

# Information Retrieval

## Topic- Scoring, Term Weighting, The Vector Space Model (tf-idf weighting)

### Lecture-24

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# Content

- Collection frequency
- Document frequency
- tf-idf weighting

# Frequency in document vs. frequency in collection

- In addition, to term frequency (the frequency of the term in the document) . . .
- . . .we also want to use the frequency of the term in the collection for weighting and ranking.

# Desired weight for rare terms

- Rare terms are more informative than frequent terms.
- Consider a term in the query that is rare in the collection (e.g., arachnocentric).
- A document containing this term is very likely to be relevant.
  - We want high weights for rare terms like arachnocentric.

# Desired weight for frequent terms

- Frequent terms are less informative than rare terms.
- Consider a term in the query that is frequent in the collection (e.g., GOOD, INCREASE, LINE).
- A document containing this term is more likely to be relevant than a document that doesn't . . .
- . . . but words like GOOD, INCREASE and LINE are not sure indicators of relevance.
- → For frequent terms like GOOD, INCREASE, and LINE, we want positive weights . . .
- . . . but lower weights than for rare terms.

# Document frequency

- We want high weights for rare terms like ARACHNOCENTRIC.
- We want low (positive) weights for frequent words like GOOD, INCREASE, and LINE.
- We will use document frequency to factor this into computing the matching score.
- The document frequency is the number of documents in the collection that the term occurs in.

# idf weight

- $df_t$  is the document frequency, the number of documents that  $t$  occurs in.
- $df_t$  is an inverse measure of the informativeness of term  $t$ .
- We define the idf weight of term  $t$  as follows:
- $idf_t = \log_{10} (N/df_t)$   
( $N$  is the number of documents in the collection.)
- $idf_t$  is a measure of the informativeness of the term.
- $[\log N/df_t]$  instead of  $[N/df_t]$  to “dampen” the effect of idf
- Note that we use the log transformation for both term frequency and document frequency.

# Examples for idf

- Compute  $\text{idf}_t$  using the formula:  $\text{idf}_t = \log_{10} (1,000,000 / \text{df}_t)$

term	$\text{df}_t$	$\text{idf}_t$
calpurnia	1	6
animal	100	4
sunday	1000	3
fly	10,000	2
under	100,000	1
the	1,000,000	0



# Effect of idf on ranking

- idf affects the ranking of documents for queries with at least two terms.
- For example, in the query “arachnocentric line”, idf weighting increases the relative weight of ARACHNOCENTRIC and decreases the relative weight of LINE.
- idf has little effect on ranking for one-term queries.

# Collection frequency vs. Document frequency

- Collection frequency of  $t$ : number of tokens of  $t$  in the collection
- Document frequency of  $t$ : number of documents  $t$  occurs in

Word	cf	df
try	10422	8760
Insurance	10440	3997

# tf-idf weighting

- The tf-idf weight of a term is the product of its tf weight and its idf weight.

$$w_{t,d} = (1 + \log \text{tf}_{t,d}) \cdot \log (N / \text{df}_t)$$

- tf-weight
- idf-weight
- Best known weighting scheme in information retrieval
- Alternative names: tf.idf is tf x idf

# tf-idf

- Assign a tf-idf weight for each term  $t$  in each document  $d$ :

$$w_{t,d} = (1 + \log \text{tf}_{t,d}) \cdot \log (N / \text{df}_t)$$

- The tf-idf weight . . .
  - . . . increases with the number of occurrences within a document. (term frequency)
  - . . . increases with the rarity of the term in the collection. (inverse document frequency)

# Term, collection and document frequency

Quantity	Symbol	Definition
term frequency	$tf_{t,d}$	number of occurrences of $t$ in $d$
document frequency	$df_t$	number of documents in the collection that $t$ occurs in
collection frequency	$Cf_t$	total number of occurrences of $t$ in the collection

Consider the 1<sup>st</sup> table of term frequencies for 3 documents denoted Doc1, Doc2, Doc3. Compute the tf-idf weights for the terms car, auto, insurance, best, for each document, using the idf values given below.

	Doc1	Doc2	Doc3
car	27	4	24
auto	3	33	0
insurance	0	33	29
best	14	0	17

Term frequencies for 3 documents

term	$df_t$	$idf_t$
car	18,165	1.65
auto	6723	2.08
insurance	19,241	1.62
best	25,235	1.5

idf's of terms with various frequencies in the Reuters collection of 806,791 documents

Thank You