

Diagnosing Bias vs Variance

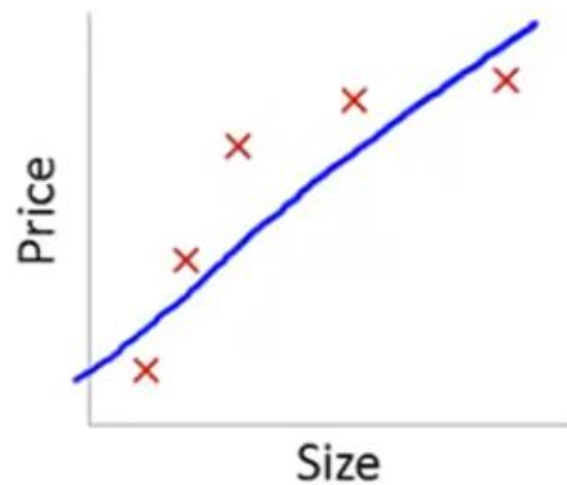
Bias and Variance

Advice for Applying Machine Learning

Introduction

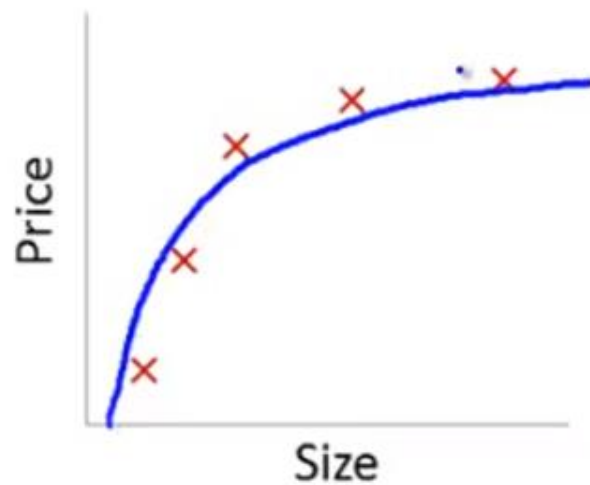
- Most of the time you will have
 - High variance (overfitting)
 - High bias (underfitting)

Bias/variance



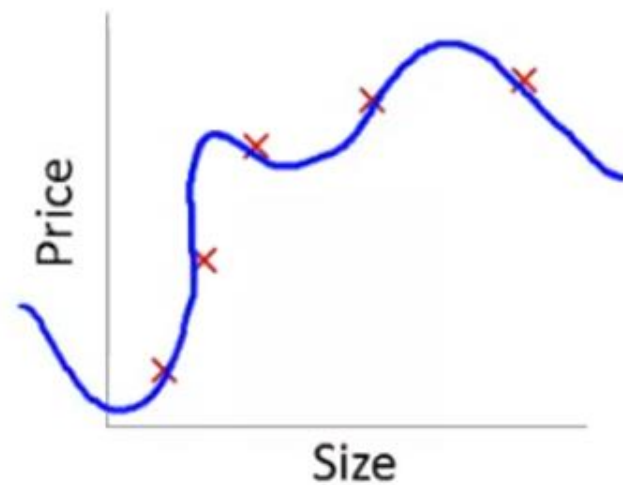
$$\theta_0 + \theta_1 x$$

High bias
(underfit)



$$\theta_0 + \theta_1 x + \theta_2 x^2$$

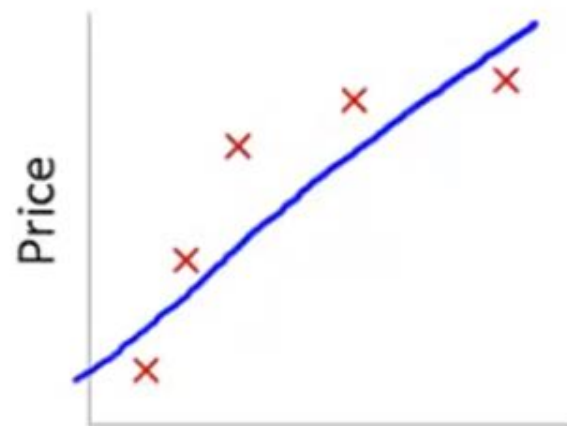
“Just right”



$$\theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$$

High variance
(overfit)

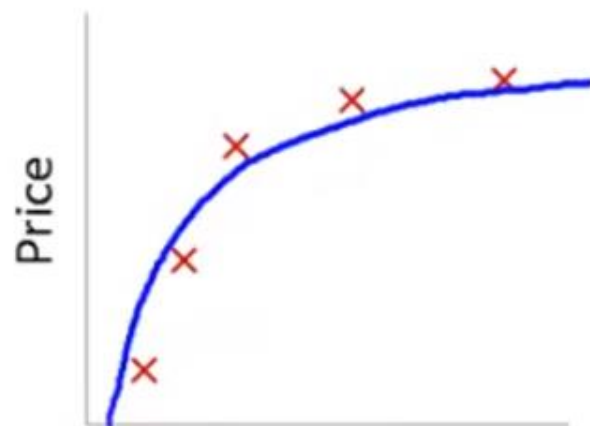
Bias/variance



Size
 $\theta_0 + \theta_1 x$

High bias
(underfit)

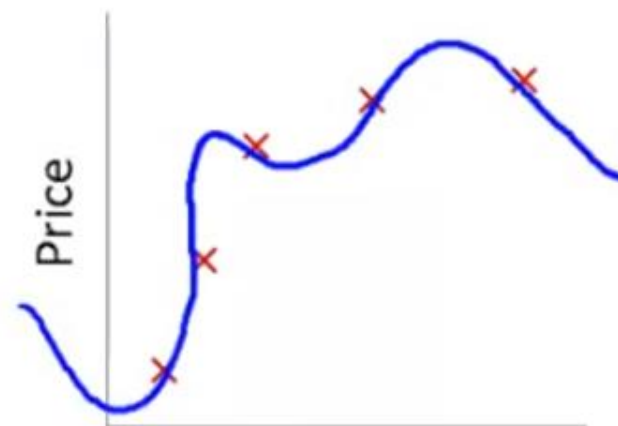
$d=1$



Size
 $\theta_0 + \theta_1 x + \theta_2 x^2$

"Just right"

$d=2$



Size
 $\theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$

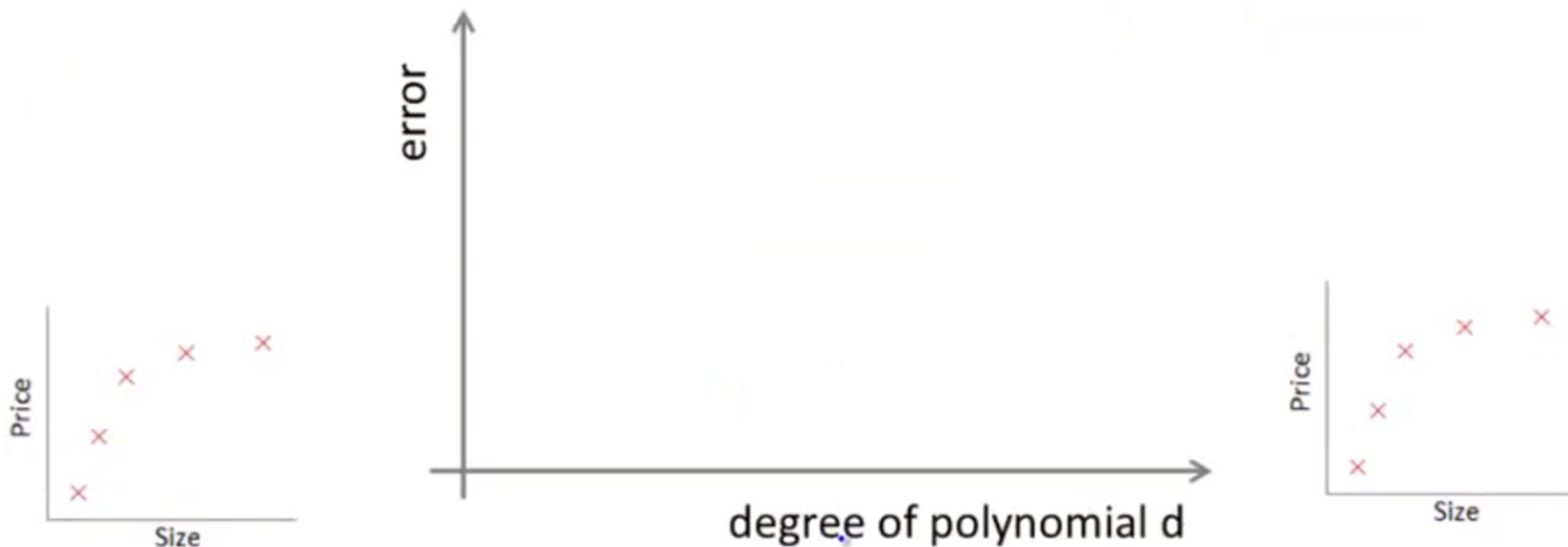
High variance
(overfit)

$d=4$

Bias/variance

Training error: $J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$

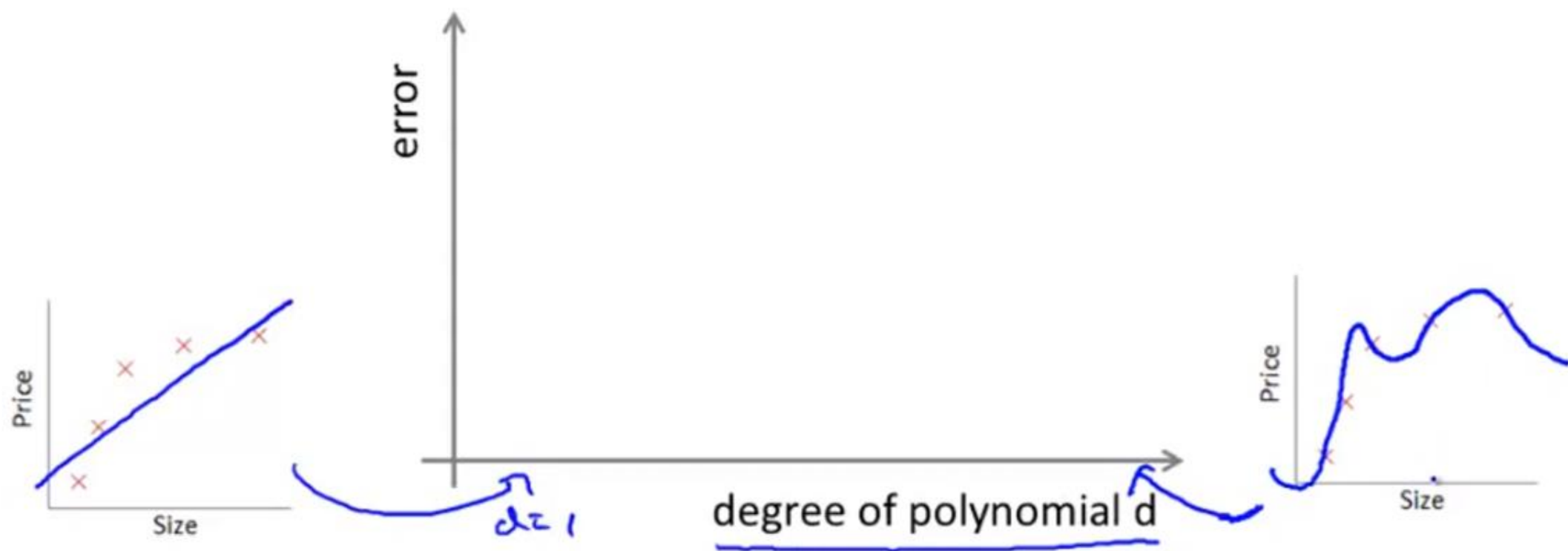
Cross validation error: $J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$



Bias/variance

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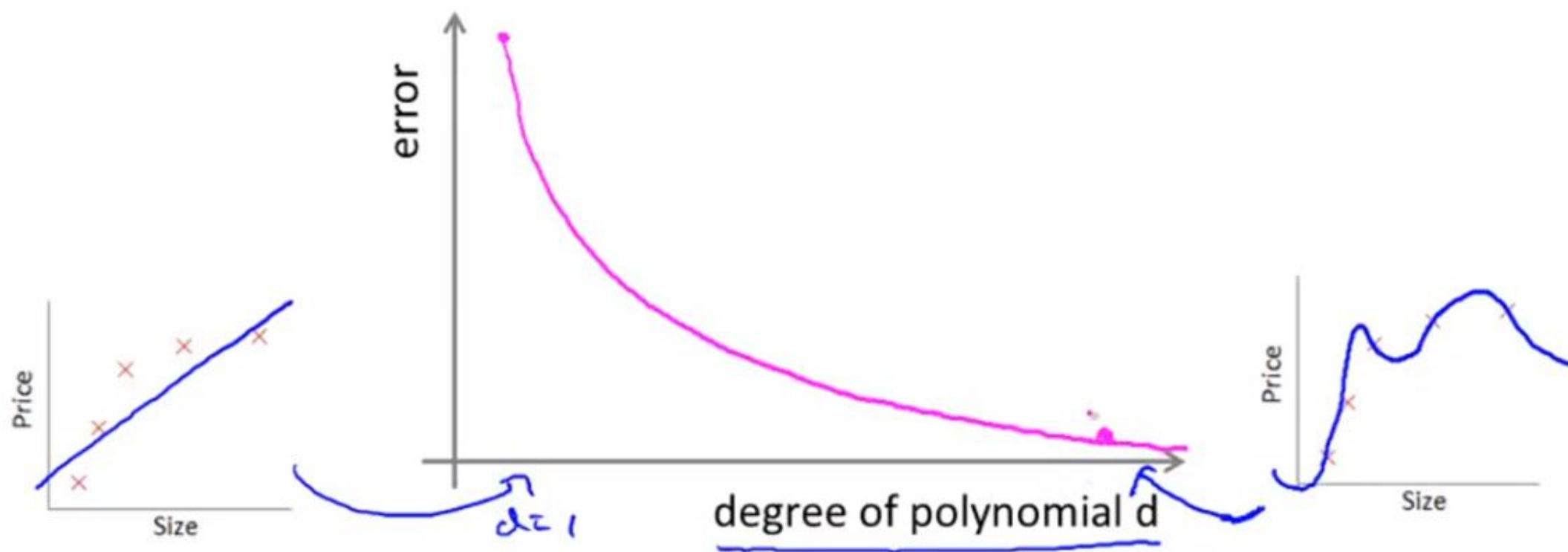
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Bias/variance

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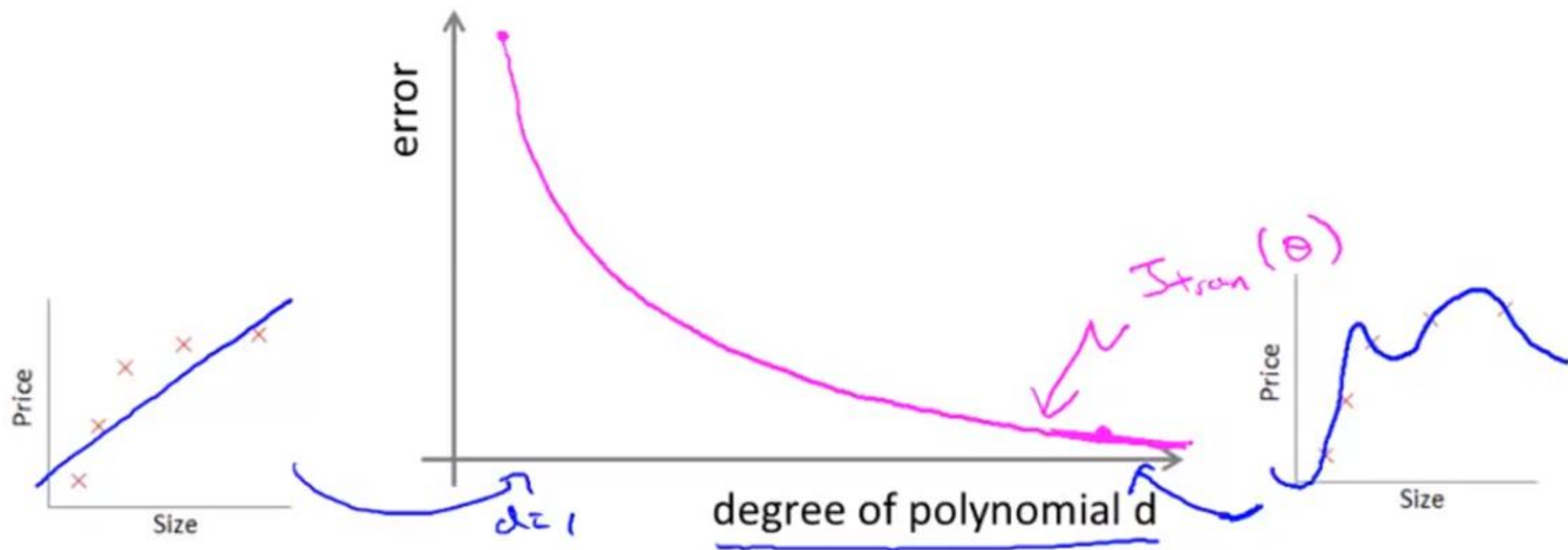
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Bias/variance

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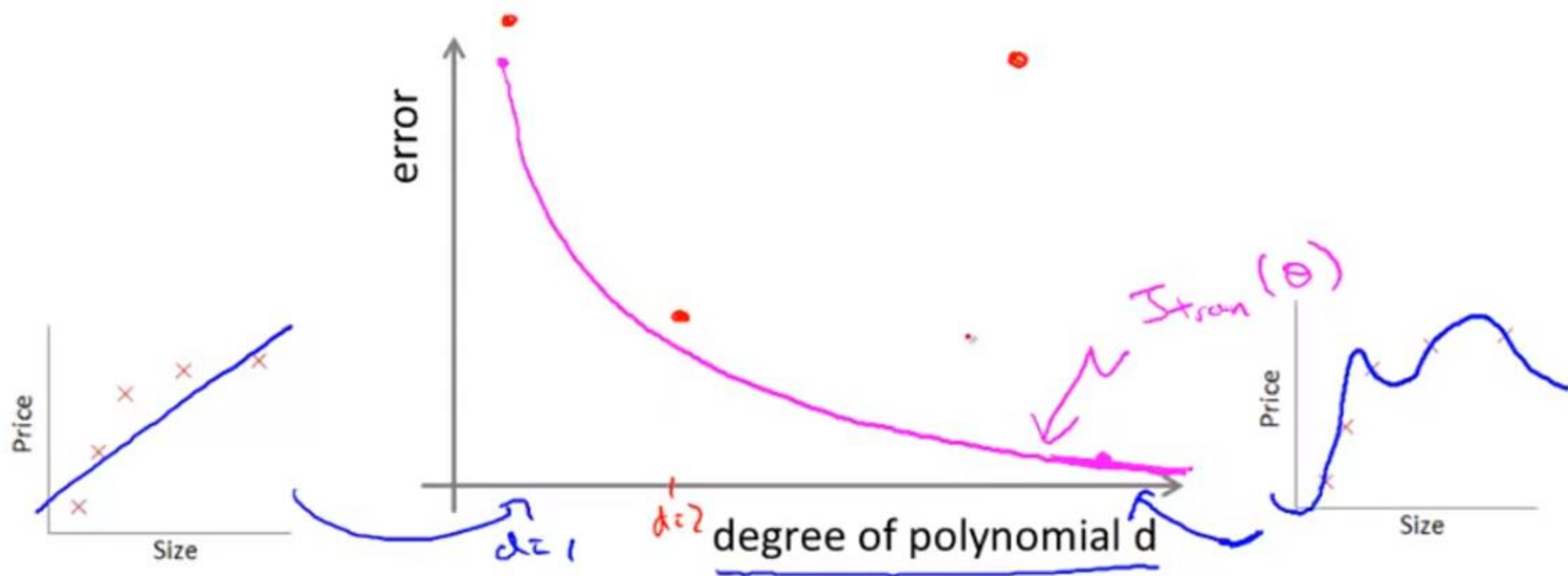
Cross validation error: $J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$ (or $J_{test}(\theta)$)



Bias/variance

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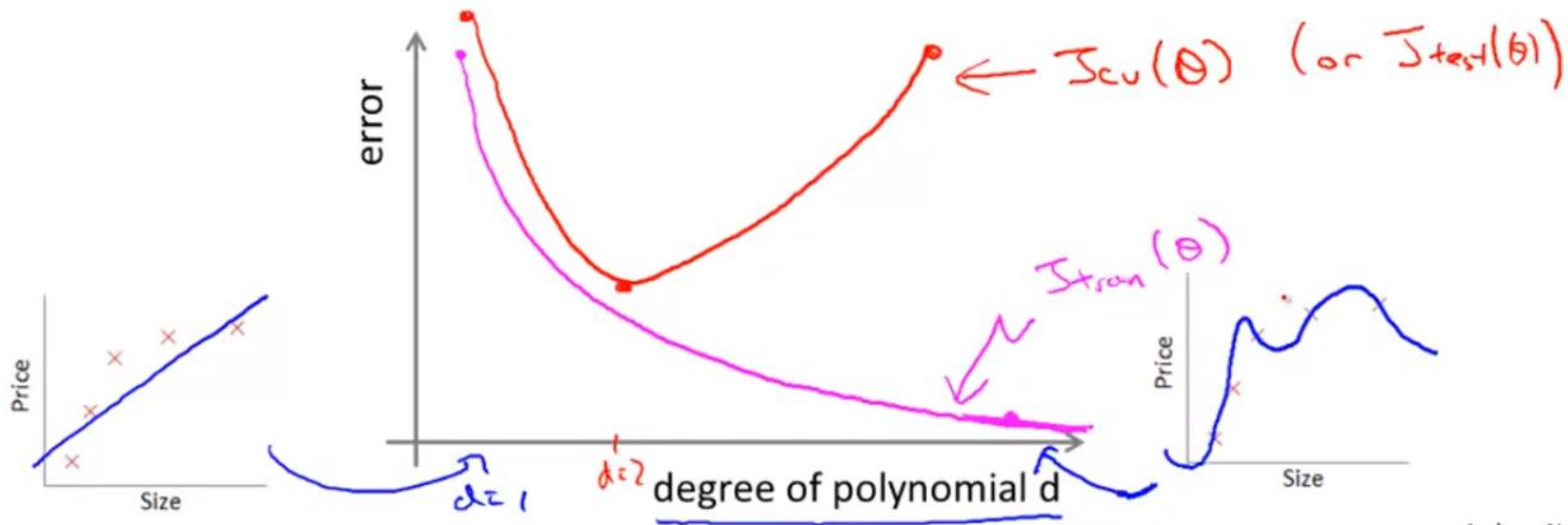
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Bias/variance

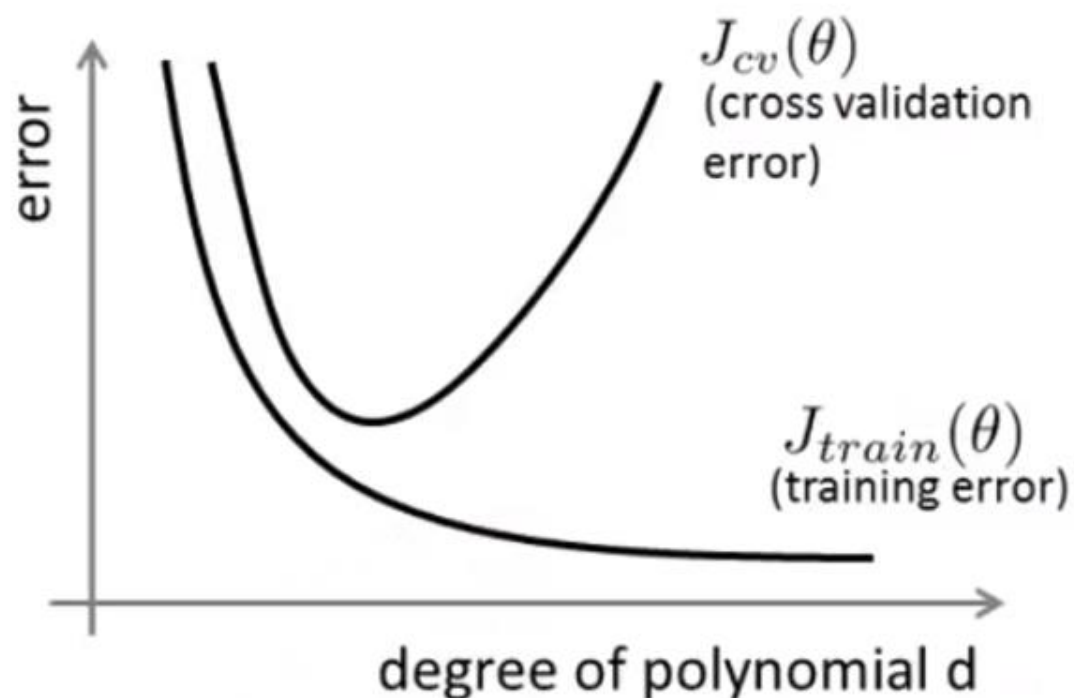
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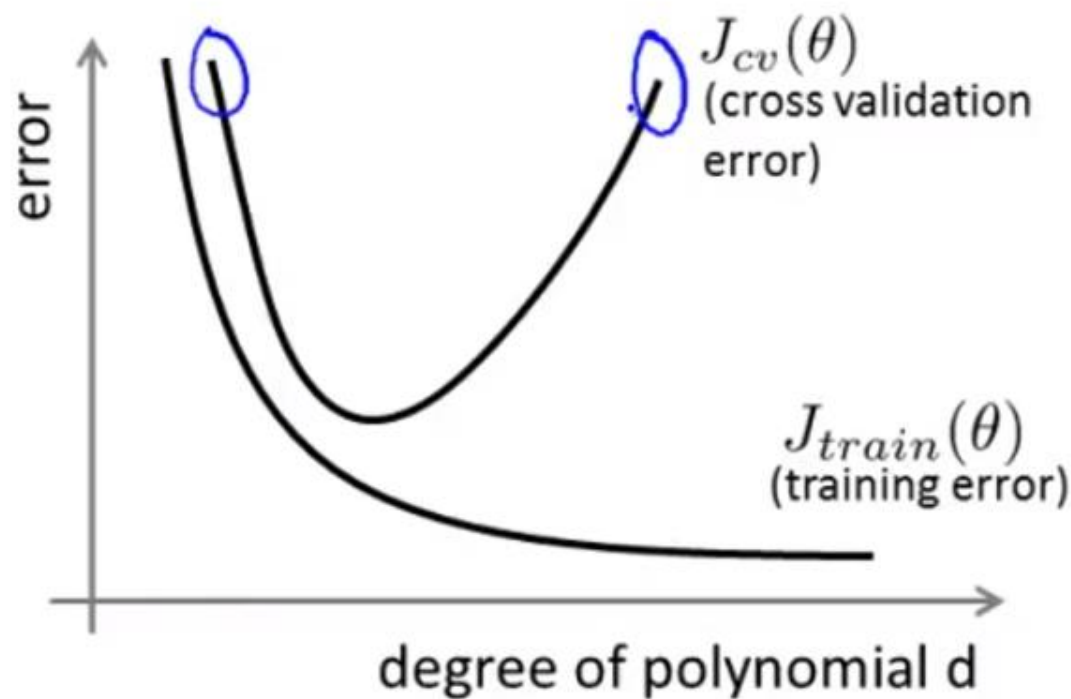
Diagnosing bias vs. variance

Suppose your learning algorithm is performing less well than you were hoping. ($J_{cv}(\theta)$ or $J_{test}(\theta)$ is high.) Is it a bias problem or a variance problem?



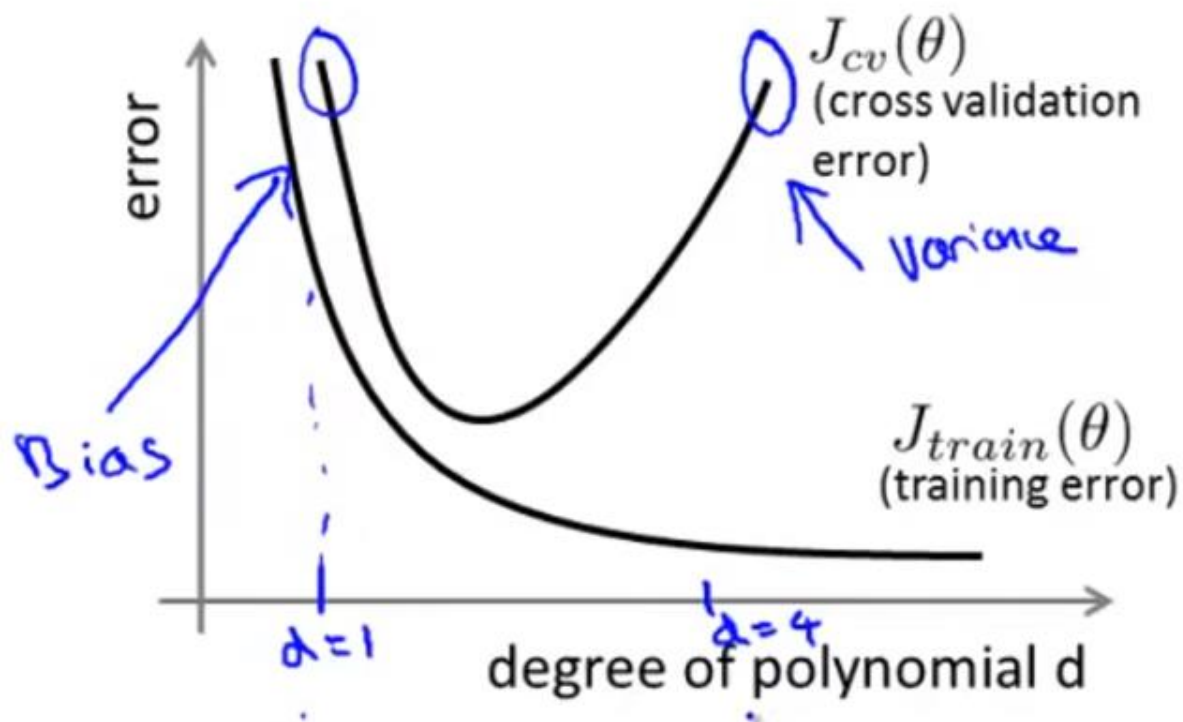
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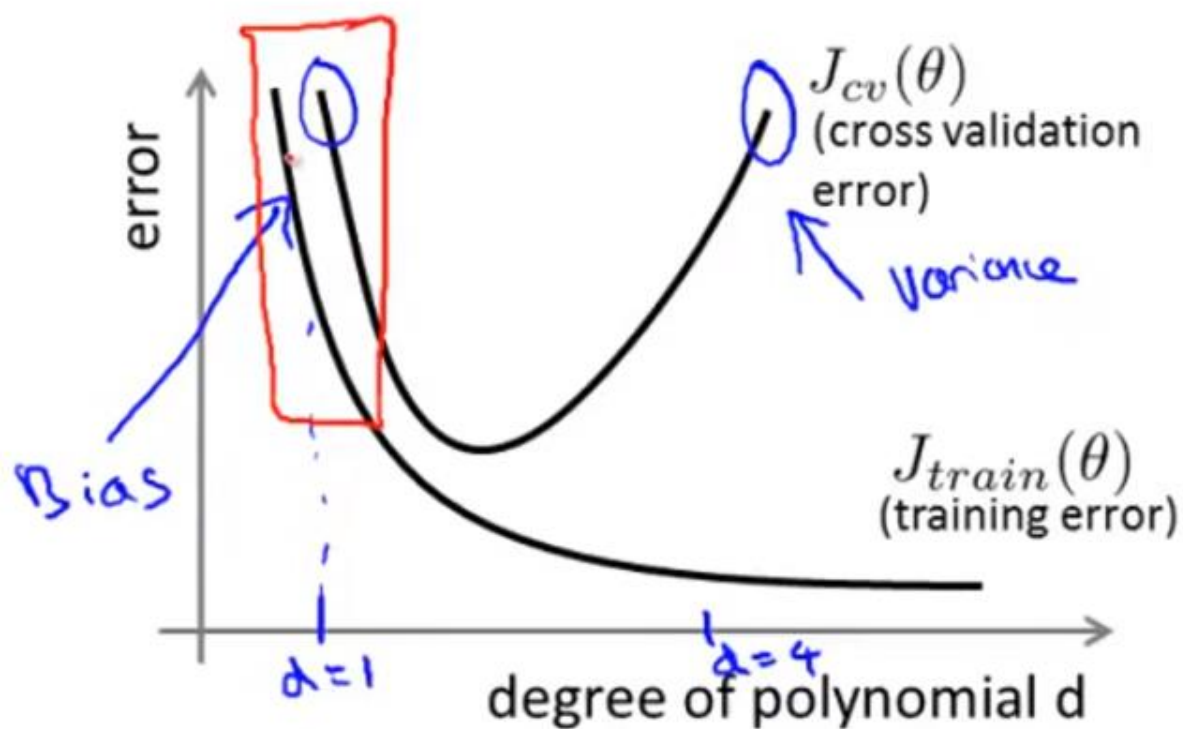
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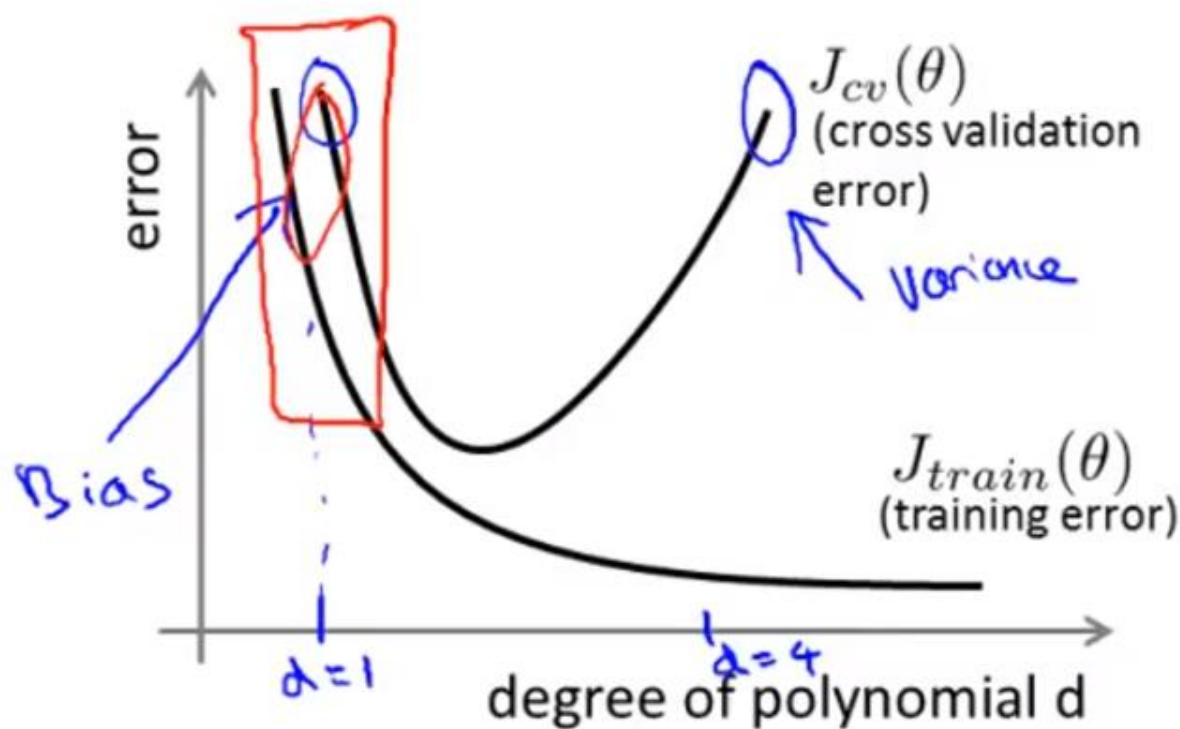


Bias (underfit):

Variance (overfit):

Diagnosing bias vs. variance

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Bias (underfit):

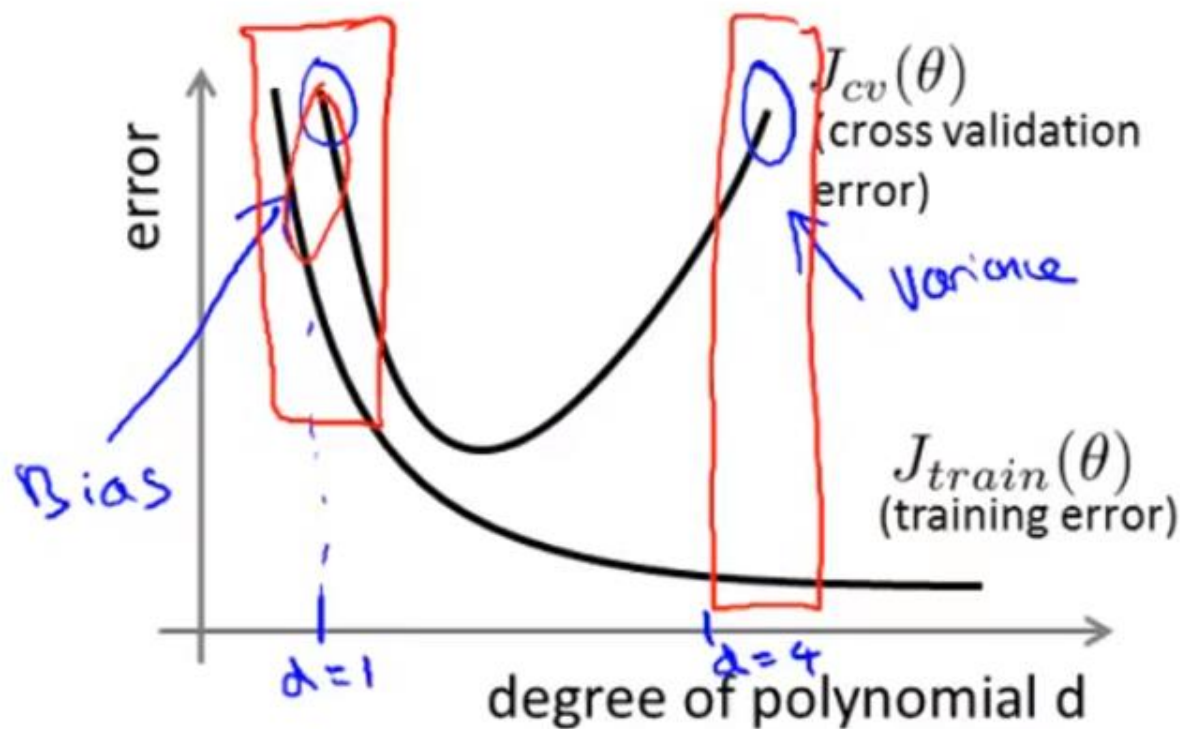
$J_{train}(\theta)$ will be high

$$J_{cv}(\theta) \approx J_{train}(\theta)$$

Variance (overfit):

Diagnosing bias vs. variance

Suppose your learning algorithm is performing less well than you were hoping. ($J_{cv}(\theta)$ or $J_{test}(\theta)$ is high.) Is it a bias problem or a variance problem?



Bias (underfit):

$$\left. \begin{array}{l} J_{train}(\theta) \text{ will be high} \\ J_{cv}(\theta) \approx J_{train}(\theta) \end{array} \right\}$$

Variance (overfit):

$$\left. \begin{array}{l} J_{train}(\theta) \text{ will be low} \\ J_{cv}(\theta) \gg J_{train}(\theta) \end{array} \right\}$$

\Rightarrow

Exercise

- Suppose you have a classification problem. The (misclassification) error is defined as $\frac{1}{m} \sum_{i=1}^m \text{err}(h_{\theta}(x^{(i)}) - y^{(i)})$ and the cross validation (misclassification) error is similarly defined, using the cross validation examples $(x_{CV}^{(1)}, y_{CV}^{(1)}), \dots, (x_{CV}^{m_{cv}}, y_{CV}^{m_{cv}})$
- Suppose your training error is 0.10, and your cross validation error is 0.30. What problem is the algorithm most likely to be suffering from?
 - High bias (overfitting)
 - High bias (underfitting)
 - High variance (overfitting)
 - High variance (underfitting)