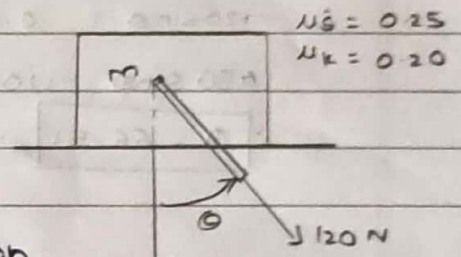


03/05/21

Engineering mechanics

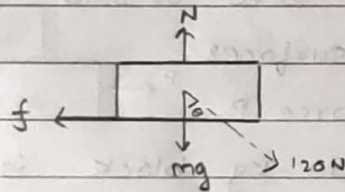
## Assignment 3 : Friction

3.2) Considering only values of  $\theta$  less than  $90^\circ$ , determine the smallest value of  $\theta$  for which motion of the block to the right is impending when a)  $m = 30 \text{ kg}$ , b)  $m = 40 \text{ kg}$ .



→ Considering the FBD of block,

Let  $f$  be the frictional force acting on block.



$$\sum F_y = 0$$

$$N - mg - 120 \cos \theta = 0$$

$$\therefore N = mg + 120 \cos \theta$$

$$N = 30 \times 9.81 + 120 \cos \theta$$

$$N = 294.3 + 120 \cos \theta \quad \text{--- (1)}$$

$$\sum F_x = 0$$

$$-f + 120 \sin \theta = 0 \quad \text{--- (2)}$$

$$f = f_{\max} = \mu_s N = 0.25 N$$

$$\therefore f = 0.25 (294.3 + 120 \cos \theta)$$

$$120 \sin \theta = 0.25 (294.3 + 120 \cos \theta)$$

$$480 \sin \theta - 120 \cos \theta = 294.3$$

$$\therefore \boxed{\theta = 50.54^\circ} \quad \dots \text{ [when } m = 30 \text{ kg]}$$

b)  $m = 40 \text{ kg}$

$$\therefore N = 392.4 + 120 \cos \theta$$

$$f = \mu_s N = 0.25 N = 0.25 (392.4 + 120 \cos \theta)$$

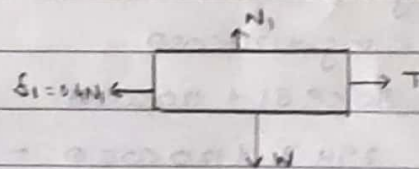
$$\therefore 120 \sin \theta = 0.25 (392.4 + 120 \cos \theta)$$

$$480 \sin \theta - 120 \cos \theta = 392.4$$

$$\therefore \boxed{\theta = 66.51^\circ} \dots [\text{when } m = 40 \text{ kg}]$$

3.5) The coefficients of friction are  $\mu_s = 0.40$  and  $\mu_k = 0.30$  between all surfaces of contact. Determine the force  $P$  for which motion of the 30-kg block is impending if cable AB, a) is attached as shown, (b) is removed.

a) FBD of 20 kg block,



$$\sum F_y = 0$$

$$\therefore W = N_1$$

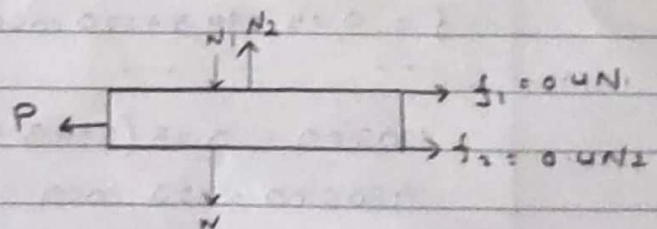
$$\therefore N_1 = 20 \times 9.81 = 196.2 \text{ N}$$

$$\therefore \sum F_x = 0 \quad f_1 = 0.4 N_1$$

$$\therefore T = f_1 = 0.4 \times 196.2$$

$$f_1 = 78.48 \text{ N}$$

FBD of 30 kg block,



$$\sum F_y = 0$$

$$W + N_1 = N_2$$

$$\therefore N_2 = 294.3 + 196.2 = 490.5 \text{ N}$$



$$\therefore f_2 = 0.4 \times N_2 = 0.4 \times 490.5 = 196.2 \text{ N}$$

$$\sum F_x = 0$$

$$P = f_1 + f_2$$

$$= 78.48 + 196.2$$

$$\therefore P = 274.68 \text{ N}$$

Force  $P$  for which motion of 30 kg block is impending when string AB attached is 274.68 N

b) String AB is removed.

$$\sum F_y = 0$$

$$N = W = (20 + 30) \times 9.81$$

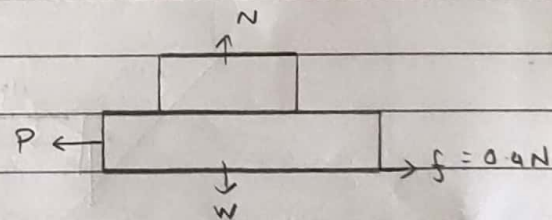
$$\therefore N = 490.5 \text{ N}$$

$$\sum F_x = 0$$

$$P = f$$

$$= 0.4 \times 490.5$$

$$P = 196.2 \text{ N}$$



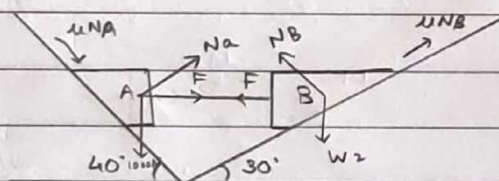
$P$  for which motion of 30 kg block is impending when string AB is removed is 196.2 N

- 3.7) Two blocks weighing  $w_1$  and  $w_2$  are resting on two inclined planes as shown. If  $w_1 = 1000\text{N}$ , determine the minimum and maximum value of  $w_2$  for which equilibrium can exist.

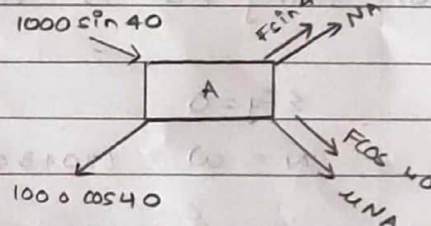
Friction angle  $= 20^\circ$  $w_1 = 1000\text{N}$  $w_2$  $40^\circ$   $30^\circ$ 

→  $\theta = 20^\circ$ ,  $\mu = \tan \theta = \tan 20^\circ$

Case 1:  $w_2 > w_1$  (for  $w_{\text{max}}$ )



FBD of block A



$$\sum F_y = 0$$

$$1000 \cos 40 - F \sin 40 = N_A \quad (1)$$

$$\sum F_x = 0$$

$$1000 \sin 40 + F \cos 40 + \mu N_A = 0 \quad (2)$$

From eq (1) and (2)

$$F_{AB} = -1732.16\text{N} = 1732.16\text{N} (\leftarrow)$$

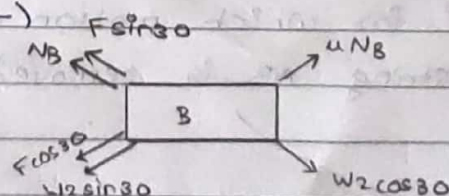
Now, FBD of B,

$$\sum F_y = 0$$

$$N_B = w_2 \cos 30 - F \sin 30 \quad (3)$$

$$\sum F_x = 0$$

$$\mu N_B = F \cos 30 + w_2 \sin 30 \quad (4)$$



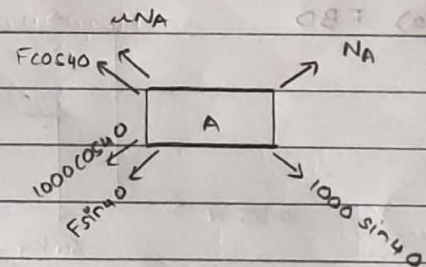
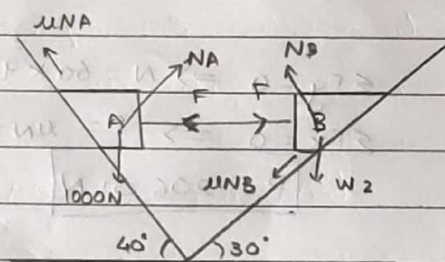


Solving eq. (3) and (4)

$$N_B = 7642.687 \text{ N}$$

$$\therefore W_2(\text{max}) = 9825.078 \text{ N}$$

Case 2:  $W_2 < W_1$  [for  $W_2(\text{min})$ ]



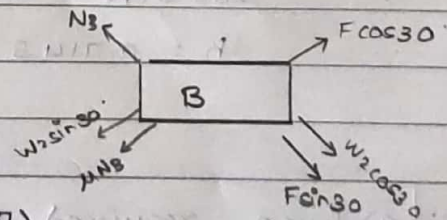
$$\sum F_y = 0 \Rightarrow N_A = 1000 \cos 40 + F \sin 40 \quad (5)$$

$$\sum F_x = 0 \Rightarrow \mu N_A = 1000 \sin 40 - F \cos 40 \quad (6)$$

Solving eq. (5) and (6)

$$F = 363.94 \text{ N}$$

Now, FBD of block B.



$$\sum F_y = 0 \Rightarrow N_B = W_2 \cos 30 + F \sin 30 \quad (7)$$

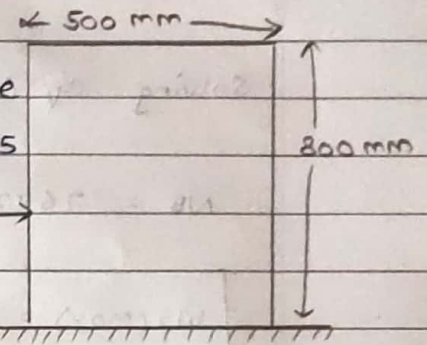
$$\sum F_x = 0 \Rightarrow \mu N_B + W_2 \sin 30 = F \cos 30 \quad (8)$$

Solving (eq.), 7 and 8,

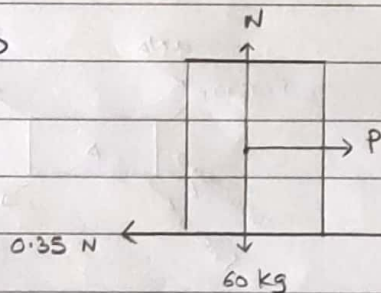
$$W_{\min} = 305.36 \text{ N}$$

$\therefore$  The max and min value of  $W_2$  for which equilibrium can exist is  $9825.078 \text{ N}$  and  $305.36 \text{ N}$  respectively.

- 3.12) A 60 kg cupboard is to be shifted to the right, as between cupboard and floor is 0.35 as shown in figure. Determine
- a) The force required to move the cupboard and b) The largest allowable value of  $h$  if the cupboard is not to tip over.



→ a) FBD



$$\sum F_y = 0 \Rightarrow N = 60 \times 9.81$$

$$\sum F_x = 0 \Rightarrow P = \mu N = 0.35 \times 60 \times 9.81$$

$$\therefore P = 206.01 \text{ N}$$

b) To tip over,  $\sum M_B = 0$

$$\therefore -(60 \times 9.81 \times 0.25) + (P \times h) = 0$$

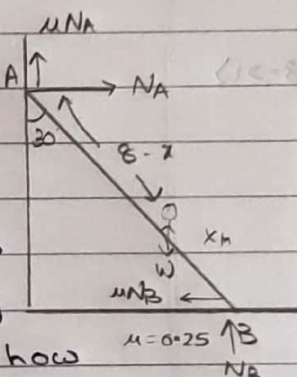
$$\therefore 206.01 \text{ N} = 147.15$$

$$\therefore h = 0.7143 \text{ m} = 714.3 \text{ mm}$$

- $\therefore$  a) force required to move the cupboard is 206 N  
 b) largest allowable value of 'h' is 714.3 mm.



3.15) A weightless ladder of length 8 m is resting against a wall and floor. A man of weight 500 N wants to climb up the ladder. Determine a) how much distance can he climb without slipping. b) If another man weighing 800 N wants to climb up the same ladder, how much the distance he can walk along the ladder without slipping?



Ans. a)  $\sum F_y = 0 \Rightarrow uN_A + N_B = 500 \text{ N} \quad \text{--- (1)}$

$\sum F_x = 0 \Rightarrow N_A = uN_B \quad \text{--- (2)}$

Solving eq. (1) and (2), we have:

$N_A = 117.64 \text{ N}, \quad N_B = 470.59 \text{ N}$

then  $\sum M_B = 0$

$500(x \sin 30) - N_A(8 \cos 30) - uN_A(8 \sin 30) = 0$

$x = 3.73 \text{ m}$

$\therefore$  The man can climb upto a distance of 3.73 m up the ladder without slipping.

b)  $\sum F_x = 0 \Rightarrow N_A = uN_B \quad \text{--- (3)}$

$\sum F_y = 0 \Rightarrow uN_A + N_B = 800 \quad \text{--- (4)}$

Solving eq. (3) and (4) we get

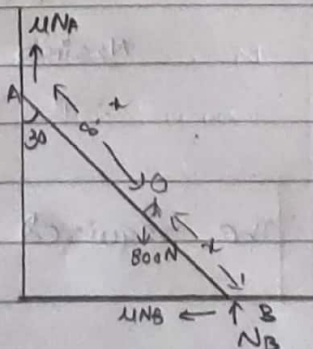
$N_A = 188.235 \text{ N}, \quad N_B = 752.941 \text{ N}$

Now,  $\sum M_B = 0$

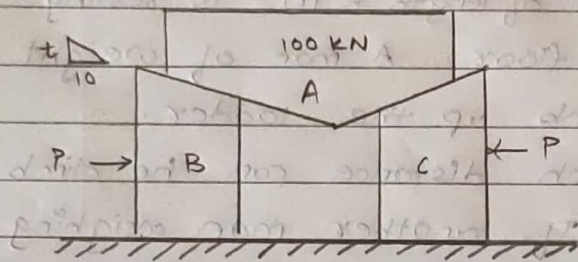
$800(x \sin 30) - uN_A(8 \sin 30) - N_A(8 \cos 30) = 0$

$\therefore x = 3.73 \text{ m}$

$\therefore$  A man weigh 800 N can climb upto 3.73 m without slipping.



3.21)



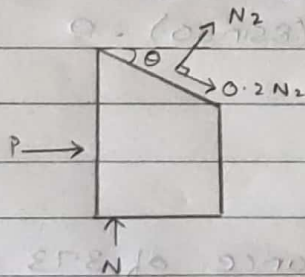
$$\text{Slope } 1:10 \Rightarrow \tan \theta = \frac{1}{10}$$

$$\therefore \theta = \tan^{-1}\left(\frac{1}{10}\right) = 5.71^\circ$$

$$\sum F_y = 0 \Rightarrow 2N = 100$$

$$\therefore N = 50 \text{ kN}$$

Isolating wedge B as shown,



$$\sum F_y = 0$$

$$\therefore 50 + N_2 \cos \theta - 0.2 N_2 \sin \theta = 0$$

$$\therefore N_2 = -51.27 \text{ kN}$$

$$\sum F_x = 0$$

$$N_2 \sin \theta + P + 0.2 N_2 \cos \theta - 0.25 \times 50 = 0$$

$$\therefore P = 27.80 \text{ kN}$$

$\therefore$  The required magnitude of horizontal force P is 27.80 kN