

# Thesis Stage - II

## Hugoniot Characterization of alloys using molecular dynamics simulation

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**(ME22MTECH02001)**

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MD simulations

# Presentation Outline

- 1 Recap
- 2 Simulation Results
- 3 Interatomic Potential I: (V)
- 4 Interatomic Potential II: (P)
- 5 Tungsten Heavy Alloy 90W-7Ni-3Fe
- 6 Results and Conclusion
- 7 Future work

# Recap

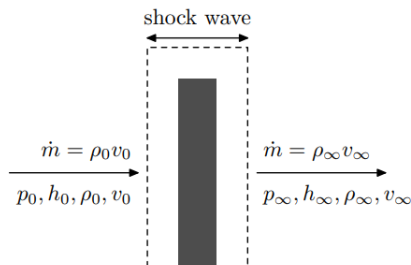
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# Hugoniot curve

Characteristics described by Hugoniot relation

- Equation of state
- Phase transition
- Material strength (Shock compressibility)

under **extreme conditions**



Passing of a shock wave

# Hugoniot curve

## Conservation equations

$$\rho(u_s - u_p) = \rho_0 u_s$$

$$P - P_0 = \rho_0 u_s u_p$$

$$E - E_0 = \frac{1}{2}(P + P_0)(V_0 - V)$$

Under **wide range** of pressure , the relation between  $u_s$  and  $u_p$  is linear

$$u_s = C_0 + \lambda u_p$$

## Hugoniot curve

$$P_H(V) = \frac{\rho_0 C_0^2 (1 - V/V_0)}{[1 - \lambda(1 - V/V_0)]^2}$$

# Objective

- Relation between  $U_s$  and  $U_p$  for SC-AI and WHA
- Obtain Hugoniot Curve for SC-AI and WHA
- MD Framework for material characterization and validation

# Simulation Results

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# The science behind MD simulations

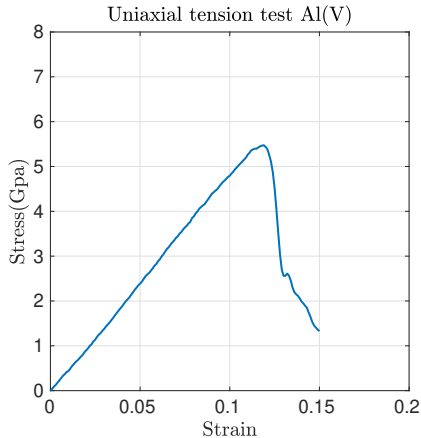
- Each of  $N$  particle is a point mass
- Particles interact via empirical force laws
  - **all physics** in energy potential
  - many-body forces (EAM)
- Numerical integration Newton's equations of motion
  - $F = ma$
  - set of  $3N$  coupled ODEs
- Properties obtained via time averaging
- Seed velocity; Zero Force



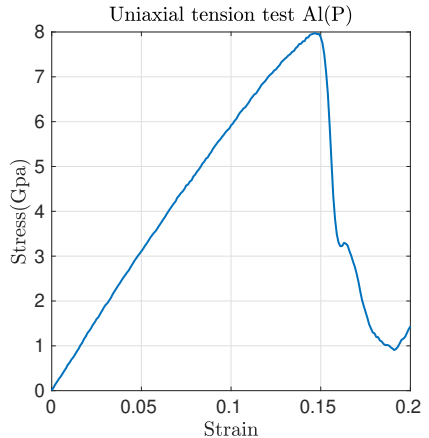
# Simulation setup

- Single crystal fcc micro structure
- Simulation box of dimension  $10a \times 10a \times 200a$
- Lattice parameter( $a$ ) =  $4.05 \text{ \AA}$
- Equilibrated at 300K and 0 bar
- Time step 1 femto second
- Computation time 8 pico second

# Stress - Strain plot for Aluminium



$$E_{vel} = 44.2 \text{ GPa}$$

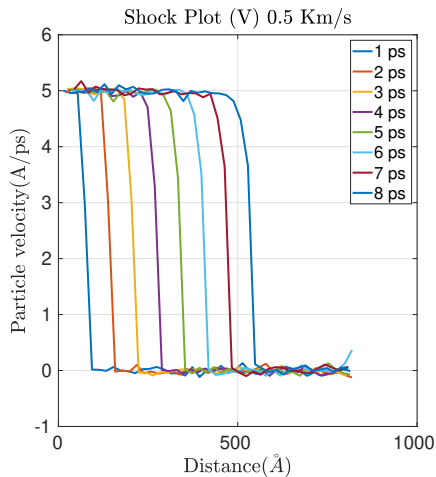


$$E_{pres} = 69.1013 \text{ GPa}$$

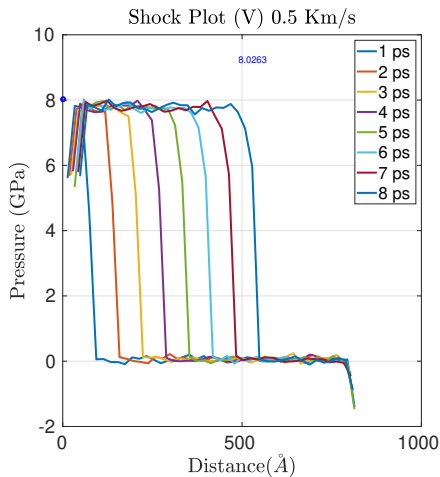
# Interatomic Potential I: (V)

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## Velocity EAM



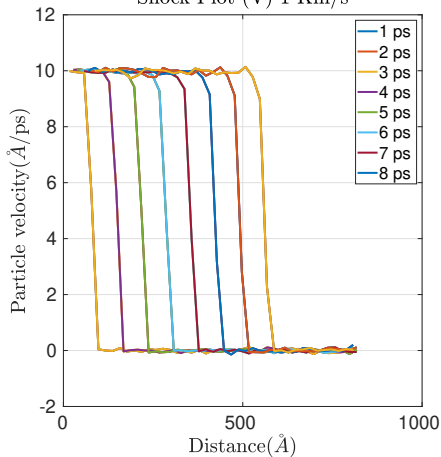
$$U_s = 6.5 \text{ km/s}$$



$$P_{max} = 8.0283 \text{ GPa}$$

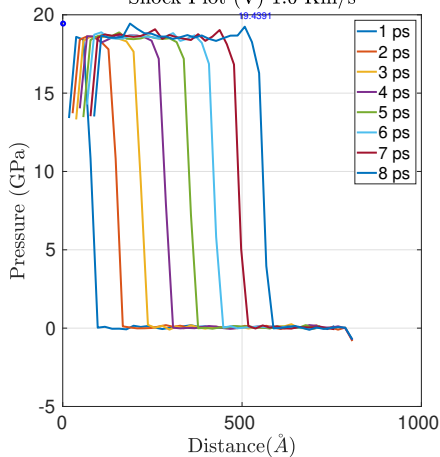
## Velocity EAM

Shock Plot (V) 1 Km/s



$$U_s = 7 \text{ km/s}$$

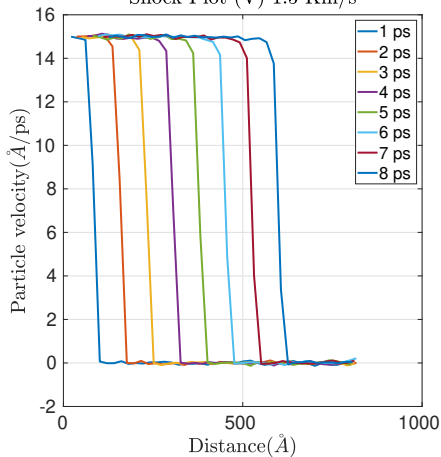
Shock Plot (V) 1.0 Km/s



$$P_{max} = 19.4391 \text{ GPa}$$

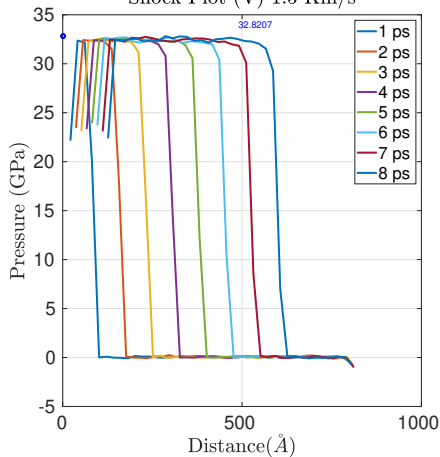
# Velocity EAM

Shock Plot (V) 1.5 Km/s



$$U_s = 7.4985 \text{ km/s}$$

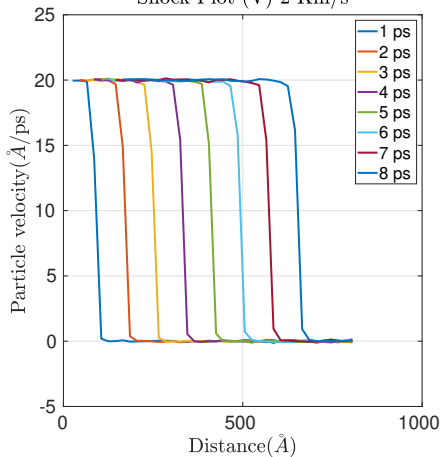
Shock Plot (V) 1.5 Km/s



$$P_{max} = 32.8207 \text{ GPa}$$

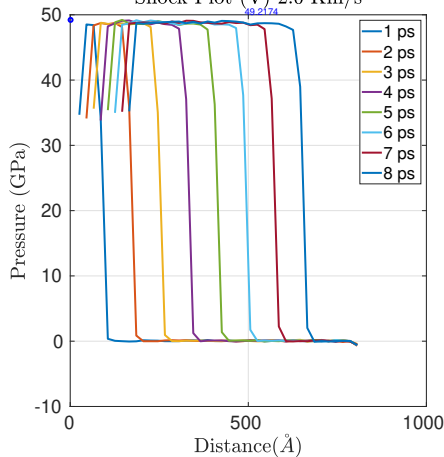
# Velocity EAM

Shock Plot (V) 2 Km/s



$$U_s = 7.9225 \text{ km/s}$$

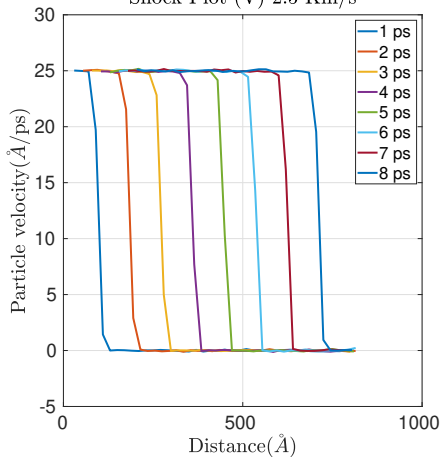
Shock Plot (V) 2.0 Km/s



$$P_{max} = 49.2174 \text{ GPa}$$

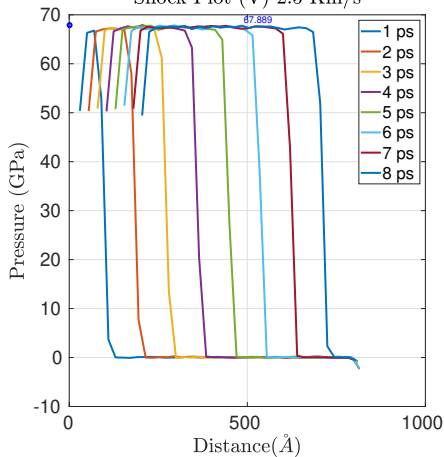
## Velocity EAM

Shock Plot (V) 2.5 Km/s



$$U_s = 8.756 \text{ km/s}$$

Shock Plot (V) 2.5 Km/s

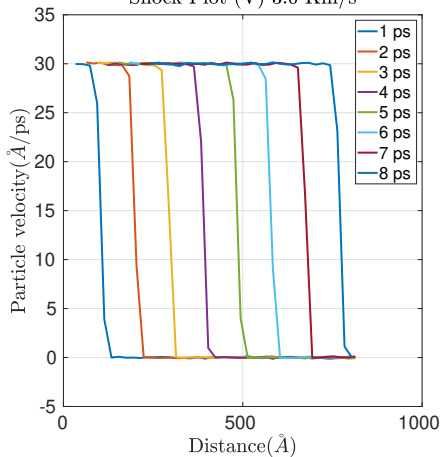


$$P_{max} = 67.889 \text{ GPa}$$



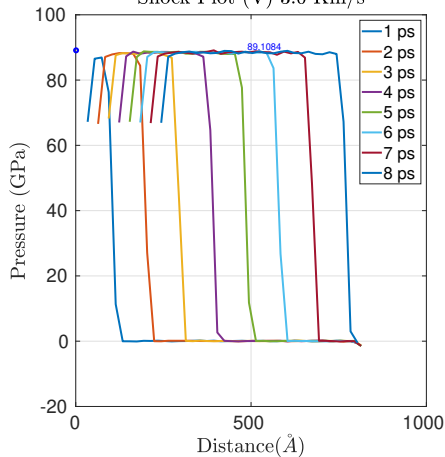
# Velocity EAM

Shock Plot (V) 3.0 Km/s



$$U_s = 9.5 \text{ km/s}$$

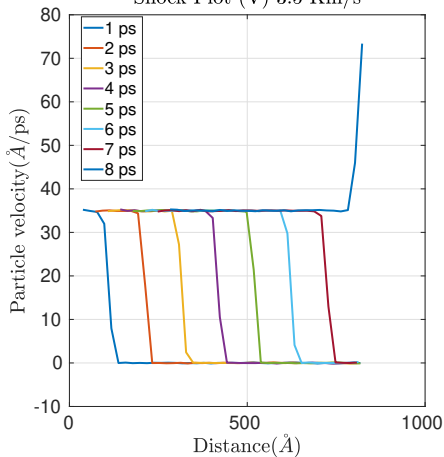
Shock Plot (V) 3.0 Km/s



$$P_{max} = 89.1084 \text{ GPa}$$

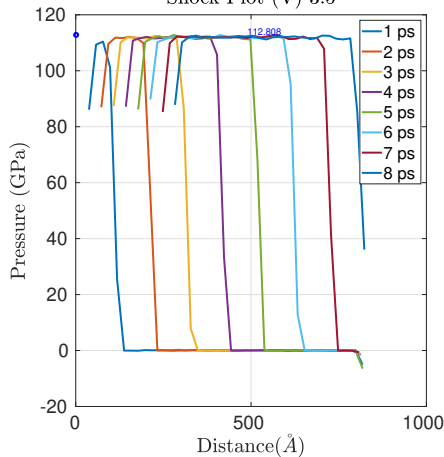
## Velocity EAM

Shock Plot (V) 3.5 Km/s



$$U_s = 10.14 \text{ km/s}$$

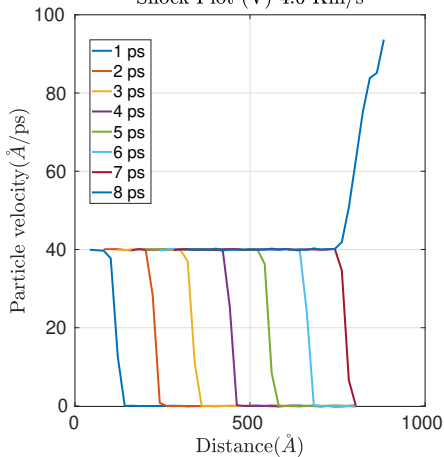
Shock Plot (V) 3.5



$$P_{max} = 112.808 \text{ GPa}$$

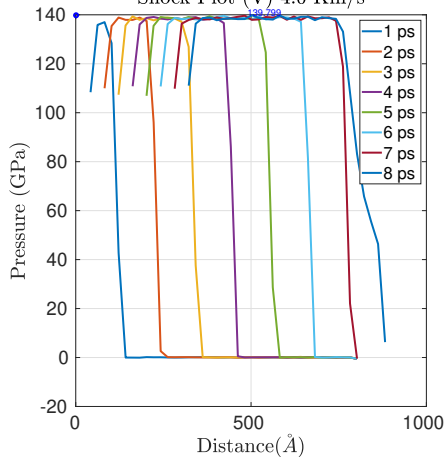
## Velocity EAM

Shock Plot (V) 4.0 Km/s



$$U_s = 10.86 \text{ km/s}$$

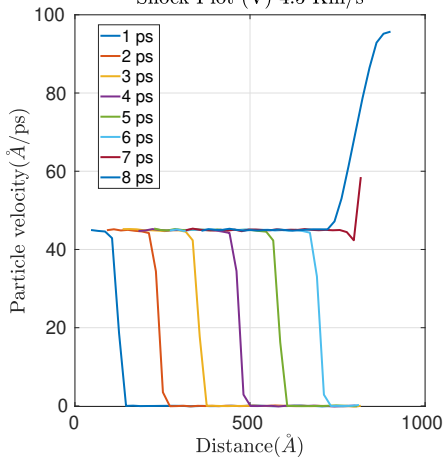
Shock Plot (V) 4.0 Km/s



$$P_{max} = 139.799 \text{ GPa}$$

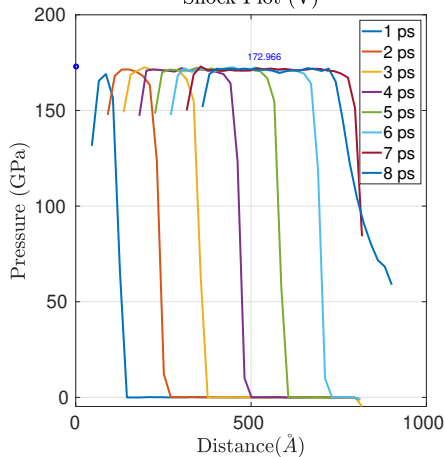
## Velocity EAM

Shock Plot (V) 4.5 Km/s



$$U_s = 11.5 \text{ km/s}$$

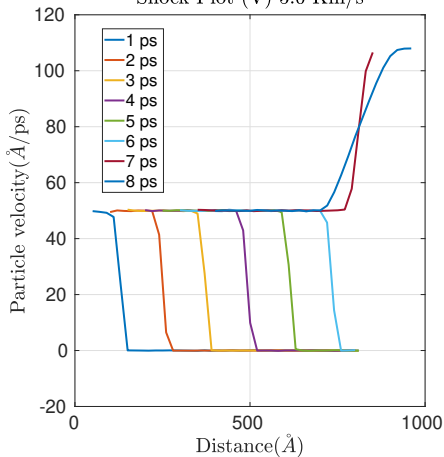
Shock Plot (V)



$$P_{max} = 172.966 \text{ GPa}$$

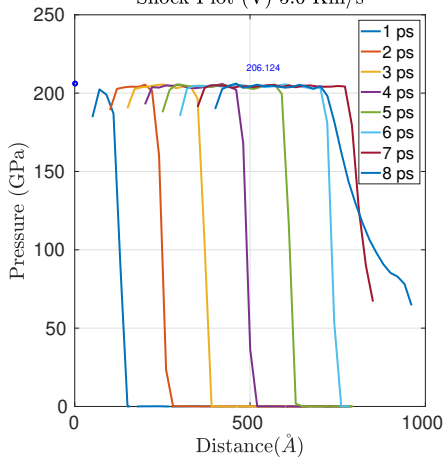
# Velocity EAM

Shock Plot (V) 5.0 Km/s



$$U_s = 12.14 \text{ km/s}$$

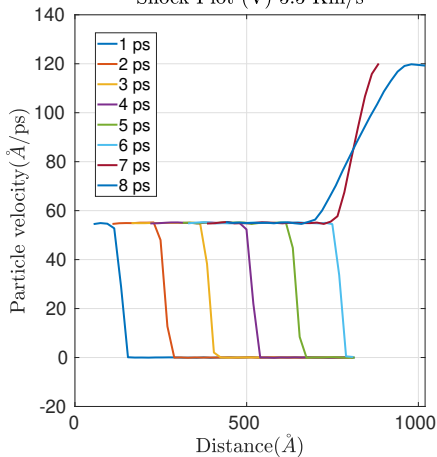
Shock Plot (V) 5.0 Km/s



$$P_{max} = 206.124 \text{ GPa}$$

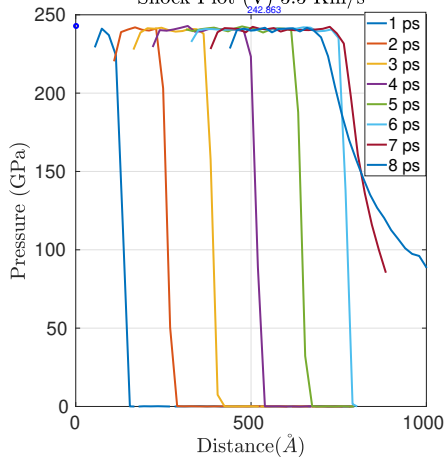
# Velocity EAM

Shock Plot (V) 5.5 Km/s



$$U_s = 12.785 \text{ km/s}$$

Shock Plot (V) 5.5 Km/s

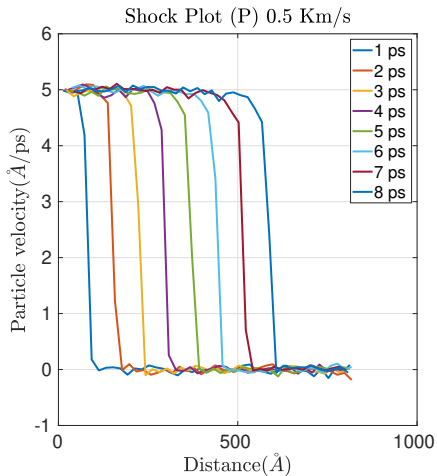


$$P_{max} = 242.863 \text{ GPa}$$

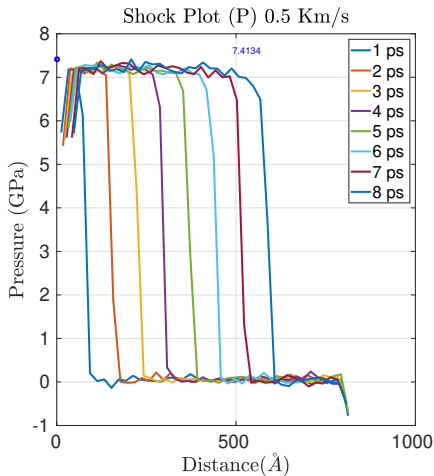
# Interatomic Potential II: (P)

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# Pressure EAM



$$U_s = 6.5 \text{ km/s}$$

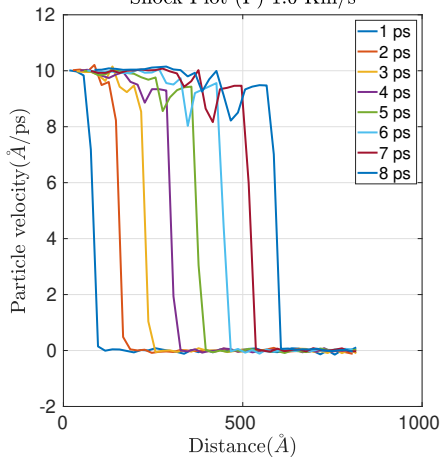


$$P_{max} = 7.4134 \text{ GPa}$$



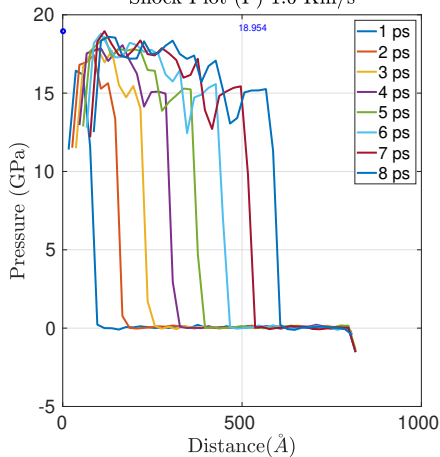
# Pressure EAM

Shock Plot (P) 1.0 Km/s



$$U_s = 7.286 \text{ km/s}$$

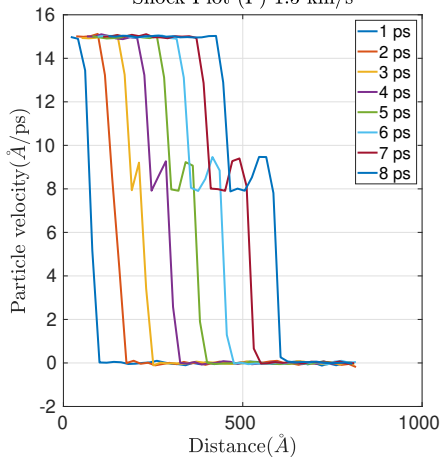
Shock Plot (P) 1.0 Km/s



$$P_{max} = 18.954 \text{ GPa}$$

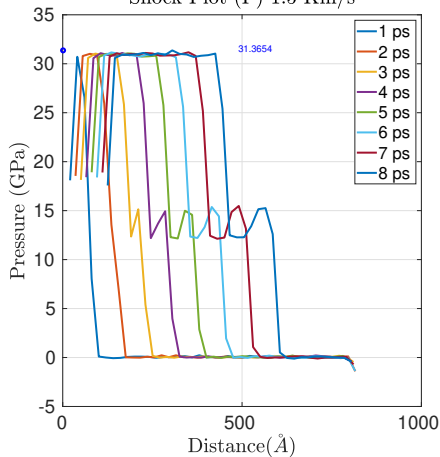
# Pressure EAM

Shock Plot (P) 1.5 km/s



$$U_s = 7.499 \text{ km/s}$$

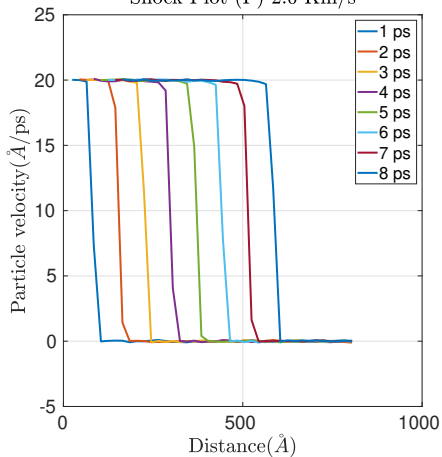
Shock Plot (P) 1.5 Km/s



$$P_{max} = 31.3654 \text{ GPa}$$

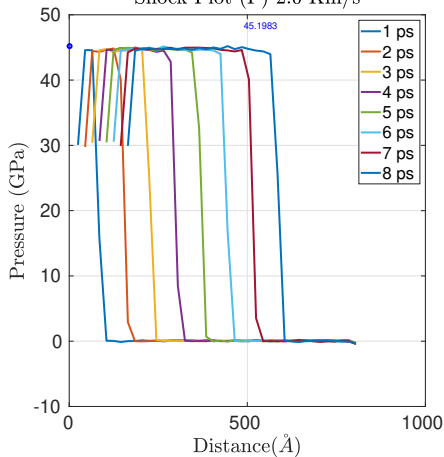
## Pressure EAM

Shock Plot (P) 2.0 Km/s



$$U_s = 8.0 \text{ km/s}$$

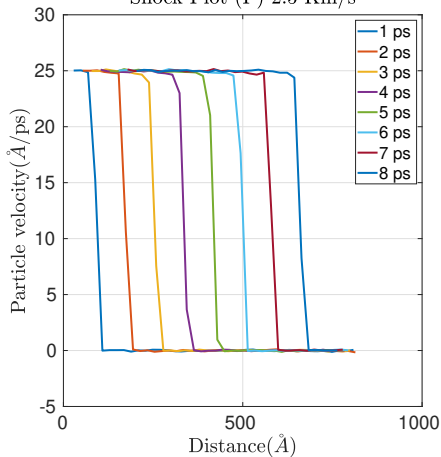
Shock Plot (P) 2.0 Km/s



$$P_{max} = 45.1983 \text{ GPa}$$

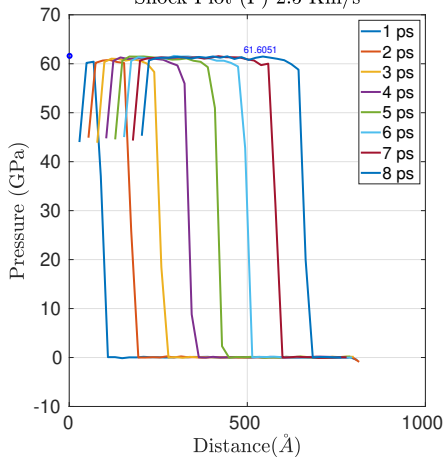
# Pressure EAM

Shock Plot (P) 2.5 Km/s



$$U_s = 8.2107 \text{ km/s}$$

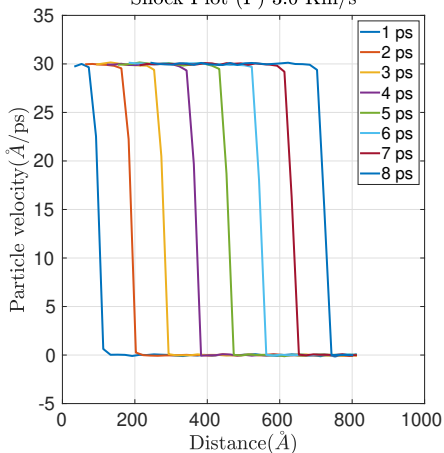
Shock Plot (P) 2.5 Km/s



$$P_{max} = 61.6051 \text{ GPa}$$

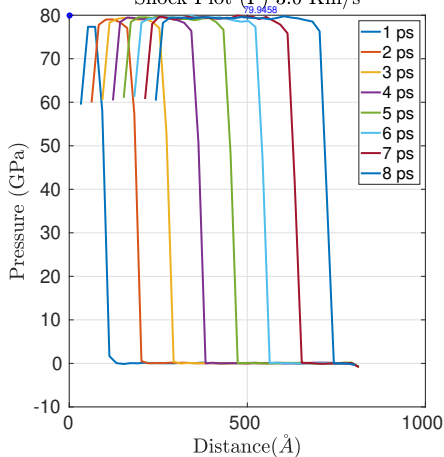
# Pressure EAM

Shock Plot (P) 3.0 Km/s



$$U_s = 8.998 \text{ km/s}$$

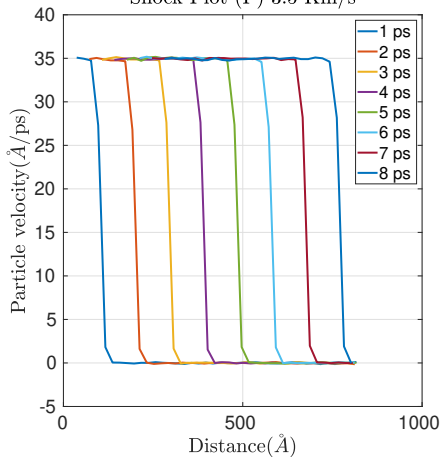
Shock Plot (P) 3.0 Km/s



$$P_{max} = 79.9458 \text{ GPa}$$

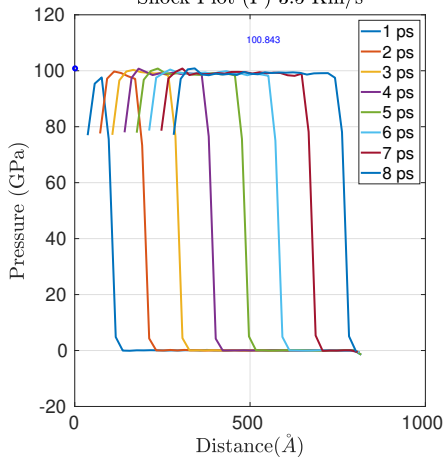
# Pressure EAM

Shock Plot (P) 3.5 Km/s



$$U_s = 9.5 \text{ km/s}$$

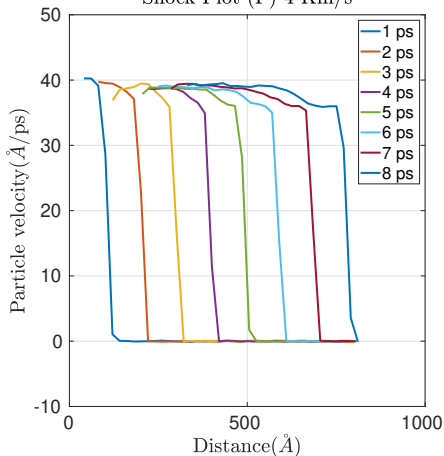
Shock Plot (P) 3.5 Km/s



$$P_{max} = 100.843 \text{ GPa}$$

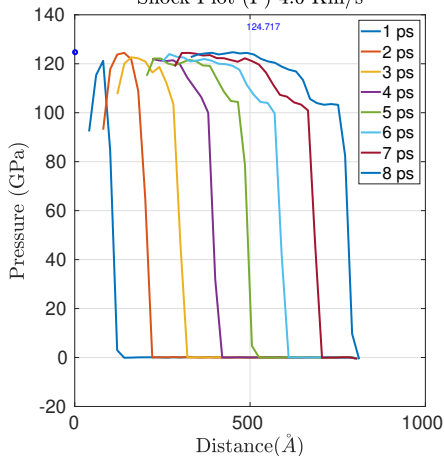
# Pressure EAM

Shock Plot (P) 4 Km/s



$$U_s = 9.767 \text{ km/s}$$

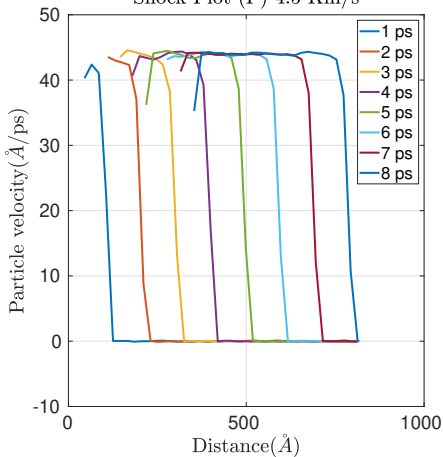
Shock Plot (P) 4.0 Km/s



$$P_{max} = 124.717 \text{ GPa}$$

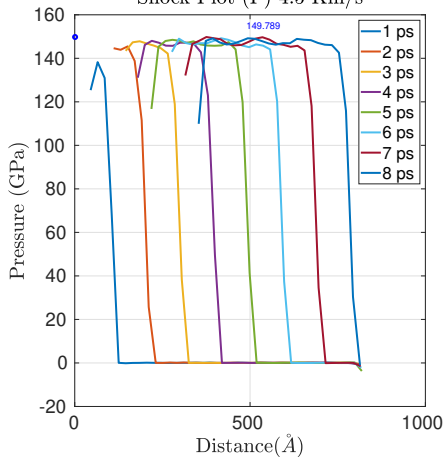
# Pressure EAM

Shock Plot (P) 4.5 Km/s



$$U_s = 9.824 \text{ km/s}$$

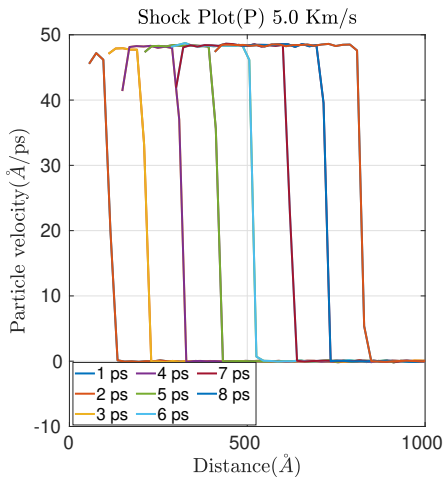
Shock Plot (P) 4.5 Km/s



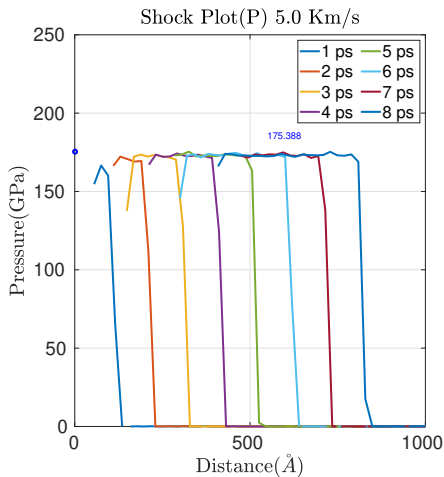
$$P_{max} = 149.789 \text{ GPa}$$



# Pressure EAM

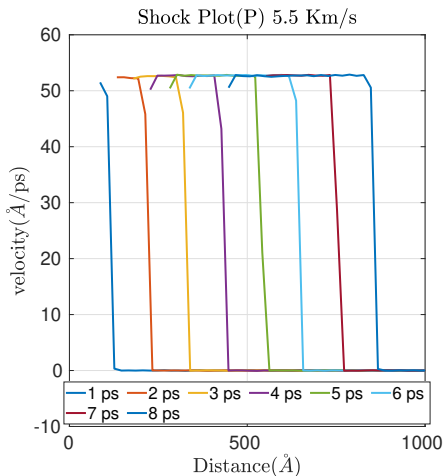


$$U_s = 10.3 \text{ km/s}$$

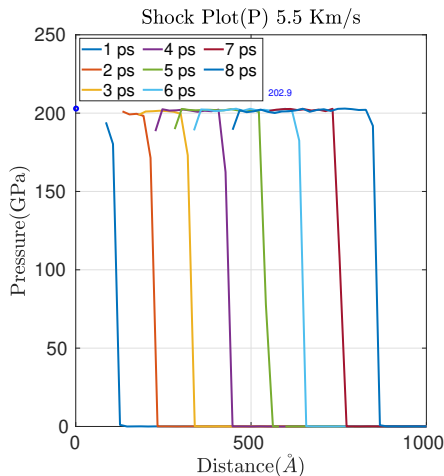


$$P_{max} = 175.388 \text{ GPa}$$

# Pressure EAM

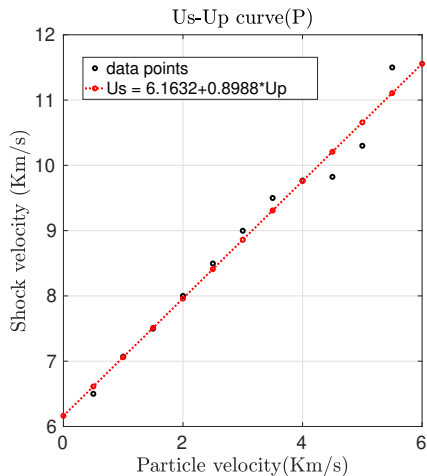


$$U_s = 12.785 \text{ km/s}$$

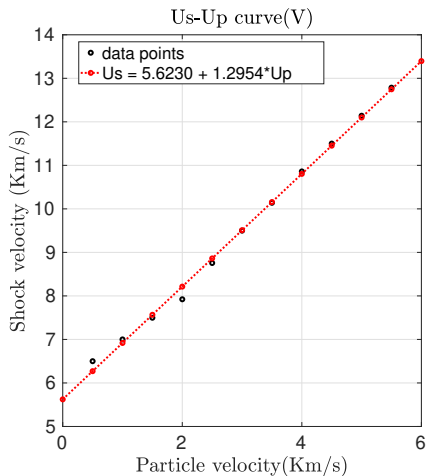


$$P_{max} = 202.9 \text{ GPa}$$

# Us – Up curve

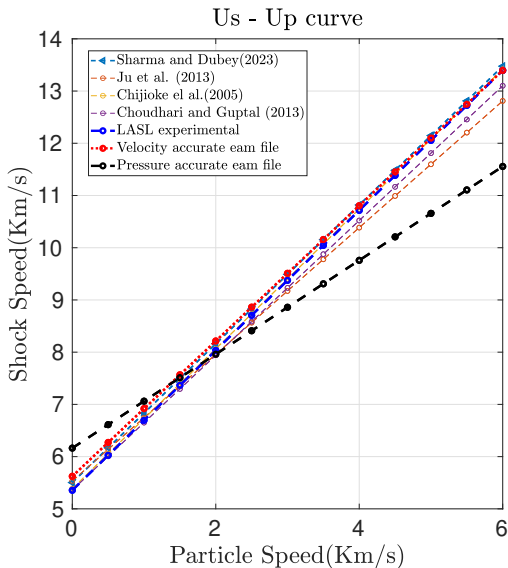


R-square = 0.9777

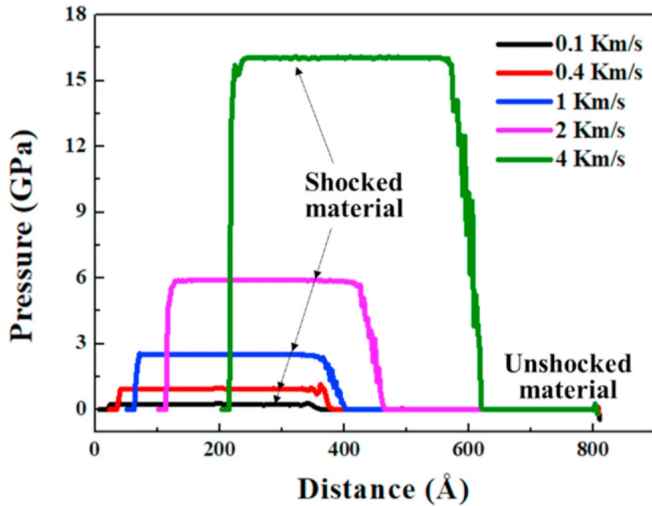


R-square = 0.9964

# Us - Up Curve

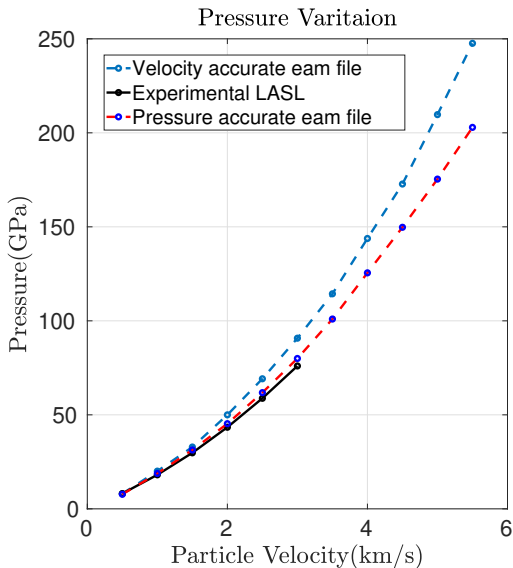


# Pressure Profile

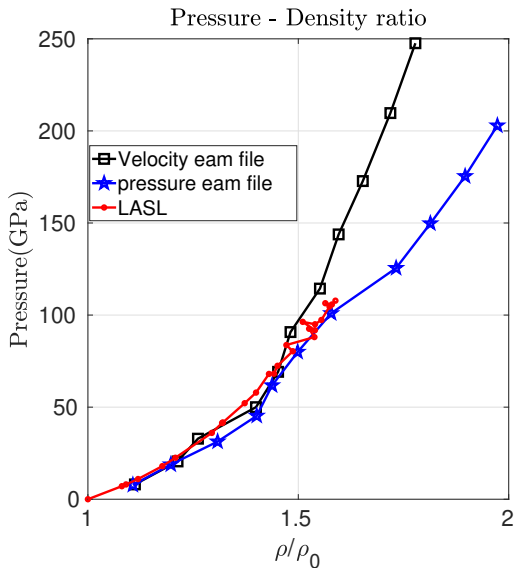


Sharma and Dubey (2023)

# Pressure Variation



# Hugoniot curve



# Tungsten Heavy Alloy 90W-7Ni-3Fe

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# Why Tungsten heavy alloys

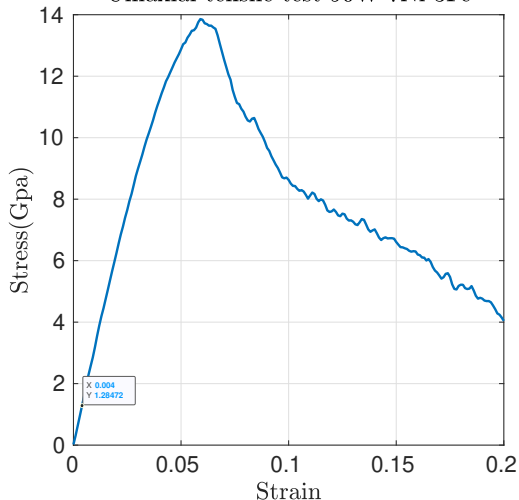
- distinctive combination of yield strength, elongation and density
- better ductility under compression and tension
- **WHA foams** supposed to have better strength to weight ratio

# Simulation setup

- Single crystal bcc micro structure
- Simulation box of dimension  $30a \times 30a \times 400a$
- Lattice parameter( $a$ ) =  $3.165 \text{ \AA}$
- Equilibrated at 300K and 0 bar
- Time step 1 femto second
- Computation time 5 pico second

# Stress - Strain curve for WHA

Uniaxial tensile test 90W-7Ni-3Fe

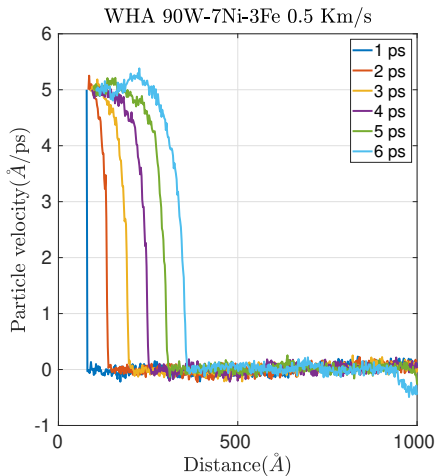


$$E_{Sim} = 321.85 \text{ GPa}$$

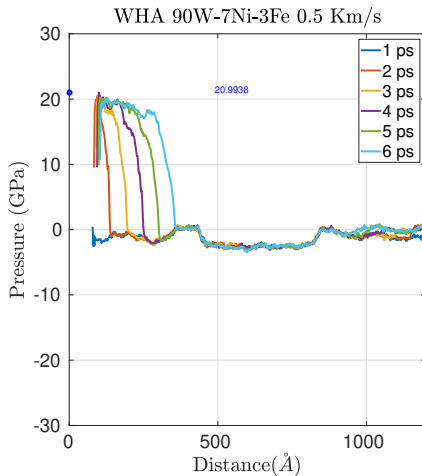
$$E_{exp} = 310 \text{ GPa}$$

$$\% \text{ Error} = 3.8$$

## WHA



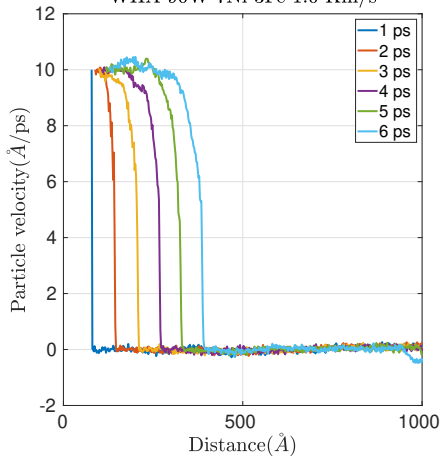
$$U_s = 5.49 \text{ km/s}$$



$$P_{max} = 20.9938 \text{ GPa}$$

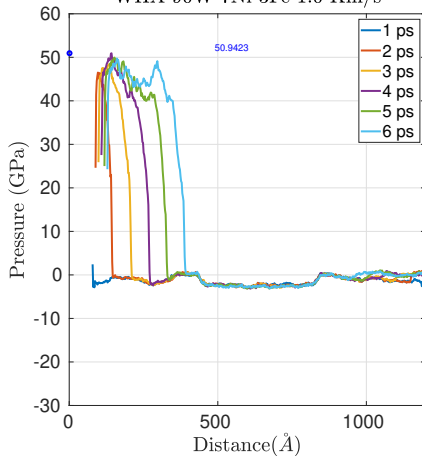
## WHA

WHA 90W-7Ni-3Fe 1.0 Km/s



$$U_s = 6.133 \text{ km/s}$$

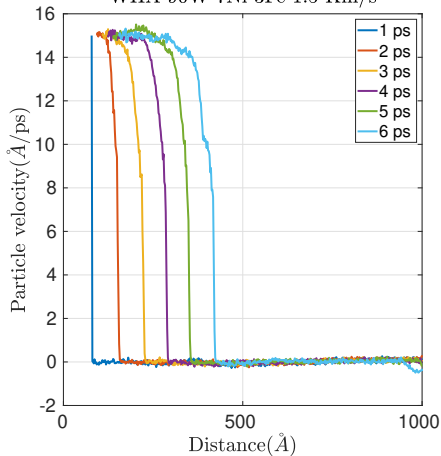
WHA 90W-7Ni-3Fe 1.0 Km/s



$$P_{max} = 50.9423 \text{ GPa}$$

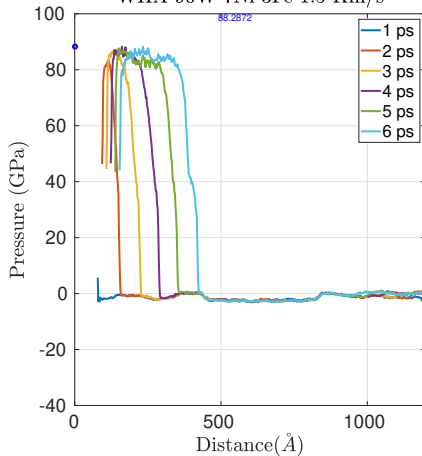
## WHA

WHA 90W-7Ni-3Fe 1.5 Km/s



$$U_s = 6.649 \text{ km/s}$$

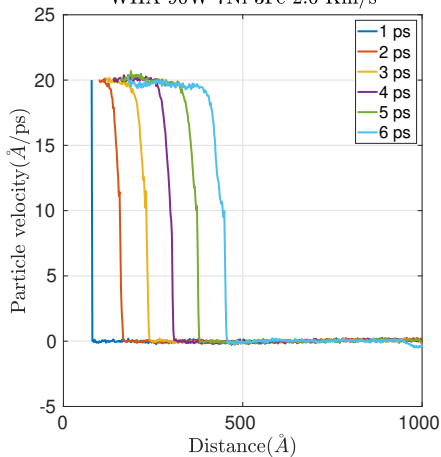
WHA 90W-7Ni-3Fe 1.5 Km/s



$$P_{max} = 88.2872 \text{ GPa}$$

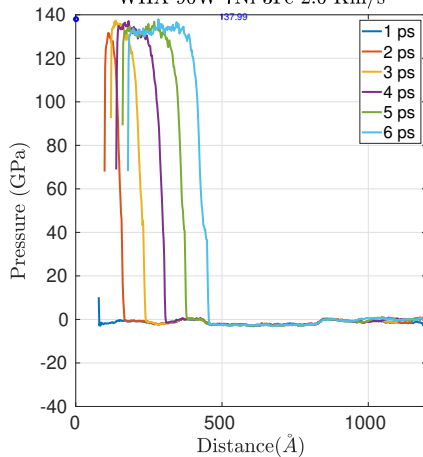
## WHA

WHA 90W-7Ni-3Fe 2.0 Km/s



$$U_s = 7.2 \text{ km/s}$$

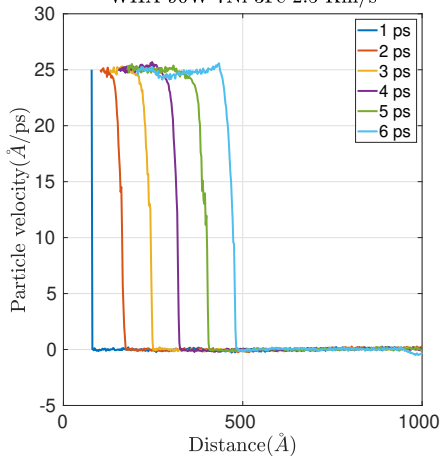
WHA 90W-7Ni-3Fe 2.0 Km/s



$$P_{max} = 137.99 \text{ GPa}$$

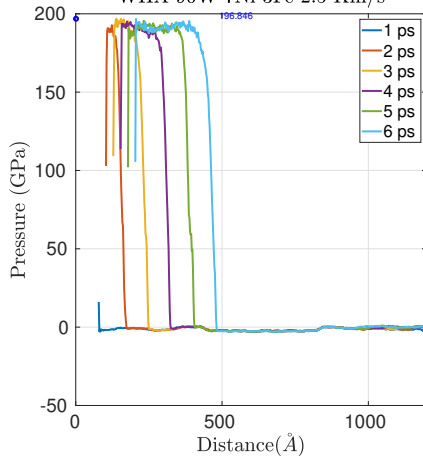
## WHA

WHA 90W-7Ni-3Fe 2.5 Km/s



$$U_s = 7.7 \text{ km/s}$$

WHA 90W-7Ni-3Fe 2.5 Km/s

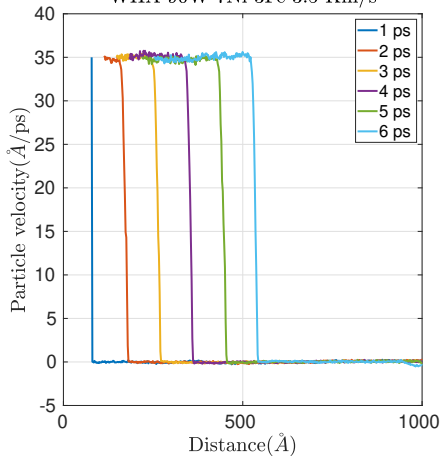


$$P_{max} = 196.846 \text{ GPa}$$



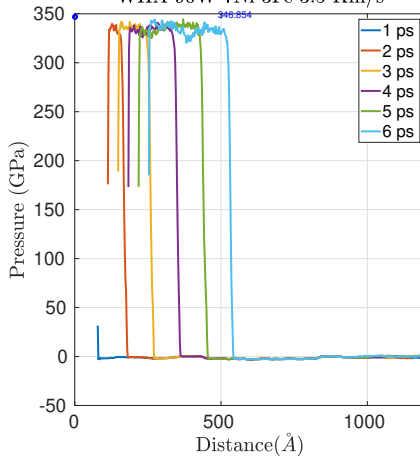
## WHA

WHA 90W-7Ni-3Fe 3.5 Km/s



$$U_s = 9.14 \text{ km/s}$$

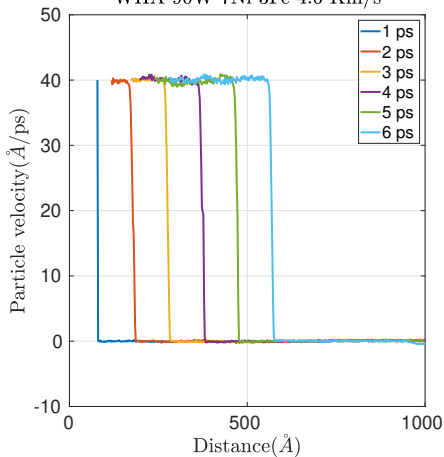
WHA 90W-7Ni-3Fe 3.5 Km/s



$$P_{max} = 346.854 \text{ GPa}$$

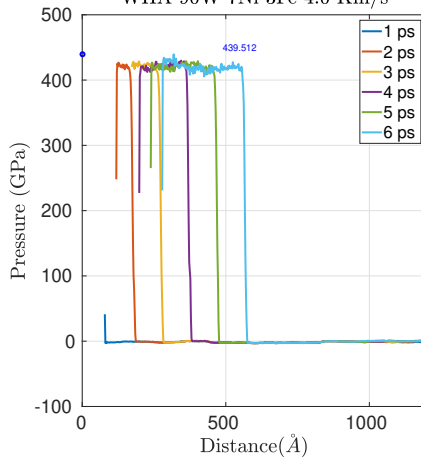
## WHA

WHA 90W-7Ni-3Fe 4.0 Km/s



$$U_s = 9.697 \text{ km/s}$$

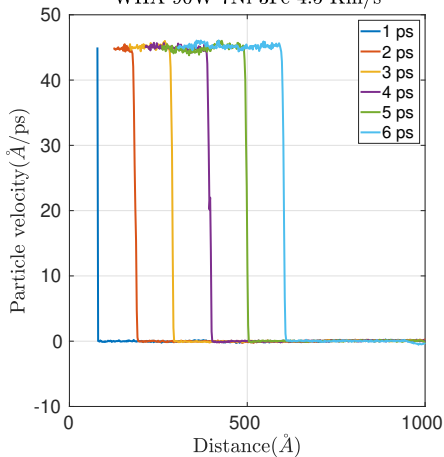
WHA 90W-7Ni-3Fe 4.0 Km/s



$$P_{max} = 439.512 \text{ GPa}$$

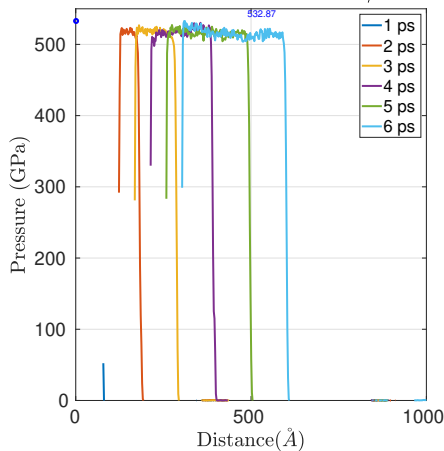
## WHA

WHA 90W-7Ni-3Fe 4.5 Km/s



$$U_s = 10.45 \text{ km/s}$$

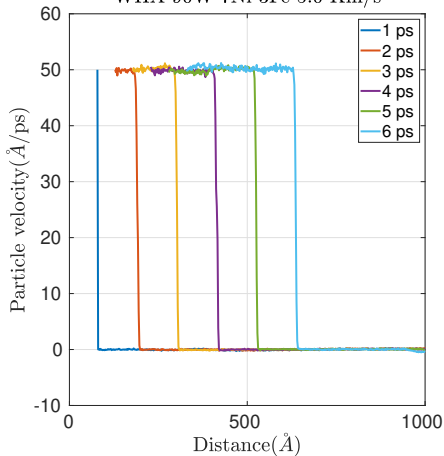
WHA 90W-7Ni-3Fe 4.5 Km/s



$$P_{max} = 532.87 \text{ GPa}$$

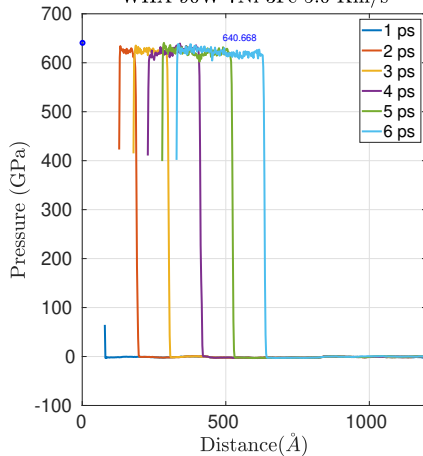
## WHA

WHA 90W-7Ni-3Fe 5.0 Km/s



$$U_s = 11.245 \text{ km/s}$$

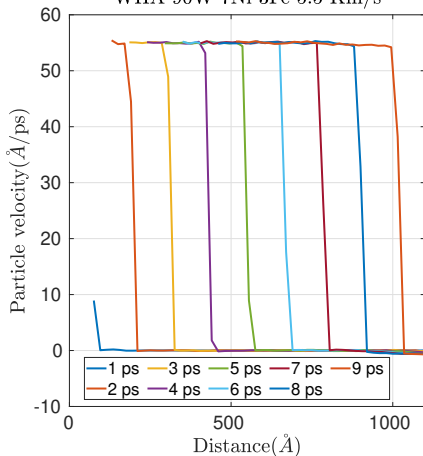
WHA 90W-7Ni-3Fe 5.0 Km/s



$$P_{max} = 640.668 \text{ GPa}$$

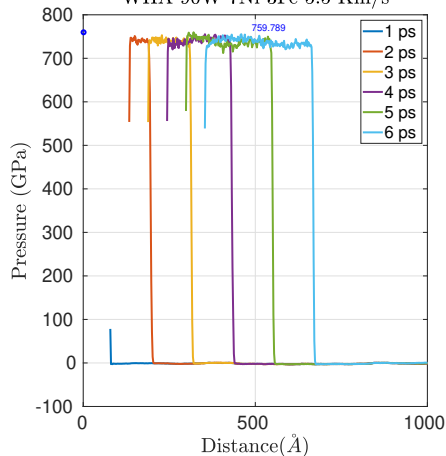
## WHA

WHA 90W-7Ni-3Fe 5.5 Km/s



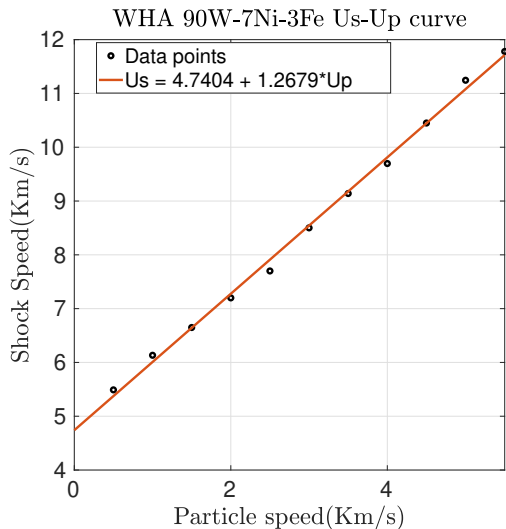
$$U_s = 11.78 \text{ km/s}$$

WHA 90W-7Ni-3Fe 5.5 Km/s

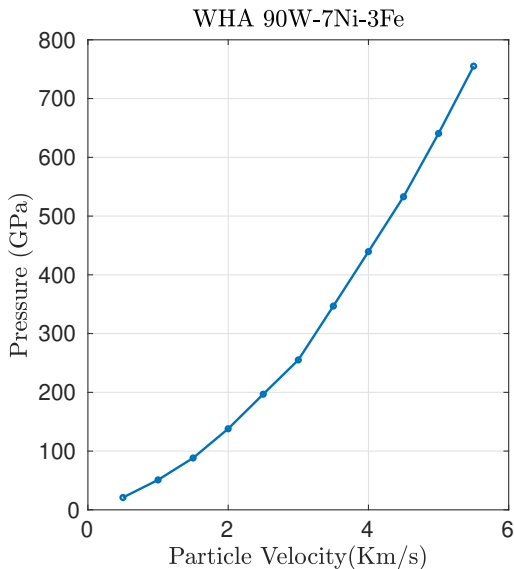


$$P_{max} = 755.21 \text{ GPa}$$

# Us-Up Curve



# Pressure Variation



# Results and Conclusion

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# Results and discussion

- LAMMPS code for shock loading has been developed
- Linear relationship for  $U_s - U_p$  has been reproduced
  - found to be in close agreement with theoretical and experimental results
- Hugoniot curve has been reproduced
  - found to be in close agreement with LASL experimental results
- Alloys with custom composition have been successfully modeled
  - further validation required

# Future work

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# Future Work:

- Plastic Deformation
- Metal Foams, such as:
  - \* Aluminium
  - \* Tungsten heavy alloy
- Shock propagation time
- Experimental validation.

# “Thank you !”

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