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# Statistical Analysis of Reliability and Survival Data: Rotterdam Dataset

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## Authors

Aksoy, Barış r0869901

Heller, Jack r0862809

Zdravković, Aleksandra r0869484

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# 1 Exploratory Data Analysis

These data sets are used in the paper by Royston and Altman that is referenced below. The Rotterdam data is used to create a fitted model, and the GBSG data for validation of the model. The paper gives references for the data source.

There are 43 subjects who have died without recurrence, but whose death time is greater than the censoring time for recurrence. A common way that this happens is that a death date is updated in the health record sometime after the research study ended, and said value is then picked up when a study data set is created. But it raises serious questions about censoring. For instance subject 40 is censored for recurrence at 4.2 years and died at 6.6 years; when creating the endpoint of recurrence free survival (earlier of recurrence or death), treating them as a death at 6.6 years implicitly assumes that they were recurrence free just before death. For this to be true we would have to assume that if they had progressed in the 2.4 year interval before death (while off study), that this information would also have been noted in their general medical record, and would also be captured in the study data set. However, that may be unlikely. Death information is often in a centralized location in electronic health records, easily accessed by a programmer and merged with the study data, while recurrence may require manual review. How best to address this is an open issue.

Table 1: Data description

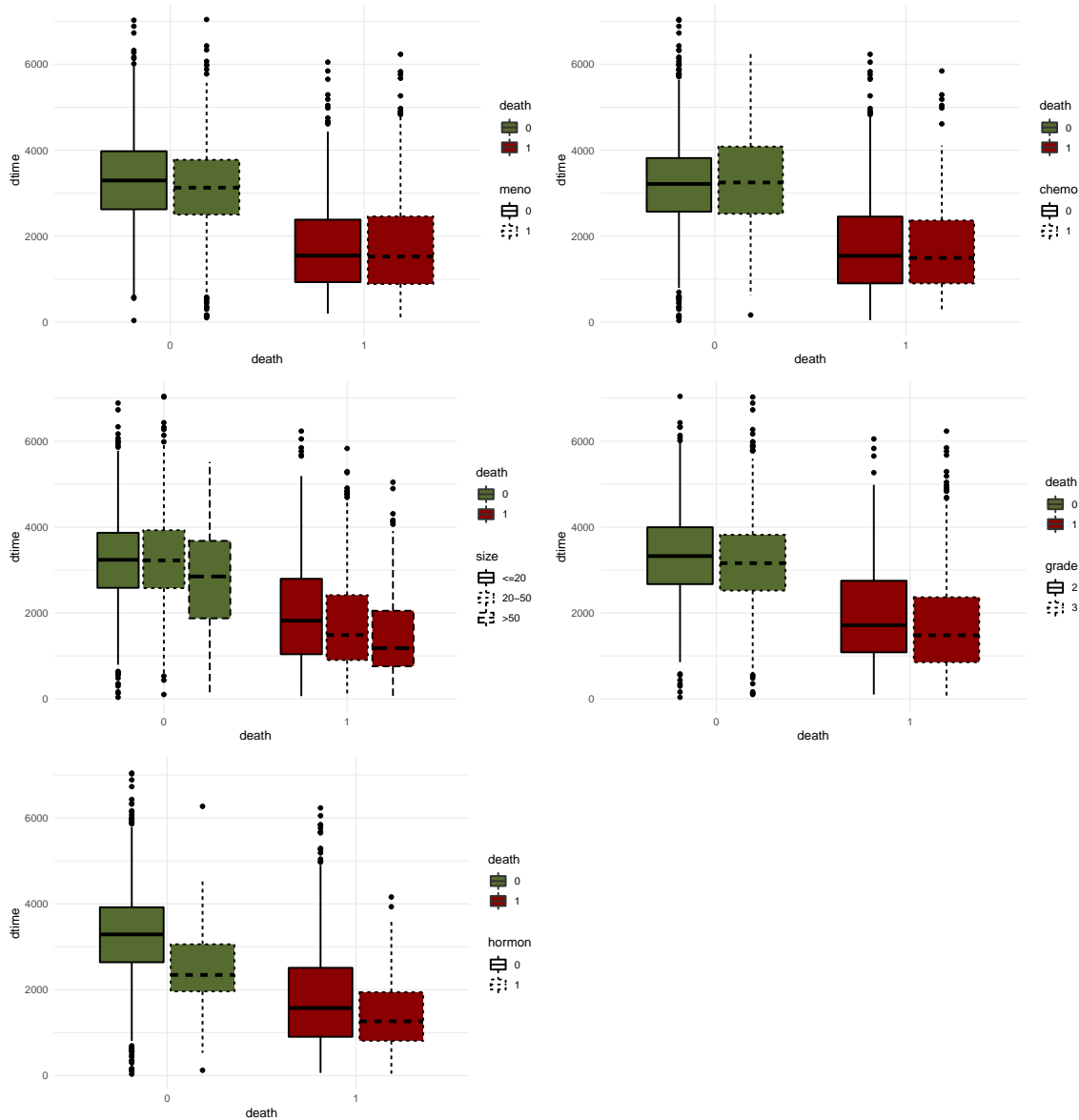
pid	Patient identifier
year	Year of surgery
age	Age at surgery
meno	Menopausal status (0 = premenopausal, 1 = postmenopausal)
size	Tumor size, a factor with levels $\leq 20$ , 20-25, $> 50$
grade	Differentiation grade
nodes	Number of positive lymph nodes
pgr	Progesterone receptors (fmol/l)
er	Estrogen receptors (fmol/l)
hormon	Hormonal treatment (0=no, 1=yes)
chemo	Chemotherapy
rtime	Days to relapse or last follow-up
recur	0 = no relapse, 1 = relapse
dtime	Days to death or last follow-up
death	0 = alive, 1 = dead

Table 1 explains the covariates in the Rotterdam dataset.

## 1.1 Categorical Variables

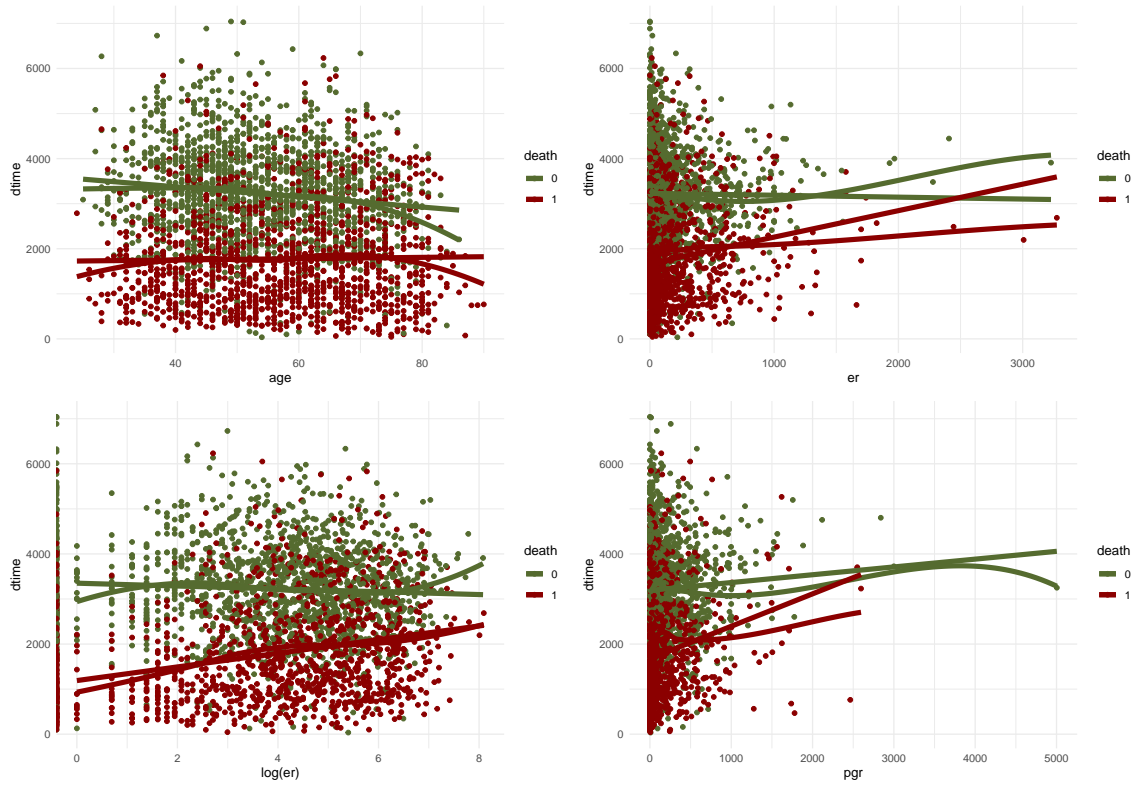
When we investigate the categorical variables, we see that some have a larger difference between time until death than others. When we first investigate menopause, we see that menopausal patients are very similar in their death time. A very similar pattern is observed for chemotherapy but the patients that did not die had a slightly higher time before leaving the study. While size, having three levels, needs to be interpreted slightly differently. With patients that died, the larger cancer cells certainly caused it to happen sooner. This makes intuitive sense that more severe cancer would have more long term health risks. Among patients that do not die, only

the extremely large cancer patients had a much lower recurrence time. While small and medium patients had a very similar response. Grade had a very similar response among all patients with higher grade patients living slightly shorter lives. Patients given hormonal therapy seem to have a smaller tail among patients that died; meaning those who relapse are more likely to do it soon after treatment. Surviving patients that had hormonal therapy also appear to be censored more quickly than those who do not receive the treatment.



## 1.2 Continuous Variables

Among continuous variables, we first investigated age. We plotted a both the lowess curve and the linear model to see if they match. If so, they most likely have data with a limited skew and do not require transformation for modeling. We first evaluated age and there was not a difference between the linear and lowess curves. Next, we investigated the relationship between er and death time. Here we see a large deviation which was corrected for again with a log transform. Finally, we evaluated pgr and it had a good fit overall.



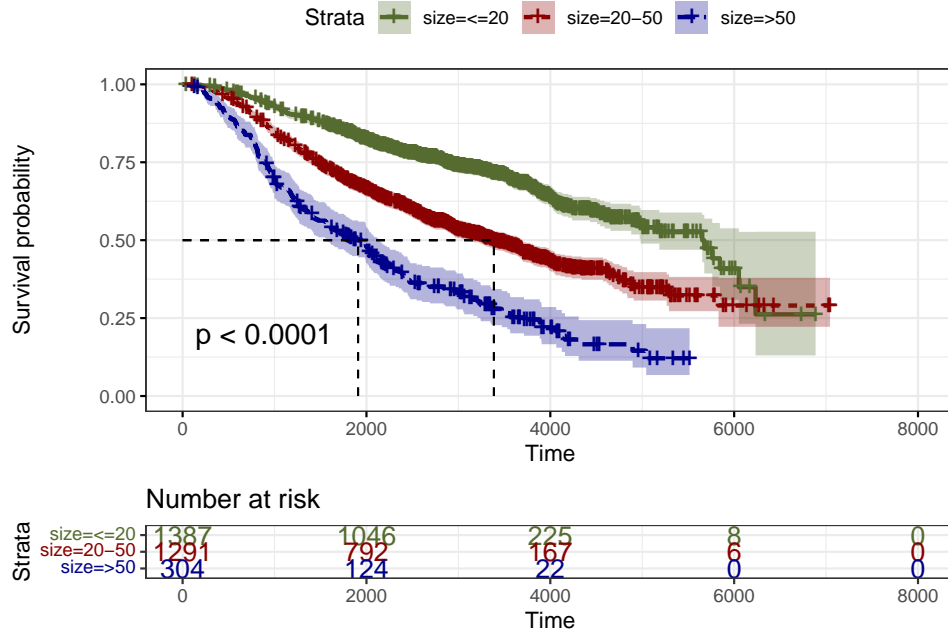
## 2 Further Analysis

Now the focus will be on the response variable, the censoring indicator, and the categorical variable.

### 2.1 Survival Distrubution by Levels of *Size*, *Meno*, *Hormon*, and *Chemo*

For each of the levels of the categorical variables, we will compute the survival distribution and interpret the results.

### 2.1.1 Size



The horizontal axis represents time in days, and the vertical axis shows the probability of surviving, or the proportion of people surviving. The lines represent survival curves of the three groups. A vertical drop in the curves indicates an event. The vertical tick mark on the curves means that a patient was censored at this time.

Table 2: Summary of the model.

	records	n.max	n.start	events	rmean	se(rmean)	median	0.95LCL	0.95UCL
Size ( $\leq$ 20)	1387	1387	1387	414	4721.199	119.40159	5653	4983	
Size (20–50)	1291	1291	1291	646	3807.025	95.52799	3386	3084	3690
Size ( $>$ 50)	304	304	304	212	2537.178	148.10071	1909	1566	2141

At time zero, the survival probability is 1.0 (or 100% of the participants are alive). At time 2250, the probability of survival is approximately 0.625 for size  $\geq$  50, and 0.85 for size  $<$  50.

From Table 2 can be seen that the median survival for Size 50 is 5653, for Size 20-50 is 3386, and for Size  $>$  50 is 1909. This suggests worse survival for patients with tumor of larger size. However, to evaluate whether this difference is statistically significant requires a formal statistical test, a subject that is discussed in the next sections.

### 2.1.2 Menopause

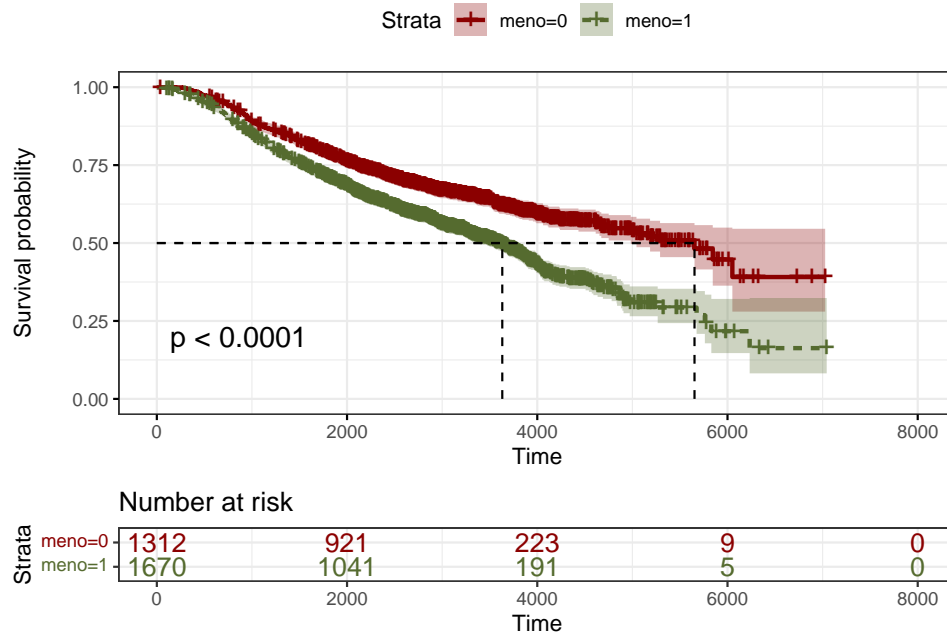


Table 3: Median survival times for each group.

	records	n.max	n.start	events	rmean	se(rmean)	median	0.95LCL	0.95UCL
Meno = 0	1312	1312	1312	468	4622.427	108.80722	5653	4983	
Meno = 1	1670	1670	1670	804	3672.887	92.46545	3632	3368	3813

At time zero, the survival probability is 1.0 (or 100% of the participants are alive). At time 2200, the probability of survival is approximately 0.75 for non-menopausal patients, and 0.825 for menopausal patients.

From Table 3 can be seen that the median survival is 5653 for non-menopausal patients, and 3632 for menopausal, suggesting worse survival for patients that have gone through menopause.

### 2.1.3 Hormonal Treatment

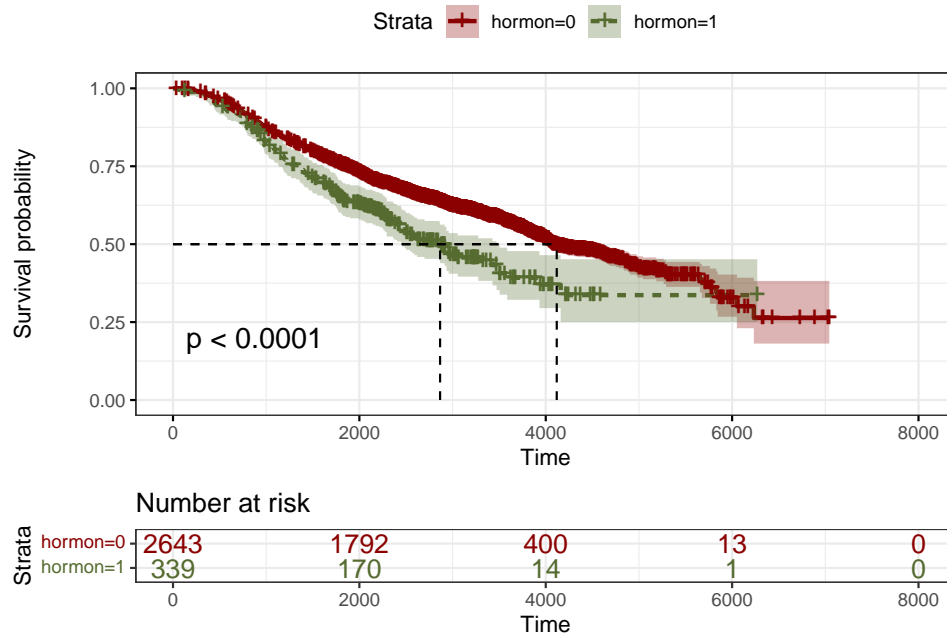


Table 4: Median survival times for each group.

	records	n.max	n.start	events	rmean	se(rmean)	median	0.95LCL	0.95UCL
hormon=0	2643	2643	2643	1113	4159.588	76.57099	4118	3988	4614
hormon=1	339	339	339	159	3659.665	203.38456	2866	2450	3472

At time zero, the survival probability is 1.0 (or 100% of the participants are alive). At time 2200, the probability of survival is approximately 0.75 for premenopausal patients, and 0.825 for postmenopausal patients.

From Table 4 can be seen that the median survival is 4118 for patients that went through hormonal therapy, and 2866 for those who did not, suggesting slightly worse survival for patients that have gone through the hormonal therapy. However, to evaluate whether this difference is statistically significant requires a formal statistical test, a subject that is discussed in the next sections.

### 2.1.4 Chemotherapy

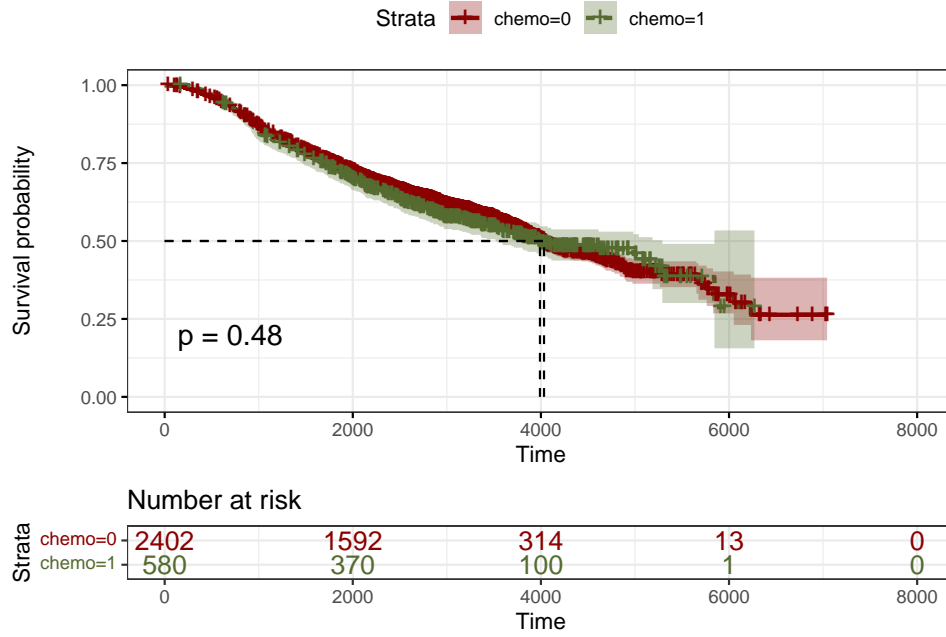


Table 5: Median survival times for each group.

	records	n.max	n.start	events	rmean	se(rmean)	median	0.95LCL	0.95UCL
chemo=0	2402	2402	2402	1014	4103.663	80.06765	4033	3885	4239
chemo=1	580	580	580	258	4080.311	162.59049	3990	3522	5291

At time zero, the survival probability is 1.0 (or 100% of the participants are alive). At time 2200, the probability of survival is approximately 0.75 for premenopausal patients, and 0.825 for postmenopausal patients.

From Table 5 can be seen that the median survival is 4118 for patients that went through hormonal therapy, and 2866 for those who did not, suggesting slightly better survival for patients that have gone through chemotherapy. However, to evaluate whether this difference is statistically significant requires a formal statistical test, a subject that is discussed in the next sections.

## 2.2 Confidence Intervals and Estimators by Levels of *Size*, *Meno*, *Hormon*, and *Chemo*

For each level we will obtain an appropriate estimator and confidence interval for the 3 quartiles of the survival curves and interpret the results.

We first evaluate size and see similar results to what was observed in the EDA barcharts. We see that at the 25th percentile, size >50 has a very significant difference from the other two groups. With this being significantly smaller, their dtime is significantly smaller. This intuitively makes sense that a person who has larger cancer would have a worse life expectancy. However, this phenomenon has faded by the 50th percentile and persists through the 75th. This means that if a person survives the initial hurdle after surgery, they are not expected to be significantly different from the rest of the population.

When we investigate the effect of menopause on survival, we see that generally people that are menopausal have lower survival times. This is supported by that at the 25th, 50th, and 75th



Table 6: Estimates and confidence intervals for 3 quartiles for each level of covariates *size*, *chemo*, *meno*, *hormon*.

	$\hat{q}_1$	5%	95%	$\hat{q}_2$	5%	95%	$\hat{q}_3$	5%	95%
Size ( $\leq 20$ )	2880	2590	3315	5653	4983	NA	NA	6051	NA
Size (20–50)	1476	1361	1623	3386	3084	3690	NA	5830	NA
Size ( $> 50$ )	890	809	999	1909	1566	2141	3714	3240	4309
Chemo = 0	1812	1677	1957	4033	3885	4239	NA	6051	NA
Chemo = 1	1699	1455	1954	3990	3522	5291	NA	5845	NA
Meno = 0	2115	1944	2371	5653	4983	NA	NA	NA	NA
Meno = 1	1571	1424	1723	3632	3368	3813	5762	5266	NA
Hormon = 0	1882	1742	1994	4118	3988	4614	NA	6051	NA
Hormon = 1	1361	1140	1618	2866	2450	3472	NA	NA	NA

percentiles, there is no overlap in the quantiles' confidence intervals. This means that at all stages, a menopausal person would have a shorter life. However, this could be due to other covariates such as the fact that all menopausal people are women or that they tend to be older.

We next evaluate the effect of hormonal treatment. We see here that those who received hormonal treatment generally have a lower survival time. We also see that there is no overlap between the confidence intervals indicating that not only did they have a large difference, but it sustained itself throughout the entire distribution of patients.

Finally, we evaluate the effect of chemotherapy. Here we see that generally chemotherapy patients live longer. However, this only becomes significant at the 75th percentile. This means that generally patients that receive chemotherapy are not significantly affected until they live for a long time.

## 2.3 Test of Differences Between the Survival Curves

Table 7: Stratified log-rank test for differences in menopause.

	$\chi^2$	df	p-value
Stratified by Chemo	69.59	1	0
Stratified by Size	42.53	1	0
Stratified by Hormon	44.06	1	0

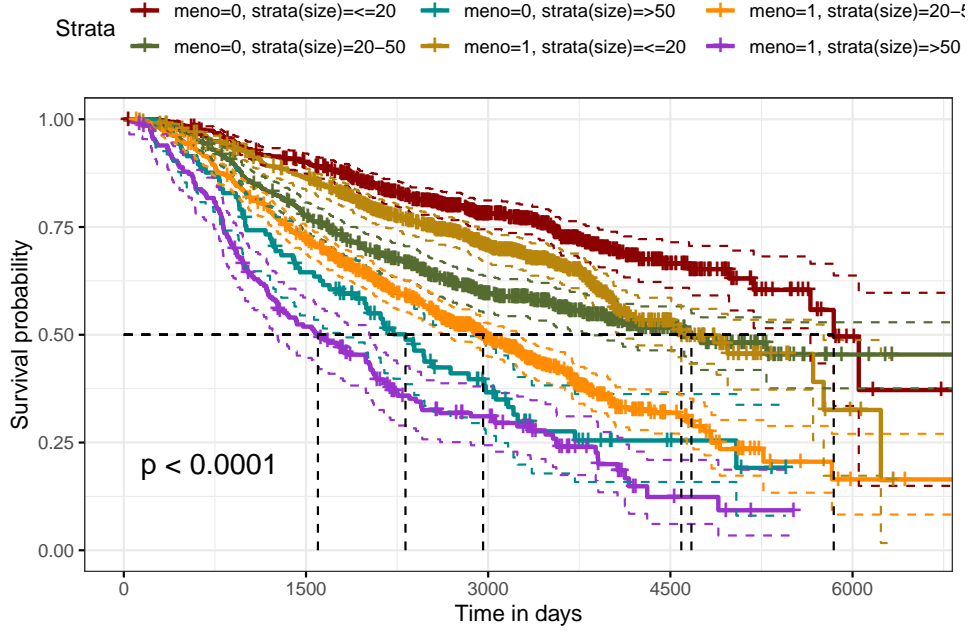


Figure 1: Independent variable meno stratified by size of the tumor.

In this setting we chose to use the log-rank test. This is because we do not want to weight any observations more heavily than others. Thus, we set  $W(Y(j)) = 1$ . The log-rank test is the most powerful so it is the best choice. However, this test is only the most powerful when the hazard rates are proportional to each other within populations. For this reason, we stratify the model to identify its impacts and make sure no assumptions are violated.

What we see when we perform this stratification is a very large difference between someone without menopause and small cancer cells and someone who is menopausal and has very large cancer cells. We also see that stratifying on age has the best fit.

### 3 Modeling

#### 3.1 Semiparametric Proportional Hazards Model

For semiparametric proportional hazards model, we proceed as follows:

The variable *size* is a categorical variable with 3 levels. We recode the levels Size (20 – 50) and Size (> 50) as binary variables, and take the level Size ( $\leq 20$ ) as reference level. We then estimate the full model, only excluding variables *rtime* and *recur*, since they are not the chosen event of interest.

Table 8: AIC values for models selected by stepwise AIC procedure, and backward selection procedure.

	Stepwise AIC	Backward Selection
AIC	18543.63	18546.82

For model selection with all covariates, we first fit a full model to apply backward selection procedure. By excluding the covariate with the largest p-value in each iteration, we ended up with the

model where significant covariates are *size*, *age*, *grade*, *nodes*, *pgr*, *meno*, *hormon*.

Next, we run stepwise AIC selection in both directions. This resulted with the model where significant covariates are *size*, *age*, *grade*, *nodes*, *pgr*.

To decide which procedure should be used to choose the model, we approach from 2 different points. From a logical point of view, the model including hormonal treatment is reasonable since it might have a direct influence on survival time. If we compare AIC of both models, from Table 8 we see that there is no huge difference ( $1.8544 \times 10^4$  and  $1.8547 \times 10^4$ , respectively). So we decide to go with the model selected based on p-value since it includes hormon in exchange of acceptable increase in AIC.

Table 9: Relative risks and CI for each covariate

	$\chi^2$	df	p-value
Stratified by Chemo	69.59	1	0
Stratified by Size	42.53	1	0
Stratified by Hormon	44.06	1	0

Estimation and CI of relative risks for every pair of levels of the categorical variables are as below: HR of chemo vs non-chemo: 1.0423 with 95%CI [0.91353 1.18914] HR of meno vs non-meno: 0.8160 with 95%CI [0.69415 0.95916] HR of hormon treatment vs no treatment: 1.7815 with 95%CI [0.69415 0.95916] HR of size20-50 vs size<=20: 0.8650 with 95%CI [0.78503 0.95308] HR of size>50 vs size<=20: 0.9678 with 95%CI [0.79736 1.17457] HR of size>50 vs size20-50:  $\exp(\text{Beta}(\text{size}>50) - \text{Beta}(\text{size}20-50)) = \{\exp(\text{fit\_ph4coefficients}['\text{as.factor}(\text{size}) > 50']) / \exp(\text{fit\_ph4coefficients}['\text{as.factor}(\text{size}) 20-50'])\} = 1.118818$  with 95%CI [??] HR of age i vs age i-1: 1.0075 with 95%CI [1.00110 1.01387] HR of grade 3 vs grade 2: 1.0575 with 95%CI [0.95655 1.16910] HR of recur vs non-recur: 0.0131 with 95%CI [0.01043 0.01646] HR of rtime i vs rtime i-1: 0.9985 with 95%CI [0.99841 0.99854]

Table 10: Proportional Hazard Test

	chisq	df	p
meno	4.3296389	1	0.0374542
hormon	0.7301267	1	0.3928421
as.factor(size)	5.2190506	2	0.0735695
age	13.9604002	1	0.0001867
as.factor(grade)	3.1603999	1	0.0754447
nodes	3.9615599	1	0.0465505
pgr	41.7855085	1	0.0000000
GLOBAL	60.9142139	8	0.0000000

We run a statistical test based on Schoenfeld residuals for proportional hazard assumption for each covariate included in the Cox fit. From the output, one can see that test is statistically significant for some covariates like age, pgr, and meno with nodes and grade being a borderline case. The global test is also significant. So we can state that proportional hazard assumption is violated since there is significant dependency between Schoenfeld residuals and time.

Table 11: Parametric Model Evaluation

	AIC
log(normal)	24031.88
weibull	24120.92
exponential	24259.09
log(logistic)	24045.35

### 3.2 Parametric Regression Models

We first evaluate parametric models based on variables already selected in the previous section. Here we are comparing log (normal), weibull, exponential, and log (logistic) distributions. This is done by using AIC and identifying if the additional parameters are worth it. What we see is that the log(normal) distribution has the best AIC at  $2.4031876 \times 10^4$ . It should be noted that these AIC values can not be directly compared to the semi-parametric values. We are able to estimate the linear coefficients to be the negative of the log(normal) coefficients due to the normality of this distribution. These can be seen in Table 12.

Table 12: Parametric Model Coefficient Comparison

	estimate	std.error	statistic	p.value	2.5 %	97.5 %	Linear Coefficient
(Intercept)	9.36	0.14	65.91	0.0000000	9.08	9.64	-9.36
meno1	-0.07	0.08	-0.87	0.3856042	-0.22	0.09	0.07
hormon1	0.16	0.07	2.08	0.0379496	0.01	0.30	-0.16
as.factor(size)20-50	-0.34	0.05	-6.76	0.0000000	-0.44	-0.24	0.34
as.factor(size)>50	-0.61	0.08	-7.60	0.0000000	-0.77	-0.45	0.61
age	-0.01	0.00	-2.98	0.0029221	-0.01	0.00	0.01
as.factor(grade)3	-0.27	0.05	-4.97	0.0000007	-0.38	-0.17	0.27
nodes	-0.08	0.01	-14.38	0.0000000	-0.09	-0.07	0.08
pgr	0.00	0.00	4.81	0.0000015	0.00	0.00	0.00

When we look at our categorical variable, hormon, it is significant and the confidence interval confirms this as it does not contain 0. However, it should be noted that this is a borderline case.