

## Assignment 2

200020038

To use gauss elimination method to solve system of linear equations.

### Assignment - 2

Cross Elimination method.

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & \dots & a_{1n} \\ a_{21} & & & & \\ a_{31} & & & & \\ \vdots & & & & \\ a_{n1} & & & & a_{nn} \end{bmatrix}$$

Cross Elimination Algorithm Applied.

~~Pivoting~~

for  $i = \del{1:n-1}$  {

Pivoting {

~~for~~ for  $j = i+1 : n$

If  ~~$|a_{ji}| > |a_{ii}|$~~   $|a_{ji}| > |a_{ii}|$

Then Replace  $i$ th &  $j$ th row.

~~Set~~ & Do corresponding change in  $b$  }

Row subtraction

for  $j = i+1 : n$  {  
 $\text{factor} = A(j, i) / A(i, i)$

Row  $j \leftarrow \text{factor} \times \text{Row } i$

do corresponding ~~with~~  $\}$

return  $A \& b$

Back Substitution.

$$\begin{bmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ 0 & a_{22} & \dots & a_{2n} \\ 0 & 0 & \dots & \vdots \\ 0 & 0 & \dots & \vdots \\ \vdots & \vdots & \dots & \vdots \\ 0 & 0 & \dots & \vdots \\ 0 & 0 & \dots & a_{nn} \end{bmatrix}$$

Let  $n \times 1$  array  $x$

for  $i = 1 : n$   $\Rightarrow b(i) = - \sum_{j=1}^{n+1-i} a_{n+1-i, n-j} x(n-j)$   
 $\{ \text{val} = b(n+1, i) \}$

while  $j > 1$

$\{ \text{val} = \text{val} - A(n+1-i, n+2-j) x(n+2-j) \}$   
 $j = j - 1$

$\text{val} = \text{val} / A(n+1-i, n+1-i)$



$$x(n+1-i) = \text{val}$$

return x

// here x is solution.

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```
1 A = load('A.txt');
2 b = ones(1,15);
3 b = b.*40;
4 x = GEM(A,b);
5 plot(x);
6
7
8
```

Workspace

Name	Value
A	15x15 double
b	1x15 double
x	1x15 double

Command Window

```
>> main
No. of operations in Gauss elimination
2345

No. of operations in back-substitution
225

fx >>
```

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```

1 function x = GEM(A,b)
2 [m n] = size(A);
3 counter = 0;
4 for i = 1:m-1
5     var = A(i,1);
6     for j = i+1:m
7         if abs(A(j,1)) > abs(var)
8             temp = A(i,1);
9             A(i,:) = A(j,:);
10            A(j,:) = temp;
11            temp1 = b(i);
12            b(i) = b(j);
13            b(j) = temp1;
14            b(j) = temp1;
15            var = A(i,1);
16        end
17    end
18    for j = i+1:m
19        factor = A(j,i)/A(i,i);
20        counter = counter + 1;
21        A(j,:) = A(j,:) - factor*A(i,:);
22        counter = counter + n+1-j + n - 1;
23        b(j) = b(j) - factor*b(i);
24        counter = counter + 2;
25    end
26 end
27
28 disp("No. of operations in Gauss elimination");
29 disp(counter);
30

```

Workspace

Name	Value
A	15x15 double
b	1x15 double
x	1x15 double

Command Window

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```

19 factor = A(j,i)/A(i,i);
20 counter = counter + 1;
21 A(j,:) = A(j,:) - factor*A(i,:);
22 counter = counter + n+1-j + n - 1;
23 b(j) = b(j) - factor*b(i);
24 counter = counter + 2;
25 end
26
27 disp("No. of operations in Gauss elimination");
28 disp(counter);
29
30 x = BackSubstitution(A,b);
31
32 return
33 end
34
35
36

```

Workspace

Name	Value
A	15x15 double
b	1x15 double
x	1x15 double

Command Window

fx >> |

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FILE NAVIGATE EDIT BREAKPOINTS RUN

Current Folder: D:\matlab

Editor - D:\matlab\BackSubstitution.m

```

1 function result = BackSubstitution(A,b)
2 [n] = size(A);
3 x = 1:n;
4 counter = 0;
5 for i = 1:n
6     val = b(n+1-i);
7     j = i;
8     while j>1
9         val = val - A(n+1-i,n+2-j)*x(n+2-j);
10        counter = counter + 2;
11        j = j-1;
12    end
13    val = val / A(n+1-i,n+1-i);
14    counter = counter + 1;
15    x(n+1-i)=val;
16 end
17 disp("No. of operations in back-substitution");
18 disp(counter);
19 result = x;
20 return
21 end
22
23

```

Workspace

Name	Value
A	15x15 double
b	1x15 double
x	1x15 double

Command Window

No. of operations in back-substitution  
225

UTF-8 BackSubstitution Ln 6 Col 20

