
0%| | 0/1500000 [00:00<?, ?it/s]
```

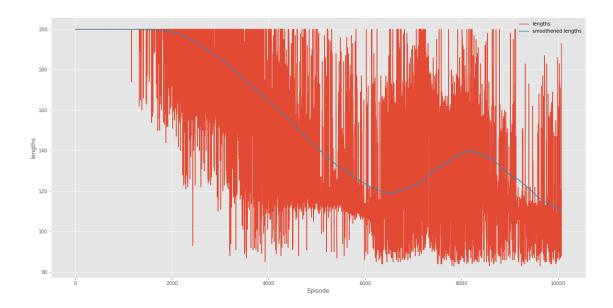
Plot the returns, lengths and losses obtained while running DQN on the mountaincar environment.

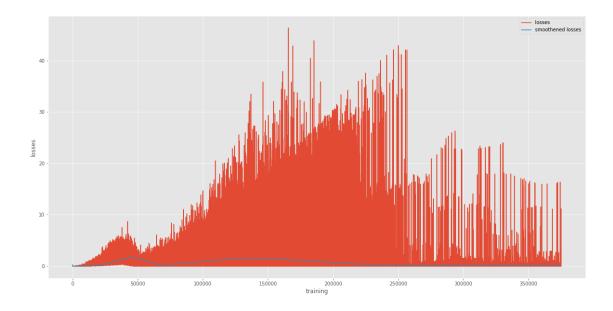
```
[26]: smooth_returns = rolling_average(returns, window_size=1500)
    episodes = range(len(returns))
    plt.plot(episodes, returns, label="returns")
    plt.plot(episodes, smooth_returns, label="smoothened returns")
    plt.xlabel('Episode')
    plt.ylabel('Return')
    plt.legend(loc='best')
    plt.show()
```

```
smooth_lengths = rolling_average(lengths, window_size=1500)
plt.plot(episodes, lengths, label="lengths")
plt.plot(episodes, smooth_lengths, label="smoothened lengths")
plt.xlabel('Episode')
plt.ylabel('lengths')
plt.legend(loc='best')
plt.show()

smooth_losses = rolling_average(losses, window_size=20_000)
training = range(len(losses))
plt.plot(training, losses, label="losses")
plt.plot(training, smooth_losses, label="smoothened losses")
plt.xlabel('training')
plt.ylabel('losses')
plt.legend(loc='best')
plt.show()
```







**AcroBot** Test your implentation on the acrobot environment. Training will take much longer than in the previous homeworks, so this time you won't have to find good hyper-parameters, or to train multiple runs. This cell should take about 60-90 minutes to run. After training, run the last cell in this notebook to view the policies which were obtained at 0%, 25%, 50%, 75% and 100% of the training.

```
[28]: env = envs['acrobot']
gamma = 0.99
```

```
# we train for many time-steps; as usual, you can decrease this during
→ development / debugging.
# but make sure to restore it to 1_500_000 before submitting.
num steps = 1 500 000
num_saves = 5 # save models at 0%, 25%, 50%, 75% and 100% of training
replay size = 200 000
replay_prepopulate_steps = 50_000
batch_size = 64
exploration = ExponentialSchedule(1.0, 0.05, 1_000_000)
# this should take about 90-120 minutes on a generic 4-core laptop
dqn_models, returns, lengths, losses = train_dqn(
   num_steps,
   num_saves=num_saves,
   replay_size=replay_size,
   replay_prepopulate_steps=replay_prepopulate_steps,
   batch_size=batch_size,
   exploration=exploration,
   gamma=gamma,
)
assert len(dqn_models) == num_saves
assert all(isinstance(value, DQN) for value in dqn models.values())
# saving computed models to disk, so that we can load and visualize them later.
checkpoint = {key: dqn.custom_dump() for key, dqn in dqn_models.items()}
torch.save(checkpoint, f'checkpoint_{env.spec.id}.pt')
```

```
0%| | 0/1500000 [00:00<?, ?it/s]
```

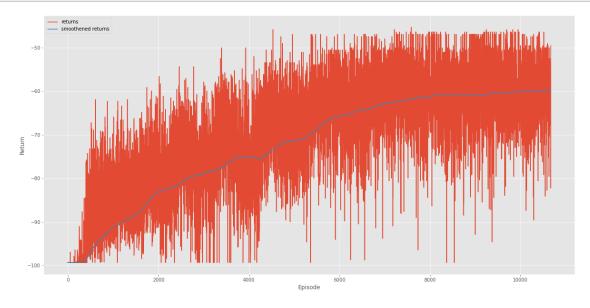
Plot the returns, lengths and losses obtained while running DQN on the acrobot environment.

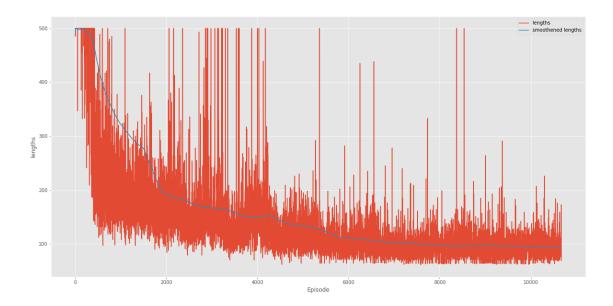
```
[29]: smooth_returns = rolling_average(returns, window_size=1500)
    episodes = range(len(returns))
    plt.plot(episodes, returns, label="returns")
    plt.plot(episodes, smooth_returns, label="smoothened returns")
    plt.xlabel('Episode')
    plt.ylabel('Return')
    plt.legend(loc='best')
    plt.show()

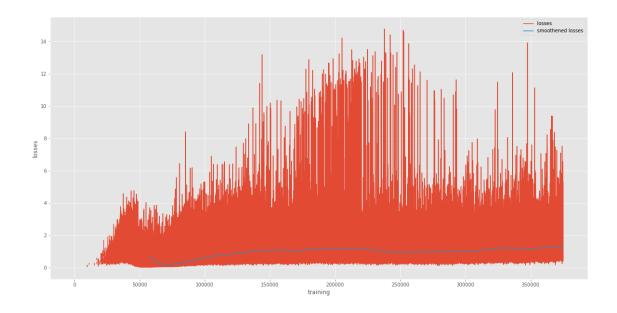
smooth_lengths = rolling_average(lengths, window_size=1500)
```

```
plt.plot(episodes, lengths, label="lengths")
plt.plot(episodes, smooth_lengths, label="smoothened lengths")
plt.xlabel('Episode')
plt.ylabel('lengths')
plt.legend(loc='best')
plt.show()

smooth_losses = rolling_average(losses, window_size=20_000)
training = range(len(losses))
plt.plot(training, losses, label="losses")
plt.plot(training, smooth_losses, label="smoothened losses")
plt.xlabel('training')
plt.ylabel('losses')
plt.legend(loc='best')
plt.show()
```







**LunarLander** Test your implentation on the lunarlander environment. Training will take much longer than in the previous homeworks, so this time you won't have to find good hyper-parameters, or to train multiple runs. This cell should take about 60-90 minutes to run. After training, run the last cell in this notebook to view the policies which were obtained at 0%, 25%, 50%, 75% and 100% of the training.

```
[17]: env = envs['lunarlander']
gamma = 0.99
```

```
# we train for many time-steps; as usual, you can decrease this during
→ development / debugging.
# but make sure to restore it to 1_500_000 before submitting.
num steps = 1 500 000
num_saves = 5 # save models at 0%, 25%, 50%, 75% and 100% of training
replay size = 200 000
replay_prepopulate_steps = 50_000
batch_size = 64
exploration = ExponentialSchedule(1.0, 0.05, 1_000_000)
# this should take about 90-120 minutes on a generic 4-core laptop
dqn_models, returns, lengths, losses = train_dqn(
   num_steps,
   num_saves=num_saves,
   replay_size=replay_size,
   replay_prepopulate_steps=replay_prepopulate_steps,
   batch_size=batch_size,
   exploration=exploration,
   gamma=gamma,
)
assert len(dqn_models) == num_saves
assert all(isinstance(value, DQN) for value in dqn models.values())
# saving computed models to disk, so that we can load and visualize them later.
checkpoint = {key: dqn.custom_dump() for key, dqn in dqn_models.items()}
torch.save(checkpoint, f'checkpoint_{env.spec.id}.pt')
```

```
0%| | 0/1500000 [00:00<?, ?it/s]
```

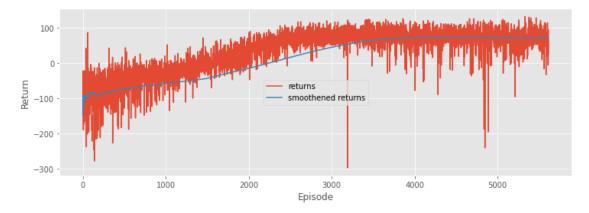
Plot the returns, lengths and losses obtained while running DQN on the lunarlander environment.

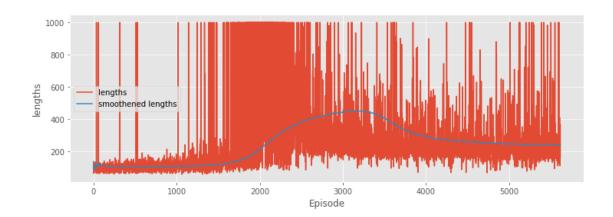
```
[18]: smooth_returns = rolling_average(returns, window_size=1500)
    episodes = range(len(returns))
    plt.plot(episodes, returns, label="returns")
    plt.plot(episodes, smooth_returns, label="smoothened returns")
    plt.xlabel('Episode')
    plt.ylabel('Return')
    plt.legend(loc='best')
    plt.show()

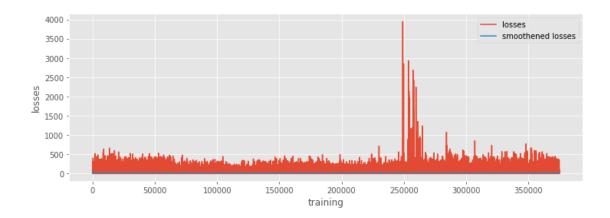
smooth_lengths = rolling_average(lengths, window_size=1500)
```

```
plt.plot(episodes, lengths, label="lengths")
plt.plot(episodes, smooth_lengths, label="smoothened lengths")
plt.xlabel('Episode')
plt.ylabel('lengths')
plt.legend(loc='best')
plt.show()

smooth_losses = rolling_average(losses, window_size=20_000)
training = range(len(losses))
plt.plot(training, losses, label="losses")
plt.plot(training, smooth_losses, label="smoothened losses")
plt.xlabel('training')
plt.ylabel('losses')
plt.legend(loc='best')
plt.show()
```







# 1.1.8 Visualization of the trained policies!

Run the cell below and push the buttons to view the progress of the policy trained using DQN.

```
[19]: buttons_all = []
      for key_env, env in envs.items():
              checkpoint = torch.load(f'checkpoint_{env.spec.id}.pt')
          except FileNotFoundError:
              pass
          else:
              buttons = []
              for key, value in checkpoint.items():
                  dqn = DQN.custom_load(value)
                  def make_callback(env, dqn):
                      def button_callback(button):
                          for b in buttons_all:
                              b.disabled = True
                          render(env, lambda state: dqn(torch.tensor(state,
       →dtype=torch.float)).argmax().item())
                          for b in buttons_all:
                              b.disabled = False
                      return button_callback
                  button = widgets.Button(description=f'{key.replace("_", ".")}%')
                  button.on_click(make_callback(env, dqn))
                  buttons.append(button)
```

### lunarlander:

```
HBox(children=(Button(description='00.0%', style=ButtonStyle()), Button(description='25.0%', style=ButtonStyle...
```

### 1.1.9 Q7 (2 pts): Analysis

For each environment, describe the progress of the training in terms of the behavior of the agent at each of the 5 phases of training (i.e. 0%, 25%, 50%, 75%, 100%). Make sure you view each phase a few times so that you can see all sorts of variations.

Say something for each phase (i.e. this exercise is worth 1 point for every phase of every environment). Start by describing the behavior at phase 0%, then, for each next phase, describe how it differs from the previous one, how it improves and/or how it becomes worse. At the final phase (100%), also describe the observed behavior in absolute terms, and whether it has achieved optimality.

#### **CartPole**

- 0%) The agent fails almost immediately by exceeding the angle limit.
- 25%) It is better than before but fails mainly by exceeding the distance limit.
- 50%) Length and returns are higher, suggesting improvement. The pole is oscillating a few times before failing.
- 75%) Not much improvement in the length of the episode or returns, although the agent has gotten better at balancing the pole. It fails in the first oscillation but is able to control the angular velocity of the pole better before failing due to distance limit.
- 100%) Seems to be a downgrade from the previous phase, Angular velocity control has worsened, yielding poorer rewards. The agent has not achieved optimal behavior; it is not capable of balancing the pole for the entire time frame.

## MountainCar

- 0%) The car cannot climb the hill, stuck in the valley.
- 25%) No visible improvement.
- 50%) Agent has learned to go back and use momentum to climb the hill.
- 75%) Reduced episode length with increased returns Agent is taking lesser oscillations/time to reach goal.
- 100%)Optimal behavior achieved, since not much change in behaviour since last phase.

### Acrobot

- 0%) The agent has no knowledge how to reach the mark.
- 25%) It is able to hit the mark most times.
- 50%) It reaches faster to the mark, when succeeds but is now more prone to failiure.
- 75%) Consistently hits the mark, huge improvement from previous phase.
- 100%) The Agent has learned to solve the evironment consistently within a good time frame, achieved optimal behavior.

#### LunarLander

- 0%) The agent cannot land, crashes on the land.
- 25%) The agent has learned to hover and control. It lands at a higher speed if it is at the center where the goal is; hovers around if at the sides.
- 50%) The agent lands successfully at least in the vicinity of the goal consistently.
- 75%) The agent lands again in the vicinty but much quicker this time. Also the agent is more prone to crashing the lander.
- 100%) Agent has achieved near optimal behavior. The lander lands consistently at the goal spot without crashes, no improvements can be done.