

# Lecture 7: Recursion in Java

Creation Through Self-Referral Dynamics

#### Wholeness of the Lesson

Computation of a function by recursion involves repeated self-calls of the function. Recursion is implicit also at the design level when a reflexive association is present. Recursion mirrors the self-referral dynamics of consciousness, the unified field, on the basis of which all creation emerges.

## Outline of Topics

- Recursion Defined and two examples: Factorial and Fibonacci
- Other Examples
  - Reversing characters in a string
  - Finding the minimum element in an array
- Recursive Utility Functions
  - Example: Binary Search
  - Example: Another FindMin recursion

#### Recursion - Basic Idea

- **Recursion**: The definition of an operation in terms of itself.
  - Solving a problem using recursion depends on solving smaller occurrences of the same problem.
- A Java method is **recursive**, or exhibits recursion, if in its body it calls itself.
  - It is a powerful substitute for *iteration* (loops)
  - Particularly well-suited to solving certain types of problems (problems which can naturally be broken down into subproblems).

## Why Recursion?

- A different way of approaching problems
- Can solve some kinds of problems better than iteration
- Leads to elegant and simple code (when used well)
- Some programming languages ("functional" languages such as Scheme, ML, and Haskell) use recursion exclusively (no loops)

#### Recursion in Java

- In order for a self-calling method to be a *valid* recursion (one that eventually terminates), the following criteria must be met:
  - Base Case Exists. The method must have a base case which returns a value without making a self-call.
  - Self-calls Lead to Base Case. For every input to the method, the sequence of self-calls must eventually lead to a self-call in which the base case is accessed.

## First Example: factorial

Definition of factorial:

```
For any positive integer n:

n! = n \times (n-1) \times (n-2) \times ... \times 3 \times 2 \times 1

0! = 1
```

Another way of defining factorial using (mathematical) recursion.
 n! = n x (n-1)!
 0! = 1.

• In Java:

```
int factorial(int n) {
    //base case
    if(n == 0 || n == 1) {
        return 1;
    }
    return n * factorial(n-1);
}
```

Demo: Observe the sequence of self-calls in executing factorial on input 12. See package lesson7.fibfactorial.

## Example: Implementing factorial Iteratively

```
int factorial(int n) {
   if(n == 0 | | n == 1) {
        return 1;
   int result = 1;
   for(int i = 1; i <= n; ++i) {
         result *= i;
   return result;
```

Hmmm how many behind me?

#### Exercise 7.1



- You are standing in line, waiting to get into an event (like a movie or a concert). You are at the front of the line. You wonder "How many people are in line behind me?" The line is long, so there is no way for you to count the number of people in line yourself. You decide to use recursion.
- For this task, we make the following rule: Each person in line is allowed to ask the person directly behind him one question.
- What question should you, and the person behind you, and the person behind him,... ask? How can the answers lead to a solution to the problem?

#### The idea

- With recursion, you break up a big problem into smaller occurrences of that same problem.
  - In this problem, each person can solve a small part of the problem.
    - What is a small version of the problem that would be easy to answer?
    - What information from a neighbor might help?

#### Recursive Solution

The question to ask: "How many people are behind you?"

Suppose Person C is behind Person B and person B is behind Person A. If Person C answers "There are N people behind me", then Person B knows there are N+1 persons behind him. Then, when person A asks the question to Person B, Person B will answer "N+1".

The last person in line has no one behind him, so he will answer "0".



#### Recursive Solution In Code

demo in package lesson7.howmanybehind

```
public class Person {
   String name;
   Person behind;
   Person(String n) {
       name = n;
   int answerToQuestion() {
        if(behind == null) return 0 ;
        else return behind.answerToQuestion() + 1;
public class PersonLine {
   private Person[] personLine;
   PersonLine(Person[] persons) {
       personLine = persons;
   public int howManyInLine() {
        return personLine[0].answerToQuestion() + 1;
```

## Another Example of Recursion

The Fibonacci numbers are defined as follows:

$$F_0 = 0$$
,  $F_1 = 1$ ,  $F_2 = 1$ ,  $F_3 = 2$ ,  $F_4 = 3$ ,  $F_5 = 5$ ,...,  $F_n = F_{n-1} + F_{n-2}$ , ...

The nth Fibonacci number can be computed by:

Demo: Observe the sequence of self-calls - package lesson7.fibfactorial

## Design Guideline

No recursion should involve a large amount of redundant computation.

Usually, if a recursion *does* involve redundant computations, it can be rewritten as a loop or by using a more efficient recursive strategy.

<u>Example</u>: We have seen how there is a great deal of redundant computation in the recursive computation of Fibonacci numbers.

#### Exercise 7.2

• Rewrite the function that computes the nth fibonacci number iteratively (using a loop instead of recursion).

```
public class Fib {
    public int fib(int n) {
        //implement
        return 0;
    }

    public static void main(String[] args) {
        Fib f = new Fib();
        System.out.println(f.fib(10));
    }
}
```

#### Solution

```
//Uses extra space for storage
public class Fib {
    int[] store;

public int fib(int n) {
        store = new int[n+1];
        store[0] = 0;
        store[1] = 1;

    for(int i = 2; i <= n; i++) {
            store[i] = store[i-1] + store[i-2];
        }
        return store[n];
    }
}</pre>
```

```
//No extra space used
public int fib2(int n) {
    int previous1, previous2;
    if(n == 0 || n == 1) return n;
    previous1 = 1;
    previous2 = 0;
    int current = previous1 + previous2;
    for(int i = 0; i < n-2; ++i) {</pre>
        int temp = previous1 + current;
        previous2 = previous1;
        previous1 = current;
        current = temp;
    return current;
```

#### Main Point

Java supports the creation of recursive methods, characterized by the fact that they call themselves in their method body. A self-calling method is a valid recursive function if it contains a base case - a branch of code that exits the method under certain conditions but does not involve a self-call – and if the sequence of self-calls, on any input to the method, always converges to the base case. Likewise, a quest for self-knowledge not based in the direct experience of the "Self" is endless (and baseless).

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  - Example: Binary Search
  - Example: Another FindMin recursion

## Example: Reversing a String

Attempt to reverse the order of the characters in an input String by using the following strategy:

- Remove the 0<sup>th</sup> character ch from the input string and name the modified string t.
- Reverse t and append ch.

Thinking recursively. Assume the recursion produces the expected output, and find a way to combine the base case output with the output from the recursive step.

## Implementation

```
static String reverse(String s) {
  if(s == null || s.length() == 0) return s;
  String first = "" + s.charAt(0);
  return reverse(s.substring(1)) + first;
}
```

## Recursive Implementations of a Utility Method

• Sorting, searching, and other manipulations of characters in a string or elements in arrays or lists are often done recursively. Sometimes (but not always), an implementation of such a utility provides a public method

```
public <return-value-type> thePublicMethod(params)
```

whose signature and return type make sense to potential users, and a private recursive method

```
private <ret-value-type> privateRecurMethod(otherParams)
```

which does the real work and is designed to call itself.

Also: sometimes it is convenient to make these methods static.

## Example: Finding the Minimum Value in a List

Attempt to find the minimum Integer in a List of Integers, using the following recursive strategy:

- Remove the Oth element from the list and call it first
- Recursively find the min in the remaining list, call it recurFind
- If first < recurFind, return first; otherwise, return recurFind.

Thinking recursively. After processing the 0<sup>th</sup> element, assume the findMin operation works correctly on the remaining elements.

## Implementation

```
public Integer findMin(List<Integer> list) {
    if(list == null || list.isEmpty()) return null;
    return recurFindMin(list);
}
private Integer recurFindMin(List<Integer> list) {
    Integer first = list.remove(0);
    if(list.isEmpty()) return first;
    Integer recFind = recurFindMin(list);
    return recFind.compareTo(first) < 0 ? recFind : first;
}</pre>
```

## Example: Recursive Min Again

 Providing a public and private version makes it possible to find min without modifying input list

```
public Integer findMin(List<Integer> list) {
    if(list == null || list.isEmpty()) return null;
    return recurFindMin(list, 0);
}
private Integer recurFindMin(List<Integer> list, int index) {
    Integer first = list.get(index);
    if(index==(list.size() - 1)) return first;
    Integer recFind = recurFindMin(list, index + 1);
    if(first.compareTo(recFind) < 0) return first;
    else return recFind;
}</pre>
```

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#### Example: Iterative Binary Search

The logic in the iterative version of BinarySearch is very similar

```
public static boolean binSearchIt(int[] arr, int x) {
    if(arr == null || arr.length == 0) return false;
    int lower = 0;
    int upper = arr.length -1;
   while(true) {
        if(lower > upper) return false;
        int mid = (lower + upper)/2;
        if(x == arr[mid]) return true;
        if(x < arr[mid]) { //search left</pre>
            upper = mid - 1;
        } else { //x > arr[mid], search right
            lower = mid + 1;
```

#### Example: Recursive Binary Search

• Public version for clients. Private version with extra parameters for selfcalls.

```
public static boolean search(int[] arr, int x) {
    if(arr == null || arr.length == 0) return false;
    return recSearch(arr, x, 0, arr.length - 1 );
private static boolean recSearch(int[] arr, int x,
        int lower, int upper){
    if(lower > upper) return false;
    int mid = (upper + lower) / 2;
    if(x == arr[mid]) return true;
    if(x < arr[mid])</pre>
        return recSearch(arr, x, lower, mid - 1);
    else
        return recSearch(arr, x, mid + 1, upper);
```

### Summary

- A Java method is *recursive*, or exhibits recursion, if in its body it calls itself.
- A recursion is *valid* if the following criteria are met:
  - The method must have a base case which returns a value without making a self-call.
  - For every input to the method, the sequence of self-calls eventually leads to a self-call in which the base case is accessed.
- Sometimes recursion leads to redundant computations, which lead to slow running times (like Fibonacci). In such cases, an implementation using iteration instead of recursion should be done.
- When recursion is used to provide utility function support, the public method signature that is exposed to the client reveals only the parameters that are relevant for the client not the special parameters that may be needed to implement the recursion.

## Connecting the Parts of Knowledge With the Wholeness of Knowledge

#### Recursion creates from self-referral activity

- 1. In Java, it is possible for a method to call itself.
- 2. For a self-calling method to be a legitimate recursion, it must have a base case, and whenever the method is called, the sequence of self-calls must converge to the base case.
- **Transcendental Consciousness:** TC is the self-referral field of existence, at the basis of all manifest existence.
- 4. Wholeness moving within itself: In Unity Consciousness, one sees that all activity in the universe springs from the self-referral dynamics of wholeness. The "base case" the reference point is always the Self, realized as Brahman.