

1	2	3
8		4
7	6	5

8-puzzle game

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Heuristic functions for 8 puzzle

- **h1(s)**=Number of misplaced tiles w.r.t goal state.
- **h2(s)**= Euclidean distance between current state s and the goal state.

$$x = (x_1, x_2, \dots, x_n) \quad \text{and} \quad y = (y_1, y_2, \dots, y_n)$$

then

$$d = \sqrt{(x_1 - y_1)^2 + (x_2 - y_2)^2 + \dots (x_n - y_n)^2}$$

1	2	3
8		4
7	6	5

goal

2	8	3
1	6	4
7		5

initial

2	8	3
1		4
7	6	5

$h1(A)=3$

2	8	3
1	6	4
	7	5

$h1(B)=6$

2	8	3
1	6	4
7	5	

$h1(C)=6$

$h1(s)$ =Number of misplaced tiles w.r.t goal state.

$h2(s)$ = Euclidean distance between current state and goal state

$h2(A)= 9.27$

$h2(B)= 13.11$

$h2(c)= 12.17$

$h3(s)$ =Number of in place tiles w. r. t goal state.

$h3(A)= 6$

$h3(B)= 3$

$h3(c)=3$

Various distances which can be used for 8-puzzle

- Euclidean (L2 Norm) distance
- Manhattan distance
- Mahalanobis distance
- Jaccard distance
- Cosine distance
- Edit distance (<https://www.geeksforgeeks.org/edit-distance-dp-5/>)
- Hamming distance
- P-Norm distance

Node structure of Linked list for 8-puzzle

Board position Node (C)	father of C Node	$g(C)$	PTR to child	Heuristic Value of C	PTR To NEXT
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Two Linked lists

1. **OPEN**- contains nodes to be processed
2. **CLOSED**- Contains nodes already processed

**Cost of getting from Parent node to child node is 1
throughout (uniform cost)**