

Q7. An object is suspended in a wind tunnel and the force measured for various winds velocity is given:-

v	10	20	30	40	50	60	70	80
F	25	70	380	550	610	1220	830	1450

We know that for $v=0 \Rightarrow F=0$

\therefore Second-order polynomial regression must PASS through ORIGIN.

$$\Rightarrow y = a_1 x + a_2 x^2$$

This can be written as

$$\begin{bmatrix} x_1 & x_1^2 \\ x_2 & x_2^2 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} a_1 \\ a_2 \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$$

$$X A = Y$$

$$\text{Calculate } A = (X^T X)^{-1} X^T Y$$

where $X = \begin{bmatrix} 10 & 100 \\ 20 & 400 \\ 30 & 900 \\ 40 & 1600 \\ 50 & 2500 \\ 60 & 3600 \\ 70 & 4900 \\ 80 & 6400 \end{bmatrix}$ $Y = \begin{bmatrix} 25 \\ 70 \\ 380 \\ 550 \\ 610 \\ 1220 \\ 830 \\ 1450 \end{bmatrix}$

$$(X^T X)^{-1} = 10^{-3} \begin{bmatrix} 0.7984 & -0.0118 \\ -0.0118 & 0.0002 \end{bmatrix}$$

this gives us $\Rightarrow a_1 = 7.7710$ $a_2 = 0.1191$