Generic deterministic problem

$$V(s(0)) = \max_{c} \{ \int_{0}^{\infty} e^{-\rho t} r(s(t), c(t)) dt \}$$
  
$$ds_{i}(t) = \mu_{i}(s(t), c(t)) dt \text{ for } i \in \{1, \dots, n_{s}\}$$

State variables:  $s_i(t)$  for  $i \in \{1, ..., n_s\}$ Control variables:  $c_i(t)$  for  $i \in \{1, ..., n_c\}$ 

Return function: r(s(t), c(t))

Transition function:  $\mu_i(s(t), c(t))$  for  $i \in \{1, ..., n_s\}$ 

$$\mathrm{HJB:}\, \rho V(s) = \max_{c} \bigl\{ r\bigl(s(t),c(t)\bigr) + \nabla V \cdot \mu\bigl(s(t),c(t)\bigr) \bigr\}$$

Neoclassical growth model: (slides 16+, Moll Julia code)

$$r(s(t), c(t)) = \frac{(c(t))^{1-\sigma}}{1-\sigma}$$
  

$$\mu_1(s(t), c(t)) = As(t)^{\alpha} - \delta s(t) - c(t)$$

Consumption saving model: (Moll notes, Julia code)

$$\begin{split} r\big(s(t),c(t)\big) &= \frac{\big(c(t)\big)^{1-\sigma}}{1-\sigma} \\ \mu_1\big(s(t),c(t)\big) &= r \times s(t) - c(t) \end{split}$$