



- Notes :
1. All questions carry marks as indicated.
 2. Solve Question 1 OR Questions No. 2.
 3. Solve Question 3 OR Questions No. 4.
 4. Solve Question 5 OR Questions No. 6.
 5. Solve Question 7 OR Questions No. 8.
 6. Solve Question 9 OR Questions No. 10.
 7. Use of non programmable calculator is permitted.

1. a) If $L\{tf(t)\} = -\frac{d}{ds}\bar{f}(s)$, then find $L\{t \cos 2t\}$. 4

b) Find $L^{-1}\left\{\frac{s}{(s^2 + a^2)^2}\right\}$ by convolution theorem. 5

c) Find the Fourier sine transform of $e^{-|x|}$ and hence show that 5
$$\int_0^{\infty} \frac{x \sin mx}{1+x^2} dx = \frac{\pi}{2} e^{-m}, m > 0$$

OR

2. a) $\frac{d^2y}{dt^2} + 2\frac{dy}{dt} + 5y = e^{-t} \sin t, y(0) = 0$ and $y'(0) = 1$, using Laplace transform. 7

b) Express $f(x) = \begin{cases} 1, & |x| < 1 \\ 0, & |x| > 1 \end{cases}$, as Fourier integral and hence evaluate $\int_0^{\infty} \frac{\sin \lambda}{\lambda} d\lambda$. 7

3. a) Find z - transform of $\frac{1}{n+1}$. 7

b) Find inverse z - transform of $\frac{z^2 + z}{(z-1)(z^2+1)}$ by partial fraction method. 7

OR

4. a) Solve $y_{n+2} + 3y_{n+1} + 2y_n = u_n$, given that $y_0 = 1, y_n = 0$ for $n < 0$. 7

b) Find inverse z - transform of $\frac{z^3}{(z-2)^3}, |z| > 2$. 7

5. a) Investigate the linear dependence of the vectors 7
 $X_1 = (1, 2, 4), X_2 = (2, -1, 3)$
 $X_3 = (0, 1, 2), X_4 = (-3, 7, 2)$
and if possible find the relation between them.

- b) Use Sylvester's theorem to show that $\sin^2 A + \cos^2 A = I$, where $A = \begin{bmatrix} 1 & 2 \\ -1 & 4 \end{bmatrix}$. 7

OR

6. a) Find the singular values decomposition of the matrix $A = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}$. 7

- b) Find largest eigen value and corresponding eigen vector for the matrix $A = \begin{bmatrix} -4 & -5 \\ 1 & 2 \end{bmatrix}$. 7

7. a) Let X be the random variable having density function 7

$$f(x) = \begin{cases} e^{-x}, & x \geq 0 \\ 0, & x < 0 \end{cases}$$

Find (i) $E(X)$ (ii) $\text{Var}(X)$ (iii) σ_X

- b) An insurance salesman sells policies to 5 men all of identical age and in good health. The probability that a man of this particular age will be alive 30 yrs. is $2/3$. Find the probability that in 30 yrs, (i) all 5 men, (ii) at least 3 men (iii) only 2 men (iv) at least 1 man (v) at most 1 man will be alive. 7

OR

8. a) A random variable X has density function given by, 7

$$f(x) = \begin{cases} 2e^{-2x}, & x \geq 0 \\ 0, & x < 0 \end{cases}$$

Find the moment generating function and also first four moment about the origin.

- b) If the probability that an individual suffers a bad reaction from injection of a given serum is 0.001, determines the probability that out of 2,000 individuals
a) exactly 3 b) more than 2 c) at least 4 will suffer a bad reaction. 7

9. a) Find multiple linear regression equation of X_1, X_2 and X_3 from the data relating to three variables given below: 7

X_1	4	6	7	9	13	15
X_2	15	12	8	6	4	3
X_3	30	24	20	14	10	4

- b) Calculate mode for the following frequency distribution. 7

Size	0 - 5	5 - 10	10 - 15	15 - 20	20 - 25	25 - 30	30 - 35	35 - 40
Frequency	9	12	15	16	17	15	10	13

OR

10. a) The following are the marks of 150 students in an examination. 7

Marks	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80
No. of Students	10	40	20	0	10	40	16	14

Calculate Karl Person's coefficient of Skewness.

- b) Find the measure of Skewness on the basis of moments. 7

x	2	3	4	5	6
f	1	3	7	3	1
