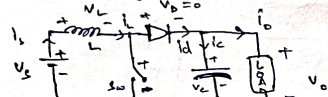


Electric Vehicles

Step-Up Regulator [Boost Converter]



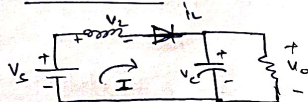
$$i_d = i_c + i_o$$

switch ON

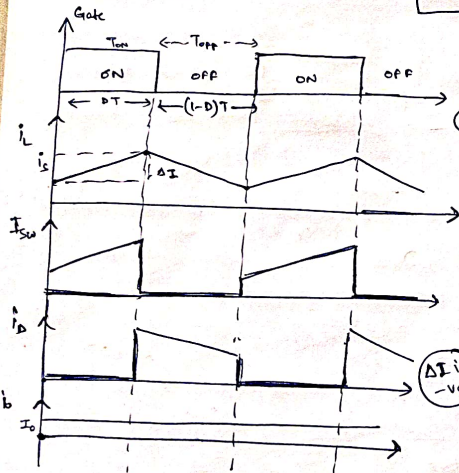


LSD

switch OFF



Working of Boost Converter
switch is ON / OFF



$$V_s - V_L = 0$$

$$V_s = L \frac{di}{dt}$$

$$V_s = L \frac{\Delta I}{T_{ON}}$$

$$T_{ON} = \frac{L \Delta I}{V_s} \quad (1)$$

$$V_s - V_L - V_o = 0$$

$$V_s + L \frac{\Delta I}{T_{OFF}} - V_o = 0$$

$$T_{OFF} = \frac{V_o - V_s}{L \Delta I} \quad (2)$$

$$(1) \geq (2)$$

$$L \Delta I = V_s \cdot T_{ON} = T_{OFF} (V_o - V_s)$$

$$\Rightarrow V_s = D T = (V_o - V_s) (1 - D) T$$

$$\Rightarrow \frac{V_o - V_s}{V_s} = \frac{D}{1 - D}$$

$$\Rightarrow \frac{V_o}{V_s} = \frac{1}{1 - D}$$

Since $0 < D < 1$, so

$$V_o \geq V_s \quad \text{step up}$$

step up

$$\Delta I_L = \frac{V_s D \cdot I_o}{L} = \frac{V_s \cdot D}{f L}$$

Find ΔI ΔV_c
charging & Discharging

may show linear (no parabola)

$$T_{ON} + T_{OFF} = T$$

$$T \cdot \frac{L \Delta I}{V_s} + \frac{L \Delta I}{(V_o - V_s)} = \frac{1}{f}$$

$$\Delta I = \frac{V_s D}{f L}$$

Ripple in Input Current

$$\# V_c = \frac{1}{C} \int i_c dt$$

$$\Delta V_c = \frac{1}{C} \int_0^{T_{ON}} I_o dt = \frac{I_o \cdot T_{ON}}{C} = \frac{I_o \cdot D}{C \cdot f}$$

Critical Values of L & C

when $i_L(\min) = 0$

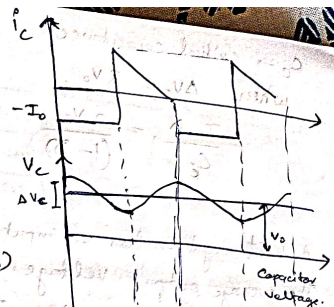
$$\Delta I = 2 I_L = 2 I_s$$

$$\Rightarrow \frac{V_s D}{L \cdot f} = 2 \times \left(\frac{V_o \cdot I_o}{V_s} \right)$$

$$\Rightarrow \frac{V_s D}{L \cdot f} = 2 \times \frac{V_o \cdot I_o}{V_s (1 - D)}$$

$$L_c = \frac{V_s \cdot D \cdot (1 - D)}{2 \times I_o \times f}$$

critical inductance.



Capacitor Voltage.

$$\Delta V_c = \frac{I_o \cdot D}{C \cdot f}$$

$$\Delta I = \left(\frac{V_s D}{V_o} \right) \left(\frac{1}{f L} \right) (V_s - V_o)$$

$$\Delta I = \frac{V_s D}{f L}$$

$$\Delta V_c = \frac{I_o \cdot D}{C \cdot f}$$

$$\Delta I = \frac{V_s D}{f L}$$

$$\Delta V_c = \frac{I_o \cdot D}{C \cdot f}$$

$$\Delta I = \frac{V_s D}{f L}$$

$$\Delta V_c = \frac{I_o \cdot D}{C \cdot f}$$

$$\Delta I = \frac{V_s D}{f L}$$

$$\Delta V_c = \frac{I_o \cdot D}{C \cdot f}$$

$$\Delta I = \frac{V_s D}{f L}$$

$$\Delta V_c = \frac{I_o \cdot D}{C \cdot f}$$

$$\Delta I = \frac{V_s D}{f L}$$

$$\Delta V_c = \frac{I_o \cdot D}{C \cdot f}$$

$$\Delta I = \frac{V_s D}{f L}$$

$$\Delta V_c = \frac{I_o \cdot D}{C \cdot f}$$

$$\Delta I = \frac{V_s D}{f L}$$

$$\Delta V_c = \frac{I_o \cdot D}{C \cdot f}$$

$$\Delta I = \frac{V_s D}{f L}$$

$$\Delta V_c = \frac{I_o \cdot D}{C \cdot f}$$

$C_c \rightarrow$ critical capacitance.

When $\Delta V_c = 2V_o$

$$\frac{I_o \cdot D}{C_c f} = \frac{2V_o}{(1-D)} \Rightarrow C_c = \frac{I_o \cdot D \cdot (1-D)}{2 \cdot V_o \cdot f}$$

A boost regulator has an input voltage of $V_s = 15V$. The average output voltage is $(15V = V_o)$. Average load current $I_o = 0.5$ Amp. The switching frequency is $f = 25KHz$. If $L = 150 \mu H$, $C = 220 \mu F$

Determine:

- Duty cycle (D)
- Ripple current of Inductor (ΔI)
- Peak current of Inductor
- Ripple Voltage of Filter Capacitor (ΔV_c)
- Critical Value of L_c & C_c

(a) $D = \frac{V_o}{V_s} = \frac{15}{15} = 1$ $\Rightarrow 1-D = \frac{V_s}{V_o} = \frac{1}{3}$ $\Rightarrow D = \frac{2}{3} = 0.67$

(b) $\Delta I = \frac{V_s \cdot D}{f \cdot L} = \frac{15 \cdot \frac{2}{3}}{25 \cdot 10^3 \cdot \frac{1}{3}} = \frac{10^3 \times 2}{5 \times 3 \times 150} = 0.88 A$

(c) $I_{peak} = I_s + \frac{\Delta I}{2} = \frac{V_o \cdot I_o}{V_s} + \frac{0.88}{2} = \frac{15 \cdot 0.5}{15} + 0.44 = 1.5 + 0.44 = 1.94 A$

(d) $\Delta V_c = \frac{I_o \cdot D}{f \cdot C} = \frac{0.5 \cdot \frac{2}{3}}{25 \cdot 10^3 \cdot \frac{1}{3}} = \frac{10^3 \times 1}{25 \times 220} = 0.181 V$

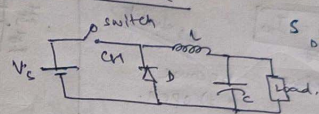
(e) $L_c = \frac{5 \times \frac{2}{3} \times \frac{1}{3}}{2 \times 0.5 \times 25 \cdot 10^3} = \frac{1}{5} \times \frac{2}{5} \times 10^{-3} = 44 \mu H$

$C_c = \frac{0.5 \times \frac{2}{3} \times \frac{1}{3}}{2 \times 5 \times 25 \cdot 10^3} = 0.44 \mu F$

Buck Converter

Step Down Chopper

DC-DC Converter

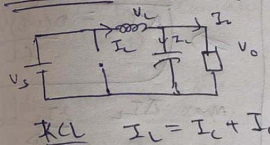


$0 < t < T_{on} \Rightarrow CH \Rightarrow ON \quad D \Rightarrow OFF$

$T_{on} < t < T \Rightarrow CH \Rightarrow OFF \quad D \Rightarrow ON$

$D = \frac{T_{on}}{T}$

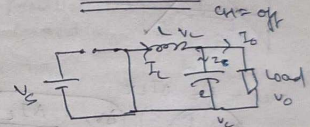
$0 < t < T_{on} \quad (CH=ON)$



$KVL \quad I_L = I_c + I_o$

$KVL \quad V_L = (V_s - V_o)$

$T_{on} < t < T$



$KVL \rightarrow I_L = I_c + I_o$

$KVL \rightarrow V_L = -V_o$

for inductor, Volt Sec Balance (VSB)

$\Rightarrow L \frac{di}{dt} = V_L$ charging = Discharging. $\int V_L dt = 0$

in Capacitor, Amp-sec Balance.

$I_L = C \frac{dv_c}{dt} \quad \int dv_c = \frac{1}{C} \int I_c dt$

$\Delta V_c = 0$
average cap current = 0

Avg o/p voltage (VSB)

$\int V_L dt = 0$

$(V_s - V_o) T_{on} + (-V_o)(T - T_{on}) = 0$

$(V_s - V_o) D = V_o$

$V_o = D V_s$

$V_o < V_s$

Avg inductor current

$$\int I_L dt = 0$$

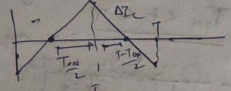
$$(I_L - I_o) T_{ON} + (I_L - I_o) (T - T_{ON}) = 0$$

$$I_L = I_o$$

Avg = DC value because $C \Rightarrow$ open.
AC current

Ripple in o/p voltage

$$I_c = I_L - I_o$$



$$\text{area} = \Delta I_L T$$

$$\Delta V_c = \frac{\Delta I_L}{8fc}$$

Ripple in o/p voltage

Critical Inductance

$$I_L = \frac{\Delta I_L}{2}$$

$$I_o = \frac{D(1-D)V_c}{2fLc}$$

$$\frac{DV_c}{R} = \frac{D(1-D)V_c}{2fLc}$$

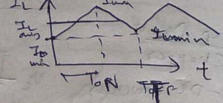
$$L_c = \frac{(1-D)R}{2f}$$

$$\{I_{max} = I_c + \frac{\Delta I_L}{2}\}$$

$$I_o(\text{avg}) = I_o(\text{avg}) \sqrt{1-D}$$

Ripple in inductor current

$$\Delta I_L = I_{max} - I_{min}$$



$$0 < t < T_{ON}$$

$$V_L = L \frac{\Delta I_L}{T_{ON}} = V_s - V_o$$

$$\Delta I_L = (V_s - V_o) DT$$

$$\Delta I_L = \frac{D(1-D)V_s}{fL}$$

$$\text{max } \Delta I_L \quad \frac{dI_L}{dt} = 0$$

$$\text{at } D = 0.5$$

$$(\Delta I_L)_{max} = 0.5 \times 0.5 \frac{V_s}{fL}$$

$$\text{max supply} = \frac{V_s}{4fL}$$

Critical Capacitance

$$(V_o(\text{min}) = 0) \rightarrow V_o = \frac{DV_c}{2}$$

$$V_o - \frac{\Delta V_o}{2} = 0$$

$$\Delta V_o = \frac{\Delta V_o}{2}$$

$$P_{Vs} = \frac{\Delta I_L}{2 \cdot 8fc} = \frac{V_s D(1-D)}{16f^2 L}$$

$$C_c = \frac{1}{4fR}$$

Buck Boost Converter

reducibility of V_o is different w.r.t V_s

$$V_o = \frac{V_s \cdot D}{1-D}$$

$0 < D < 0.5$ $V_o < V_s$ Buck SD
 $0.5 < D < 1$ $V_o > V_s$ Boost SU

$$I_L = \frac{I_o}{1-D}$$

$$\Delta I_L = \frac{DV_s}{fL} \text{ (Boost)}$$

$$\Delta V_c = \frac{I_o D}{fc} \text{ Boost}$$

L_c & I_c same as Boost

$$C_c = \frac{D}{2fR}$$

Avg supply current
 $V_s I_s = V_o I_o$

Multiphase Buck Converter (Interleave)

Parallel connection

Motor, Inverter, Charger, Fuel Tank, Engine, Control Module

Chargers standards

- CCS
- CHAdeMO
- SAE J1772
- Tesla Supercharger

wireless chargers
Inductive → Resonant
Magnetic

Under infinite energy source



Adjustable

Energy Sources

$$E = V + \frac{1}{2} mv^2 + mgh$$

$$E = \frac{1}{2} Li^2 + \frac{1}{2} CV^2$$

$$P_{loss} = \alpha P^2 + P_o (SOE(t))$$

$$P = \frac{dE}{dt}$$



$$\rightarrow E_{\text{loss cycle}} = \int P_{loss} = \alpha P^2 + P_o SOE(t) dt$$

$$\Rightarrow SOE(t) = SOE(t_0) + \frac{\int P(t) - P_{load}(t) dt}{E_{stored}}$$



$$\eta_{round} = \frac{\text{Energy Delivered}}{\text{Energy Supplied}}$$

Energy Supplied = 10 kWh.
 Energy Stored = 9 Wh.
 Energy Delivered during Disch = 8.5 kWh.

$$\eta_{\text{max}} = \frac{\text{Energy Delivered}}{\text{Energy Supplied}} \times 100$$

$$\eta_{\text{max}} = \frac{8.5}{10} \times 100 = 85\%$$

$$I = C \frac{dV}{dt}$$

$$\text{DOD} = \frac{\int i_{\text{dis}} dt}{\text{Capacity}}$$

$$= \frac{\text{Initial} - \text{Final}}{\text{Initial}} \times 100 = \frac{100 - 60}{100} \times 100 = 40\%$$

$$(1) \text{ DOD after 5 hrs} = 40\%$$

$$(2) \text{ SOC} = \frac{\text{Remain Capacity}}{\text{Initial Capacity}} = \frac{60}{100} \times 100 = 60\%$$

$$\text{DOD} = 1 - \text{SOC} = 1 - 0.6 = 0.4$$

(3) Average Current Drawn

$$I = \frac{P}{V} = \frac{500}{12} = 41.67 \text{ A}$$

(4) Power = VI

$$60 \text{ Ah} = 41.67 \times t$$

$$t = \frac{60 \times 3}{12.5} = \frac{12 \times 3}{2.5} = \frac{36}{2.5} = 14.4 \text{ h}$$

SAC 31772

Chadano

Combined charging system.

CCT

$$V_o = DV_s, \Delta I_L = \frac{D(1-D)V_c}{fL}, \Delta V_c = \frac{\Delta I_L}{8fc}, \text{SDL}$$

$$(I_{\text{dis}})_{\text{avg}} = D I_L, (I_o)_{\text{avg}} = (1-D) I_L, Q = \frac{1}{4fR} \left(\frac{I_o}{I_L} \right)$$

Boost

$$V_o = \frac{V_c}{1-D}, I_L = \frac{I_o}{1-D}, \Delta I_L = \frac{DV_c}{fL}, \Delta V_c = \frac{I_o D}{fc}$$

$$L_c = \frac{R(1-D)^2 D}{2f}, C_c = \frac{D}{2fR}$$

Boost

$$V_o = \frac{D}{1-D} V_s$$

$$V_o = \frac{V_c}{(1-D) + \frac{r}{R(1-D)}}, \frac{V_o}{V_s} = \frac{D}{(1-D) + \frac{r}{R(1-D)}}$$

PPC

$$P_{\text{ac}} = V_{\text{ac}} \times I_{\text{ac}}, V_{\text{ac}} = \sqrt{2} V_{\text{ph}} \cos \theta, I_{\text{ac}} = \sqrt{2} I_{\text{ph}} \cos \theta$$

$$P_{\text{ac}} = 2 V_{\text{ph}} I_{\text{ph}} \cos^2 \theta$$

$$P_{\text{ac}} = V_{\text{ph}} I_{\text{ph}}$$

low freq DC link power

$$P_o = V_{\text{dc}} \times I_o, I_{\text{dc}} = \frac{V_{\text{ph}} I_{\text{ph}}}{V_{\text{dc}}}$$

Duty Cycle of Boost Switch

$$D = 1 - \frac{V_{\text{ac}}}{V_{\text{dc}}} = 1 - \frac{\sqrt{2} V_{\text{ph}} \cos \theta}{V_{\text{dc}}}$$

$$I_{\text{peak}} = \sqrt{2} I_{\text{ph}}, \Delta I_L = \frac{V_i I_{\text{ph}} (\text{peak})}{(P-P)}$$

peak to peak ripple current

$$\Delta I_L (R) = \frac{V_{\text{ac}} \cdot D}{fL} \leftarrow (\text{Boost})$$

$$I_{\text{RMS}} = \frac{I_{\text{ph}}}{\sqrt{2}}$$

Avg Current in Rectifier

$$I_{\text{diode}} = \frac{\sqrt{2}}{\pi} I_{\text{ph}}$$

$$\text{Power} = V_{\text{ph}} \cdot I_{\text{ph}}$$

Power factor correction

$$I_{\text{RMS}} = \frac{I_{\text{ph}}}{\sqrt{2}}$$

• Switch & Diode Avg current

$$I_S = D \times I_{AC} \Rightarrow \langle I_S \rangle = I_{ph} \left(\frac{2\sqrt{2}}{\pi} - \frac{V_{PM}}{V_{dc}} \right)$$

(Diode) $i_D = (1-D) i_{AC}$ $\langle I_D \rangle = \frac{V_{PM} I_{ph}}{V_{dc}}$

• RMS

$$I_S(RMS) = I_{ph} \sqrt{1 - \frac{8\sqrt{2}}{3\pi} \frac{V_{PM}}{V_{dc}}}$$

$$I_{D(RMS)} = I_{ph} \sqrt{\frac{8\sqrt{2}}{3\pi} \frac{V_{PM}}{V_{dc}}}$$

(MOSFET) loss

$$P_S = R_{DS} \times I_S^2(RMS)$$

Diode conduction loss

$$P_D = \frac{1}{f} I_{D(ave)} + \frac{1}{f} I_D^2(RMS)$$

⊗ Super Capacitor

→ regenerative, start stop of EV, Electrical energy (lithium) + uses ions

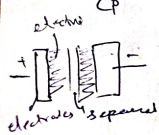
high capacitance (3300F)

low voltage 2.5-2.7



charging & discharging

$$I_C = (C_0 + kV) \frac{dV}{dt}$$



Energy storage Capacitor

$$W_u = \frac{1}{2} C (V_{max}^2 - V_{min}^2)$$

discharge ratio (d) = $\frac{V_{min}}{V_{max}} \times 100$

$$C = C_0 + C_1 = C_0 + kV$$

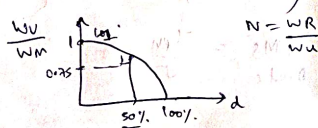
$$Q = CV \quad I = \frac{dQ}{dt}$$

$$I = C \frac{dV}{dt}$$

$$W = \int P \cdot dt = \int V \cdot I_C \cdot dt$$

$$W = \frac{1}{2} \left[C_0 + \frac{4}{3} kV \right] V^2$$

$$W_u = W_{max} \left(1 - \frac{d^2}{100} \right)$$



$V \downarrow$ (charge), $V \uparrow$ (discharge)

redirection phenomenon → dynamic variation of properties of SC due to change mitigation.

charging

$$di = \frac{V_P}{V_M} \times 100$$

$$df = \frac{V_P}{V_M} \times 100$$

$$V_C = V_i + \frac{1}{C} \int i_C dt$$

$$\frac{df}{100} = \frac{d_i V_M}{100} + \frac{I_C}{C} T_{ch}$$

$$T_{ch} = \frac{(df - d_i)}{100} \frac{V_M C}{I_C}$$

$$W_{lost} = I^2 R \Delta T$$

$$W_{loss} = I_C V_M C \cdot R (df - d_i)$$

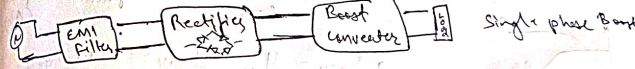
disadv

- high self-discharge
- low voltage of cell
- cannot be used for AC

Adv

- high capacitance
- longer life cycle
- rapid charging

same for discharge just $dt \rightarrow -dt$



PFC

$$L = \frac{\sqrt{2} V_{in} D_{min}}{f_s \Delta I_L}$$

igbt → insulated gate bipolar transistor

Energy Sources

$$E = U + mgh + \frac{1}{2} mv^2$$

$$E = E_{mag} + E_{el}$$

$$E = \frac{1}{2} LI^2 + \frac{1}{2} CV^2$$

$$E = \int P dt$$

Power → W, kW, MW

Energy → J, kWh

$$P_{loss} = \alpha P^2 + P_0 [SOE(t)]$$

$$SOE(t) = SOE(t_0) + \frac{(P(t) - P_{loss}(t))}{E_{stored}} dt$$

$$P_{out} = \frac{E_d}{E_{ch}} \rightarrow \text{recovered during discharge}$$

$$\text{efficiency} = \frac{E_d}{E_{ch}} \rightarrow \text{spent in charge}$$

Electrical
chemical
magnetic
Air, water, rocks, Retort

$$DoD = \frac{\text{Energy Extracted}}{\text{Capacity}}$$
 depth of discharge

Batteries

- Lithium Ion
- Nickel Metal Hydride (NiMH)
- Solid State

Solid State

- uses electrolytes
- Safe

NiCd

aviation, portable electronics power tools

$$SoC = \frac{Cap - \text{Extracted}}{Cap}$$
 State of charge

- High energy density
- Efficient
- long cycles

no env impact
high cost
heat issues

NiMH

Hybrid EV

less env impact

Durable
Safe
cost

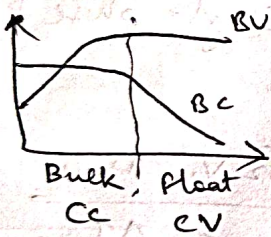
Nickel Oxide Hydroxide

Charging Cycle

charging EE to battery to q charge

Constant current

Constant voltage



Discharging

drawn EE from battery to power device

$$SoC = \frac{Q_{rem}}{Q_{Tot}} \times 100$$

$$E_{ren} = V_{reg} \times \frac{1}{2} m v^2$$

$$\text{Distance} = \frac{Av \cdot \text{Energy}}{(\text{Power} / \text{Km})}$$

expensive low den

$$E = V \times Q$$

Energy kWh
Storage capacity

Capacity (Ah)
Voltage (V)

General

noise less Smart grid

- reduce emissions
- cost eff due in long run
- renewable source
- life cycle assessm

better vehicle dynamics

tax incentives

lowly carbon fuel

low maintenance

- range problems
- battery replacement
- limited infrastructure to charge

High initial cost

Heat

7 < P < 22 Normal Power AC/DC

22 < P < 200 kW High Power Charging DC

- Motor
- Battery Pack
- Fuel Tank
- Engine
- Inverters
- Controller
- Battery Mgmt
- Charger

1W	12 kWh
3W	3-8
4W	21
4W(2)	(30-80)

Private Public Semi

Begin Breaking Syst