

Cuprins

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Alocarea dinamică a memoriei.

Tipuri specifice.

Laborator 1

16. Scrieți funcții pentru implemetarea operațiilor specifice pe matrice de numere reale cu m linii și n coloane: suma, diferența și produsul al două matrice, produsul dintre o matrice și un scalar real, transpusa unei matrice, norme matriceale specifice¹, citirea de la tastatură a componentelor unei matrice, afișarea componentelor matricei. Pentru cazul particular al unei matrice patratice de ordin n , să se testeze dacă aceasta satisface criteriul de dominanță pe linii² sau pe coloane³. Se vor folosi tablouri bidimensionale alocate static.

```
1  #include <iostream>
2  #include <cmath>
3
4  constexpr int MAX_SZ = 8;
5  int readSize(const char* name) {
6      int res;
7      do {
8          std::cout << name << ": ";
9          std::cin >> res;
10     } while (res <= 0 || res >= MAX_SZ);
11     return res;
12 }
13
14 void assert(bool cond, const char* msg) {
15     if (!cond) throw std::logic_error(msg);
16 }
17
18 struct Mat {
19     double data[MAX_SZ][MAX_SZ] {};
20     int m, n;
21
22     Mat() : m(0), n(0) {}
23     Mat(int m, int n) : m(m), n(n) {}
24 }
```

¹Dacă $A \in \mathcal{M}_{m \times n}(\mathbb{R})$, atunci $\|A\|_1 = \max_{1 \leq j \leq n} \sum_{i=1}^m |a_{ij}|$, $\|A\|_\infty = \max_{1 \leq i \leq m} \sum_{j=1}^n |a_{ij}|$, $\|A\|_F = \sqrt{\sum_{i=1}^m \sum_{j=1}^n a_{ij}^2}$.

² $A \in \mathcal{M}_n(\mathbb{R})$ este strict diagonal dominantă pe linii dacă $|a_{ii}| > \sum_{\substack{j=1 \\ j \neq i}}^n |a_{ij}|$, pentru orice $i = 1, \dots, n$.

³ $A \in \mathcal{M}_n(\mathbb{R})$ este strict diagonal dominantă pe colonane dacă $|a_{jj}| > \sum_{\substack{i=1 \\ i \neq j}}^n |a_{ij}|$, pentru orice $j = 1, \dots, n$.

```

25     static Mat read() {
26         Mat res(readSize("m"), readSize("n"));
27
28         for (int i = 0; i < res.m; ++i)
29             for (int j = 0; j < res.n; ++j)
30                 std::cin >> res.data[i][j];
31         return res;
32     }
33     void setSize(int m, int n) {
34         this->m = m;
35         this->n = n;
36     }
37     double& at(int i, int j) { return data[i][j]; }
38     double at(int i, int j) const { return data[i][j]; }
39
40     void print(const char* name) const {
41         std::cout << name << " = Mat " << m << "x" << n << "{\n";
42         for (int i = 0; i < m; ++i) {
43             for (int j = 0; j < n; ++j)
44                 std::cout << at(i, j) << " ";
45             std::cout << "\n";
46         }
47         std::cout << "}\n";
48     }
49 private:
50     enum class Type { Row, Col };
51     template<Type type>
52     bool isStrictlyDiagonallyDominantImpl() const {
53         assert(m == n, "Matrix must be square");
54         for (int i = 0; i < m; ++i) {
55             double val = std::abs(at(i, i));
56             double sum = -val;
57             for (int j = 0; j < m; ++j)
58                 sum += std::abs(type == Type::Col ? at(j, i) : at(i, j));
59             if (sum >= val) return false;
60         }
61         return true;
62     }
63
64     template<Type type>
65     double normImpl(int sz1, int sz2) const {
66         double max = -1;
67         for (int j = 0; j < sz1; ++j) {
68             double x = 0;
69             for (int i = 0; i < sz2; ++i)
70                 x += std::abs(type == Type::Col ? at(j, i) : at(i, j));
71             if (x > max) max = x;
72         }
73         return max;
74     }

```

```

75 public:
76     double norm1() const { return normImpl<Type::Row>(n, m); }
77     double normInf() const { return normImpl<Type::Col>(m, n); }
78     double normF() const {
79         double res = 0;
80         for (int i = 0; i < m; ++i)
81             for (int j = 0; j < n; ++j)
82                 res += at(i, j) * at(i, j);
83
84         return std::sqrt(res);
85     }
86     bool isStrictlyRowDiagonallyDominant() const {
87         return isStrictlyDiagonallyDominantImpl<Type::Row>();
88     }
89     bool isStrictlyColDiagonallyDominant() const {
90         return isStrictlyDiagonallyDominantImpl<Type::Col>();
91     }
92 };
93
94 Mat& add(const Mat& a, const Mat& b, Mat& res) {
95     assert(a.m == b.m && a.n == b.n, "Sizes don't match, can't add");
96     res.setSize(a.m, a.n);
97     for (int i = 0; i < a.m; ++i)
98         for (int j = 0; j < a.n; ++j)
99             res.at(i, j) = a.at(i, j) + b.at(i, j);
100     return res;
101 }
102 Mat& mul(double a, const Mat& b, Mat& res) {
103     res.setSize(b.m, b.n);
104
105     for (int i = 0; i < res.m; ++i)
106         for (int j = 0; j < res.n; ++j)
107             res.at(i, j) = a * b.at(i, j);
108     return res;
109 }
110 Mat& neg(const Mat& a, Mat& res) { return mul(-1, a, res); }
111 Mat& sub(const Mat& a, const Mat& b, Mat& res) {
112     return add(a, neg(b, res), res);
113 }
114 Mat& mul(const Mat& a, const Mat& b, Mat& res) {
115     assert(a.n == b.m, "Sizes don't match, can't multiply");
116     res.setSize(a.m, b.n);
117
118     for (int i = 0; i < res.m; ++i)
119         for (int j = 0; j < res.n; ++j) {
120             res.at(i, j) = 0;
121             for (int k = 0; k < a.n; ++k)
122                 res.at(i, j) += a.at(i, k) * b.at(k, j);
123         }
124     return res;

```

```

125 }
126 Mat& trans(const Mat& a, Mat& res) {
127     assert(a.data != res.data, "Can't calculate the transpose inplace");
128     res.setSize(a.n, a.m);
129
130     for (int i = 0; i < res.m; ++i)
131         for (int j = 0; j < res.n; ++j)
132             res.at(i, j) = a.at(j, i);
133     return res;
134 }

```

Laborator 2

18. Scrieți funcții pentru implementarea operațiilor specifice pe vectori din \mathbb{R}^n : suma, diferența și produsul scalar al doi vectori, produsul dintre un vector și un scalar real, negativarea unui vector, norma euclidiană a unui vector, citirea de la tastatură a celor n componente ale unui vector, afișarea componentelor vectorului sub forma unui n -uplu de elemente. Se vor folosi tablouri unidimensionale alocate dinamic.

```

1  #include <iostream>
2  #include <utility>
3  #include <cmath>
4
5  constexpr size_t getSize(const std::initializer_list<double>& l) {
6      size_t n = 0;
7      auto it = l.begin();
8      auto end = l.end();
9      while (it++ != end) ++n;
10     return n;
11 }
12 constexpr int MAX_SZ = 256;
13 size_t readSize(const char* name) {
14     int res;
15     do {
16         std::cout << name << ": ";
17         std::cin >> res;
18     } while (res <= 0 || res >= MAX_SZ);
19     return res;
20 }
21
22 void assert(bool cond, const char* msg) {
23     if (!cond) throw std::logic_error(msg);
24 }
25
26 struct Vec {
27     double *_begin, *_end;
28
29     constexpr double* begin() { return _begin; }
30     constexpr const double* begin() const { return _begin; }
31 }

```

```

32
33 constexpr double* end() { return _end; }
34 constexpr const double* end() const { return _end; }
35
36 constexpr Vec() : _begin(nullptr), _end(nullptr) {}
37 explicit Vec(size_t n) : _begin(new double[n]), _end(_begin+n) {}
38 Vec(std::initializer_list<double> list) : Vec(getSize(list)) {
39     auto it = _begin;
40     for (const auto& v : list) *(it++) = v;
41 }
42 Vec(const Vec&) = delete;
43 Vec(Vec&& rhs) noexcept
44     : _begin(std::exchange(rhs._begin, nullptr)),
45     _end(std::exchange(rhs._end, nullptr)) {}
46
47 Vec& operator=(const Vec&) = delete;
48 Vec& operator=(Vec&& rhs) noexcept {
49     this->~Vec();
50     _begin = std::exchange(rhs._begin, nullptr);
51     _end = std::exchange(rhs._end, nullptr);
52     return *this;
53 }
54
55 ~Vec() { delete[] _begin; }
56
57 constexpr size_t size() const { return _end - _begin; }
58
59 constexpr double& operator[](size_t i) { return _begin[i]; }
60 constexpr const double operator[](size_t i) const { return _begin[i]; }
61
62 void setSize(size_t n) {
63     if (size() == n) return;
64     *this = Vec(n);
65 }
66
67 friend std::ostream& operator<<(std::ostream& s, const Vec& v) {
68     s << "(";
69     double* it = v._begin;
70     for (double* end = v._end - 1; it < end; ++it)
71         s << *it << ", ";
72
73     if (it < v._end) s << *it;
74
75     return s << ")";
76 }
77 static Vec read() {
78     Vec res(readSize("n"));
79     for (auto& v: res) std::cin >> v;
80     return res;
81 }

```

```

82     double norm() const;
83 };
84 void assertSizes(const Vec& a, const Vec& b) {
85     assert(a.size() == b.size(), "Sizes don't match");
86 }
87
88 Vec& add(const Vec& a, const Vec& b, Vec& res) {
89     assertSizes(a, b);
90     res.setSize(a.size());
91     auto aIt = a.begin();
92     auto bIt = b.begin();
93     for (auto& v : res) v = *(aIt++) + *(bIt++);
94     return res;
95 }
96
97 Vec& mul(double a, const Vec& b, Vec& res) {
98     res.setSize(b.size());
99     auto it = b.begin();
100    for (auto& v : res) v = a * (*(it++));
101    return res;
102 }
103
104 Vec& neg(const Vec& b, Vec& res) { return mul(-1, b, res); }
105
106 Vec& sub(const Vec& a, const Vec& b, Vec& res) {
107     return add(a, neg(b, res), res);
108 }
109 double dot(const Vec& a, const Vec& b) {
110     double res = 0;
111     assertSizes(a, b);
112     auto bIt = b.begin();
113     for (auto& v : a) res += v * (*(bIt++));
114     return res;
115 }
116 double norm(const Vec& a) {
117     return std::sqrt(dot(a, a));
118 }
119 double Vec::norm() const {
120     return ::norm(*this);
121 }

```