

# Statistical Analysis of Reliability and Survival Data: Rotterdam Dataset

#### Authors

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### 1 Exploratory Data Analysis

These data sets are used in the paper by Royston and Altman that is referenced below. The Rotterdam data is used to create a fitted model, and the GBSG data for validation of the model. The paper gives references for the data source.

There are 43 subjects who have died without recurrence, but whose death time is greater than the censoring time for recurrence. A common way that this happens is that a death date is updated in the health record sometime after the research study ended, and said value is then picked up when a study data set is created. But it raises serious questions about censoring. For instance subject 40 is censored for recurrence at 4.2 years and died at 6.6 years; when creating the endpoint of recurrence free survival (earlier of recurrence or death), treating them as a death at 6.6 years implicitly assumes that they were recurrence free just before death. For this to be true we would have to assume that if they had progressed in the 2.4 year interval before death (while off study), that this information would also have been noted in their general medical record, and would also be captured in the study data set. However, that may be unlikely. Death information is often in a centralized location in electronic health records, easily accessed by a programmer and merged with the study data, while recurrence may require manual review. How best to address this is an open issue.

Table 1: Data description

pid	Patient identifier					
year	Year of surgery					
age	Age at surgery					
meno	Menopausal status $(0 = premenopausal, 1 = postmenopausal)$					
size	Tumor size, a factor with levels $\leq 20, 20-25, > 50$					
grade	Differentiation grade					
nodes	Number of positive lymph nodes					
pgr	Progesterone receptors (fmol/l)					
er	Estrogen receptors (fmol/l)					
hormon	Hormonal treatment (0=no, 1=yes)					
chemo	Chemotherapy					
rtime	Days to relapse or last follow-up					
recur	0 = no relapse, 1 = relapse					
$\operatorname{dtime}$	Days to death or last follow-up					
death	0 = alive, 1 = dead					

Table 1 explains the covariates in the Rotterdam dataset.

# 2 Further Analysis

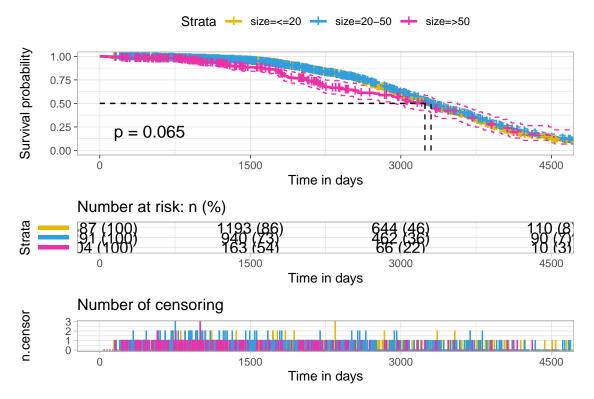
Now the focus will be on the response variable, the censoring indicator, and the categorical variable.

#### 2.1 Survival Distribution by Levels of ...

(a) For each of the levels of the categorical variable, compute the survival distribution. Plot them on the same graph. What do the graphs suggest?

#### 2.1.1 Size

```
## Call: survfit(formula = Surv(dtime, censored) ~ size, data = data)
##
                 n events median 0.95LCL 0.95UCL
##
                             3289
                                     3232
## size=<=20 1387
                     1048
                                              3370
## size=20-50 1291
                      734
                             3301
                                     3230
                                              3408
## size=>50
               304
                      123
                             3240
                                     2918
                                              3565
##
              records n.max n.start events rmean se(rmean) median 0.95LCL
                 1387
                       1387
                                1387
                                       1048 3282.860 32.47471
                                                                   3289
                                                                           3232
## size=<=20
                                        734 3342.568 39.62310
                                                                   3301
                                                                           3230
## size=20-50
                 1291
                       1291
                                1291
## size=>50
                  304
                         304
                                 304
                                        123 3083.707 104.26023
                                                                   3240
                                                                           2918
##
              0.95UCL
                 3370
## size=<=20
## size=20-50
                 3408
## size=>50
                 3565
##
    time n.risk n.event n.censor
                                        surv
                                                  upper
                                                            lower
                                 0 0.9992790 1.0000000 0.9978674
## 1
       36
            1387
                       1
## 2
       64
            1386
                       1
                                 0 0.9985580 1.0000000 0.9965631
                                 0 0.9978371 1.0000000 0.9953951
## 3
       97
            1385
                       1
                                 0 0.9971161 0.9999422 0.9942980
                       1
## 4
     101
            1384
## 5
     129
            1383
                       1
                                 0 0.9963951 0.9995542 0.9932460
## 6 141
            1382
                       0
                                 1 0.9963951 0.9995542 0.9932460
                          Strata → size=<=20 → size=20-50 → size=>50
        1.00
Survival probability
        0.75
        0.50
        0.25
                 p = 0.065
        0.00
                              2000
                                              4000
                                                               6000
                                                                               8000
                                              Time
            Number at risk
                              2000
                                              4000
                                                                               8000
                                                              6000
                                              Time
```



The horizontal axis represents time in days, and the vertical axis shows the probability of surviving, or the proportion of people surviving. The lines represent survival curves of the three groups. A vertical drop in the curves indicates an event. The vertical tick mark on the curves means that a patient was censored at this time.

At time zero, the survival probability is 1.0 (or 100% of the participants are alive). At time 2250, the probability of survival is approximately 0.625 for size>=50, and 0.85 for size<50. The median survival is approximately 3300 for size>=50, and a bit more for other two groups, suggesting slightly worse survival for patients with tumor of larger size. However, to evaluate whether this difference is statistically significant requires a formal statistical test, a subject that is discussed in the next sections.

The median survival times for each group can be seen from:

##		records	n.max	n.start	events	rmean	se(rmean)	median	0.95LCL
##	size=<=20	1387	1387	1387	1048	3282.860	32.47471	3289	3232
##	size=20-50	1291	1291	1291	734	3342.568	39.62310	3301	3230
##	size=>50	304	304	304	123	3083.707	104.26023	3240	2918
##		0.95UCL							
##	size=<=20	3370							
##	size=20-50	3408							
##	size=>50	3565							

#### 2.2 Confidence Intervals and Estimators by Levels of ...

(b) For each level obtain an appropriate estimator and confidence interval for the 3 quartiles of the survival curves. Interpret the results.

## 2.3 Test of Differences Between the Survival Curves

(c) Conduct a single test of differences between the survival curves. Justify your choice of test.