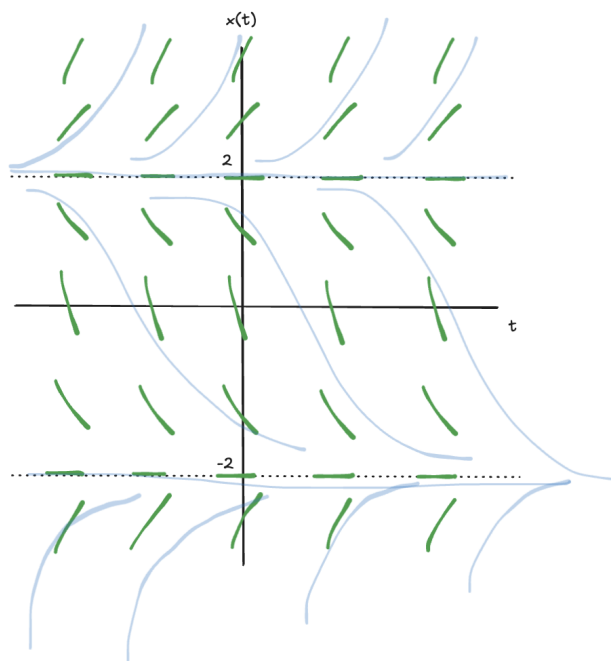


Problem 1: Interpret $x' = \sin x$ s flow on a line. The fixed points are $2k\pi$ for $k \in \mathbb{Z}$

Problem 2: $x' = 4x^2 - 16$

$x = 2$ is a unstable fixed point. $x = -2$ is a stable fixed point.

$$\begin{aligned}\frac{dx}{dt} &= 4x^2 - 16 \\ \frac{dx}{4x^2 - 16} &= dt \\ \frac{1}{16} \left(\frac{dx}{x-2} - \frac{dx}{x+2} \right) &= dt \\ \frac{1}{16} (\ln|x-2| - \ln|x+2|) &= t + c \\ \ln \left| \frac{x-2}{x+2} \right| &= 16t + 16c \\ \left| \frac{x-2}{x+2} \right| &= e^{16t+16c} \\ \frac{x-2}{x+2} &= ke^{16t} \\ x-2 &= Ce^{16t}(x+2) \\ x(1 - Ce^{16t}) &= 2Ce^{16t} + 2 \\ x &= \frac{2Ce^{16t} + 2}{1 - Ce^{16t}}\end{aligned}$$



Problem 3: $x' = x - x^3$

$x = -1, 1$ are stable fixed points. $x = 0$ is an unstable fixed point.

