

ARTIFICIAL INTELLIGENCE II



UNIT-6

Symbolic Reasoning Under Uncertainty



Objectives of unit 6

- 6.1 Introduction To Nonmonotonic Reasoning**
- 6.2 Logics For Non-monotonic Reasoning**

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6.1 Introduction To Nonmonotonic Reasoning

- **Symbolic reasoning under uncertainty** deals with situations where knowledge is incomplete, inconsistent, or subject to change.
 - Traditional logic assumes that knowledge is static and complete, but real-world scenarios often involve uncertainty.
- **Nonmonotonic reasoning** provides a framework to reason in dynamic and uncertain environments where conclusions can be revised.



6.1 Introduction To Nonmonotonic Reasoning

Nonmonotonic Reasoning

Definition: Nonmonotonic reasoning is a type of reasoning where adding new knowledge can invalidate previous conclusions.

- It models real-world reasoning, handling incomplete or evolving knowledge.

Key Characteristics:

1. Revisable Conclusions:

- Conclusions may be withdrawn if new evidence contradicts them.
- Example: "Birds fly" is revised when we learn about penguins.

2. Default Reasoning:

- Assumes defaults unless proven otherwise.
- Example: Assume someone is alive unless there's evidence they are not.

3. Handles Incomplete Knowledge:

- Works with limited or uncertain information to infer conclusions.



6.1 Introduction To Nonmonotonic Reasoning

Applications of Nonmonotonic Reasoning

- **Expert Systems:** Revising medical diagnoses as new symptoms are observed.
- **Autonomous Agents:** Adjusting plans in dynamic environments.
- **Knowledge Representation:** Modeling laws, ethics, or any domain with evolving rules.



6.2 Logics for Nonmonotonic Reasoning

1. Default Logic

- **Introduced by:** Raymond Reiter (1980).
- Uses **default rules** to infer conclusions unless contradicted.
- A default rule has the form: **$A : B / C$**
- If A (precondition) is true and B (justification) is consistent, conclude C.
- **Example:** Rule: "If an animal is a bird and it's consistent that it can fly, assume it can fly."
- **Default:** $\text{Bird}(x) : \text{CanFly}(x) / \text{CanFly}(x)$
- If $\text{Bird}(\text{Tweety})$ and no evidence against $\text{CanFly}(\text{Tweety})$, conclude $\text{CanFly}(\text{Tweety})$.



6.2 Logics for Nonmonotonic Reasoning

2. Autoepistemic Logic

- Focuses on reasoning about an agent's knowledge of itself. Introduces the modal operator L to represent "known" facts. Example: $\neg L(A)$ means "I do not know A ." Example: If an agent knows $L(\text{Bird}(\text{Tweety}))$ but does not know $L(\text{CanFly}(\text{Tweety}))$, it reasons about the lack of knowledge to infer.



6.2 Logics for Nonmonotonic Reasoning

3. Circumscription

Minimizes abnormalities by assuming normality unless specified otherwise.

If $\text{Abnormal}(x)$ represents "x is abnormal," circumscription minimizes $\text{Abnormal}(x)$.

Example: Knowledge Base:

- $\text{Bird}(x) \rightarrow \text{CanFly}(x)$
- $\text{Abnormal}(x) \rightarrow \neg \text{CanFly}(x)$

Circumscription assumes $\text{Abnormal}(x)$ is false unless explicitly stated (e.g., penguins are abnormal birds).



6.2 Logics for Nonmonotonic Reasoning

4. Logic Programming with Negation as Failure

Assumes a statement is false if it cannot be proven true.

Commonly used in Prolog.

Example: Rule: CanFly(X) :- Bird(X), not Abnormal(X).

If Bird(Sparrow) and no evidence of Abnormal(Sparrow), conclude CanFly(Sparrow).

5. Modal Nonmonotonic Logics

Uses modal operators like \Box (necessarily) and \Diamond (possibly) to reason about uncertainty.

Example:

$\Box P \rightarrow Q$ means "If P is necessarily true, then Q."



6.2 Logics for Nonmonotonic Reasoning

Symbolic Reasoning Under Uncertainty

1. Bayesian Logic

Combines probabilistic reasoning with symbolic representation.

Example: "Given symptoms S , what is the probability of disease D ?"

2. Fuzzy Logic

Handles vague and imprecise information.

Example: "The room is warm" might have a truth value of 0.8.

3. Dempster-Shafer Theory

Represents degrees of belief instead of strict probabilities.

4. Markov Logic Networks

Combines first-order logic with probabilistic graphical models.



Conclusion

- Nonmonotonic reasoning provides a foundation for reasoning under uncertainty, enabling systems to adapt to new information.
- It is widely used in AI applications like expert systems, autonomous agents, and knowledge representation.
- The choice of nonmonotonic logic depends on the application and computational constraints.

