

1 Top-Down Parsing

- Top-down vs. bottom-up
 - less powerful
 - more complicated to generate intermediate code or perform semantic routines
 - easier to implement, especially recursive descent
- Top-down parser
 - builds the parse tree from the root down
 - follows leftmost derivation; herefore, it is called $LL(k)$
 - we always expand the topmost symbol on the stack (leftmost in derivation)
- Top-down procedure ($k=1$ lookahead)
 - utilize stack memory m
 - start with pushing initial nonterminal S
 - at any moment
 - if a terminal is on the top of the stack
 - if it matches the incoming token, the terminal is popped and the token is consumed
 - error otherwise
 - if a nonterminal is on the top of the stack
 - we need to replace it by one of its productions
 - must predict the correct one in a predictive parser (if more than one alternative)
 - errors possible in a predictive parser if none predicted
 - successful termination
 - only on empty stack and $EOF \neq k$ incoming
- Some other properties
 - actual program tokens are never on the stack
 - the stack contains predicted tokens expected on input
 - we must make correct predictions for efficiently solving alternatives

Example 1.1 Use the unambiguous expression grammar to top-down parse id+id*id

☛ Problems to handle in top-down parsing

- left recursive productions (direct or indirect)
 - infinite stack growth
 - can always be handled
- non-deterministic productions (more than one production for a nonterminal)
 - may be handled, or not, by left-factorization
 - verified by *First* and *Follow* sets (must be pairwise disjoint for the same nonterminal)

2 Left Recursion

☛ Top-down parsers cannot handle left-recursion

- any direct left-recursion can be removed with equivalent grammar
- indirect left-recursions can be replaced by direct, which subsequently can be removed

☛ Removing direct left recursion:

- separate all left recursive from the other productions for each nonterminal
- $A \rightarrow A\alpha \mid A\beta \mid \dots$
 $A \rightarrow \gamma_1 \mid \gamma_2 \mid \dots$
- introduce a new nonterminal A'
- change nonrecursive productions to
- $A \rightarrow \gamma_1 A' \mid \gamma_2 A' \mid \dots$
- replace recursive productions by
 $A' \rightarrow \epsilon \mid \alpha A' \mid \beta A' \mid \dots$

Example 2.1 Remove left recursion from $R = \{E \rightarrow E+T \mid T\}$
 $R = \{E \rightarrow TA', A' \rightarrow +TA' \mid \epsilon\}$

☛ Removing all left recursions (direct and indirect):

- Order all nonterminals (new added nonterminals go in the rear)
- Sequence through the list; For each nonterminal B
 - for all productions $B \rightarrow A\beta$, where A precedes B on the list

- suppose all productions for A are $A \rightarrow \alpha_1 \mid \alpha_2 \mid \dots$
- replace them by $B \rightarrow \alpha_1\beta \mid \alpha_2\beta \mid \dots$
- when finished, remove all immediate left recursions for B

3 Non-determinism



Often grammar is nondeterministic

- more than one choice of a production per non-terminal



Backtracking implementation is infeasible

- we use lookahead token to make predictions
- if k tokens are needed to look ahead, then grammar is $LL(k)$
- left-factorization reduces k
- there are $LL(k>1)$ grammars that are not $LL(k-1)$ - as said before, left-factorization may or may not help

Example 3.1 *if then [else]* is an example of not- $LL(1)$ construct and cannot be reduced to $LL(1)$, but it may be solved in $LL(1)$ -parser using other techniques such as by ordering productions.



For predictions, use

- left factorization to alter grammar (reduce k) if needed
- *FIRST* and *FOLLOW* sets to verify and construct actual predictions
 - given nondeterministic production
 $N \rightarrow \alpha \mid \beta$
 compute *FIRST* of non-empty right hand sides
 compute *FOLLOW*(N) is also $\rightarrow \epsilon$
 - all sets must be disjoint pairwise (not account for empty symbol) for the production to be $LL(1)$
 - The entire grammar is $LL(k)$ where k is the max ($LL(?)$) over each production

3.1 Left factorization

- ✎ Combines alternative productions starting with the same prefixes
 - this delays decisions about predictions until new tokens are seen
 - this is a form of extending the lookahead by utilizing the stack
 - bottom-up parsers extend this idea even further

Example 3.2 $R = \{S \rightarrow ee \mid bAc \mid bAe, A \rightarrow d \mid cA\}$ has problems with $w = bcde$. Change to $R = \{S \rightarrow ee \mid bAQ, Q \rightarrow c \mid e, A \rightarrow d \mid cA\}$.

- ✎ FIRST and FOLLOW sets are means for verifying $LL(k)$ and constructing actual predictions
 - they are **sets of tokens** that may come on the top of the stack (consume upcoming token)
 - parsers utilizing them are called *predictive parsers*

- ✎ FIRST(α) algorithm:

Note that we compute FIRST of right hand sides of non-deterministic productions and not individual nonterminals unless needed in the algorithm

- If α is a single element (terminal/token or nonterminal) or ϵ
 - if $\alpha = \text{terminal } y$ then $\text{FIRST}(\alpha) = \{y\}$
 - if $\alpha = \epsilon$ then $\text{FIRST}(\alpha) = \{\epsilon\}$
 - if α is nonterminal and $\alpha \rightarrow \beta_1 \mid \beta_2 \mid \dots$ then $\text{FIRST}(\alpha) = \cup \text{FIRST}(\beta_i)$
- $\alpha = X_1 X_2 \dots X_n$
 - set $\text{FIRST}(\alpha) = \{ \}$
 - for $j = 1..n$ include $\text{FIRST}(X_j)$ in $\text{FIRST}(\alpha)$, but STOP when X_j is not *nullable*
 - ✎ X is nullable if $X \rightarrow \epsilon$, directly or indirectly
 - ✎ terminal is of course never nullable
 - if X_n was reached and is also nullable then include ϵ in $\text{FIRST}(\alpha)$

Example 3.3 $R = \{S \rightarrow Ab \mid Bc, A \rightarrow Df \mid CA, B \rightarrow gA \mid e, C \rightarrow dC \mid c, D \rightarrow h \mid i\}$
 $\text{FIRST}(Ab) = \{h, i, c, d\}$, $\text{FIRST}(Bc) = \{e, g\}$.

- ✎ FOLLOW($A \in N$) :

Note that FOLLOW(A) never contains ϵ

Note that we compute FOLLOW of left hand side if there is empty production alternative

- If $A=S$ then put end marker (e.g., EOF token) into $FOLLOW(A)$ and continue
- Find all productions with A on rhs: $Q \rightarrow \alpha A \beta$
 - if β begins with a terminal q then q is in $FOLLOW(A)$
 - if β begins with a nonterminal then $FOLLOW(A)$ includes $FIRST(\beta) - \{\epsilon\}$
 - if $\beta=\epsilon$ or when β is nullable then include $FOLLOW(Q)$ in $FOLLOW(A)$



Grammar is one-lookahead top-down predictive, LL(1), when

- or every pair of productions with the same *lhs* such as $X \rightarrow \alpha \mid \beta$
 - $FIRST(\alpha)-\epsilon$ and $FIRST(\beta)-\epsilon$ are disjoint
 - if α is nullable (i.e., $\alpha=\epsilon$ or $\epsilon \in FIRST(\alpha)$) then $FIRST(\beta)$ and $FOLLOW(X)$ are disjoint
 - same for β



LL($k>1$) parsers are generally infeasible due to size (program or table)

Example 3.4 Check if the unambiguous expression grammar is LL(1). Use \$ as end-marker.

- 1) Remove left-recursion (apply)
- 2) Apply left-factorization (none apparent)

Resulting rules={

$E \rightarrow TQ$
 $Q \rightarrow +TQ \mid -TQ \mid \epsilon$
 $T \rightarrow FR$
 $R \rightarrow *FR \mid /FR \mid \epsilon$
 $F \rightarrow (E) \mid id$

}

E is unambiguous LL(0)

Q has alternative productions: LL(1)

$FIRST(+TQ) = \{+\}$
 $FIRST(-TQ) = \{-\}$
 $FOLLOW(Q) = FOLLOW(E) = \{ \$,) \}$

T is unambiguous LL(0)

R has alternatives LL(1)

$FIRST(*FR) = \{*\}$
 $FIRST(/FR) = \{/ \}$
 $FOLLOW(R) = \{ +, -,), \$ \}$

F has alternatives LL(1)

$FIRST((E)) = \{(\}$
 $FIRST(id) = \{id\}$

Grammar is LL(1) (max value among all non-terminals).



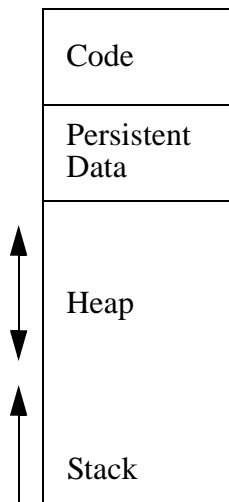
How to use predict?

- suppose grammar is LL(0) or LL(1)
 - meaning all sets for the same nonterminal are pairwise disjoint
- suppose that s is the next top of the stack symbol
- suppose that tk is the next input token (one lookahead)
- suppose X is deterministic with $X \rightarrow \alpha$
 - use the production, even if empty, no predictions needed
- suppose X is nondeterministic with $X \rightarrow \alpha \mid \beta$
 - compute $\text{First}(\alpha)$ and $\text{First}(\beta)$
 - if tk is in neither $\text{First}(\alpha)$ nor $\text{First}(\beta)$ then error
 - if $\epsilon \notin \text{First}(\alpha)$ then predict $X \rightarrow \alpha$ when $tk \in \text{First}(\alpha)$
 - if $\epsilon \in \text{First}(\alpha)$ then predict $X \rightarrow \alpha$ when $tk \in \text{First}(\alpha) \cup \text{Follow}(X)$
 - same on β
- suppose X is nondeterministic and includes the empty production as well
 - as above, except that predict the empty production when $tk \in \text{Follow}(X)$
 - even better - predict the empty production when no other production can be predicted

4 Process Memory, Stack, Activation Records

- Each process operates in its own (virtual) process space
 - size depending the addressing space and user's quota
 - in older OS heap space could have been common between processes, resulting in one process bring down other processes or even the OS
 - a process doesn't have direct access outside of the process space
 - elements
 - code
 - main, functions
 - persistent space
 - global data, local persistent data
 - stack
 - function call management with Activation Records (AR)
 - heap
 - dynamic memory, controlled by heap manager
 - under direct control of the program (C/C++)
 - garbage collection (Java)

Figure 4.1 Process space (Heap and Stack can be reversed).

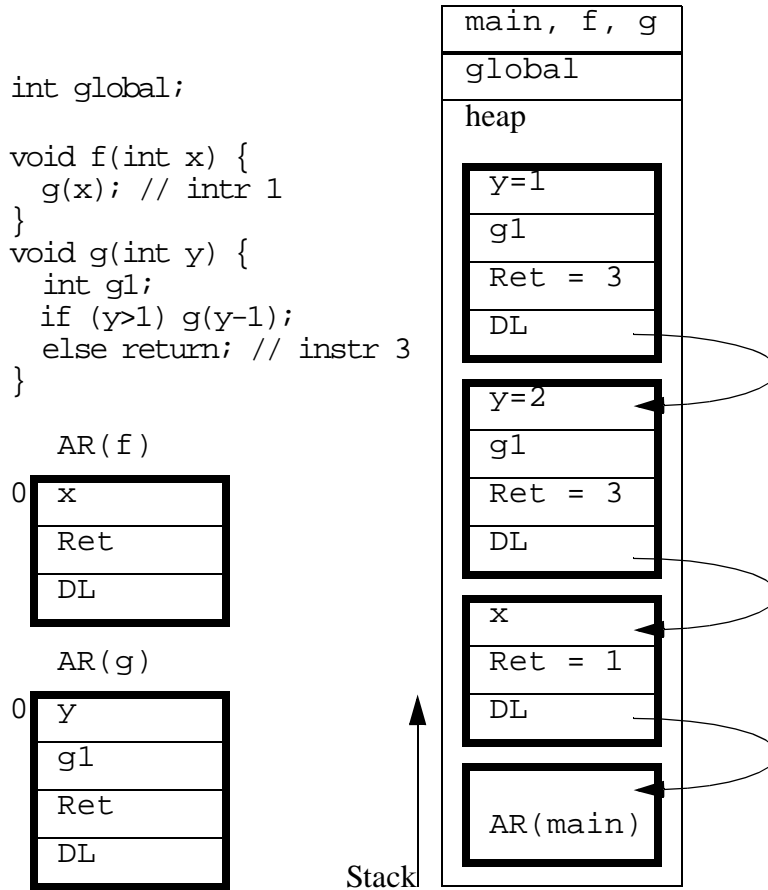


- Heap and Stack may compete for the same storage

4.1 Stack and ARs

- Stack is accessed indirectly (HLL) to manage
 - function calls
 - local scopes
- Compiler generates one AR per function
 - AR is a memory template specifying the relative location of the AR elements
 - automatic data
 - parameters and returning data
 - address of the next instruction
 - Static Link
 - used for accessing data in enclosed scopes
 - not needed in languages w/o scoped functions
 - Dynamic Link
 - pointing to the previous AR
 - actual activation records are allocated on the stack for **each** function call
 - multiple allocations for recursive calls
 - TOS is always the AR for the currently active function

Example 4.1 Example of ARs and runtime stack. Assume main calls $f(2)$. Details of the AR for main are not shown.



5 Recursive Descent Parsing

- Top-down parsers can be implemented as *recursive descent* or *table-driven*
- Recursive descent parsers utilize the machine stack to keep track of parse tree expansion. This is very convenient, but may be less efficient in larger compilers due to function calls
- Recursive descent parser processes production right hand sides following leftmost derivation (left to right), one right hand side at a time, and performs two actions:
 - if the next symbol is a terminal and it matches the next token in the sentence then the token is matched against the token from the scanner
 - consumed if matching (get the next token)
 - error if not matching
 - if the next symbol is a nonterminal then a function is called to process that nonterminal
- Initially, the starting nonterminal is used (that is, the function for the starting nonterminal is called)
- Recognition succeeds only when the input is exhausted (EOF token reached) and the initial call (see above) returns
 - this needs to be checked in the function that made the initial call to the initial nonterminal. This function can be the main function or some additional parser() function
- Each function is implemented to perform
 - Prediction if needed (if more than one production on a nonterminal)
 - The two basic actions while moving left-to-right in on the symbols of the predicted right hand side
- First modify if needed and validate grammar to be LL(1) by computing needed First and Follow sets
- Useful assumptions to consider
 - each function is called with unconsumed token, and returns with unconsumed token
 - each nonterminal has a corresponding single function named after the nonterminal

5.1 Parsing

- Parsing is accomplished as detailed above
- With only parsing, the only possible outcome is

- OK - when the successful termination encountered (see above)
- Error - error message and exit, no recovery

➤ If grammar is validated as LL(1), you can predict the empty production (if applicable) when no other production is predicted (no need to check the Follow set)

➤ Suggested to use void functions and use all explicit returns only

Example 5.1 Try to write a recursive descent parser for

$R = \{ \begin{array}{l} S \rightarrow bA \mid c \\ A \rightarrow dSa \mid \epsilon \end{array} \}.$

First, validate LL(1)

S: $\text{First}(bA) = \{b\}$, $\text{First}(c) = \{c\}$ thus LL(1)

A: $\text{First}(dSa) = \{d\}$, $\text{Follow}(A) = \{a, \$\}$ thus LL(1)

Thus the grammar is LL(1).

Assume `tk` is a token storage available and modifiable in all functions, and assume `scanner()` returns the next token

```
void parser(){
    tk=scanner();
    S();
    if (tk.ID == EOFtk)
        printf("Parse OK");
    else error(); // error message detail not shown, exit, no recovery
}

void S()
    if (tk.ID == b) {                // predicts S→bA since b∈First(bAa)
        tk=scanner();                // processing b, consume matching tokens
        A();                         // processing A
        return;
    }
    else if (tk.ID == c) {           // predict S→c
        tk=scanner();                // consume c
        return;                      // explicit return
    }
    else error();
}

void A()
    if (tk.ID == d) {                // predicts A→dSa
        tk=scanner();                // processing d
        S();                         // processing S
        if (tk.ID == a) {            // processing a
            tk=scanner();
            return;
        }
        else error();
    }
    else                             // predicts A→ε
        return;                      // explicit return
                                     // or could check tk ∈ Follow(A)
```

5.2 Tree Generation

- ✎ The parser above can be easily modified to generate parse tree, with the following changes
 - every function generates zero or one node and returns pointer to what was generated
 - every function stores or disposes tokens that are consumed
 - structural tokens are disposed, semantics tokens are stored
- ✎ Useful assumptions and suggestions to modify recursive descent parser to generate the parse tree
 - every function creating a node will label the node with the name of the nonterminal function
 - every function making calls to other nonterminal function(s) will collect returned pointers and attach to its node
 - every function will return its node
 - every function will store tokens carrying any semantics information (ID, number, operator)
 - the maximum number of children is the maximum number of nonterminal in any production
 - the maximum number of tokens to be stored in a node is the maximum number of semantics tokens in any production

Example 5.2 Modify the previous code to generate parse tree. Suppose b and d tokens need to be retained while c does not.

Max one child needed per node since at most one nonterminal on the right hand side of any production.

Max two tokens need to be stored in a node as one production use two semantics tokens.

Assume `node_t` structure with `label`, `token1`, `token2`, and `child`.

Assume `getNode(label)` allocates `node_t` node and labels it.

```
node_t parser(){
    node_t *root;
    tk=scanner();
    root = S();
    if (tk.ID == EOFtk)
        printf("Parse OK");
    else error(); // error message detail not shown, exit, no recovery
    return root;
}
```

```

node t* S()
    node t *p = getNode(S);    // label the node with S
    if (tk.ID == b) {
        p->token1 = tk;        // store b in the tree
        tk=scanner();
        p->child = A();
        return p;
    }
    else if (tk.ID == c) {
        tk=scanner();          // c not needed to be stored
        return p;              // could also return NULL since
                                // the node is empty in this case
    }
    else error();
}

node t* A()
    if (tk.ID == d) {
        token t p = getNode(A); // label the new node with A
        p->token1 = tk;
        tk=scanner();
        p->child = S();
        if (tk.ID == a) {
            p->token2 = tk;
            tk=scanner();
            return p;
        }
        else error();
    }
    else
        return NULL;           // empty production so no node generated

```
