Classification and Representation

Logistic Regression

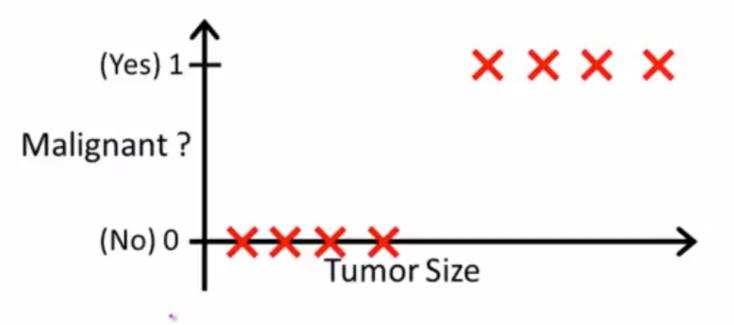
- → Email: Spam / Not Spam?
- Online Transactions: Fraudulent (Yes / No)?
- Tumor: Malignant / Benign ?

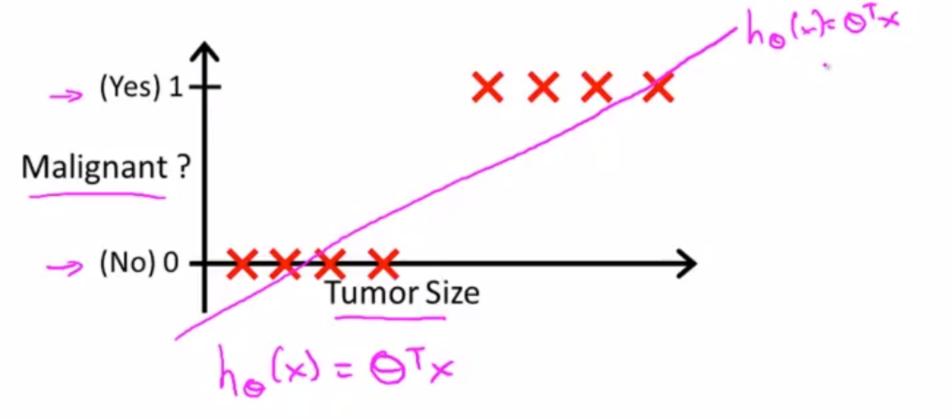
- Email: Spam / Not Spam?
- Online Transactions: Fraudulent (Yes / No)?
- Tumor: Malignant / Benign ?

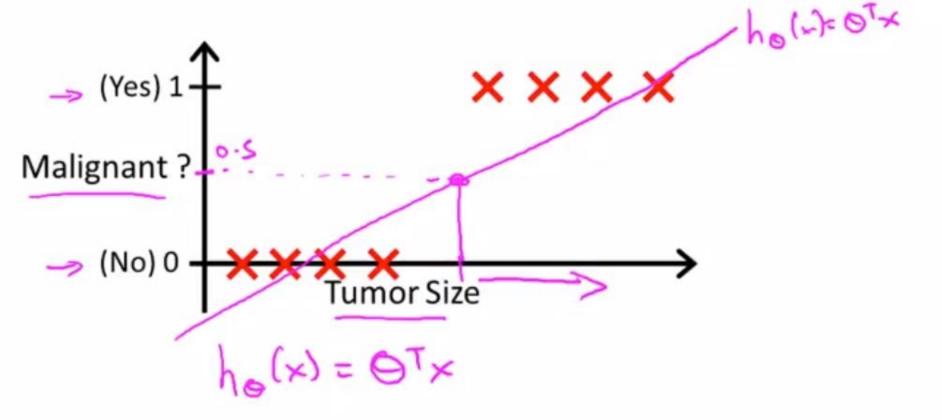
```
y \in \{0,1\} 0: "Negative Class" (e.g., benign tumor) 1: "Positive Class" (e.g., malignant tumor)
```

- -> Email: Spam / Not Spam?
- Online Transactions: Fraudulent (Yes / No)?
- Tumor: Malignant / Benign ?

$$y \in \{0,1\}$$
 0: "Negative Class" (e.g., benign tumor) 1: "Positive Class" (e.g., malignant tumor)



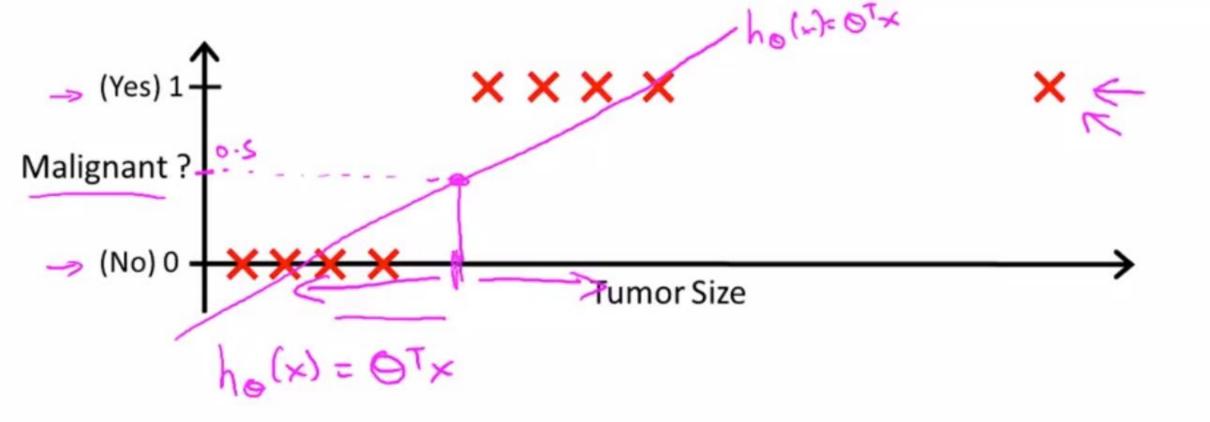




 \rightarrow Threshold classifier output $h_{\theta}(x)$ at 0.5:

$$\longrightarrow$$
 If $h_{\theta}(x) \geq 0.5$, predict "y = 1"

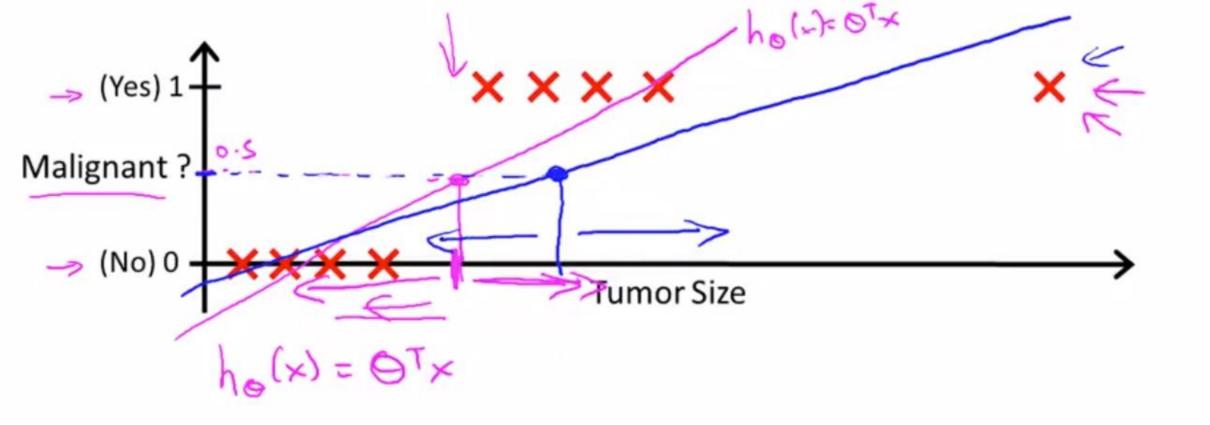
If $h_{\theta}(x) < 0.5$, predict "y = 0"



 \rightarrow Threshold classifier output $h_{\theta}(x)$ at 0.5:

$$\rightarrow$$
 If $h_{\theta}(x) \geq 0.5$, predict "y = 1"

If $h_{\theta}(x) < 0.5$, predict "y = 0"



 \rightarrow Threshold classifier output $h_{\theta}(x)$ at 0.5:

$$\rightarrow$$
 If $h_{\theta}(x) \geq 0.5$, predict "y = 1"

If $h_{\theta}(x) < 0.5$, predict "y = 0"

Classification:
$$y = 0$$
 or 1

$$h_{\theta}(x)$$
 can be > 1 or < 0

Classification:
$$y = 0$$
 or 1

$$h_{\theta}(x)$$
 can be > 1 or < 0

Exercise

Which of the following statements is true?

- If linear regression doesn't work on a classification task as in the previous example, applying feature scaling may help.
- If the training set satisfies $0 \le y(i) \le 1$ for every training example (x(i),y(i)), then linear regression's prediction will also satisfy $0 \le h(x) \le 1$ for all values of x.
- If there is a feature x that perfectly predicts y, i.e if y=1 when x≥c and y=0 whenever x<c (for some constant c), then linear regression will obtain zero classification error.
- None of the above statements are true.

Classification:
$$y = 0$$
 or 1

$$h_{\theta}(x) \text{ can be } > 1 \text{ or } < 0$$

Logistic Regression:
$$0 \le h_{\theta}(x) \le 1$$

Classification:
$$y = 0$$
 or $\frac{1}{\sqrt{2}}$

$$h_{\theta}(x) \text{ can be } \ge 1 \text{ or } \le 0$$

Logistic Regression:
$$0 \le h_{\theta}(x) \le 1$$