

① Find the middle by slow fast approach  
↳ add a corner case if (fast == null) { even case }

↳ Prev will be one node before slow.

② Right Head = mid.next  
mid.next = null;

M. sort (head) Left half ]  
M. sort (right Head) Right half ] sorting

③ Merging

④ Make temp Linked List

temp → head [ dummy node ]  
temp.data = -1

if (Left.data < Right.data) {  
temp.add(Left.data); }

else {  
temp.add(Right.head.data); }

if elements are remaining add all them.

↳ in final list remove first the dummy node

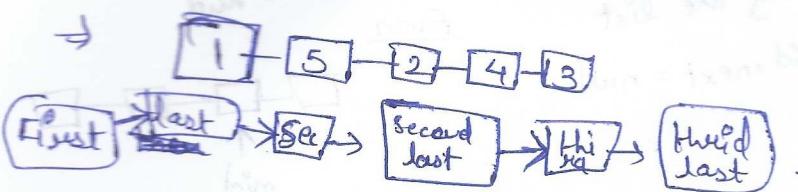
# # Zig Zag Linked List

→ We have given a Linked List

$$L(1) \rightarrow L(2) \rightarrow L(3) \rightarrow L(4) \rightarrow L(5) \rightarrow L(6) \rightarrow L(7)$$

We need to convert it in zigzag form

Example - 



## Approach

① find mid Node ( $mid = 1^{st} \text{ half last node}$ )

(slow → fast approach)

② Reverse second half

③ divide the both L.L

(Because it's hard to travel backwards in L.L)

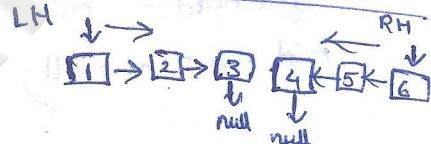
④ Alternate merging

↳ Node LH = 1st half head  
(left head)

Node RH = 2nd half head  
(right head)

Node NextL, NextR  
(next left, next right)

while ( $LH \neq \text{null}$  &  $RH \neq \text{null}$ ) {

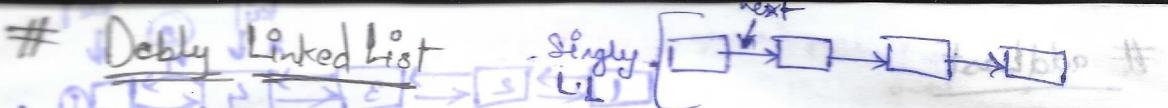


Zigzag

{  
    next L = LH.next  
    LH.next = RM  
    next R = RH.next  
    RH.next = next L

update {  
    RM = nextR  
    LH = nextL

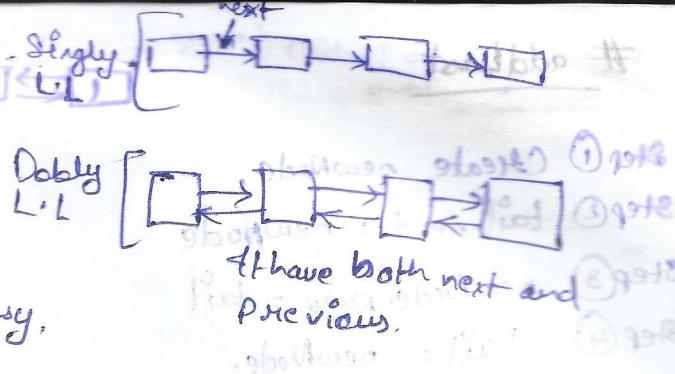
}



↳ It have both next and prev.

↳ Therefore travelling

backward in this is more easy.



Code →

Class DoubleLL {

    Class Node {

        int data;

        Node next;

        Node prev;

    } public Node (int data) {

        Constructor

            this.data = data;

            this.next = null;

            this.prev = null; }

    public static Node head;

    public static Node tail;

    public static int size;

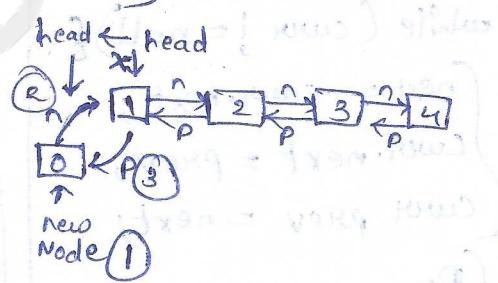
## # Add First

Step 1) Create node;

Step 2) newNode.next = head;

Step 3) head.prev = newNode;

Step 4) head = newNode;



## Corner Cases

if (head == null) {  
    head = tail = newNode;  
    return; }

## # Remove First

Step 1) Case 1: head = head.next;

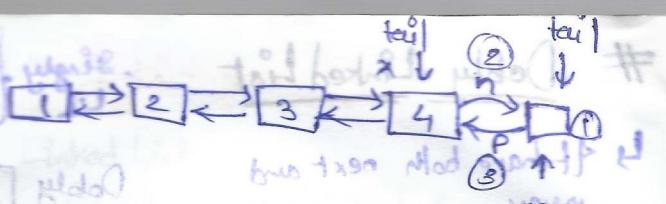
Step 2) head.prev = null;

Step 3) size--;

please take a look at this part \*

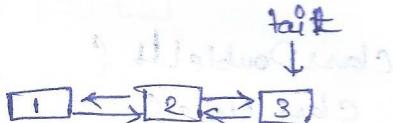
## # addLast

- Step ① Create newNode.  
 Step ② tail.next = newNode  
 Step ③ newNode.prev = tail  
 Step ④ tail = newNode.



## # RemoveLast

- Node temp = tail;  
 Step ① tail = tail.prev;  
 Step ② tail.next = null;  
 return temp.data;



## # Reverse a Doubly LL.

2 Node curr = head;  
 Node prev = null;  
 Node next;

```
while (curr != null) {
    next = curr.next;
    curr.next = prev;
    curr.prev = next;
    update {
        prev = curr;
        curr = next
    }
}
```

here just link the head with tail and tail with head

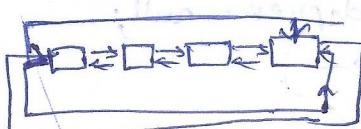
example → head.prev = tail;  
 tail.next = head;

## # Circular Linked List

Circular Doubly Linked List



Circular Doubly Linked List

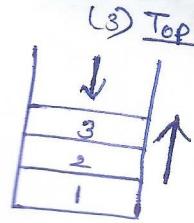


- Doubly list is asked rarely.



# Stacks →   
 Explicit (made by us)   
 implicit (made by computers automatically)

- Operations
    - ① Push  $O(1)$
    - ② Pop  $O(1)$
    - ③ Peek  $O(1)$
- Every operation  
for only top element



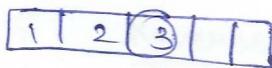
(LIFO)

Last In First Out

## Implementation -

Arrays

fixed size



- Stack == full

As array is of fixed size there we does not prefer this for Stack.

# Stack → using ArrayList.

ArrayList

variable size



last element = top

LinkedList

variable size



Head = Top

here head is top because head is the only element on which we can perform the tasks with  $O(1)$  time complexity.

Push → To add element

```
public static void push(int data)
{
    list.add(data);
}
```

Pop → To remove

```
public static int pop()
{
    if list is empty
        if (isEmpty())
            return -1;
        int top = list.get(list.size() - 1);
        list.remove(list.get() - 1);
        return top;
}
```

Peek

```
public static int peek()
{
    if the list is empty
        if (isEmpty())
            return -1;
        return list.get(list.size() - 1);
}
```

IsEmpty

```
→ public static boolean isEmpty()
{
    return list.size() == 0;
}
```

## # Stack → Using Linked list

↳ Here top is considered as head.

1) IsEmpty → to check whether the L.L is empty or not.

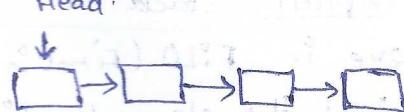
```
→ public static boolean isEmpty () {  
    return head == null ;  
}
```

2) push

↳ As the top is head always

so we would use add-

-First function.



3) pop

```
if (isEmpty ()) {  
    return -1 ;  
}
```

```
int top = head.data
```

```
head = head.next;
```

```
return top;
```

4) peek

```
if (isEmpty ()) {  
    return -1 ;  
}  
return head.data;
```

## # Stack using ICF

Just ~~forget~~ write

```
import java.util.*;
```

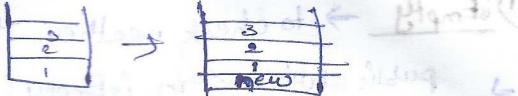
Without Functions Stack < Integer > s = new Stack <>();

① s.push();

② s.pop();

③ s.peek();

④ s.isEmpty();

~~Push~~ at the bottom of the stack 

→ we will solve with recursion

→ In recursion there have implicit stack in which there is FILO (First in last out) it will hold the elements till we push the desired element at the base and then we will add the elements one by one. by our stack.

## # Reverse a String using stack

↳ Most easiest thing to do in stack is this

- ① Just add the elements.
- ② And then print the elements
- ③ Due to LIFO, stack will be automatically reversed.

Approach

- ① push all elements
- ② peek - pop.

## # Reverse a Stack → We are told to make a stack that is Reversed flat of original.

→ example Input

3
2
1

Output

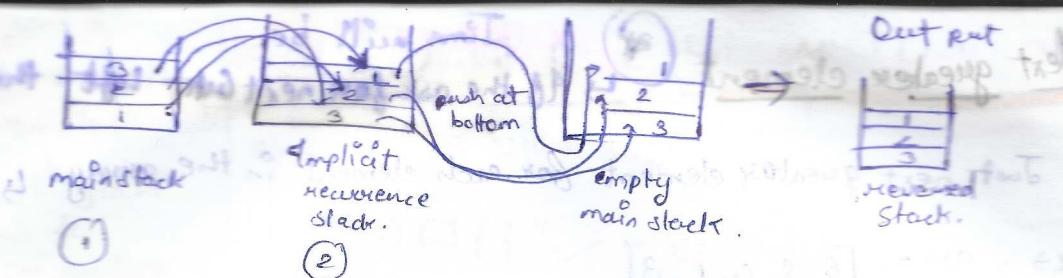
1
2
3

→ By brute force approach then we will need extra memory so to save memory and time we will use recursion

Approach

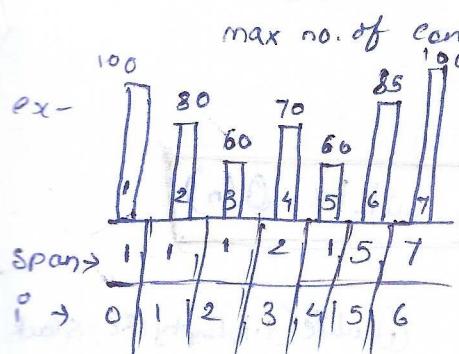
Step ① add all the elements in recursion stack  
base case → until our stack become empty.

Step ② backtrack all the element in the main stack but use push at bottom So the stack will be empty.



## Q# Stock span problem

$i = \text{index}$



max no. of consecutive days for which  $\text{price} \leq \text{today's price}$   
including the day itself

$\therefore$  For this we derive a formula  
 $\text{Span} = i - \text{prevHigh}(i)$

Ex- for day 4

$$\Rightarrow 3 - 1 = 2$$

but this take so much time  
 $O(n^2)$

Now [optimized sol] using Stack  $\leftarrow$  our stack will store the indexes of the stock price

$\hookrightarrow$  we will make an stack which store the value of a stock

$\hookrightarrow$  If the current stock price is ~~great~~ smaller than previous stock price store the value of stock in the Stack.

$\hookrightarrow$  And in array stores  $\left[ \begin{array}{c} \text{Index of} \\ \text{current} \end{array} \right] - \left[ \begin{array}{c} \text{Index of} \\ \text{Prev high} \end{array} \right]$

but if the curr stock price is greater then prev stock price remove the prev from stack and check again until find a stock price that is greater.

$\hookrightarrow$  If found the the greater price stock

and if not and the stack became empty then

store in array  $\rightarrow \left[ \begin{array}{c} \text{Index of} \\ \text{curr} \end{array} + 1 \right]$

## #1 Next greater element

Time will be

If the ask for next Gt. Left the method

Just next greater element for each element in the array.

Ex- arr = [6, 8, 0, 1, 3]

next Greater = [8, -1, 1, 3, -1]

If found no greater element then -1 or if no element after that then also -1.

### Brute Force

↳ Nested Loop

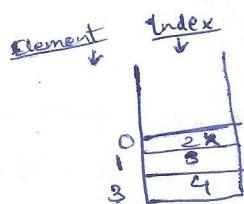
Time will be  $O(n^2)$

• For Optimised with Stack ↗

[arr] = [6, 8, 0, 1, 3]

next Greater = [8, -1, 1, 3, -1]

→ here we check from backwards.



→ for 3

stack is empty ∴ -1

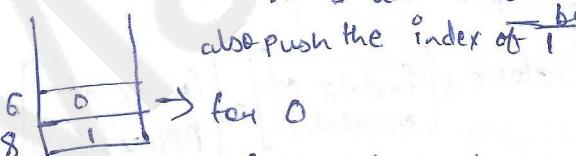
→ and also push the index of 3 in stack

for 1

6 is greater

∴ 3 add in this

also push the index of 1 but add backwards



→ for 0

1 is greater and next

∴ 1

push i of 0

→ For 8.

0 is smaller ∴ pop

1 is small ∴ pop

3 is small ∴ pop

New empty ∴ -1

push index of 8

For 6, 8 is next greater

and further element will be greater because

8 has popped them all out who were smaller than him

∴ 8 add in next greater  
push index of 6

Done return next greater array.

① while(s.isEmpty & stack

s.pop()

② if stack.empty

nextGreater = -1

else

nextGreater = s.peak()

③ s.push(element)



## # Valid Parentheses

(date)

thought

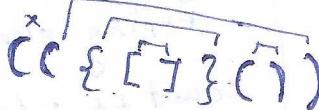
then about loop  
from 0 to n  
they can ask for  
next smaller left or right

Ex - String will be given

$$s = " () [ ] \{ \} " \quad s = "[ ] " x$$

$$s = " () " \quad s = "[ ( \{ \} ) ] " \checkmark$$

- ① Opening will be first and each opening will have its own closing.

Ex - 

$\Rightarrow$  ① Opening bracket

s.push();

② Closing bracket

↳ check does its pair present at top

if not return False;

↳ if yes s.pop() and continue;

③ At last check if the string is empty or not

if empty  $\rightarrow$  return True;

if not  $\rightarrow$  return False;

## # Duplicate Parenthesis

↳ we have given an string

$((a+b)+(c+d))$  ✓ this does not contain any duplicate parenthesis.

$(( (a+b)+(c+d) ))$  ✗ this contains a duplicate parenthesis.

$((a)+(b))$  ✓

\* logic

$\rightarrow$  If there is no information bet' these parenthesis then it is duplicate. means they are of no use.

## Approach (stack)

if ~~count < 1~~ means no other data bet' parenthesis b means duplicate. if ~~count > 1~~ continue.

Code for this

```
→ int count = 0
while (s.peek() == '(') {
    s.pop()
    count++
}
```

[count < 1 → duplicate] else (c)

```
s.pop() ← c
```

① if found and

opening bracket ~~operator~~ ~~else a mark~~  
operator (+, -, \*, %)  
or (a, b, c)

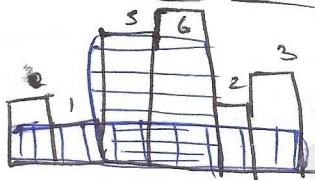
Push ( );

② if found closing

int count = 0;  
try to find is closing by  
popping elements.

count++; for the no. of  
elements popped.

## # Max Area in Histogram



maximum area in rectangle

it can be any rectangle

Or area = height × width.

② height → this will be the height of bar

③ width → For this

Next Smaller Left

Next Smaller Right

$$\text{width} = j - i - 1$$

For these we will use  
the concepts used in next greater

two arrays  
of nsl (next smaller left)

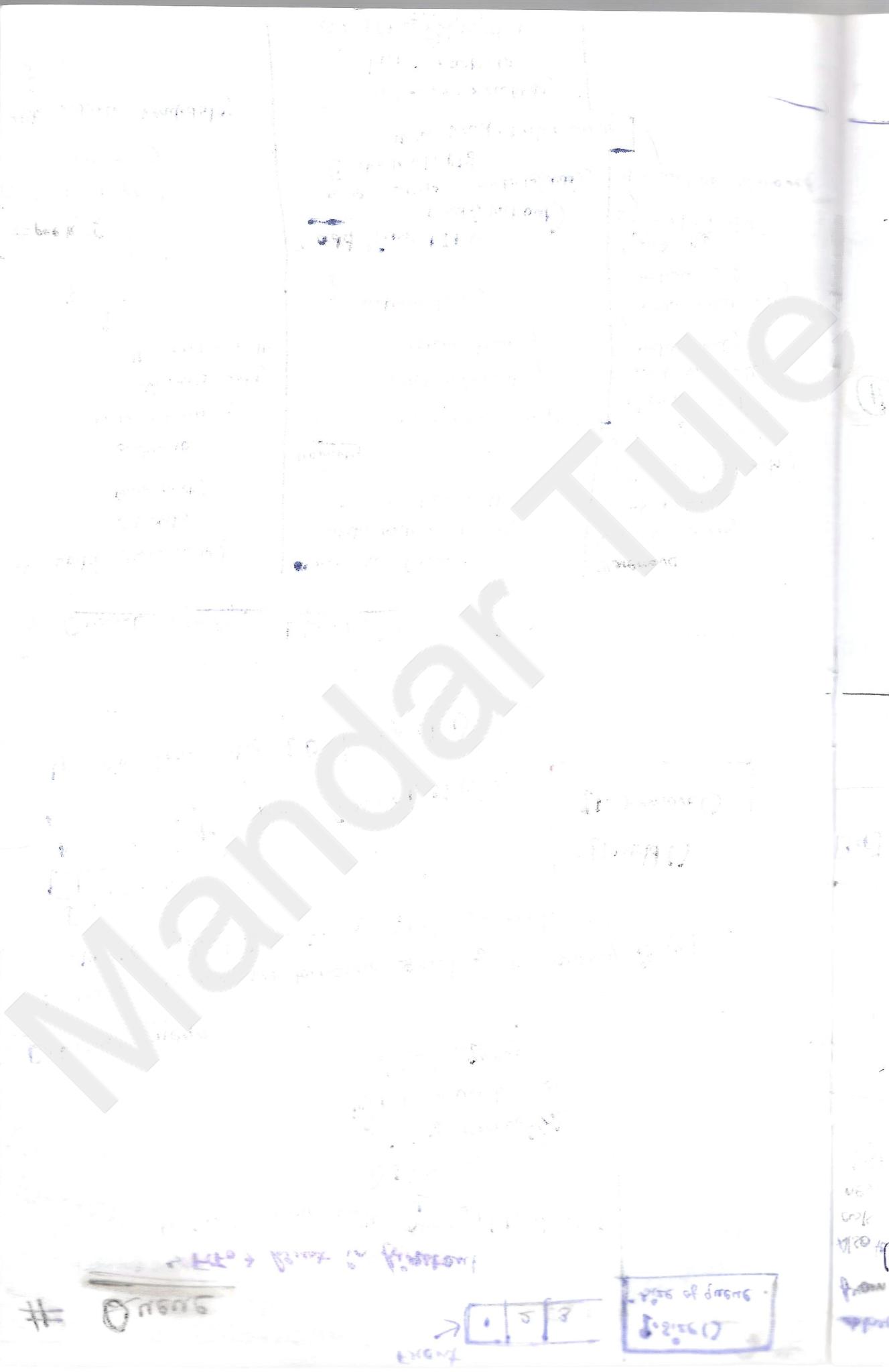
[-1 -1 1 5 1 2 0]

width of bar between two smaller bar.

④ then we will calculate the max area

nsl (next smaller right) \* when no smaller left put -1

nsr (j) \* when no smaller right put n



# # Queue

Front



q.size()

= size of queue.

↳ FIFO → first in first out

↳ Can be made with array, L.L, Stack?

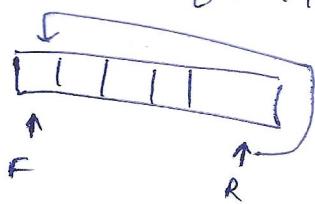
i) fixed size

ii) T.C of remove( $O(n)$ )

iii) But we use this for circular queue.

## Circular queue

↳ Here as we get towards end of the array it get to the first index by a special formula.



$$\text{Rear} = (\text{Rear} + 1) \% \text{size}$$

↳ So here the T.C is  ~~$O(n)$~~   $O(1)$ .

q1.add()

q1.remove()

# # Queue using Linked List

```
→ static class Node {
    int data;
    Node next;
}

// constructor
Node (int data) {
    this.data = data;
    this.next = null;
}
```

## # peek &

```
(1) Check isEmpty()
    → return -1;

else
    return head.data;
```

```
static class Queue {
    static Node head=null;
    static Node tail=null;
```

## //empty

```
public static boolean isEmpty () {
    if (head==tail==null)
        return true;
    else
        return false;
}
```

## //add (use FIFO)

FIFO in last out

Node newNode = new Node(data);

(1) check isEmpty

then head=tail=newNode

(2) tail.next = newNode;

tail = newNode

(3)

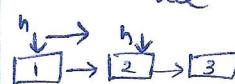
## //remove

(1) check isEmpty
 → return -1;

(2) int val = head.data;

(3) if single element
 if (tail==head) {
 head=tail=null;
 return val;
 }

(4) head = head.next;
 return val



This will be removed

## # Queue using JCV

```
→ import java.util.*;
```

```
public class Queue {
    }
```

```
    public static void main (String args[]) {
        }
```

functions

- ① add
- ② remove
- ③ isEmpty
- ④ peek

→ Queue is not written here because  
Queue is not class. (Answer)

→ Queue is a interface so we cannot make a  
class of queue.

we can use → `LinkedList<>()`

or → `ArrayDeque<>()`

`Queue<Integer> q = new LinkedList<>()`

- ① add
- ② remove
- ③ isEmpty
- ④ peek

## # Queue using Two Stacks

by keeping ↓

`push O(n)` or `pop O(n)`

```
static class Queue {
    static Stack<Integer> s1 = new Stack<>()();
    static Stack<Integer> s2 = new Stack<>()();
}
```

//empty

```
public static boolean isEmpty () {
    return s1.isEmpty ();
}
```

//add

```
public static void add (int data) {
    }
```

```
    //transferring elements from s1 to s2
    while (!s1.isEmpty ()) {
        int temp = s1.pop ();
        s2.push (temp);
    }
}
```

//adding new element
 s1.push (data);

//transferring the elements back

```
while (!s2.isEmpty ()) {
    int temp = s2.pop ();
    s1.push (temp);
}
}
```

//remove

```
public static int remove () {
    if (isEmpty ()) {
        System.out.println ("Queue is empty");
        return -1;
    }
    return s1.pop ();
}
```



① add

- ① S1 empty add here ✓
- ② S1 if not S2

transfer all elements

② S1 push

- ① S2 S1
- ② put all elements back

Use the other bucket  
to store the elements  
while adding element in  
first stack.

③ peek

```
if (isEmpty ()) {
    System.out.println ("Queue is empty");
    return -1;
}
```

```
return s1.peek ();
}
```

## # Stack using 2 Queues

### // add (push)

- ↳ add the 1<sup>st</sup> element in Q<sub>1</sub>
- ↳ then add the elements in the queue that have already elements.

### Pop

- ↳ put the elements one by one in another queue until we get to the last element.
- ↳ then at last element return the last element.
- ↳ For another pop use the filled queue as the primary one and other as secondary and then repeat the above process.

### static class Stack {

```
static Queue<Integer> q1 = new LinkedList<>();
static Queue<Integer> q2 = new LinkedList<>();
```

1/2/3/4

Q<sub>2</sub>

Stack

### //empty

```
public static boolean isEmpty() {
```

```
    return q1.isEmpty() && q2.isEmpty();
```

### //add

```
public static void push(int data) {
```

```
    if (!q1.isEmpty()) {
```

```
        q1.add(data);
```

```
    } else { q2.add(data); }
```

```
}
```

### //remove - O(n)

```
public static int pop() {
```

```
    if (isEmpty()) {
```

```
        System.out.println("Stack is Empty");
```

```
        return -1;
```

```
    }
```

if there are two cases

int top = -1;

```
if (!q1.isEmpty()) {
```

```
    while (!q1.isEmpty()) {
```

```
        top = q1.remove();
```

```
        if (q1.isEmpty()) {
```

```
            break;
```

```
        q2.add(top);
```

```
}
```

```
else { // case 2
```

```
    while (!q2.isEmpty()) {
```

```
        top = q2.remove();
```

```
        if (q2.isEmpty()) {
```

```
            break;
```

```
    q1.
```

## # First non-repeating letter in a stream of characters

flipkart

ex- aabccxb

T.C  $\rightarrow$  Big O(n)

① freq [ ] = [26] - for 'a' to 'z' storing the frequency of each character.

② Queue <Character>

```
for (int i=0; i<str.length(); i++) {
    ch = str.charAt(i);
    q.add(ch);
}
```

output

a -> b bb X

```
freq [ch - 'a'] ++;
```

```
while (freq [q.peek()] != 1) {
```

```
    q.remove();
}
```

if q.empty()  $\rightarrow$  -1

else print (q.peek());

}

\* Almost in all questions in which it is written "stream of characters"  
queue is used. Almost all!

## # Interleave or shuffle 2 halves of Queue (evenLength.)

ex- 1 2 3 4 5 6 7 8 9 10

$\Rightarrow$  1 6 2 7 3 8 4 9 5 10

Step ① - size of q.size()

- ② Queue first  $\rightarrow$  size/2 // make a new queue with first half elements original que.
- ③ remove first element from new queue and add at back of original
- ④ then transfer the first element of original at last

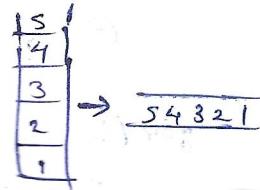
Repeat this until the Queue first became empty.

## # Queue Reversal

ex - 1 2 3 4 5

final → 5, 4, 3, 2, 1.

- ① Put the elements in stack 1 2 3 4 5 →
- ② put back in queue



## # Deque (Double ended Queue)

\* This is different  
from Dequeue

→ Queue of two mouth.

This means removing  
elements from  
queue.

### • Methods

- 1) addFirst();
  - 2) addLast();
  - 3) ~~removeFirst();~~
  - 4) removeLast();
  - 5) getFirst();
  - 6) getLast();
- Meaning as you understand by name.

Implement using JCF (Java collection Framework)

## # Java Collection Framework

Class -



Interface -



→ Implements  
→ Extends.

ArrayList -

Vector -

Stack -

LinkedList -

Linked Hash set -

Hash set -

Set ← Sorted set ←

Tree set

↓

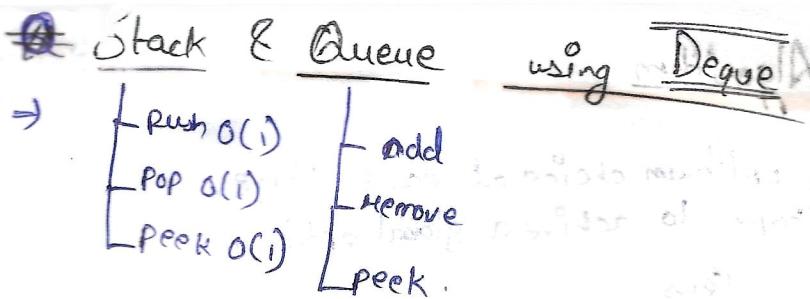
Collection

Queue ←

BiPriority Queue

Deque ←

ArrayList



→ Stack:

Push → addLast()

Pop → removeLast()

Peek → getLast()

Queue

add → addLast();

remove → removeFirst();

Peek → getFirst();

Sout.

## # Greedy Algorithm

↳ locally optimum choice at each stage and hope to achieve a global optimum.

Pros

- ↳ simple and easy
- ↳ good enough T.C

Cons

- ↳ A lot of time
- ↳ last sol<sup>n</sup> is not optimum.



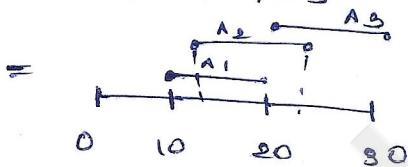
## # Activity Selection

- ↳ Start time and end time of a activity will be given
- one man can do only one work at a time (No multitask)
- Find maximum activities that can be performed ?

Ex -

$$\text{start} = [10, 12, 20]$$

$$\text{end} = [20, 25, 30]$$



So max activities = 2

A1 and A3

→ because if we start A2 the start time of A3 will be missed and we will be able to do only one activity.

- So the question is sorted with end time
- i) end time basis sort
  - A. first activity
  - ↳ end time

Max no. of activities → Non overlapping (disjoint)

↳ start time  $\geq$  last chosen action

Count ++

end time

index	start time	End time
0		
1		
2		
3		
4		

Steps

- ① sort on end time basis
- ② first end time will be the end time of last task.
- ③ for ( $i=0$ ;  $i < \text{end.length}$ )

```
if (start time  $\geq$  End time) {
```

```
    maxAct++;
```

```
    ans.add (that activity index)
```

```
    last end = activities [i] [2];
```

# Sorting in 2D Array

→ Arrays, sort (activities), Comparator, comparingDouble(0 → 0[2])

ex - 0	1	2	3
Row 1	1	2	3
Row 2	2	3	1
Row 3	3	1	2

Column 0 1 2 → on the basis of this column  
the table will sort.

enrich  
column the  
data should  
be sorted

## # Fractional KnapSack \*

→ You are given a bag which can hold limited Kg of things  
1. You have different things in different kg's and their sale value is different choose the things so that you have max value.

$$\text{Value} = [60, 100, 120]$$

$$\text{Weight} = [10, 20, 30]$$

$$\text{bag can hold} = W = 50$$

```
for (int i=n-1; i>=0; i--) {  
    if (capacity >= weight[i]) {  
        total += capacity - weight[i];  
        value += value[i];  
    } else {  
        value += val[i] / (ratio * capacity);  
        break;  
    }  
}
```

① Steps → find the rate ratio

② → make a 2D array having  
[index, weight/rate]

③ → if bag can't hold every thing add every thing.

④ → rather than add that much that the bag can hold

⑤ → priority with max rate object first.

⑥ → if not sorted sort the 2D array according to rate column.

## # Min Absolute Difference Pairs

$$2 - 1 = 1 (\text{eve})$$

$$1 - 2 = -1 \rightarrow |1 - 1| = 1$$

So here absolute difference is 1.

- We are given two arrays we need to make pairs bet<sup>n</sup> their element as the sum of their absolute difference is minimum.

ex-  $A = [1, 2, 3]$

$B = [2, 1, 3]$

ans = 0

→ So to get minimum sum the difference bet the elements should be ~~as~~ minimum.

→ take the difference bet<sup>n</sup> the elements as much closer to each other.

→ For this sort both arrays and take difference as their index wise.

→ This will give you minimum difference.

## # Max Length Chain of Pairs

- Here some pairs of elements are given you need made a chain with them but if  $(a, b)$  and  $(c, d)$  are a pair and in chain then  $b < c$  → next.

Ex- Pairs =

$(5, 24)$

$(39, 60)$

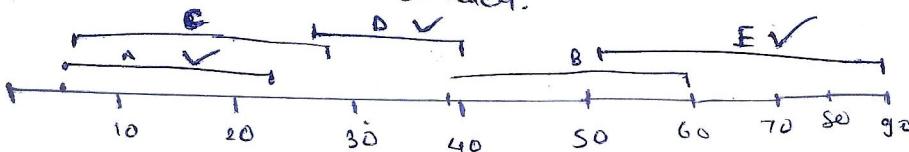
$(5, 28)$

$(27, 40)$

$(50, 90)$

Approach → this question is same as activity selection question.

→ If we arrange them in a line then the next pair will only come there if the earlier pair right element is smaller.



→ So we can pick A D E  
Max chain is 3 pairs.

Approach (Make a 2D array of [index, 1st element, 2nd element])

- ① Sort on the basis of second elements.
- ② first pair will be the first indexed pair.
- ③ Last element = 2nd element of first pair.
- ④ for ( $i=1; i < n; i++$ ) {
   
 if ( $\text{pair}[i](\text{start}) > \text{last end}$ ) {
   
 ans++; // increasing element in chain.
   
 ~~last~~ Last selected end update
 }

## # Indian coins

If you are given a mount say 590 you need to give this much to same one in minimum no. of notes

ex - You have  $[1, 2, 5, 10, 20, 50, 100, 500, 2000]$ .

So You will give  $500 \times 1$

$50 \times 1$

$20 \times 2$

→ So here we have used Greedy Approach to solve this - because we have used minimum no.

Off notes:-

but this approach will not work on every note system  
India has Canonical coin system so it works here.

## Approach-

- ① Sort descending  $[2000, 500, 100, 50, 20, 10, 5, 2, 1]$ .
- ② count = 0.
- amount = 590
- for ( $\text{int } i=0; i < n; i++$ ) {
   
 if ( $\text{coin}[i] \leq \text{amount}$ ) {
   
 while ( $\text{coin}[i] \leq \text{amount}$ ) {
   
 count++;
   
 amount -=  $\text{coin}[i]$ ;
 }
 }

}

\* Average sort (coins, Comparator reverse Order());  
to sort the array in reverse order.

But for this Integer this must be used to make array not primitive.

## # Job Sequencing Problem

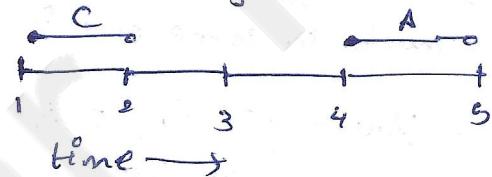
→ We are given some jobs, their deadlines and the payment we will get after doing them. each job takes 1 hour.

Ex-	Deadline	Payment
Job A =	4	20
Job B =	1	10
Job C =	1	40
Job D =	1	30

and each job only can be started before their deadline

So use greedy to get max profit

→ we will do job C = 40



### Approach

→ ① Sort Jobs (based on profit)

② time = 0

for (int i=0; i<jobs; i++) {

if (job(deadline) > time) {

add job in ans;

time++;

}

}

→ now only job A can be done because it had deadline 4.

$$\Rightarrow \text{profit} = 40 + 10 \\ = 50$$



Collections.sort (jobs, (obj1, obj2) → obj2.profit - obj1.profit);

# code to sort objects.

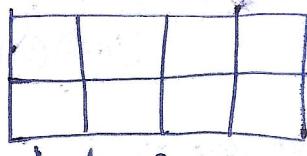
# # Chocola Problem

Q4 Min Cost to cut board into squares.

Microsoft  
Google

→ We have give a chocolate bar.

Ex -



3

we need to break this

is small pieces such

that there should be a single piece.

pieces  
of cut

1 2 1

but the twist is here is that each cut cost something and the cost differ for each cut.

the So we have to cut the chocolate in such a way that it cost minimum for cutting it.

## Imp things

- i) We have to perform each cut
- ii) After each cut chocolate breaks in pieces & then for each cut we need to pay separately
- iii) So we will do
  - a) expensive cut first
  - b) cheap cut at last.
- iv) Cost of vertical  $\rightarrow$   $\frac{\text{no. of horizontal pieces}}{\text{no. of cut pieces}} \times \text{cut price.}$

Cost of horizontal cut  $\rightarrow$   $\frac{\text{No. of vertical pieces}}{\text{No. of cut pieces}} \times \text{cut price.}$

We will make two array

$$\text{vertical cut} = [4, 3, 2, 1, 1]$$

$$\text{horizontal cut} = [4, 2, 1]$$

→ Move the pointer on both

→ perform the cut first which is costlier.

## Pseudo code

{sort hor,vert in decreasing order}

int h=0, v=0;

int hori=1, verti=1  
acc pesi

while (h < hor.length & v < vert.length){

    h < v { vert cut } else { hori cut }

    At last remain hori or verti cuts.

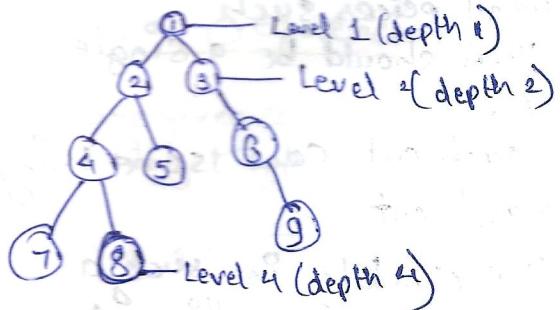
and add  
cost++;

# # Binary Tree

↳ This tree consist of max 2 nodes, i.e. 0.

- ## • Levels and Subtree

No. of leaves  $\rightarrow$  4



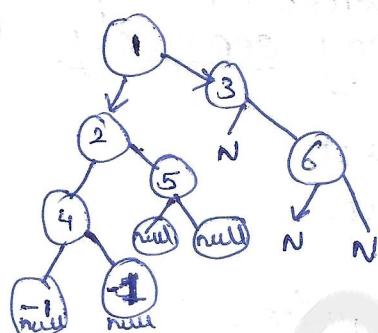
7 8 5 9

## Ancestors of 8

$$\rightarrow \{4, 2, 1\}$$

- Build Tree Preorder

1, 2, 4, -1, -1, 5, -1, -1, 3, -1, 6, -1, -1



$$-1 = \text{nullity}$$

- First take left node then right.
  - Null has no further node.

DFS → Depth first search

**BFS** → Breadth First Search

## # Tree Traversals

A) Preorder  $\rightarrow$  Prebecause root is printed first.

Li Ko

## ii) Left Subtree

iii) Right subtree

$$T(C) = \mathcal{O}(n)$$

```
public static void preOrder(Node root) {
```

11 base case

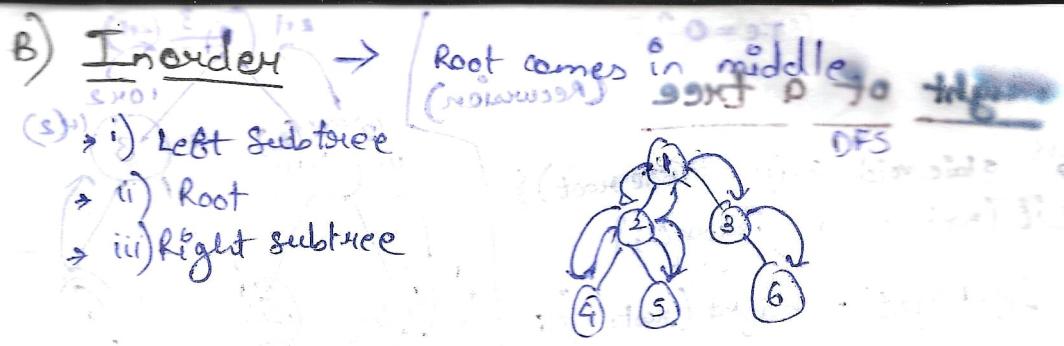
If ( $H_0$  is true)  $\frac{S}{\sqrt{S}}$

$\text{sys}(-1)j$   
 $y_{\text{elbow}}^3$

sys0( root, file + " " );

the Order (cont'd)

preOrder (root, right);



```
public static void InOrder(Node root){  

    if (root == null){  

        return;  

    }  

    InOrder (root.left);  

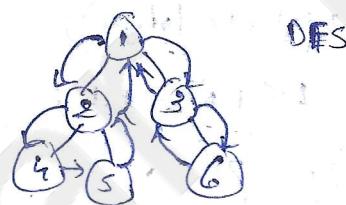
    System.out.print(root.data + " ");  

    InOrder (root.right);  

}
```

c) Postorder → root will be at last

- i) Left subtree
- ii) Right subtree
- iii) root.



```
public static void postOrder(Node root){  

    // base case  

    if (root == null){  

        return;  

    }  

    postOrder (root.left);  

    postOrder (root.right);  

    System.out.print(root.data + " ");  

}
```

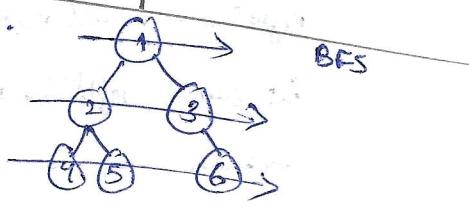
4, 5, 2, 6, 3, 1

d) Level Order → print level wise.

t.c = O(n)

In this we will use a Queue

- 1) put root in queue
- 2) print element from queue (pop Q)
- 3) add left and right element of root to Q
- 4) also add null after adding both left and right leaves so to know about next line.
- 5) another null will be added when the first null will be out of queue



1, 2, 3, 4, 5, 6

out of queue

## # Height of a tree (Recursive)

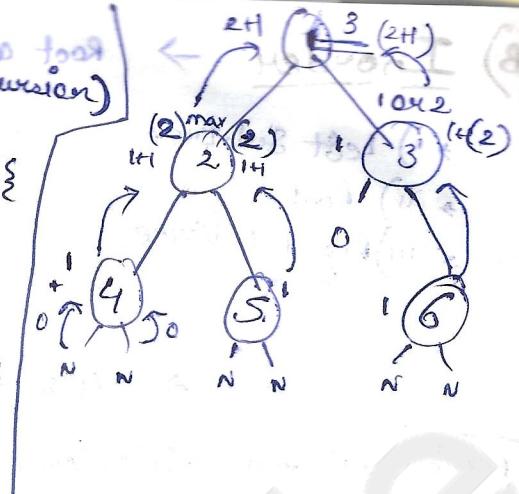
```

    static void height (Node root) {
        if (root == null) { return 0; }

        leftHeight = height (root.left);
        rightHeight = height (root.right);

        height = max (lh, rh) + 1;
    }

```



## # Count of Nodes of tree (Recursive)

```

    static void Count {
        if (root == null) {
            return 0;

        leftCount = count (root.left);
        rightCount = count (root.right);

        int treeCount = L.C + R.C + 1;
        cout (treeCount);
    }

```

## # Sum of Nodes (Recursive)

```

    static int sum {
        if (root == null) {
            return 0;

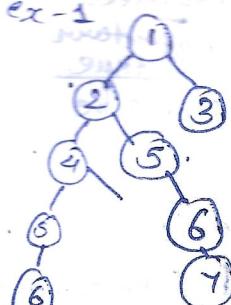
        leftSum = sum (root.left);
        rightSum = sum (root.right);

        int sum = leftSum + rightSum + root.data;
        return sum;
    }

```

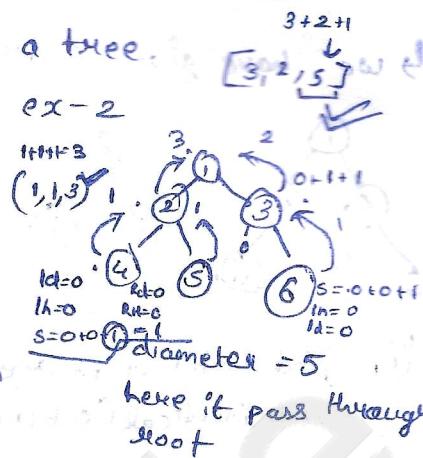
# Diameter of a Tree  $T.C = O(n^2)$   
(Approach no. 1)

→ longest distance bet two node of a tree



$$\text{diameter} = \gamma$$

here it does not pass through root node.



- diameter of that Node =  $(\frac{\text{left diameter} + \text{right diameter}}{2}) + 1$

```
→ static int diameter(Node root) {
    if (root == null) {
        return 0;
    }
```

```

int leftDia = diameter (root.left);
int rightDia = diameter (root.right);
int leftHt = height (root.left);
int rightHt = height (root.right);

```

Put self diameter = left height + Right height + 1

between  $\text{Math.max}(\text{self Diameter}, \text{Math.max}(\text{left Dia}, \text{right Diameter}))$

# Diameter (Approach 2)

class Info {  
 int diam;  
 int height; }

↳ To save the time we will return both height + diameter using a class.

left Info = diam (root.left) ]  $\rightarrow$  includes [diameter, height]  
 right Info = diam (root.right) ]  $\rightarrow$  includes [diameter, height]

$$\begin{aligned} \text{newInfo} &\leftarrow \begin{cases} \text{final Diam} = \max(\text{Info.dia}, \text{InfoDia}, \text{lh} + \text{ht}) \\ \text{final HT} = \max(\text{lh}, \text{ht}) + 1 \end{cases} \end{aligned}$$

between newInfo(Diam, ht);

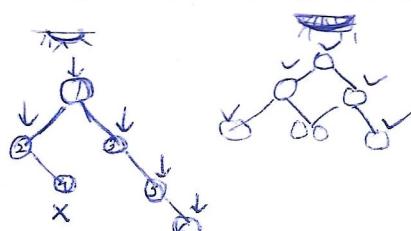
## # Subtree of another tree

↳ we have given a full tree and a sub tree.  
we have to find out if the subtree  
is a subtree of Main tree.

→ Node and position both should be same.

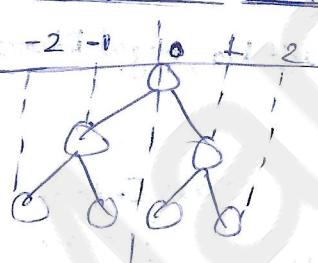
- Step
- ① find subroot in tree using any traversal
  - ② check identical (subtree, node subtree)
- Return false if
- ① node.data != subroot.data
  - ② node == null || subroot == null
  - ③ left subtree → non identical
  - ④ right subtree → non identical

## # Top view of a tree



Output : 2, 1, 3, 5, 6

## # Horizontal Distance



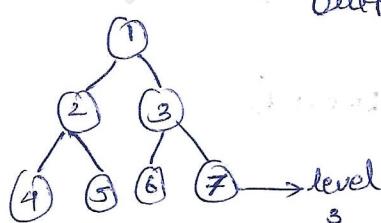
↳ if we move root.right → H.D + 1  
↳ if we move root.left → H.D - 1

## K<sup>th</sup> Level of a tree

• time Complexity = O(n)

$$2^x - 1 = 3$$

Output : 4 5 6 7



\* first level will be zero.

### Pseudo code:

```

k level (root, level, k) {
    if (root == null)
        return;
    if (level == k) {
        print (root.data)
    }
    klevel (root.left, level+1, k)
    klevel (root.right, level+1, k)
}

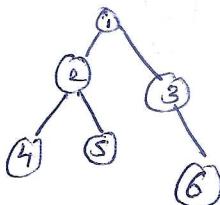
```

as we don't need to go further in tree.

## # Lowest Common Ancestor (LCA)

↳ the node at (first node) where the meet if we go up in tree

example -



$$n_1 = 4, n_2 = 6$$

$$\text{output} = 1$$

$$n_1 = 4, n_2 = 5$$

$$\text{output} = 2$$

HashMap<>();

### Approach

make array of path from leaf to root

a)  $0x - 6 \rightarrow [1 | 3 | 6]$

b)  $4 \rightarrow [1 | 2 | 4]$

Now traverse both array and the last common element will be the LCA

### # Path Finder function

- 1) check if the node node = value  
if yes add to array list return
- 2) if no add to array list and check left and right of that node.
- 3) if both right and left return null means node is not available in that direction.
- 4) Remove that node and return false
- 5) if got false from the ahead node remove the current node and return false.
- 6) Return true only if get the key

### # Optimized approach $\overset{\text{TC}}{\Rightarrow} O(n)$

- 1)  $\text{root} = \text{null}$  }  
 $\text{root} = n_1$  }  
 $\text{root} = n_2$  }  
return root

$\text{leftLca} = (\text{Node.left}, n_1, n_2);$

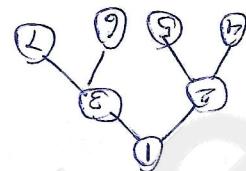
$\text{RightLca} = (\text{Node.right}, n_1, n_2);$

- 2)  $\text{rightLca} = \text{null} \rightarrow \text{return leftLca};$   
 $\text{leftLca} = \text{null} \rightarrow \text{return rightLca};$   
 $\text{right & left} \neq \text{null} \rightarrow \text{return root};$

Step ① Find my node

Out put = Node ①

$$k = 2 \\ n = 5 \\ \text{etc.}$$



# Kth Descendant of Node

if (left = -1, right = -1)  
else if (right = -1)  
    return left  
    right++  
    return right  
else (return right++  
    right++  
    return right)

if (left = -1, right = -1)  
else if (right = -1)  
    return left  
    right++  
    return right

# left n search  
# right n search

if (root == null)  
    return 0;  
if (root.left == null)  
    return 1;

if (root.right == null)  
    return 1;

min distance = dist1 + dist2

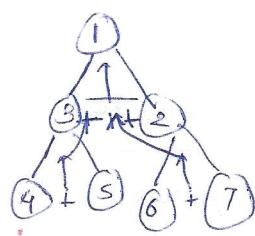
① dist1 &ca to n1  
② dist2 &ca to n2

applicable  $\rightarrow$

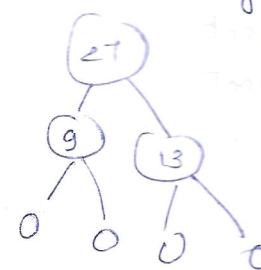
# Min distance b/w two nodes

# # Transform to Sum Tree

Each node = sum of left and right subtree.



→

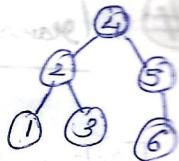


approach

```

transform(node *root)
{
    if (root == null) {
        return 0;
    }
    int leftChild = transform(root.left);
    int rightChild = transform(root.right);
    int data = root.data;
    if (root.left == null) {
        root.left = data;
    }
    if (root.right == null) {
        root.right = data;
    }
    root.data = newLeft + leftChild + newRight;
    return data;
}
  
```

# # Binary Search tree



↳ Same as binary tree with some extra properties.

- i) Left Subtree Nodes < Root
- ii) Right Subtree Nodes > Root

iii) Left and right Subtree are also BST with no duplicates.

\* So here Inorder Traversal → give sorted sequence

## # BST search Time Complexity = $O(n)$

→ if ( $k = \text{root}$ ) { return; }  
if ( $k > \text{root}$ ) search at right side  
if ( $k < \text{root}$ ) search at left side

→ But in skewed tree ex -   
Worst case

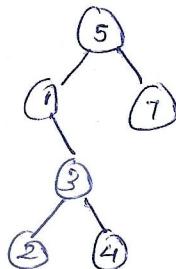
Common Strategy → Most problems will be solved using recursion  
i.e by dividing into sub problems and making recursive calls on subtrees.

## # Build a BST

→ Values [] = {5, 1, 3, 4, 2, 7}

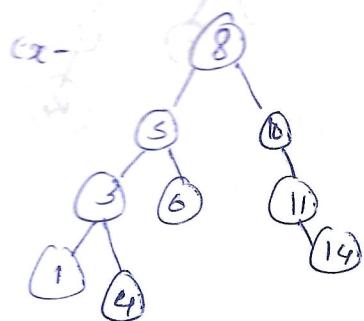
- Inorder traversal

→ 1, 2, 3, 4, 5, 7



Approach → values[i] > root → put in right subtree  
values[i] < root → put in left subtree.

## # Search in BST



$$T.C = O(H)$$

$H = \text{height}$  of tree

- key = 1
- (1) Root > key { search in left tree }
  - (2) Root < key { search in right tree }
  - (3) Root = key
    - Return true
  - (4) Else if root == null { return false }

## # Delete a Node :

### Approach

- ① find the node
- ② if case (1) return null to the parent.
- ③ and the node will be deleted automatically.

### Case I

- Replace the node with child node

### Case II

- If the node have 1 child

then the node should be deleted

and the order of BST should also not be disturbed.

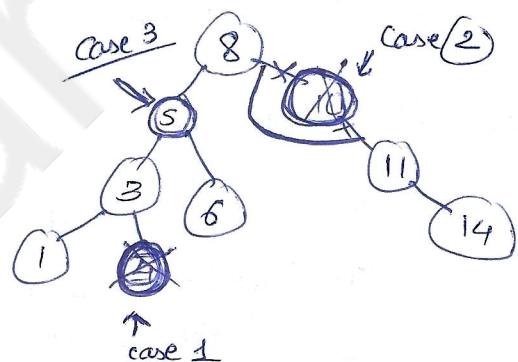
∴ we need to replace that node with inorder successor

- 1) Replace value with inorder successor
- 2) Delete the node for inorder successor

Inorder successor → Left most node in right subtree.

### Cases

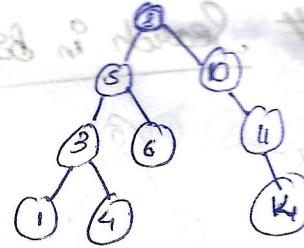
- 1) No child (Leaf Node)
- 2) One child
- 3) Two child.



## # Print in Range

Example from  $k_1=5$  to  $k_2=12$

output should be - 5, 6, 8, 10, 14.



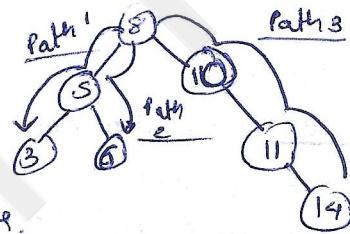
Case I if  $k_1 \leq \text{root} \leq k_2$

$\begin{cases} L \cdot R \\ \hookrightarrow R \cdot R \end{cases}$  If the value of node lies between the range print it.

Case II

$\text{root} > k_2$	else	$\text{root} < k_1$
$\begin{cases} R \cdot R \\ \text{only} \end{cases}$	$L$	$\begin{cases} R \cdot L \\ \text{only} \end{cases}$

## # Root to Leaf Paths



If we will store this path in array lists.

### Approach :

- ① Add node to array list
- ② traverse left
- ③ if found null  $\rightarrow$  print path. base case.
- ④ backtrack to parent node and remove the node from array list
- ⑤ then traverse right.

## # Validate a BST

$\Rightarrow$  BST will be given and validate it.?

### Approach 1

If inorder is sorted  
then  $\rightarrow$  BST valid ✓

### Approach 2

- ①  $\hookrightarrow$  take out max of left side =  $m_L$
- ② take out min of right side = ~~max~~  $m_R$

if  $(m_L < \text{root} < m_R) \{ \text{then BST valid} \} \checkmark$

Left subtree  $\rightarrow$   $\min = \min$   
 $\max = \text{root}/\text{parent}$

Right subtree  $\rightarrow$   $\min = \text{root}/\text{parent}$   
 $\max = \max$

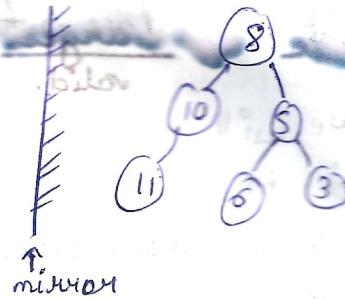
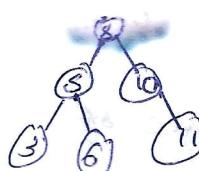
## # Mirror a BST

### Approach

① take out mirror of left subtree

② take out mirror of right subtree

③ swap them.



→ Mirror → ~~root~~ left  $\leftrightarrow$  right

## # Sorted Array $\rightarrow$ Balanced BST

arr = {3, 5, 6, 8, 10, 11, 12} (minimum possible height)

To get minimum height → find mid

recursively → take it as root

→ half elements at left and half elements at right

### Pseudo code

```
→ CreateBST(arr, st, end) {
    if (st > end)
        return null.
```

int mid = (st + end) / 2

Node root = newNode(arr[mid])

root.left = CreateBST(arr, st, mid - 1)

root.right = CreateBST(arr, mid + 1, end)

return root;

## # Convert a BST to Balanced BST

Approach → ① take out Inorder sequence of BST

② convert the arr to Balanced BST

## # Point

### largest BST valid.

↳ Here we will use the logic of isBST valid

↳ But we will make class of "Info"

This whole thing will be calculated for each node

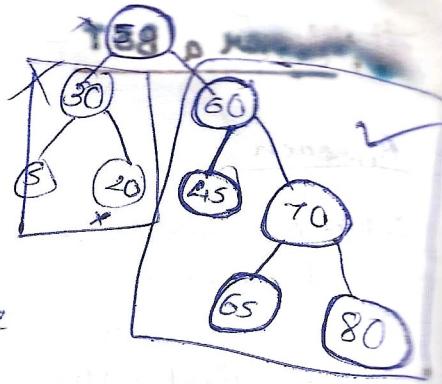
- ① Is BST (boolean) True or false
- ② size = left size + right size + 1
- ③ min =  $\min(\text{root.data}, \text{left.min}, \text{right.min})$
- ④ Max =  $\max(\text{root.data}, \text{left.max}, \text{right.max})$

for each node

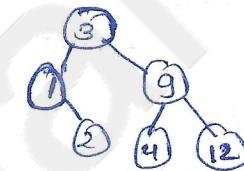
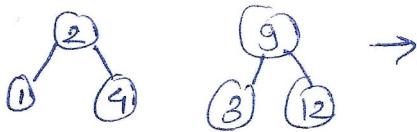
↳ we will make a static variable (max size) when the isBST  $\rightarrow$  true

max =  $\max(\text{max.current.info})$ ;

↳ And we will return max size.



## # Merge 2 BSTs



Balanced BST

### Approach →

- ① BST 1 inorder sequence (sorted)
- ② BST 2 inorder sequence (sorted)
- ③ Merge both arrays.
- ④ Sorted array  $\rightarrow$  Balanced BST

## # AVL Trees

→ only concept asked

### self-balancing BST

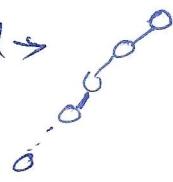
↳ we required Balanced tree to reduce T.C

for ex -  $10^5$  nodes if it's skewed  $\rightarrow$  tree

then  $T.C = 10^5$

but if balanced  $\rightarrow 5 \log 10$   
then

And  $5 \log 10 \ll 10^5$



# # Heaps / Priority Queues

↳ give first priority to the element you want.

## • Priority Queue using ICF

↳ Priority Queue <Integer> pq = new Priority Queue <>();

### Functions

At default the priority in integer is from lowest  $\rightarrow$  highest number.

- ① add() TC:  $O(\log n)$
- ② remove() TC:  $O(\log n)$
- ③ peek() TC:  $O(1)$
- ④ isEmpty()

To travel through queue for each loop

$\rightarrow$  for (int x : q) {  
    if (x == K) return true;  
}  
return false;

To change the priority (descending type) add this

Priority Queue <Integer> pq = new Priority Queue <> (Comparator. reverseOrder());

## # Priority Queue of objects

→ For this we need to make our class comparable

(Means give it the power so that it can compare)

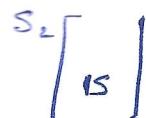
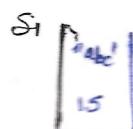
```
static class Student implements Comparable<Student> {
    String name;
    int rank;

    public Student(String name, int rank) {
        this.name = name;
        this.rank = rank;
    }
}
```

### ④ Override

```
public int compareTo(Student s2) {
    return this.rank - s2.rank;
}
```

this rank -  $S_2$  rank



if  $S_1 < S_2$  - ve  $\rightarrow S_2$  is greater

$S_1 > S_2$  + ve  $\rightarrow S_1$  is greater

$S_1 = S_2 \Rightarrow$  equal.

Output: Output will be sorted on the basis of rank

Ex - A - 2

C - 3

D - 4

B - 8.

\* To make the order reverse

we (Comparator, reverseOrder())

in side Priority Queue argument section

## 4. Reverse Order();

- o Heap [ Max heap  $\rightarrow$  PQ max. ↑ priority  
Min heap  $\rightarrow$  PQ min. ↓ priority ]

### Properties

- ① Binary tree

↳ Atmost 2 children

- ② Complete binary Tree (CBT)

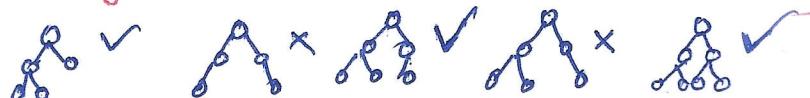
↳ CBT is a binary tree in which all levels are completely

filled except, possibly the last one

↳ It is filled from left to right, before new leaf.

↳ Means a level should be completely filled before starting to put the elements in new level

Ex -



### ③ Heap Order Property

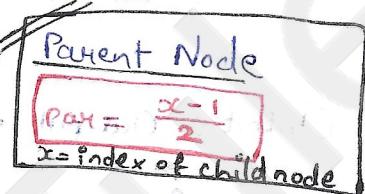
↳ Children node  $\geq$  Parent (**Min Heap**)

↳ Children node  $\leq$  Parent (**Max Heap**)

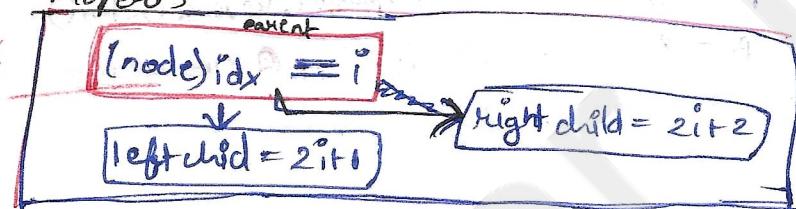
### # Heap Implementation we do it with the help of arrays

We cannot use class using class because then the add function will take more than  $\text{Log}(n)$  time.

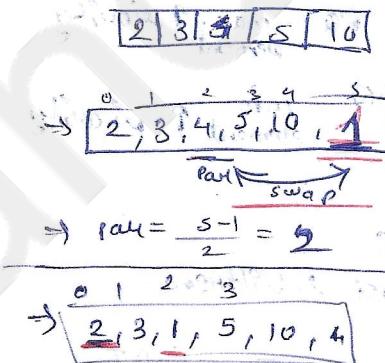
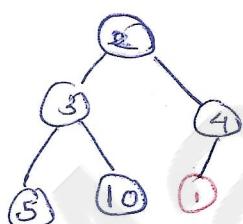
we use Array or ArrayList.



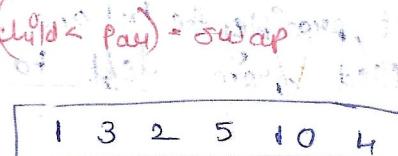
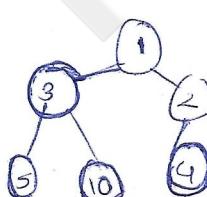
Properties



### # Insert in Heap T.C = $\log(n)$



Step 1 - add at last index  
Step 2 - fix heap.  
Step 3 -  $\text{Par} = \frac{x-1}{2}$  while  
{Step 4 - if (child val  $\leq$  parent val)  
swap (child, parent)}



# Get min in Heap.

↳ we know that in Min Heap minimum element of the Tree is root.

Peek()

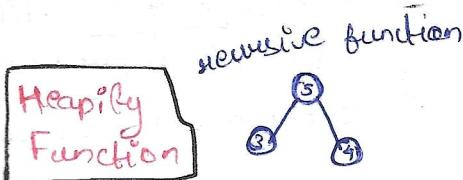
public int peek() {

return arr.get(0);

}

# Delete in Heap  $\rightarrow TC = O(\log n)$

Q. Remove min element



Steps: 1) swap 1<sup>st</sup> and last node

2) Remove last index in array list  
`arr.remove(arr.size() - 1);`

3) Fix heap  
↓ using

heapify

→ ① It compares root, leftchild, rightchild

② put the min at root =  $i$

→ 2<sup>nd</sup> min at left root =  $2i + 1$

→ and large at Right root =  $2i + 2$

# Heap Sort  $\rightarrow$  Accending  
 $\downarrow$   
 $arr = 1, 2, 3, 4, 5$  (Max heap)      Depending  
 $\downarrow$   
(Min heap)

Step 3 ① arr  $\rightarrow$  Max heap  
↓  
last level  
Non-leaf Nodes

heapify()

↳ maxheap

→ Max heap will bring the largest element at top (root)

→ then exchange it with last

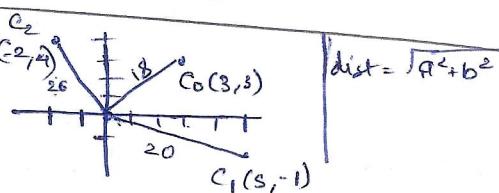
→ heapify (size 1 se kam karke)

→ first apna for heap array sorted

Step ②  $\rightarrow$  Swap (1<sup>st</sup> and last)  
 $\rightarrow$  remove last

for (0 to n-1)

# Nearby Cars  $\rightarrow$  we are at origin  $(2, 2)$   
to find K near cars?  $K = 2$



Distance from origin  $\rightarrow$

$C_0 \rightarrow 1\sqrt{2}$

$C_1 \rightarrow 2\sqrt{2}$

$C_2 \rightarrow 2\sqrt{2}$

Approach

①  $\rightarrow$  Find the distance

②  $\rightarrow$  Put that value in Priority Queue

③  $\rightarrow$  take out first K values as your ans

public int compareTo (Point p2) {

return this.distSq - p2.distSq; }

Comparing on the basis of dist Sq

Solve

- Connect N Ropes → but each time when 2 ropes connected they have charge. charge = length of x rope + length of y  
 $[4, 3, 2, 6]$  → we want to connect all rope in minimum charge
- As the charge is added each time so to have a minimum charge we will connect smallest hoop first. Doing this the charge will be lowest

→	2 + 3	Charge
		5
	5 + 4	9
	9 + 6	15
		29 //

- Approach
- ① Add all elements in PQ
  - ② Remove first element
  - ③ add them and push in PQ
  - ④ do above (3 and 4) until PQ gets ~~empty~~ 1 element
  - ⑤ last removed is answer.

This question looks like solved by Greedy algorithm as just sort and start adding them but No it gives WRONG Answer

# Weakest Soldier → 1 represent soldier, 0 represent civilians.  
 ex.  $m=4, n=4, k=2$  Row is weak if  
 → ① It is at top  
 ② It has less no. of soldier.

1 0 0 0 ← most weakest  
 1 1 1 1  
 1 0 0 0 ← second weakest  
 1 0 0 0  
 ans → R0, R2

Q. Find weakest (first two row) ?

Approach:

static class Row implements Comparable<Row> {

int soldiers;  
 int idx;

public Row(int soldiers, int idx) {

this.soldiers = soldiers;  
 this.idx = idx;

else compare on  
 the basis of  
 soldiers.

else {

return this.soldiers -

if soldiers are  
 same then compare  
 on the basis  
 of index

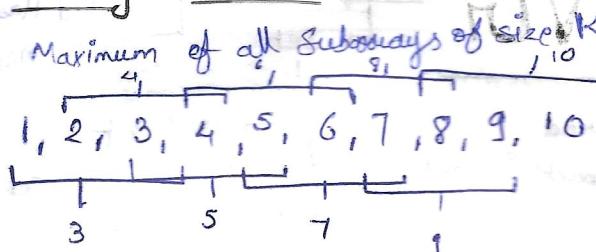
② Override

public int compareTo(Row r2) {

if(this.soldiers == r2.soldiers) {

return this.idx - r2.idx;

## Sliding Window Maximum

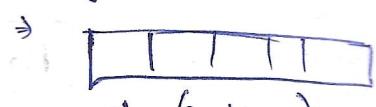


$K=3$   
window of length 3

we need to take out maximum of three element

length of result array

→ Approach ⇒ we will make max heap.



① add K nums to PQ (1st window)

② ① PQ. peek() → window[0]

③ while ( $PQ.\text{peek}().\text{idr} \leq (i-K)$ )

{  
PQ.remove();}

④ PQ.add (element next from end)

⑤ window[i] = PQ.peek()

here as in the PQ the top element will be maximum

then check whether the element at top is of that current window or not.

→ if not then remove it

→ otherwise keep it and then add the next element.

⑥ Adding many elements in PQ will do no harm at the top there always be the max element.

⑦ but check whether the element is from that current window or not

→ After making Priority Queue.

// 1st window

for (int i=0; i<k; i++) {

| PQ.add (new Pair (arr[i], i));

}

res[0] = PQ.peek().val;

taking out first max window element

for (int i=k; i<arr.length; i++) {

| while (PQ.size() > 0 & PQ.peek().idr <= (i-k)) {

| | PQ.remove();

| }

| PQ.add (new Pair (arr[i], i));

res[i-k+1] = PQ.peek().val;

if the element in top is not of current window

# # HASHING

## # HashMap

(key, value)

↓  
always  
unique

↳ unordered  
[we get data back in random form]

import java.util.HashMap;

↳ map  
↳ set  
↳ Hash map  
↳ Linked Hash map  
↳ Tree map

↳ Hash set  
↳ Linked Hash set  
↳ TreeSet.

HashMap < String, Integer > hm = new HashMap<>;  
 ↳ column 1  
↳ one datatype  
 ↳ column 2  
↳ datatype

- \* ① Put(key, value) → to update value  
→ hp.put(key, value)
- \* ② get(key) → hp.get() → or to make new node
- \* ③ containsKey(key)
- \* ④ remove(key)  
→ hp.remove()
- To check if the data with that key is present or not
- To remove (key and value) Node.

if passed a [key] ← Not existing

→ Null

keys	values
"one"	1
"two"	2
"three"	3
"four"	4

\* ⑤ Size  
→ hp.size();

\* ⑥ Empty → hp.isEmpty();

\* ⑦ Clear → hp.clear();

# Iteration on HashMap

On ② hm.entrySet()

↳ For all values set.

`Set<Integer> keys = hm.keySet();`

String

↳ this stores all the keys in set

ex- from last    keys = [one, two, three, four]

• foreach → `for (String k : keys) {`

    |    `System.out.println("key=" + k + ", value=" + hm.get(k));`

}

here → k will like iterator.

→ it will iterate till the end.

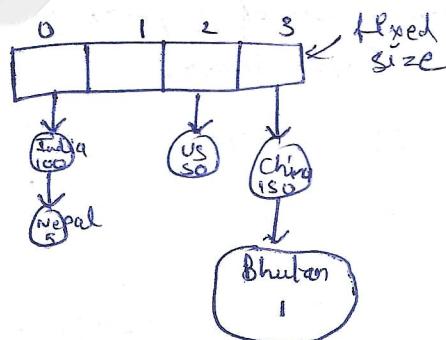
# Implementation HashMap

Was asked in Uber to implement hash

`Put(), get(), containsKey(), remove(), size()`     $O(1)$

→ this all works in the Java in the form Array of Linked List

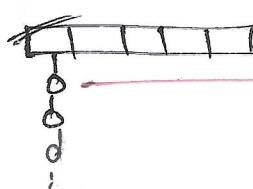
Map	
Key	value
"India"	100
"China"	150
"US"	50
"Nepal"	5



special Note

Rare case  
Worst time complexity will be  $O(n)$ . if we have such

data whose bucket index giving by hash function is same



\* When the datatype of the variables is not fixed we use generic to make them  
→ ex  $\langle K, V \rangle$  → this way any datatype can come  
→ used in implementation of hashmap.

# Linked Hash Map → everything same just it maintains the order in which the elements are inserted in it  
Keys are insertion order → it uses Doubly Linked List to maintain the order.

# Tree Map → put, get, remove are  $O(\log n)$  (BSF)  
→ Keys are sorted → Here in implementation Red Black trees are used which are self-balancing trees  
TreeMap < → hm = new TreeMap<>();

Q. Majority Element →  $Tc = O(n)$

given an arr of size find the elements that appeared more than  $[n/3]$  times.

⇒ nums[] = {1, 3, 2, 5, 1, 3, 1, 5, 1};  $n = 9$

output = 1

1 is  $n/3 = 3$  greater

ex. nums []  
{1, 2}

for ( $i=0$  to arr.length)

num = arr[i]

output {1, 2}

if (map.containskey(num))

map.put (num, map.get (num) + 1);

adding with increasing freqcy:

else

map.put (num, 1);

To traverse on a Map we need **KeySet**

→ Set<Integer> keys = map.keySet();

for (Integer key : keys) {  
    }

\* if the key exist then  
it will return it's  
frequency or and if  
not then 0.

Shortcut for increasing frequency

⇒ [map.put(arr[i], map.getOrDefault(arr[i], 0) + 1);]

Shortcut for "No need to store KeySet in any other place"

for (Integer key : map.keySet()) {  
    if (map.get(key) > arr.length / 3) {  
        System.out.println(key);  
    }  
}

# Valid Anagram.

T.C = O(n)

ex - "race" = "care"

same no. of letters

same value of letter, with same frequency.

Approach :

① HashMap < Character, Frequency >  
    → we will store char and int

② then when we will traverse  
the second string we will delete  
or remove the elements from  
map.

③ if Map is empty return True or False.  
    if found such a element which  
    is not available then return False

- # Hashset → implements using hash map.  
 ↳ Collections of unique elements.
- No duplicates
  - Unordered
  - Null is allowed
- 1) add (key)
  - 2) contains (key)
  - 3) remove (key)
  - 4) set.size();

$O(1)$

`HashSet < Integer > hs = new HashSet <>();`

## # Iteration on Hashset

### ① Using Iterators

```
→ Iterator it = set.iterator();
while (it.hasNext()) {
  print(it.next())
}
```

→ Provides a iterator  
 if  $\rightarrow$  null  
 points towards null.

→ Checks if there is  
 such an element which  
 is not traversed till now.

→ Then automatically  
 it shifts to next it.

### ② Using Advance loop

→ for each.

```
→ for (key keys)
  for (String city : cities) {
    System.out.print(city + " ");
  }
```

ex - `HashSet < String > cities = new HashSet <>();`  
`Cities.add("Nagpur");`  
`Cities.add("Mumbai");`

## # Linked HasSet → implemented using linked Hash Map. using doubly LL.

- Ordered elements.

T.C → remains same  
 just little performance drop.

→ `Linked HashSet < Integer > lns = new LinkedHashSet <>();`

# Tree Set → tree map (Red Black) (self Balancing trees) T.C = O(log N)

- Sorted in ascending order.
- Null is not allowed.
- No duplicates.

TreeSet <String> ts = new TreeSet<>();

Other properties are same.

## # Q Count Distinct elements

- use set as it contains no duplicates.
- return set size.

## # Q Union and Intersection of arrays T.C = O(m+n)

$$\text{arr1} = \{7, 3, 9\}$$

$$\text{arr2} = \{6, 3, 9, 2, 9, 4\}$$

a) Union → take a set of all elements.

- b) Intersection →
- i) add elements of one set
  - ii) traverse on the array of second.
  - iii) if the element present in set
    - ↳ a) count it;
    - b) remove that so can't be count again.
  - iv) print count.

## Q. Find Itinerary from Tickets

Journey.  
Approach → Print all the places one wise you visited.

Find the starting point

- a) Make a reverse map.
- b) find the place which is the start
- c) if the place exists in key of main map but not in to

key	value
chennai	Bengaluru
Mumbai	delhi
Goa	chennai
Delhi	Goa

to	from
B	C
D	M
C	G
C	D

→ Then just go from that key to value until last value is not a key.

## # largest subarray with sum = ~~target~~ 0

ex.  $\boxed{\text{target} = 0}$

this much has no  
value : 0

brute force → nested loops

$\Rightarrow \{15, -2, 2, -8, 1, 7, 10, 23\}$

$\boxed{\text{ans} = 5}$

largest subarray with

if (found and same sum)  
then

(Key)	(Value)
sum	index
15	0
13	1
7	3
8	4
25	6

$\text{MaxSubarray} = \underline{\text{Math.Max(index)}}$

steps:

because as we want sum = 0

so if any key is same then we can  
subtract the front and get sum as zero

## # Count no. of subarrays with sum K

T.C  $\Rightarrow O(n)$

Approach  $\rightarrow$   $i$   $j$

$\text{arr} = \{10, 2, -2, -20, 10\}$

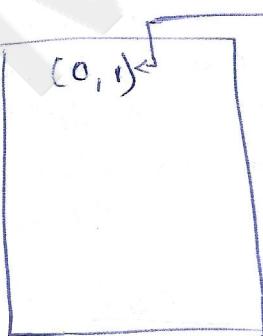
$K = -10$

$i \rightarrow$   $i^{\text{th}}$  index  
 $j \rightarrow$   $j^{\text{th}}$  index

so

$$\text{Sum}[0, j] - \text{Sum}[0, i-1] = \text{Sum}(i, j)$$

we will make Hash Map



This should be already added  
otherwise it will never  
find a 0 and  
count will  
not increase

$$\text{Sum}[j] - K = \text{Sum}[i]$$

$$\text{Sum}[j] - K = \text{Sum}[i]$$

↑  
cumulative sum  
↓  
given

→ ① First we will add  $(0, 1)$  in hash map  $0 - k = -10$

② We want  $K_{sum}$  as a subarray.

So if current  $- k = 0$  then its equal to  $K_{sum}$

③ Each time we will check the

④ Take sum =  ~~$10 \neq 0$~~  did  $0$  also frequent increase.  
ans =  ~~$0$~~   $\rightarrow$   $10 - (-10) = 20$

$\rightarrow$  ans + 1

$\rightarrow$  ans = 1

ans + get(10)

= (ans + 2)

$\rightarrow$  ans = 3

$$12 - (-10) = 22$$

$$10 - (-10) = 20$$

does not exist

does not exist

does not exist

full sum

exists

ans + (get(0))

$$0 - (-10) = 10 \text{ exist}$$

and

$[10, 2, -2, -20, 10]$

$\uparrow \uparrow \uparrow \uparrow \uparrow$

$(0, 1) \leftarrow$  already

$(10, 12)$

$(12, 1)$

$(-10, 1)$

# # Trie

## Trie

→ Prefix tree  
or  
Retrieval tree  
Retrieval tree

ex - there  
the  
The  
↑  
prefix

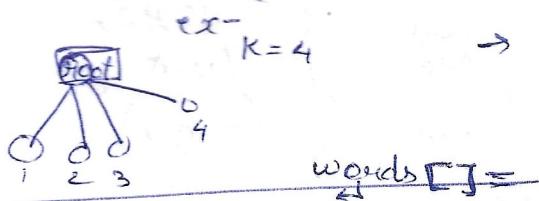
Questions  
are directly  
asked in  
Competitions  
like O-star  
various  
universities.

- ↳ Same prefix are saved only once
- ↳ used in string question

### • What is Trie?

→ It is a (K-way) tree.

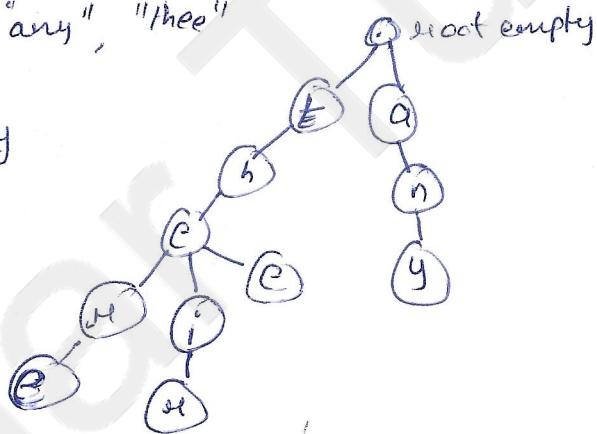
→ Saves time as height is less



① root (empty)

⇒ "the", "a", "there", "their", "any", "thee"

→ As prefix is stored only once so time is saved.



⇒ Class Node {

    Node [ ] children; 26 letters  
    boolean endOfWord;

}

# Making tree

Static class Node {

    Node children [ ] = new Node [26];  
    boolean eow = false;

    Node () {

        for (int i=0; i<26; i++) {  
            children [i] = null;

}

- Each node has 2 info
- ① the letter it's holding
  - ② end of word
- ③ → to show which letter is it holding.
- ④ → to check whether the word ends here or not.

and also a empty root node

→ public static Node root = new

↓ This root

it is always empty

just stores which elements are used in tree

## # Insert in tree

T.C  $\rightarrow O(L)$

$\hookrightarrow$  level of letters

- ① After the root we will check level by level
- ② like this each letter by letter will be stored.
- ③ And the place where word ends there we will store eow = true  
end of word

when we miss

$t-a \rightarrow$  we will get idx

ex  $F[a-a=1]$   
 $b$  is at 1st idx

### Sudocode

→ curr = root

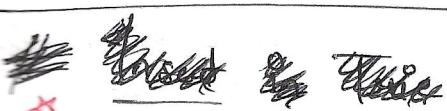
for (level = 0 to word.length())

if (curr.children[ch - 'a'] == null)  $\hookrightarrow$  new node create

else x

curr = curr.children[ch - 'a']  
 $\hookrightarrow$  idx

```
public static void insert(string word) {
    Node curr = root;
    for (int level = 0; level < word.length(); level++) {
        int idx = word.charAt(level) - 'a';
        if (curr.children[idx] == null) {
            curr.children[idx] = new Node();
        }
        curr = curr.children[idx];
        curr.eow = true;
    }
}
```

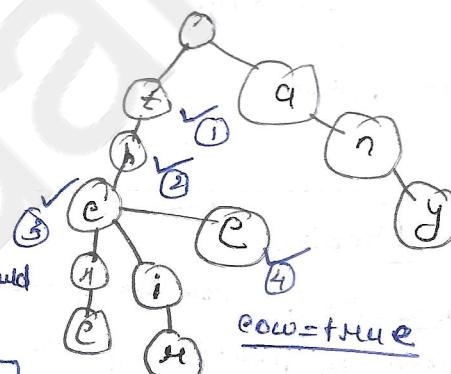


## # Search in a Tree

ex-1

Thee  
↑↑↑

- ① check at each level
- ② so at each level char should present.
- ③ And last node  
eow = true



word exists

curr = root

for (level = 0 to key)

{  $\hookrightarrow$  idx = key.charAt(level) - 'a'; }

if (curr.children[idx] == null)  $\hookrightarrow$  return false; }

curr = curr.children[idx]; }

between curr.eow = true;

This should also  
be the end of  
word.

## # Word Break Problem

T.C  
⇒ O(n).

Google

key = "I like samsung"

words[] = { I, like, Sam, Samsung, mobile, ice }

Q. Can we break the key such that each part is present  
in the dictionary / words[] as a word?

→ I like samsung → return true,  
✓ ✓ ✓

Approach. - ① create a tree from string.

public static boolean wordBreak(String key) {

    # base case

    if(key.length() == 0) return true;

    for(i=1 to i <= key.length())

        As the substring function  
        is inclusive

        if(search(key.substring(0, i)) && wordBreak(key.substring(i)))  
            return true;

}

    return false

## # Prefix Problem

30-40 min

microsoft, google

Find shortest unique prefix for every word in a given list.

Assume no word is prefix of another. → ex- apple

apple

X

no such  
case

→ Uska short name banao (nickname)  
eikh sabka (nickname) unique ho.

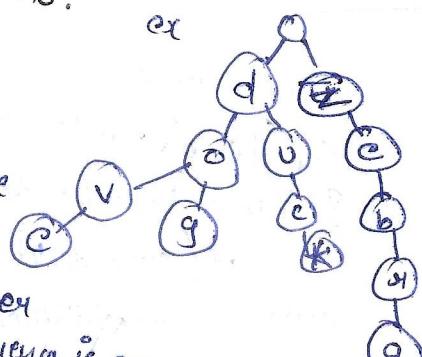
Approach = ① tree create.

② also add frequency feature in tree.

③ if the letter/char repeated increase  
the frequency.

④ the traverses each word letter by letter  
till you find a letter whose frequency is one.

⑤ and then you will find unique prefix for every word



→ ex- dov,  
dog,  
du,  
z.

RE) check root =  $\text{freq} = -1$ ) T.C = O(L)

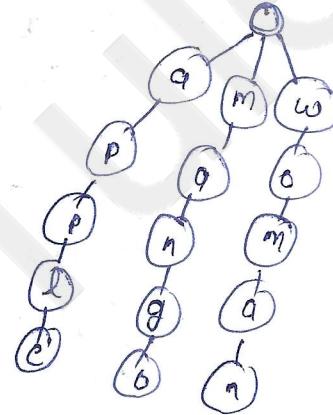
## # Q. Starts With Problem

↳ creates a function boolean which find the prefix is present or not

ex- words  $[J] = \{ \text{"apple"}, \text{"app"}, \text{"mango"}, \text{"man"}, \text{"woman"} \}$   
Prefix "app" output true, as in apple  
Prefix "moon" output false

→ Approach → ① create tree.  
② check one by one character in tree.

bool startWith(string prefix){  
 Node curr = root;  
 for(int i=0 to prefix.length();)  
 idx = prefix.charAt(p) - 'a';  
 if (curr.children[idx] == null)  
 return false;  
 else (curr = curr.children[idx]);  
 }  
 return true;



## Q Count Unique Substrings

Microsoft Google

↳ a string is given count unique number of substrings.

ex- str = "ababa" → ① a ② ab ③ aba ④ abab ⑤ ababa  
ans = 10  
⑥ b ⑦ ba ⑧ bab ⑨ babq ⑩ "" ← empty string.

# If you want all unique strings

↳ unique substring = all prefix of all suffix unique

~~Time~~ ~~Space~~  
• Trie stores unique prefix  $\rightarrow$  count of Node of trie

### Approach

① find all suffix of string

② Create trie and insert all suffix

③ Count nodes of trie

$$\text{root} \xrightarrow{\text{for } i=0 \text{ to } n} \Rightarrow \begin{matrix} \text{Unique} \\ \text{prefix} \end{matrix} = \begin{matrix} \text{Unique} \\ \text{Suff-String} \end{matrix}$$

### suffix

$\rightarrow$  for (int i=0 to n) {

str = str.substring(i)

    insert trie (str)

}

$\Rightarrow$  Count nodes as current in BST

int CountNodes(root) {

    if (root==null)

        Count=0; return 0;

    for (int i=0 to 26) {

        if (root.leftchild[i]==null)

            Count = CountNodes(root.leftchild[i]);

        return Count+1;

As we have 26 letters

so we will check if further node is present or not each time.

## # Longest Word with all Prefixes

$\Rightarrow$  ex- words = ["a", "banana", "app", "appl", "ap", "apply", "apple"]  
ans = "apple"

$\rightarrow$  because a ap app appl apple

apply is also an answer

but apple < apply  
lexicographically

[If any question has ~~goes~~ the solution that goes with prefix remember  
Trie]

so we can solve this question using tree

→ we want a longest word from a tree

whose all eof at each letter is true

→ this means all prefixes of word is present  
in the dictionary

Approach →

count the no. of root → children

↳ ① ! null

② eow = true.

Pseudo Code

→ static String ans = "" // final ans.

void longest word (root, temp){  
 if (root == null) // base case  
 return;

for (int i=0, to 26)

if (root.child[i] != null & child[i].eow == temp)

temp + add char (root)

if (temp len > ans len)

ans = temp

largestword (root.child[i], temp)

temp → delete last char of temp.

Here we did not want to sort the answer as

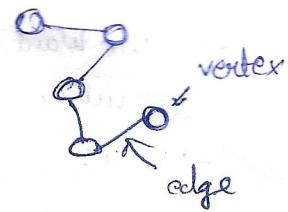
in tree the letters are stored from  $a \rightarrow z$

lexicographical order.

∴ it is already

# # Graph

network nodes



## # Edges

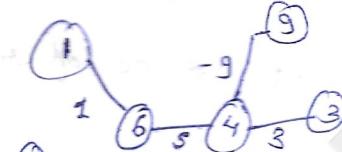
### ① Uni.-Direction



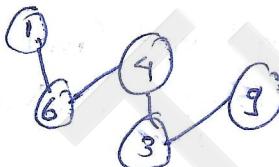
sometimes  
weight of edge

ex-

### ② Bidirectional / Un-Directed



i) weighted undirected



i) unweighted undirected.

## # Storing a Graph

### ① Adjacency List → List of List

### ② Adjacency Matrix

### ③ Edge List

### ④ 2D Matrix (Implicit Graph)

→ Adjacency List → List of List

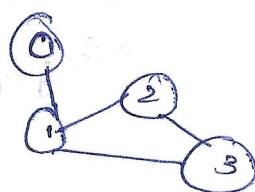
→ example -

→  $0 \rightarrow (1)$  list[0]

$1 \rightarrow (0, 2, 3)$

$2 \rightarrow (1, 3)$

$3 \rightarrow (1, 2)$



→ Data structures we can use

1) ArrayList<ArrayList>

2) Array <ArrayList> ✓ we will go with this

3) hash map <int lists>

## List of Lists

- ① takes no extra space
- ② optimized

## Array of ArrayLists <Edge>

src ✓ distination cut (weighted)  
standard = 1

## Type 2

### Adjacency Matrix.

space  $\rightarrow O(V^2)$

$V$  = vertices.

	0	1	2	3
0	0	1	0	0
1	1	0	1	1
2	0	1	0	1
3	0	1	1	0

$(i, j)$

$i \rightarrow j$  if vertex  $\rightarrow 1$

$i \rightarrow j$  if not  $\rightarrow 0$

### Disadvantages

$\hookrightarrow$  In time complexity  
can go till so big.

## Type 3

Edge List  $\rightarrow$  It stores the information of all the edges

$\rightarrow \{ \{2, 1\}, \{1, 2\}, \{1, 3\}, \{2, 3\} \}$

$\rightarrow$  we use this for some question

if with edges  $\rightarrow \{ \{S, D, W\} \}$

source desti weight

## Type 4

### Graph Implicit Graph

$\hookrightarrow$  In some questions if it is given that you need to go from one point to another in 2D Matrix then it is the use of implicit graph.

## Application of Graph

- 1. Research (map neurons)
- 2. MAPS (sorted network)
- 3. Social Networks.
- 4. Delivery network.
- 5. Physics and Chemistry (molecules).
- 6. Routing of algorithm.
- 7. Machine learning of computational graph
- 8. Dependency Graph ex-servers,
- 9. Computer vision  $\rightarrow$  Image segmentation.
- 10. Graph Databases ex-nebulia.

## # Creating a graph (Adjacency list)

ArrayList<Edge> graph

Edge = (src, dest, weight)

code

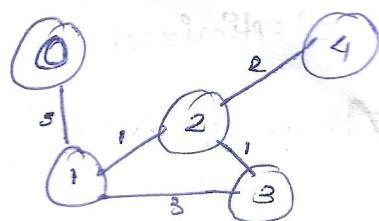
```
static class Edge {
```

```
    int src;  
    int dest;  
    int wt;
```

```
    public Edge(int s, int d, int w) {
```

```
        this.src = s;  
        this.dest = d;  
        this.wt = w;
```

Ex:



0 → {4, 5}

1 → {1, 5} {1, 2, 3} {1, 3, 5}

2 → {2, 1, 3} {2, 3, 1} {2, 4, 2}

3 → {3, 1, 2} {3, 2, 1}

4 → {4, 2, 3}

```
public static void main() {
```

```
    int v = 5;
```

no. of nodes

ArrayList<Edge> [] graph = new ArrayList[v]; // null → const array list

Array of  
ArrayList

which  
stores  
edge

↑  
name

↑  
no.  
of  
vertex

```
for (int i=0; i<v; i++) {
```

```
    graph[i] = new ArrayList<>();
```

// 0-vertex

```
graph[0].add(new Edge(0, 1, 5));
```

// 1-vertex

```
graph[1].add(new Edge(1, 0, 5));
```

```
graph[1].add(new Edge(1, 2, 1));
```

```
graph[1].add(new Edge(1, 3, 3));
```

Same of 2, 3, 4 vertex.

now printing 12's neighbours

```
> for (int i=0; i<graph[2].size(); i++) {  
    |  
    |   Edge e = graph[2].get(i);  
    |  
    |   System.out.print(e.dest);  
|  
|}
```

## # Graph Traversals

can be asked directly  
as a question

- ① Breadth First Search (BFS)
- ② Depth First Search (DFS)

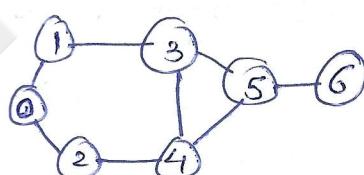
### # Breadth F S → go to immediate neighbour first,

- ↳ we need to have a boolean array of visited
- ↳ because we have cycle.
- ↳ so that each node is visited once.

visited	2	3	4	5	6
---------	---	---	---	---	---

- - ① get on any node
  - ② add its neighbours in Queue.
  - ③ print that node and mark visited.
  - ④ ~~get~~ pop element from Queue
- ↓
  - if visited ✓
    - a) → remove from Queue
    - b) → ④. Pop another element
  - if it is not visited then step
    - a) → ②③④
- ⑤<sup>while</sup> the queue is empty.

ex-



← this code is written in C++.

T.C ⇒  $O(V+E)$  → because we travel all vertices and edges.

Output :

1, 2, 3, 4, 5, 6

But if we used matrix here then the T.C will be  $O(V^2)$  so we used adjacency list.

# DFS → keep going to first neighbour.

(depth first search)

→ can be done using stack, or recursion  
(implicit stack)

Approach

① dfs (graph, curr) {  
curr → visit

then

② for (int i=0 to k)

(!vis[neigh])

dfs (neighbours)

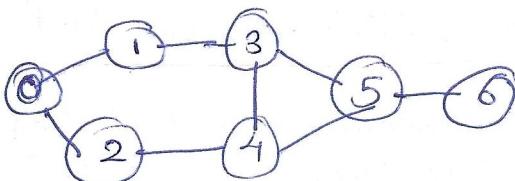
(i)

}

vis[curr] = true

y array of visited

0	1	2	3	4	5	6
0	1	2	3	4	5	6



$$T.C = O(V+E)$$

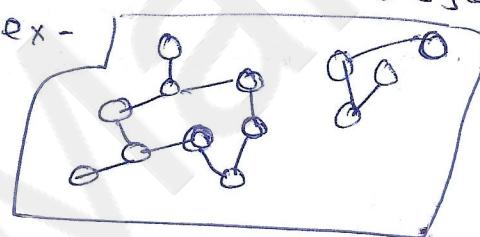
(vertices + edges)

Output : 0, 1, 3, 4, 2, 5, 6

# Q. Has Path ?  $\begin{cases} \text{src} = 0 \\ \text{dest} = 5 \end{cases}$

Is there any path from zero to 5?

→ there can also be disjoint graphs



$$T.C = O(V+E)$$

Approach

haspath(C, src, dest, vis) {

① src = dest return true,

② if (!vis[neigh]) & has path

return true {

return false;

@return