

2000 2003P

## Lagrange Interpolation

Method:

$$y = \frac{y_1 (x_2 - x_3) \dots (x_n - x_{n-1})}{(x_1 - x_2) (x_1 - x_3) \dots (x_1 - x_n)} + \dots + \frac{y_n (x_1 - x_2) \dots (x_{n-1} - x_{n-2})}{(x_n - x_1) (x_n - x_2) \dots (x_n - x_{n-1})}$$

main.m  
Take input data  
x & y

Lagrange IP  
for each x  
Calculate value,  
using above  
function

main.m  
Return values

## # Cubic Spline method.

Method

Given  $n$  points ~~on~~

Assume  $n-1$  cubic equations

$$a_i x^3 + b_i x^2 + c_i x + d_i$$

~~Assume~~ ~~first~~ equation in first

$$\text{Total of } 4 \times (n-1) = 4n - 4 \text{ unknowns.}$$

Equations used to solve.

for each interval equation satisfying values.

$$f_i(x_i) = y_i$$

$$f_i(x_{i+1}) = y_{i+1}$$

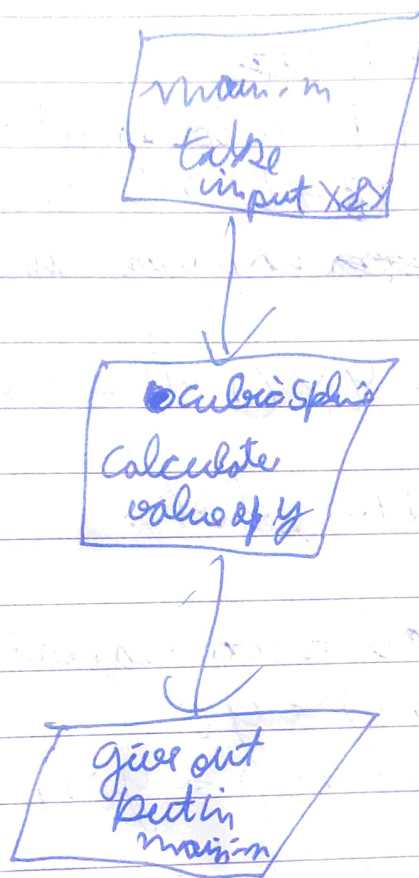
By this  $2n-2$  equations generated.

By equating derivatives we get  $n-2$

By equating second derivatives we get  $n-2$  eq.

If we assume first interval to be linear.  
we get 2 equation.  
so total of  $4n-4$  eq<sup>n</sup>.

# Flowchart



$x$

Lagrange IP  
y01

0.5

1.5

2.5

3.5

4.5

5.5

6.5

7.5

8.5

9.5

0.2351

0.6881

0.8629

0.9242

0.9531

0.9679

0.9770

0.9823

0.9872

0.9894

Cubic spline

0.2351

0.6881

0.8629

0.9242

0.9531