

25/04/2021

Engineering PhysicsTutorial - 6

1) $d_s = 0.30 \text{ cm}$
 $d_{15} = 0.62 \text{ cm}$
 $d_{25} = ?$

→ $D_n^2 = 4n\Delta R$

∴ $D_{15}^2 = 60\Delta R \quad \text{--- (1)}$

$D_s^2 = 20\Delta R \quad \text{--- (2)}$

(1) - (2) $40\Delta R = D_{15}^2 - D_s^2$

∴ $\Delta R = \frac{D_{15}^2 - D_s^2}{40} = \frac{(0.62)^2 - (0.3)^2}{40} \quad \text{--- (3)}$

$D_{25}^2 = 100\Delta R \quad \text{--- (4)}$

(4) - (2) = $80\Delta R = D_{25}^2 - D_s^2$

$2D_{15}^2 - 2D_s^2 = D_{25}^2 - D_s^2$

∴ $D_{25}^2 = 2D_{15}^2 - D_s^2$

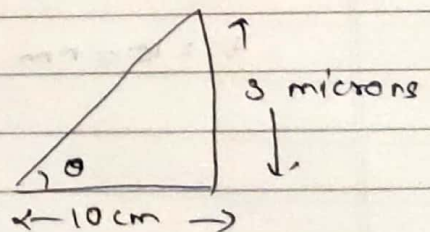
∴ $D_{25} = \sqrt{2 \times 0.62^2 - (0.3)^2} = \sqrt{0.6788} = 0.8238 \text{ cm}$

2) $\tan \theta \approx \theta = \frac{3 \times 10^{-6}}{10 \times 10^{-2}} = 3 \times 10^{-5} \text{ rad}$

∴ $\beta = \frac{\Delta}{2\mu\theta} = \frac{450 \times 10^{-9}}{2 \times 1 \times 3 \times 10^{-5}} = 75 \times 10^{-4}$

but $\beta = \frac{x}{n}$ where $x = 10 \text{ cm}$, $n = \text{number of fringes.}$

∴ $n = \frac{10 \times 10^{-2}}{75 \times 10^{-4}} \approx 13.33 \approx 13$



$$3) \quad \mu = \frac{\sin i}{\sin r}$$

$$r = \sin^{-1} \left(\frac{\sin i}{\mu} \right) = \sin^{-1} \left(\frac{\sin 30}{1.44} \right) = 20.32^\circ$$

$$\therefore \cos r = \cos(20.32^\circ) = 0.9378$$

For 5th dark band

$$2\mu t \cos r = 5\lambda$$

$$\therefore t = \frac{5 \times 5893 \times 10^{-10}}{2 \times 1.44 \times 0.9378} = 1.0884 \times 10^{-6} = 10884 \text{ \AA}$$

4) For destructive interference,

$$2\mu t \cos \theta = (2n+1) \frac{\lambda}{2}$$

$$\therefore n=0,$$

$$2(1.5)t = \frac{\lambda}{2}$$

$$t = \frac{600 \times 10^{-9}}{6}$$

$$t = 100 \text{ nm}$$

$$2\mu t = n\lambda$$

$$t = \frac{n\lambda}{2\mu} = \frac{6 \times 10^{-7}}{2 \times 10^{-3}}$$

$$t = 2 \times 10^{-7} = 200 \text{ nm}$$

6) $i = 35^\circ$, $t = 3000 \text{ \AA}$, $\mu = 1.33$

$$\mu = \frac{\sin i}{\sin r}$$

$$r = \sin^{-1} \left(\frac{\sin i}{\mu} \right) = 25.48^\circ$$

$$\therefore \cos r = \cos(25.48) = 0.9$$

Now, for minima,

$$2ut \cos r = n\lambda$$

$$\therefore \lambda = \frac{2 \times 1.33 \times 5 \times 10^{-7} \times 0.9}{n}$$

$$\lambda = \frac{12000}{n} \text{ \AA}$$

$$\therefore \lambda_1 = 12000 \text{ \AA}, \lambda_2 = 6000 \text{ \AA}, \lambda_3 = 4000 \text{ \AA}$$

7) $d_{10} = 2 \text{ mm}$, $n = 10$, $d = 500 \text{ nm}$

$$d n^2 = 4 n d R$$

$$R = \frac{d^2 n}{4 n d} = \frac{4 \times 10^{-6}}{4 \times 10 \times 500 \times 10^{-9}} = 0.2$$

$$2t = \frac{d^2 n}{4R}$$

$$2t = \frac{4 \times 10^{-6}}{4 \times 0.2}$$

$$t = 2.5 \times 10^{-6} \text{ m} = 2.5 \text{ \mu m}$$