Lesson 7: Modelling the data

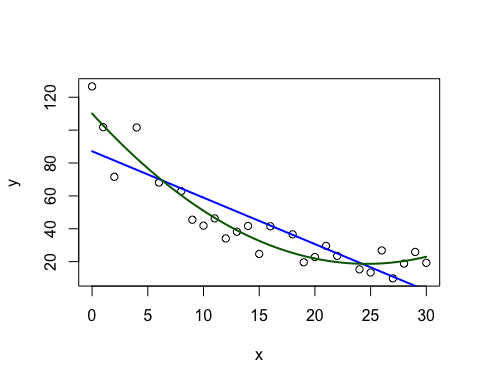
Adam Zabell

1/2/2018

# Data Modelling

After enough measurements have been made to consider your data a dataset, the next step is exploring that dataset to find trends and outliers. Most often, this includes a graph as well as a computational model which fits the data to a trendline. Modelling reduces the complexity of individual observations, which is good. However, it can only operate within the limits of the model. The linear model shown below doesn’t fit as well as the quadratic model, but deciding whether the quadratic model makes physical sense is not something the model can demonstrate.

# data taken from http://www.theanalysisfactor.com/r-tutorial-4/  
y <- c(126.6, 101.8, 71.6, 101.6, 68.1, 62.9, 45.5, 41.9, 46.3, 34.1, 38.2, 41.7, 24.7, 41.5, 36.6, 19.6, 22.8, 29.6, 23.5, 15.3, 13.4, 26.8, 9.8, 18.8, 25.9, 19.3)  
x <- c(0, 1, 2, 4, 6, 8, 9, 10, 11, 12, 13, 14, 15, 16, 18, 19, 20, 21, 22, 24, 25, 26, 27, 28, 29, 30)  
x2 <- x\*\*2  
raw <- tibble(x,y,x2)  
linearModel <- lm(y ~ x, data=raw)  
quadraticModel <- lm(y ~ x + x2, data=raw)  
plot(x,y)  
sequenceX <- seq(0,30,by=0.1)  
modeldata <- data.frame(x=sequenceX,x2=sequenceX\*\*2)  
sequenceYL <- predict(linearModel,modeldata)  
sequenceYQ <- predict(quadraticModel,modeldata)  
lines(sequenceX,sequenceYL,col='blue',lwd=2)  
lines(sequenceX,sequenceYQ,col='darkgreen',lwd=2)



Exercise 1: Rebuild this plot using ggplot  
Partially complete commands are commented out in the following code chunk.

modeldata <- modeldata %>%  
 mutate(linear=sequenceYL,quadratic=sequenceYQ)  
  
g <- ggplot(data=raw,aes(x=x,y=y)) + geom\_point()  
#g +   
# geom\_point(data= ,aes(x=x,y= ),color= ) +  
# geom\_point( , , )

## Parsing dates and times with *lubridate*

The context for most of the data we’ll encounter involve a time series, where each batch is collected at a specific date and that order of collection is a necessary component of the analysis. Dates within **R** are interpreted using the IEEE “POSIX” format, but reading data from an exterior source such as a CSV means this information arrives as a string. Functions in the **lubridate** package help to convert strings to POSIX, or combine information from multiple columns of a data.frame into a usable date format.

stringOfDates <- c("2017-12-15","2017-Dec-16","2017-12-17","2017-12-18","2017-12-19","2017-12-20","2017-12-21")  
stringOfDates + 7

## Error in stringOfDates + 7: non-numeric argument to binary operator

oneWeek <- ymd(stringOfDates)

## Warning in as.POSIXlt.POSIXct(x, tz): unknown timezone 'zone/tz/2017c.1.0/  
## zoneinfo/America/Indiana/Indianapolis'

oneWeek + 7

## [1] "2017-12-22" "2017-12-23" "2017-12-24" "2017-12-25" "2017-12-26"  
## [6] "2017-12-27" "2017-12-28"

tableOfDates <- tibble(year=rep(2017,8),  
 month=c(rep(4,3),rep(5,5)),  
 day=seq(1,8),  
 hour=rep(4,8),  
 minute=c(15,29,40,45,0,58,9,11))  
tableOfDates %$% make\_date(year,month,day) # uses the magrittr 'not a pipe' operator

## [1] "2017-04-01" "2017-04-02" "2017-04-03" "2017-05-04" "2017-05-05"  
## [6] "2017-05-06" "2017-05-07" "2017-05-08"

tableOfDates %$% make\_datetime(year,month,day,hour,minute)

## [1] "2017-04-01 04:15:00 UTC" "2017-04-02 04:29:00 UTC"  
## [3] "2017-04-03 04:40:00 UTC" "2017-05-04 04:45:00 UTC"  
## [5] "2017-05-05 04:00:00 UTC" "2017-05-06 04:58:00 UTC"  
## [7] "2017-05-07 04:09:00 UTC" "2017-05-08 04:11:00 UTC"

It helps to remember **R** uses “yyyy-mm-dd” as the default order for dates when viewing or exporting.

## Symbolic formula notation

The difficulty in using **R** for scientific modelling is that the language was built for statistical modelling. This is most obvious in the Wilkinson-Rogers notation for formula design. It is a versitile and powerful way to quickly describe the interactions between variables, but lacks an intuitive way to express basic transformations (quadratic, logrithmic, etc)

|  |  |
| --- | --- |
| Formula Notation | Common Understanding |
| y ~ x | y = *a0* + *a1*x |
| y ~ x - 1 | y = *a1*x |
| y ~ x + z | y = *a0* + *a1*x + *a2*z |
| y ~ x \* z | y = *a0* + *a1*x + *a2*z + *a3*xz |
| y ~ x + I(x^2) | y = *a0* + *a1*x + *a2*x2 |
| y ~ Gauss(amplitude,mu,sigma,x) | fit the data to a formula, defined elsewhere |

Wilkinson-Rogers notation comes into it’s own when looking for generalized interactions (and their relative importance) between the dependent variable and a collection of independent ones: the formula *y ~ Height \* Weight \* Age* would solve for eight coefficients, the linear combination for each of the three terms and the intercept. By comparison, the formula *y ~ Height + Weight + Age* would solve four coefficients, ignoring any interaction between Height, Weight, and Age.

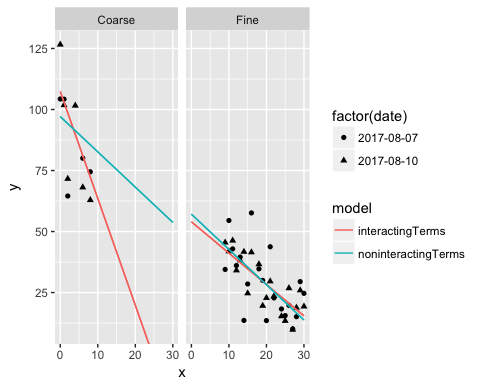
## Linear modelling

Most of time a linear model, or transforming the data into a linear model, is sufficient to establish the key relationships between variables. Let’s start by expanding the raw data.frame with additional observations and two more descriptors for the data.

newraw <- raw %>%   
 mutate(y = raw$y \* rnorm(nrow(raw),mean=1,sd=0.3)) %>%   
 rbind(raw) %>%  
 arrange(x)  
newraw$instrument <- c(rep("Coarse",12),rep("Fine",40))  
newraw$date <- c("07-08-2017","10-08-2017") %>%  
 rep(times=26) %>%  
 dmy() # as a single line without pipes: ymd( rep(c("2017-08-07","2017-08-10"),times=26) )

Now we can explore the simple linear model in context of the instrument or the date of collection.

fullModel <- lm(y ~ x \* date \* instrument, data=newraw)  
interactingTerms <- lm(y ~ x \* instrument, data=newraw)  
noninteractingTerms <- lm(y ~ x + instrument, data=newraw)  
grid <- newraw %>%  
 data\_grid(x,date,instrument) %>%  
 gather\_predictions(interactingTerms,noninteractingTerms)  
ggplot(newraw, aes(x,y,shape=factor(date))) +  
 geom\_point() +  
 geom\_line(data=grid, aes(y=pred,color=model)) +  
 coord\_cartesian(ylim=range(y)) +  
 facet\_wrap(~ instrument)



Exercise 2: Modelling with categorical variables  
Revise newraw so that the last 40 observations include a third instrument called “Ultrafine,” and rerun the models. How does this affect the regression and your interpretation?

newraw$instrument[13:52] <- rep(c(rep("Fine",2),rep("Ultrafine",2)),10)

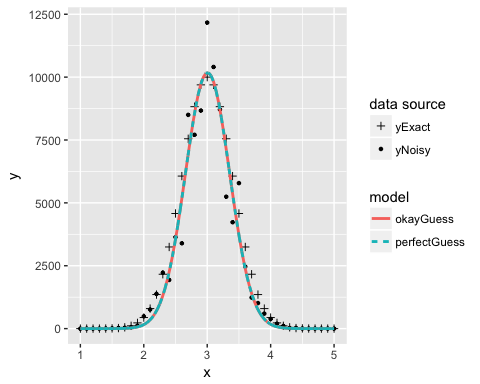
## Nonlinear modelling

Although not common when looking for relationships between variables, nonlinear models are a concern for other aspects of data evaluation (e.g. fitting a chromatogram to a Gaussian curve) or assay validation (e.g. instrument response as a function of concentration). Unlike linear modelling, which will find a single solution starting from the data itself, a nonlinear model must iterate from a starting guess for each variable. A well formed guess should converge on the correct value, but there is no general method for finding that guess.

Gauss = function(amplitude,mu,sigma,x){ amplitude\*exp(-0.5\*((x - mu)/sigma)^2) }  
x <- seq(1,5,by=0.1)  
yExact <- Gauss(10000,3,0.4,x)  
yNoisy <- yExact \* rnorm(length(yExact),mean=1,sd=0.3)  
noisyCurve <- tibble(x=x,y=yNoisy)  
perfectGuess <- nls(y ~ Gauss(a,m,s,x),   
 start=list(a=10000,m=3,s=0.4),  
 data=noisyCurve)  
okayGuess <- nls(y ~ Gauss(a,m,s,x),   
 start=list(a=max(yNoisy),m=x[yNoisy==max(yNoisy)],s=1),  
 data=noisyCurve)  
badGuess <- nls(y ~ Gauss(a,m,s,x),   
 start=list(a=1,m=1,s=1),  
 data=noisyCurve)

## Error in nls(y ~ Gauss(a, m, s, x), start = list(a = 1, m = 1, s = 1), : singular gradient

forPlot <- noisyCurve %>% rename(yNoisy=y) %>% cbind(yExact) %>% gather(yType,y,-x)  
grid <- forPlot %>%  
 data\_grid(x=seq\_range(x,100),y) %>%  
 gather\_predictions(perfectGuess,okayGuess)  
ggplot(forPlot, aes(x,y)) +  
 geom\_point(aes(shape=yType)) +  
 scale\_shape\_manual(values=c(3,20),name="data source") +  
 geom\_line(data=grid, aes(y=pred,color=model,linetype=model), size=1)



summary(perfectGuess)

##   
## Formula: y ~ Gauss(a, m, s, x)  
##   
## Parameters:  
## Estimate Std. Error t value Pr(>|t|)   
## a 1.018e+04 3.812e+02 26.71 <2e-16 \*\*\*  
## m 3.006e+00 1.506e-02 199.57 <2e-16 \*\*\*  
## s 3.484e-01 1.506e-02 23.14 <2e-16 \*\*\*  
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## Residual standard error: 773.5 on 38 degrees of freedom  
##   
## Number of iterations to convergence: 6   
## Achieved convergence tolerance: 7.351e-06

Understanding the reasoning for nonlinear model selection is a critical step before attempting that fit. The risk of non-convergence means the nonlinear model should be avoided, if possible.

# Summary

* **lubridate** functions will convert a text string to a date
* statistial modelling with Wilkinson-Rogers notation builds possible interactions into the analysis
* scientific modelling with Wilkinson-Rogers notation requires careful understanding of terms
* linear models are strongly recommended whenever possible
  + this may require a transformation of the data
  + ‘linear’ doesn’t mean ‘straight line’ when you draw the plot
* nonlinear models are dependant on a starting guess