



✓ **Congratulations! You passed!**

TO PASS 80% or higher

Keep Learning

GRADE
100%

Quiz 5

LATEST SUBMISSION GRADE

100%

1. Which of the following statements is false?

1 / 1 point

- ☐ Hybrid automata consist of modes, guards, transitions, and resets.
- ☐ Even though the individual modes are stable, the composite hybrid system need not be stable.
- ☐ Certain types of Zeno behaviors can be removed by introducing a new mode.
- ☐ The Zeno phenomenon should be addressed when designing hybrid control systems.
- ☒ Existential stability implies universal stability.

✓ **Correct**

This question tests several of the concepts introduced in lecture this week.

2. Consider the switched system

1 / 1 point

$$\dot{x} = \begin{cases} x & \text{if } x \leq 1 \\ -2x & \text{if } x > 1. \end{cases}$$

This system is Type 1 Zeno. What is the induced mode?

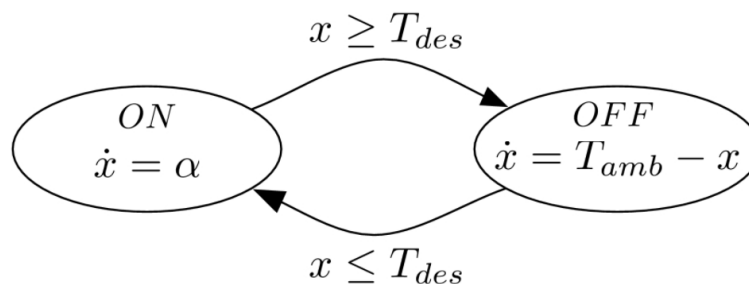
- ☐ $\dot{x} = 1$
- ☐ $\dot{x} = -x$
- ☐ $\dot{x} = x$
- ☐ $\dot{x} = -1$
- ☒ $\dot{x} = 0$

✓ **Correct**

Draw the regularized hybrid automata that corresponds with this system and compute the dynamics for the induced mode.

3. Below is shown a model of a thermostat in a building. In the model, x is the temperature and in the ON-mode, the thermostat is increasing the temperature at a rate of $\alpha > 0$, while in the OFF-mode, the thermostat is simply off. What this means is that the temperature will exponentially decay down to the ambient temperature T_{amb} . Moreover, the desired temperature in the thermostat is set to T_{des} , where we assume that $T_{des} > T_{amb}$.

1 / 1 point



Why is the hybrid automaton a bad thermostat?

- ☐ It is a Type 2 Zeno system.
- ☒ Once $x = T_{des}$ it will switch infinitely fast between the two modes.
- ☐ Once $x = T_{amb}$ it will switch infinitely fast between the two modes.
- ☐ There is nothing wrong with the hybrid automaton.

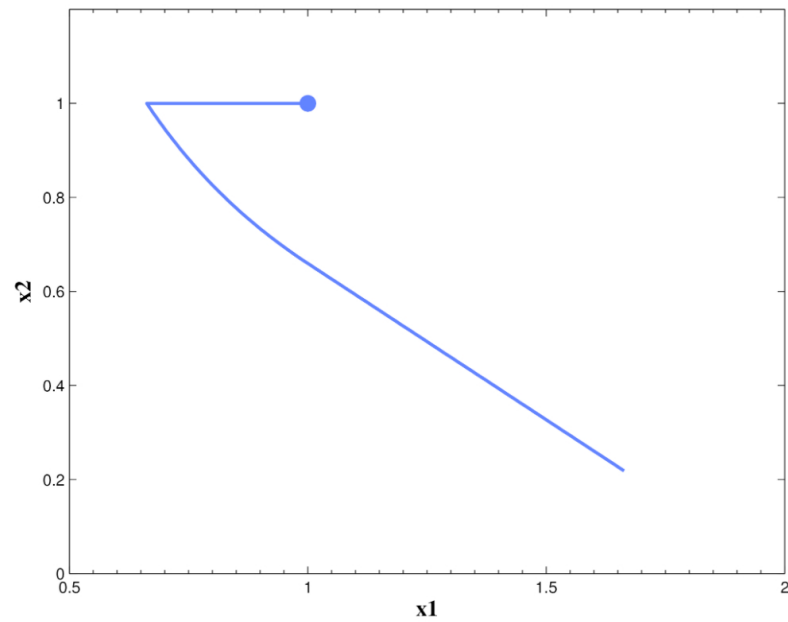
☐ It will never reach the desired temperature T_{des} .

✓ Correct

Think through the behavior of this automaton to answer the question.

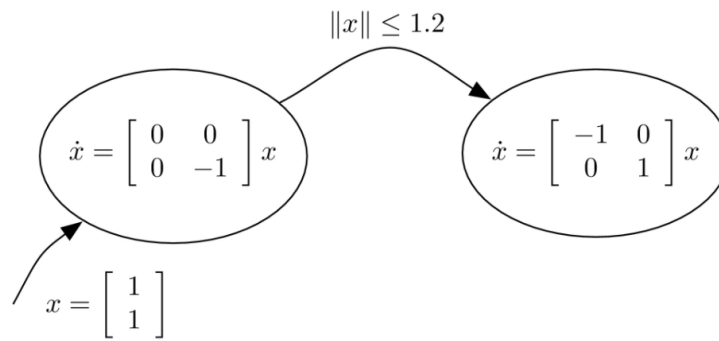
4. Consider the plot shown below, where the initial condition is $(x_1, x_2) = (1, 1)$ is marked by a solid circle.

1 / 1 point

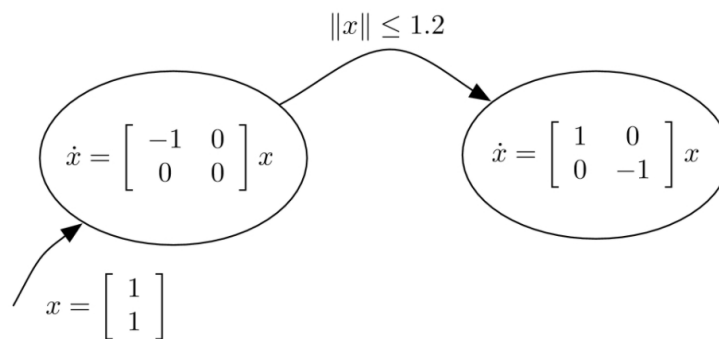


Which Hybrid Automaton was used to generate this plot?

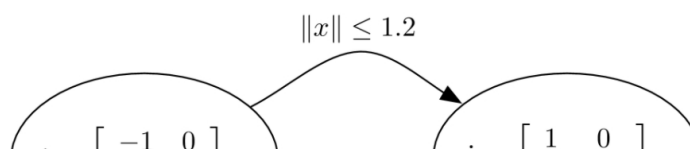
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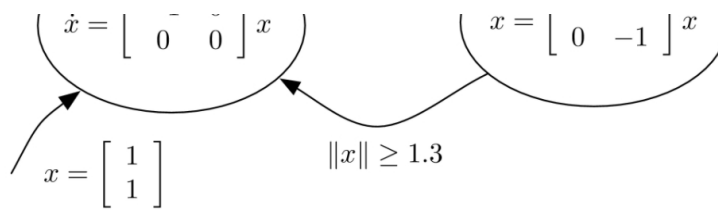


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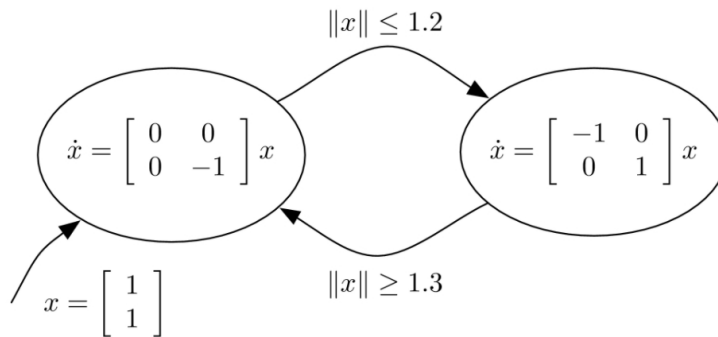


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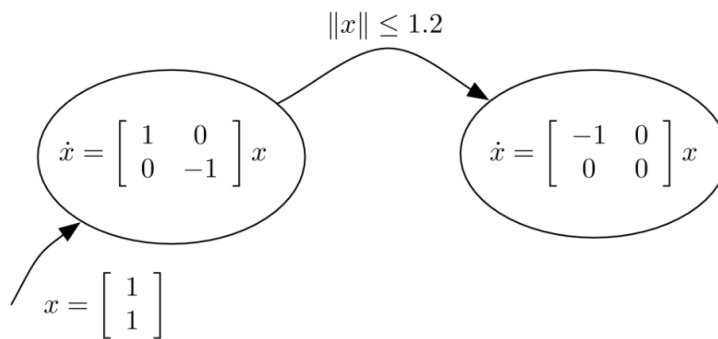




☐



☐



✓ Correct

Try to think about the switching condition and dynamics in each state separately. It may also be helpful to write out the equations for \dot{x} (taking it out of matrix form).

5. Why do we care about hybrid systems when designing robotic controllers?

1 / 1 point

- ☐ The environment is unknown and we cannot design a single controller that deals with all possible environmental conditions the robot may encounter.
- ☐ It connects to how biological systems, e.g., animals, are thought to behave.
- ☐ It makes the design task modular in that new functionality can be added onto already existing control structures.
- ☒ They all are valid concerns.
- ☐ It makes the design easier in that the design task is broken down into building blocks.

✓ Correct

This question requires you to think back to all the discussions we've had about robotics in this course.