

Observations regarding the nature of trajectory

- We can observe early stable $N_1 - N_2$ equilibrium if β is small enough i.e. $\beta < 10^{-4}$. For example Figure_1 .
- We can observe that for less value of α , the difference between number of prey & predators is more as compared to those in higher α -value before convergence.
- We can observe $N_2 \rightarrow 0$ if β too large where $\beta=0.8$. For example Figure_3
- The growth trajectories seem to follow the rationale that
- More Prey \Rightarrow More Predator \Rightarrow Less Prey \Rightarrow Less Predator \Rightarrow More Prey
- This reasoning yields two oscillatory curves describing the two species, with the prey population curve leading to the predator population curve, as seen in the map.
- The populations' trajectories are therefore convergent, meaning that the amplitudes of the oscillations seem to decrease as time progresses. This is a direct result of the logistical essence of the prey population's development.
- We can observe in Figure_4 that when $r=1$ that means prey grows logistically with intrinsic growth rate of 1, the predator consumes all the preys & get almost extinct , then again preys grow in number & predator consumes them & so on infinite cycle.
- All the images have been stored in images folder.

Figure 1

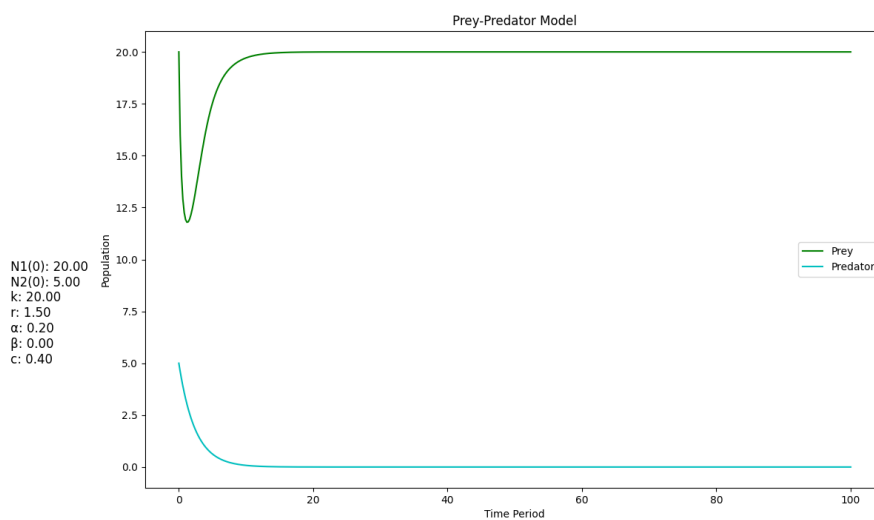


Figure 2

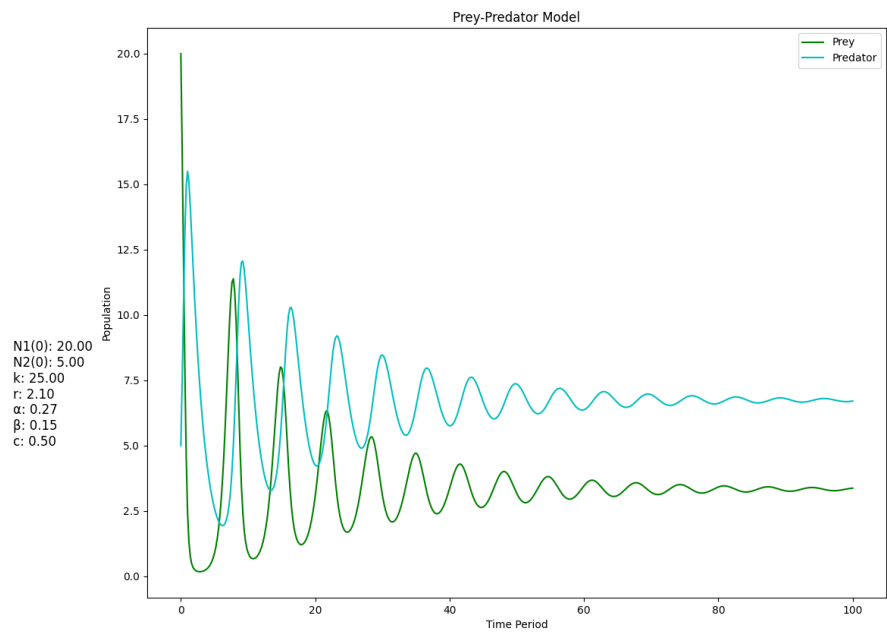


Figure 3

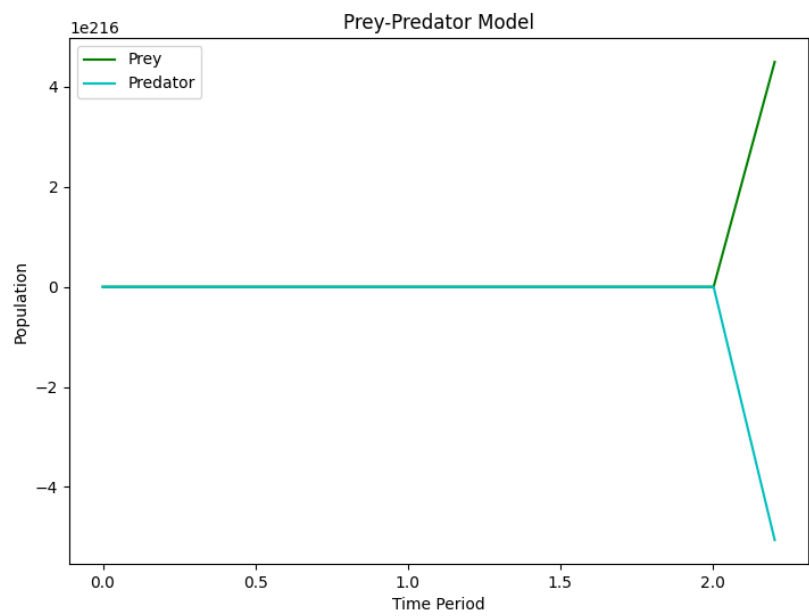
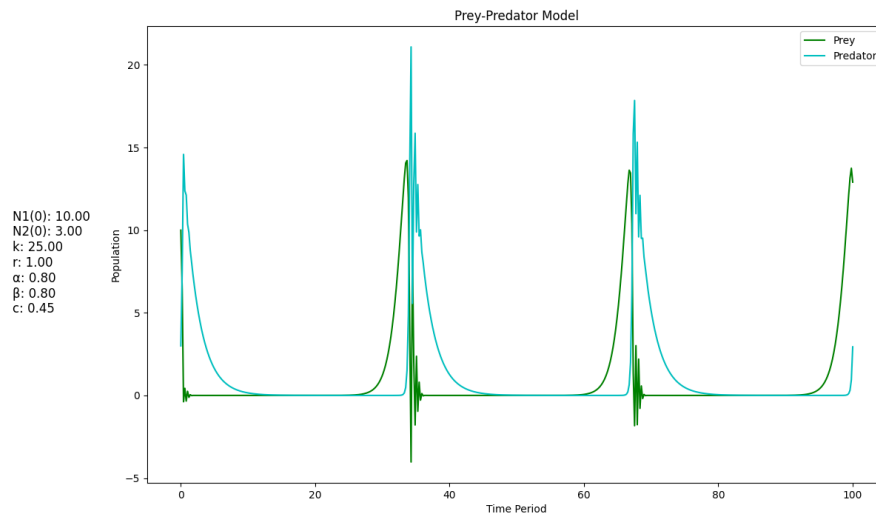


Figure 4



Different Values used to run code:

```

initial_N1 = [20, 20, 20, 10]
initial_N2 = [5, 5, 5, 3]
initial_r = [1.5, 2.1, 2.5, 1]
initial_α = [0.2, 0.27, 0.8, 0.8]
initial_β = [0.0001, 0.15, 0.8, 0.8]
initial_c = [0.4, 0.5, 0.45, 0.45]
initial_k = [20, 25, 25, 25]
initial_t = [100, 100, 100, 100]
initial_i = [500, 500, 500, 500]

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