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AI1103-Assignment 2

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Download all python codes from

https://github.com/ayushjha2612/AI11003/tree/main/Assignment2/Codes

and latex-tikz codes from

https://github.com/ayushjha2612/AI11003/tree/main/Assignment2

PROBLEM 5.27

Find the probability distribution of number of doublets in three throws of a pair of dice?

Solution

Let $X_1, X_2 \in \{1, 2, 3, 4, 5, 6\}$ represent the two dice. We have,

$$\Pr(X_1 = X_2) = \frac{1}{6} \tag{0.0.1}$$

Similarly we have,

$$\Pr(X_1 \neq X_2) = \frac{5}{6} \tag{0.0.2}$$

Let the number of doublets in three throws of a pair of dice be represented by a random variable, *X* When a pair of dice is thrown three times the number of doublets can be 0,1,2 and 3 respectively. So X can take these values

$$Pr(X = 0) = Pr(X_1 \neq X_2)^3$$
 (0.0.3)

$$=\frac{125}{216}\tag{0.0.4}$$

Similarly we have,

$$Pr(X = 1) = 3 \times Pr(X_1 \neq X_2)^2 \times Pr(X_1 = X_2)$$
(0.0.5)

$$=\frac{75}{216}\tag{0.0.6}$$

Note: 3 is multiplied as we have to select which dice will have doublet

$$Pr(X = 2) = 3 \times Pr(X_1 \neq X_2) \times Pr(X_1 = X_2)^2$$

(0.0.7)

$$=\frac{15}{216}\tag{0.0.8}$$

And lastly,

$$Pr(X = 2) = Pr(X_1 = X_2)^3$$
 (0.0.9)
= $\frac{1}{216}$ (0.0.10)

The probability distribution of number of doublets in three throws of a pair of dice can be found out at figure 0. The corresponding table can be found at table 0

No. of Doublets	Probability
0	$\frac{125}{216}$
1	$\frac{75}{216}$
2	$\frac{15}{216}$
3	$\frac{1}{216}$

TABLE 0: Probability of doublets

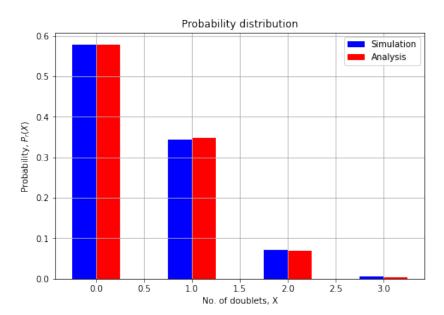


Fig. 0: Probability distribution