

Optical Tweezers

Draft Design

Jan 29, 2007

Concepts

- Concepts for 1st panel: Physics of Tweezers
 - Light is oscillating, propagating electric field
 - Electric field induces a polarization of the bead. This polarization increases with strength of electric field, and changes direction with change in direction of E-field
 - Gradient in electric field and polarization of bead causes net force towards center (**show force in x only???**)
 - Show as balance of right hand side force and left hand side force
 - Bead is under constant brownian motion
 - Distance that bead travels is balance of brownian motion versus trap strength: $\frac{1}{2} k_B T = \frac{1}{2} k_{x\text{-trap}} \langle x^2 \rangle$
 - If bead is out of trap it will just undergo brownian motion.
 - ON FREEZE FIELDS OR PAUSE view, learning goal:
 - Moving bead around changes polarization of charges and net force on bead.
 - (DON'T DO THIS?) Allows you to let go and see behavior of bead in a “static” E-field
 - How to model this???
 - Static field you won't get k-trap ... take example of when you are at zero e-field (no force).
 - (DO THIS) Possibly just allow them to move bead around during “PAUSE” (showing force vector) but not model motion of ball with static E-fields.

- Start-up ideas:
 - No bead?
 - Or bead out of beam ... with wiggle me of move bead into laser?
 - Or bead doing brownian motion with no laser on and wiggle me to turn laser on?

Physics NOT shown...

- Right now cannot change radius of bead (could add to advanced features if important).

Physics of Tweezers

User Stories:

1) Trap force like a spring:

- a. User grabs bead and moves it horizontally. Sees force grow as distance from center grows. Always towards center
- b. User goes to advanced options and sets flow going. Calculates offset of bead in x versus flow force ... $6 \pi \eta r v = k_{\text{trap}_x} X$. (They will have to estimate r of bead with ruler, viscosity and velocity are from controls.)
- c. Intensity control changes force.

2) Can control position of bead with laser:

- a. User grabs laser and drags it around seeing that bead will stay in laser beam unless user moves laser “stage” too fast. In which case bead will “pop” out of laser beam and just be doing brownian motion.
- b. Intensity control changes speed at which bead pops out.

3) ETC... I can write a ton, but before I do I want to make sure this is what Chris wants.

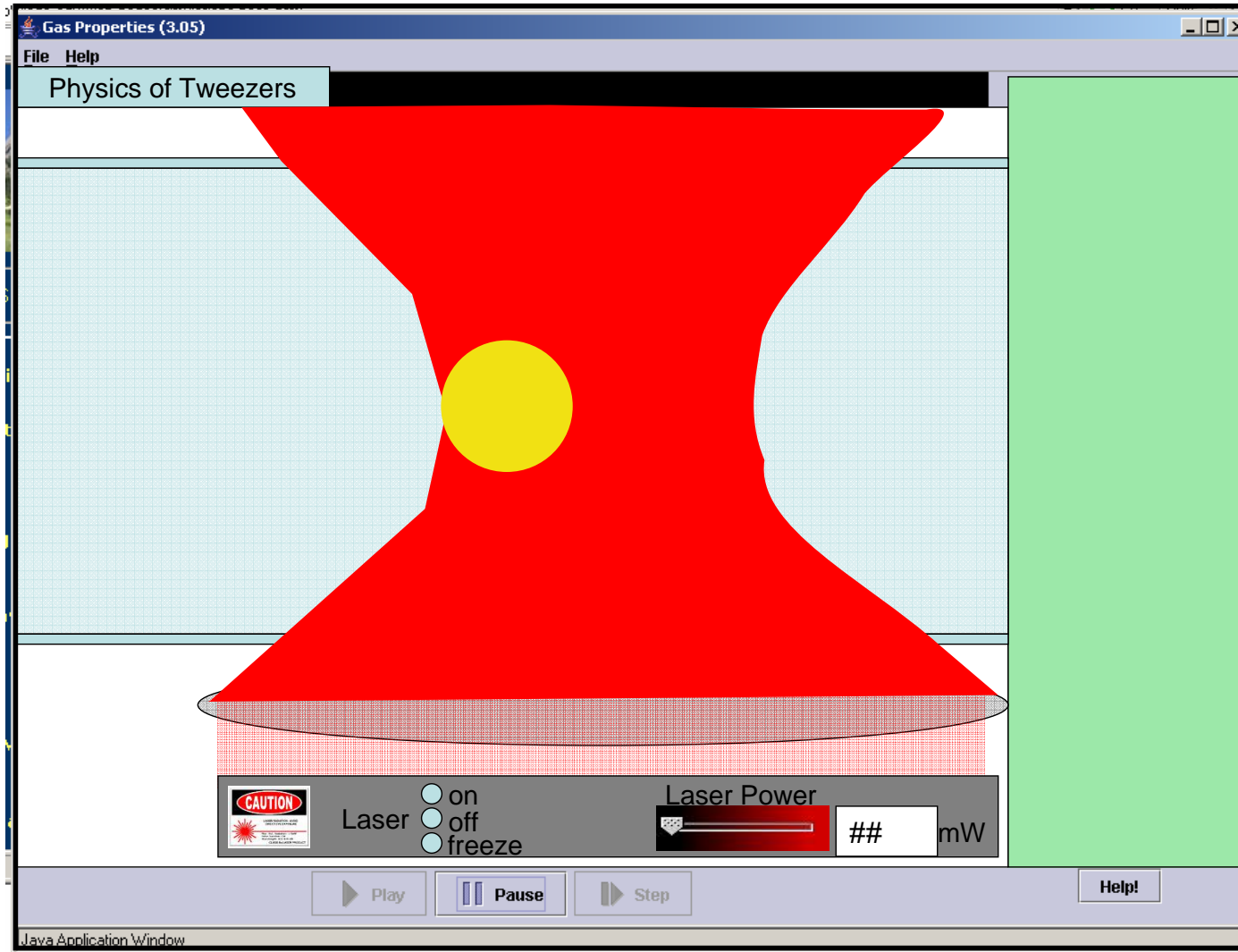
Physics of Tweezers

Dimensions:

- Bead is 200nm
- Laser waist is 500 nm

Look:

- Bead should have shading to look 3D
 - Laser should have shading so that red looks like gaussian power distribution from left to right and weaker where broader beam.
- Red should get brighter with intensity.

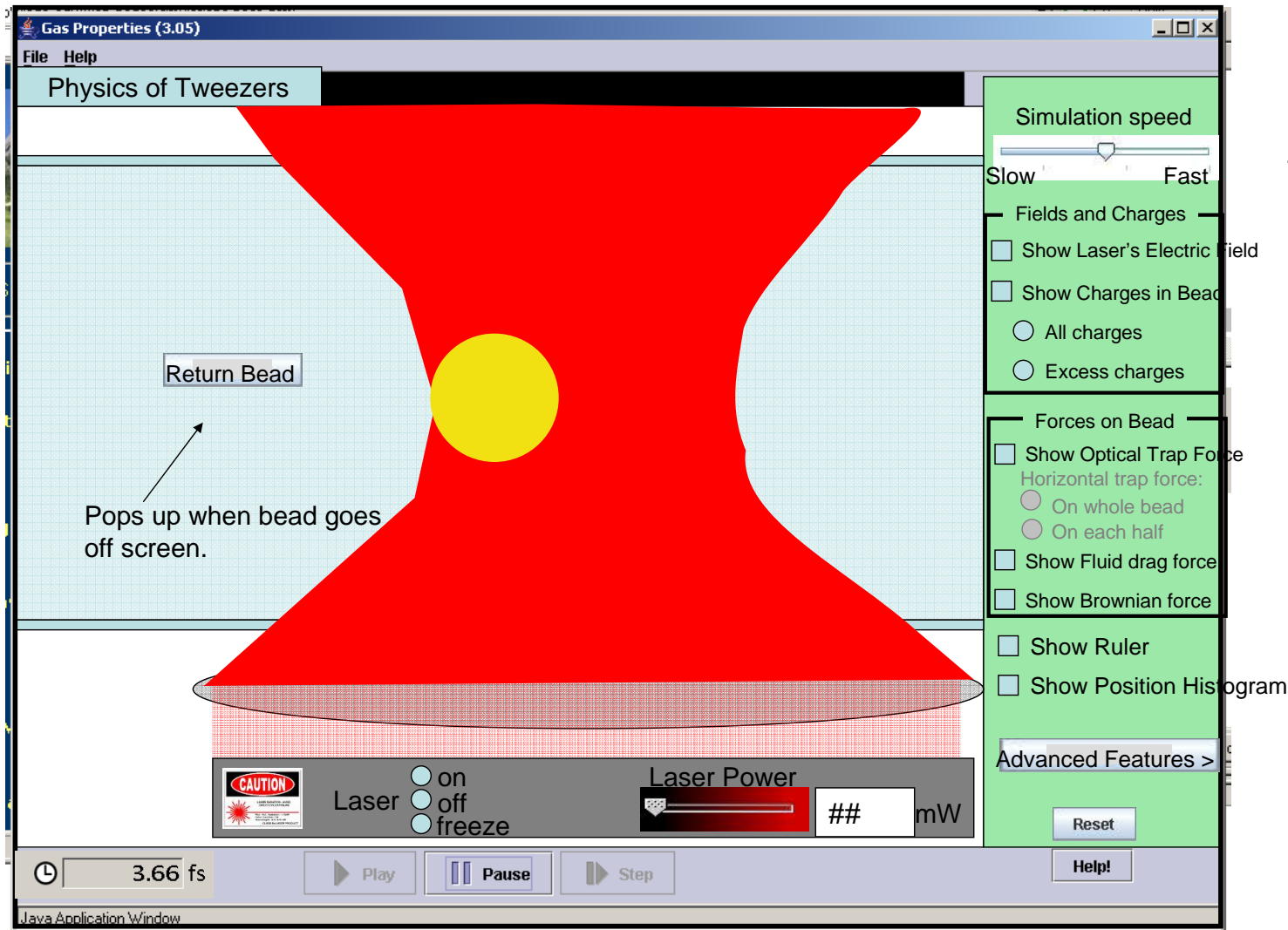
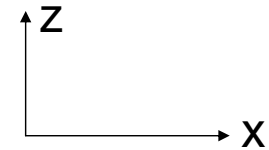


Basic idea:

- Bead in liquid undergoes brownian motion
- Laser beam ON puts force on bead that pulls it toward center of laser beam .. “traps it”
- Liquid is viscous so causes bead to always moves at terminal velocity (Force \sim velocity NOT Force \sim acceleration).

Physics of Tweezers

Sim speed = FAST (Shows only time averaged forces on bead)



Laser force is like a SPRING force:

$$F_{\text{trap}_x} = k_{\text{trap}_x} \cdot \Delta x$$

$$F_{\text{trap}_z} = k_{\text{trap}_z} \cdot \Delta z$$

Δx = distance from center in x

Δz = distance from center in z

Trap force goes to zero if bead is

Force on bead given by k_{trap} :

$$k_{\text{trap}_x} = \text{Power} / 11400$$

Power in mW, k_{trap_x} in pN/nm

k_{trap_x} is independent of z.

Power goes from 0 mW to 1000 mW

$$k_{\text{trap}_z} = k_{\text{trap}_x} / 5.6$$

$$F_{\text{drag}} = \gamma \cdot \text{velocity}$$

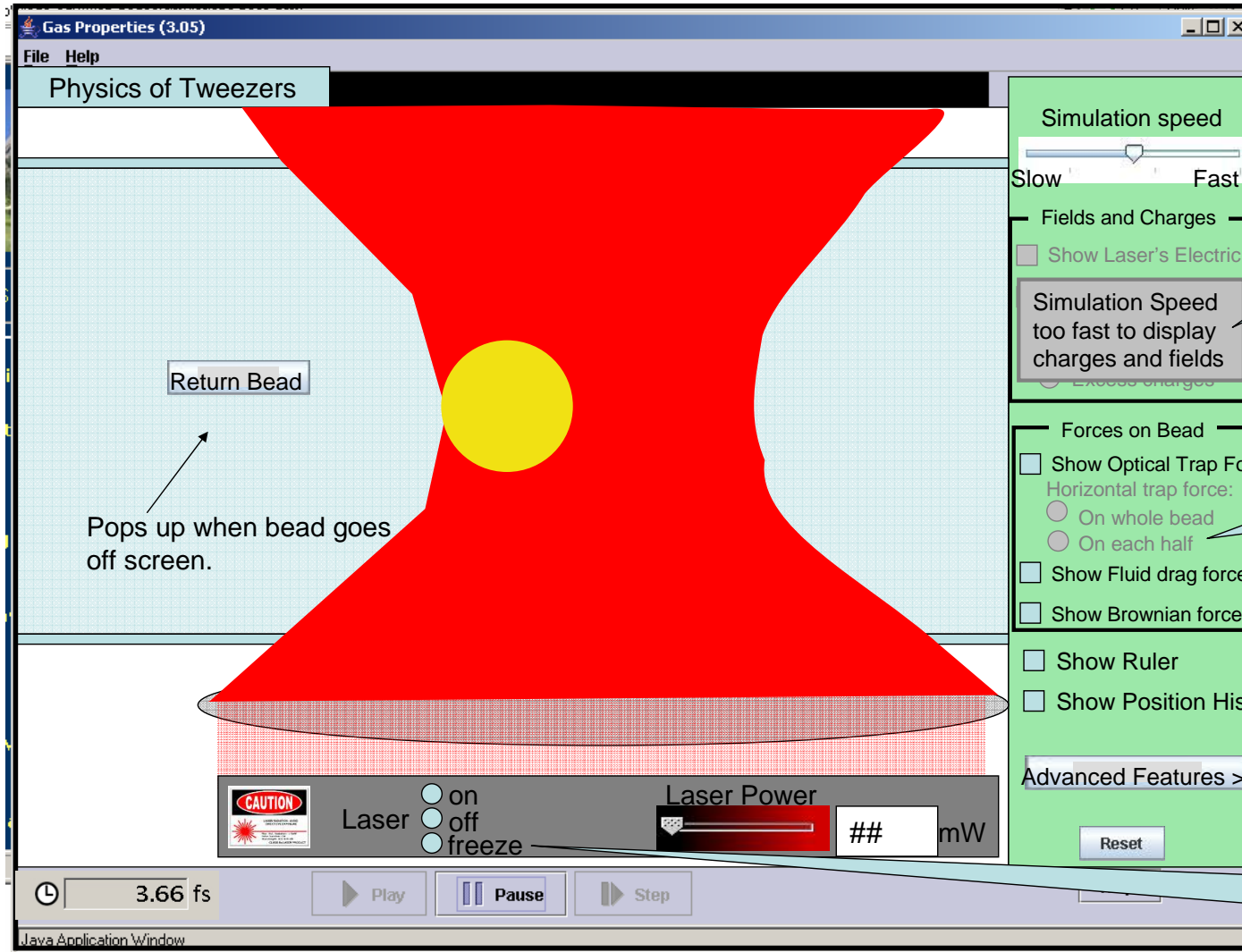
(γ = drag coefficient, will be adjustable through viscosity in advanced features)

F_{brownian} = small random kicks

Model check: If No force ... (laser off)
diffuses ~ 1 bead diameter in 1 sec

Physics of Tweezers

Sim speed = FAST (Shows only time averaged forces on bead)



If sim speed is fast, have message appear in this part of control panel that says cannot display this now.

Grey out this control if sim speed too fast to display fields and charges.

Is it reasonable to display Brownian motion forces?? Need to check modeling.

May want "laser freeze" or just use "pause" button if can allow dragging bead around if that is active?

Physics of Tweezers

Sim speed = FAST (Shows only time averaged forces on bead)

The screenshot shows the 'Physics of Tweezers' simulation window. The main area displays a yellow bead at the center of a red laser trap. The interface includes a menu bar (File, Help), a toolbar with 'Return Bead', 'Play', 'Pause', 'Step', and 'Help!', and a status bar showing '3.66 fs'. The right sidebar contains controls for 'Simulation speed' (a slider from Slow to Fast), 'Fields and Charges' (checkboxes for 'Show Laser's Electric field' and 'Show Magnetic field'), 'Simulation Speed' (a text input field), 'Forces on Bead' (checkboxes for 'Show Optical Trap Force', 'Show Fluid drag force', and 'Show Brownian force'), 'Show Ruler', and 'Show Position Histogram'. The bottom status bar includes a 'CAUTION' icon, 'Laser' controls (on/off/freeze), 'Laser Power' (a slider and a text input field), and a 'Help!' button.

Return Bead

Pops up when bead goes off screen.

Simulation speed

Slow Fast

Fields and Charges

☐ Show Laser's Electric field

Simulation Speed

too fast to

charges and fields

Excess charges

Forces on Bead

☐ Show Optical Trap Force

Horizontal trap force:

☐ On whole bead

☐ On each half

☐ Show Fluid drag force

☐ Show Brownian force

☐ Show Ruler

☐ Show Position Histogram

Advanced Features >

CAUTION

Laser

on
off
freeze

Laser Power

mW

3.66 fs

Play

Pause

Step

Help!

Java Application Window

Given range ... slider likely should be logarithmic

Allow user to grab bead and move it around and release it from any point (confined to liquid).

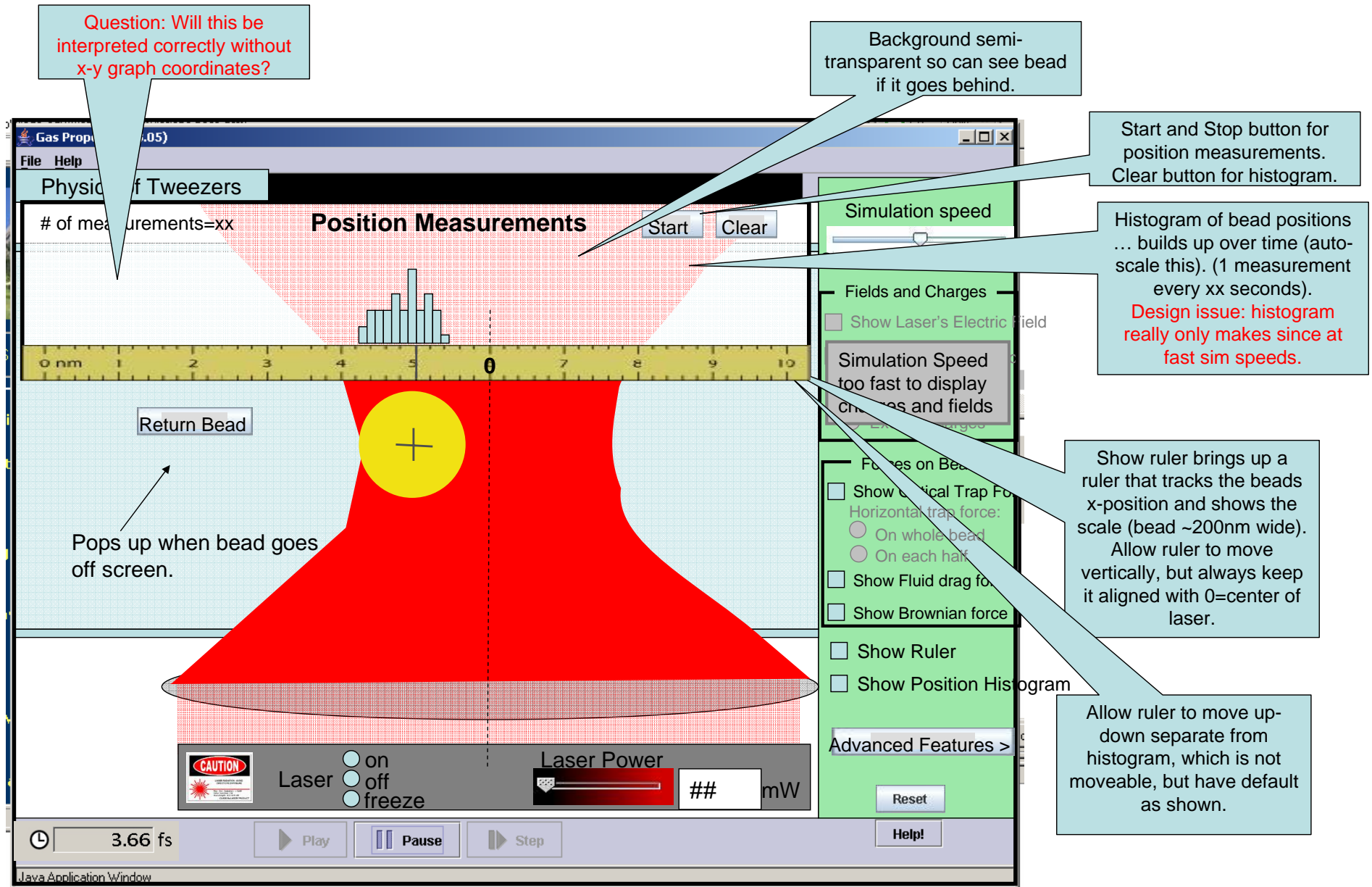
Bead should have 3D shading.

Allow user to grab base of laser and move it left-right. Speed of movement should depend on "Sim speed" ... if on slow then restrict rate of movement so as not to exceed some reasonable rate (xx nm/sec).

This clock changes as sim speed changes ...
on "slowest Sim speed" 10 sec real time = 2×10^{-15} secs in sim time.
on "fastest Sim speed" 1 sec real time = 0.1 secs in sim time. (??)

Physics of Tweezers

Sim speed = FAST (Shows only time averaged forces on bead)



Physics of Tweezers

Sim speed = SLOW (show E-field and charges.)

The screenshot shows the 'Physics of Tweezers' simulation window. The main area displays a red laser trap with a yellow bead in the center. The simulation speed is set to 'Slow'. The 'Fields and Charges' section is expanded, showing options for 'Show Laser's Electric field', 'Show Charges in Bead', 'All charges', and 'Excess charges'. The 'Forces on Bead' section is also expanded, showing options for 'Horizontal trap force', 'Show Fluid drag force', and 'Show Brownian force'. The 'Advanced Features' section is partially visible. The bottom status bar shows a time of 3.66 fs and buttons for 'Play', 'Pause', 'Step', and 'Help!'. A 'CAUTION' label is present near the laser power controls.

Return Bead
Pops up when bead goes off screen.

E-field displayed as vectors on even grid that maps laser area (as in radio wave sim).
Fading and size changes with strength

If sim speed slow enough, then allow these options.
Slow enough means: about 1 sec = 10-15 sec of sim time

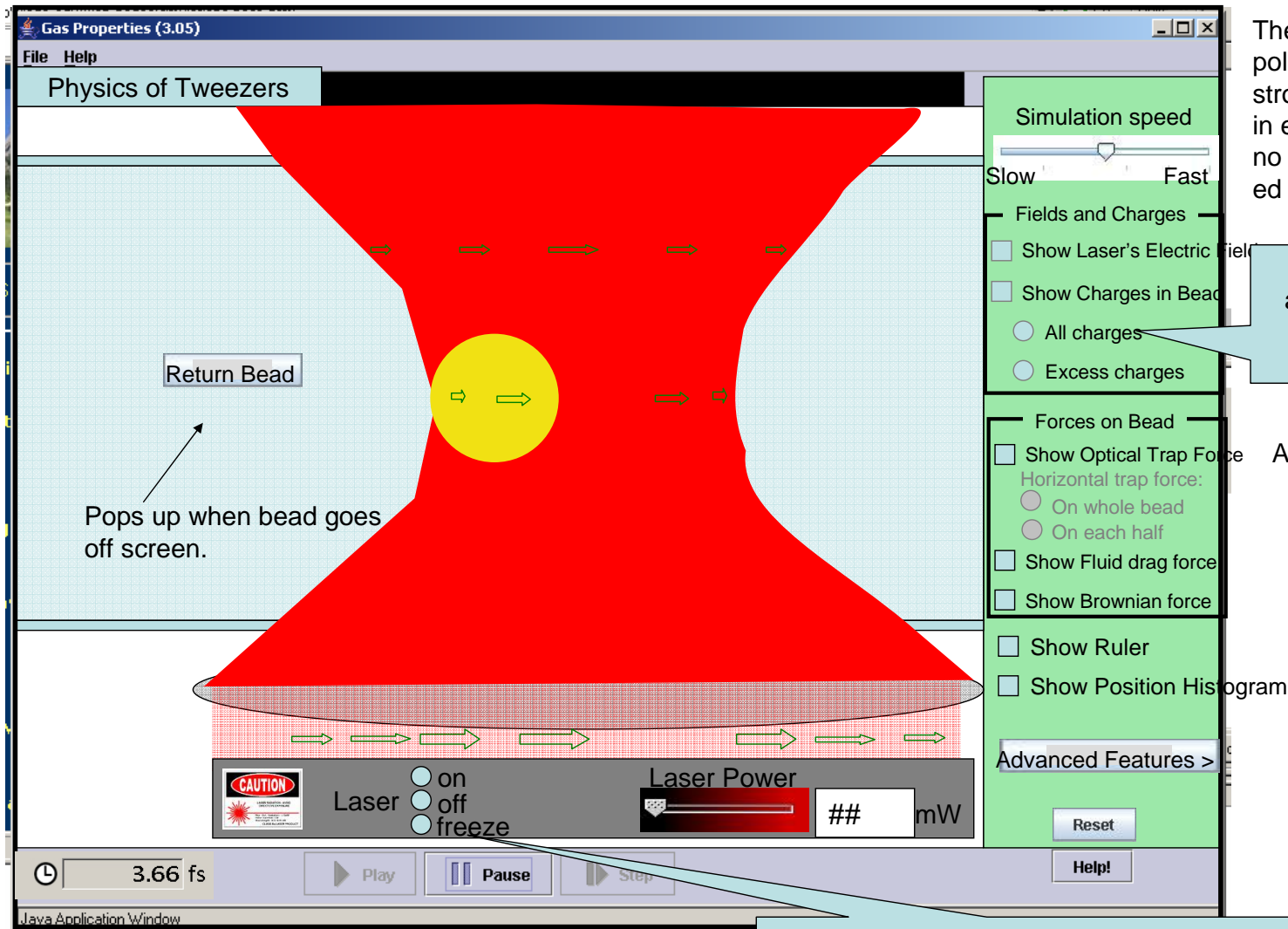
Wavelength of laser shows up in e-field grid... what wavelength do folks trap at, or do we just use He-Ne wavelength since laser is shown as red here?
He-Ne = 632 nm.
Actually is IR: 1064 nm

Simulation speed
Slow Fast
Fields and Charges
☐ Show Laser's Electric field
☐ Show Charges in Bead
☐ All charges
☐ Excess charges
Forces on Bead
☐ Horizontal trap force:
☐ On whole bead
☐ On each half
☐ Show Fluid drag force
☐ Show Brownian force
Show Ruler
Show Position Histogram
Advanced Features >
Reset
Help!

CAUTION
Laser ☐ on ☐ off ☐ freeze
Laser Power ## mW
3.66 fs
Play Pause Step
Java Application Window

Physics of Tweezers: Page 1

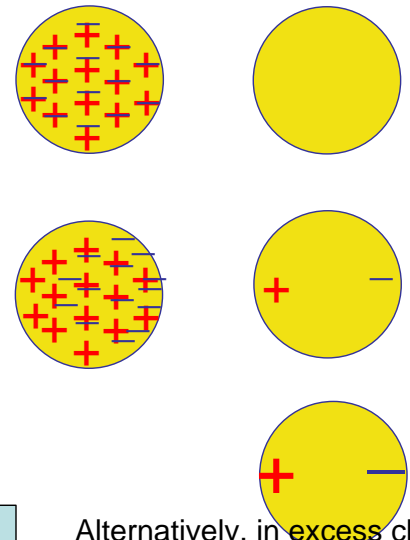
Sim speed = SLOW (show E-field and charges.)



The extent to which the bead is polarized will depend on electric field, stronger = more polarized. So as "zero" in e-field passes through, you will see no polarization. This will be Hollywooded since we only want qualitative idea.

Show charges should put grid of + and - charges, with -'s that moves slightly with E-field (creating polarization):

All charge view: Excess charge view:

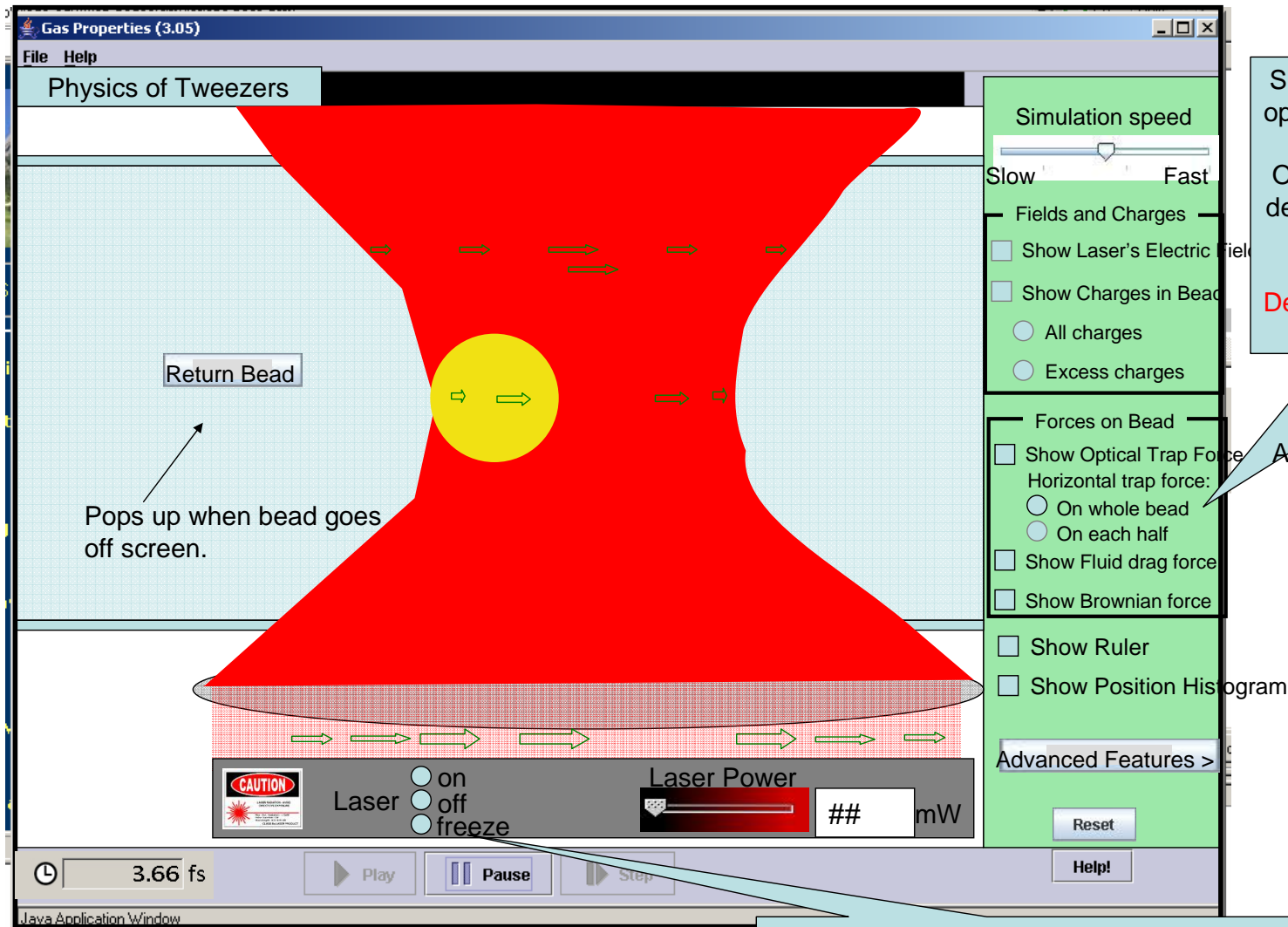


Should be able to pause or freeze laser and move bead about to see how charges and forces are different depending where you are in the beam.

Alternatively, in excess charge view could show charges all same size but more on each side as excess charge increases.

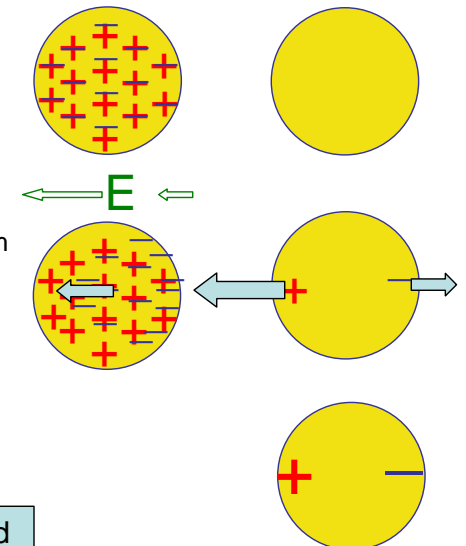
Physics of Tweezers

Sim speed = SLOW (show E-field and charges.)



Showing forces on bead... now these options are available (when sim speed is slow enough).
Optical trap force will grow and shrink depending on where you are in E-field wave cycle.
(Only show horizontal force ???
Detailed physics of vertical force is not apparent with this model)

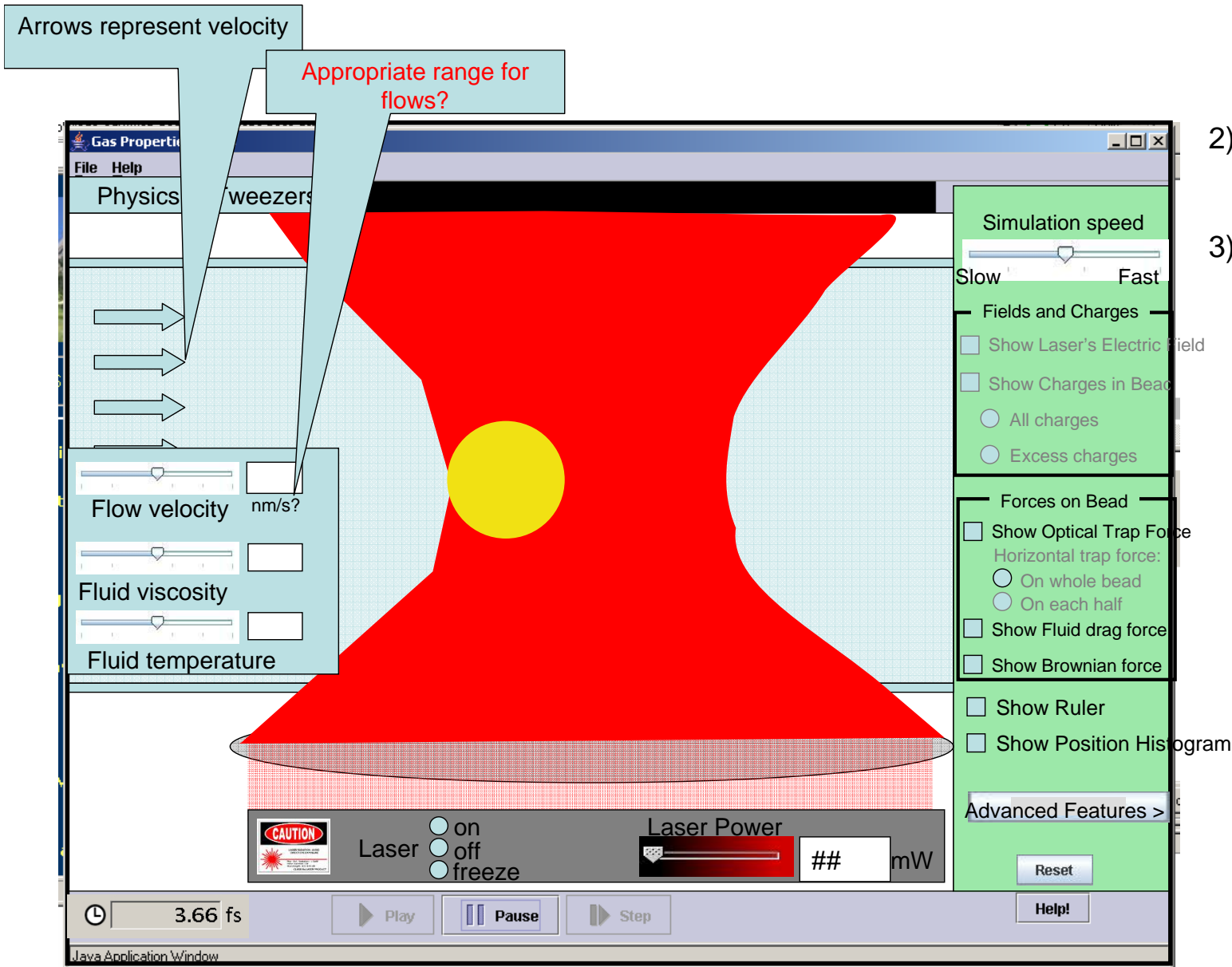
All charge view: Excess charge view:



Should be able to pause or freeze laser and move bead about to see how charges and forces are different depending where you are in the beam.

Physics of Tweezers

Sim speed = SLOW (show E-field and charges.)



- When any one of advanced options is selected then:
- 1) Sim speed skips to "fast" and if students try to readjust, does not allow student to go to slow speeds.
 - 2) Fields & charges grey out, Horizontal forces grey out.
 - 3) Bead and laser return to default location.

Advanced Features >

- ☐ Control Fluid and Flow
- ☐ Show change in momentum model for trap force
- ☐ Show potential energy graph

If Control Fluid and Flow selected, options at left appear:

$$F_{\text{drag}} = \gamma \cdot \text{velocity}$$

$$\gamma = 6 \pi \eta r$$

(η = viscosity ... will be adjustable).

r = radius of bead (not adjustable)

v = velocity of fluid relative to bead.

Temperature, will adjust F_{brownian} .

Physics of Tweezers: Page 1

Need good model of F_{trap} in this region

Physics of Tweezers

Potential energy of Trap

position

Return Bead

Pops up when bead goes off screen.

CAUTION

Laser ☐ on ☐ off ☐ freeze

Laser Power ## mW

Simulation speed

Slow Fast

Fields and Charges

☐ Show Laser's Electric field

Simulation Speed too fast to display charges and fields

Forces on Bead

☐ Show Optical Trap Force

Horizontal trap force:

☐ On whole bead ☐ On each half

☐ Show Fluid drag force

☐ Show Brownian force

☐ Show Ruler

☐ Show Position Histogram

Advanced Features >

Control Fluid and Flow

Show Trap potential energy graph

Show change in momentum model for trap force

If Show potential energy graph checked:

- 1) Graph appears at top
- 2) Curve shows $\frac{1}{2} k_{x_trap} x^2$
- 3) Little image of bead where bead is in x.
- 4) NO Units on PE curve

??? What to do with PE curve if person grabs bead and moves it up and down? Should whole curve shift up and down by appropriate amount? (That is k_{x_trap} is independent of x, but PE does go UP as bead moves vertically.).

Reset

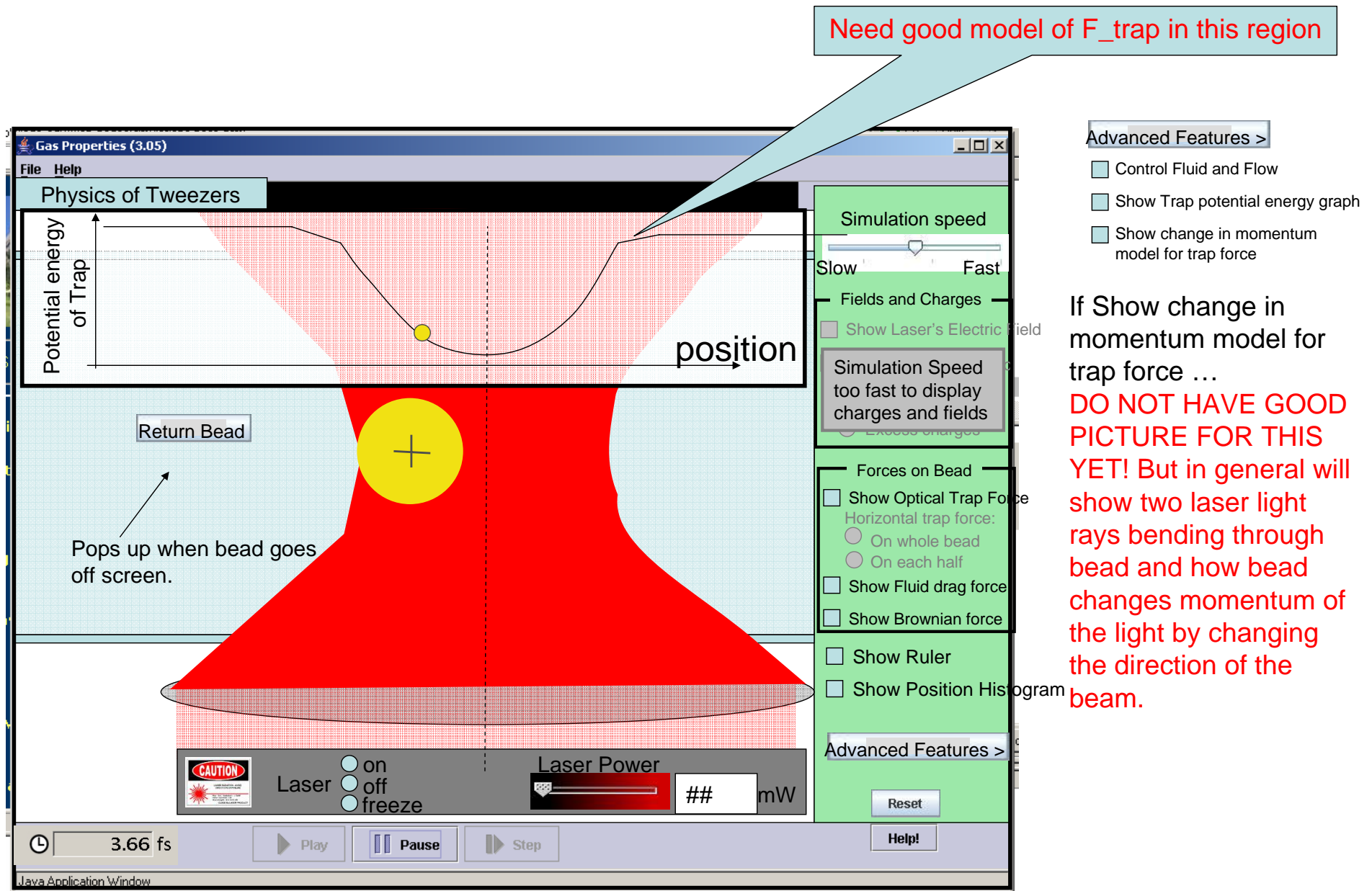
Help!

3.66 fs

Play Pause Step

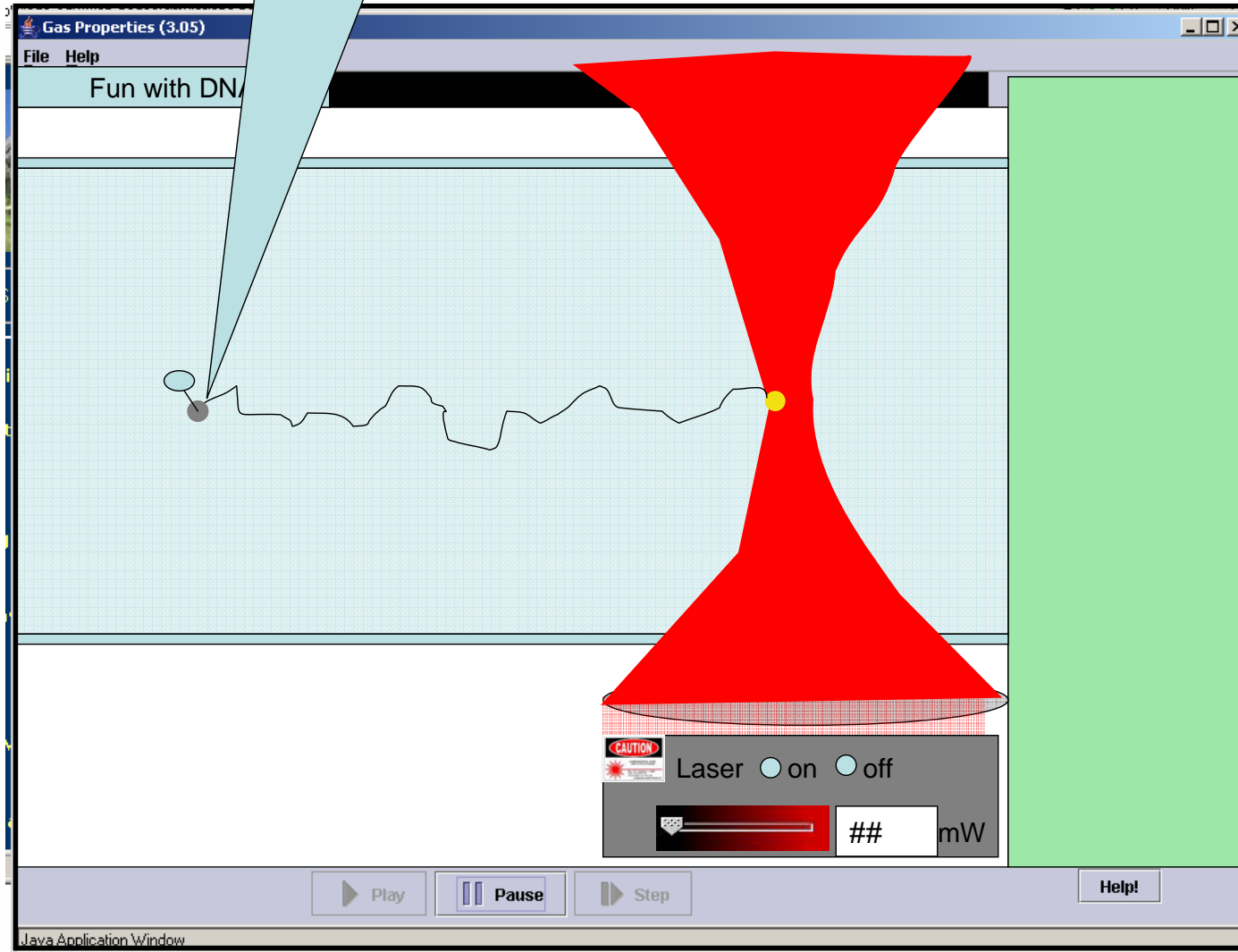
Java Application Window

Physics of Tweezers



Fun with DNA: Panel Two

Need thumbtack or something
indicating DNA stuck down on
this end

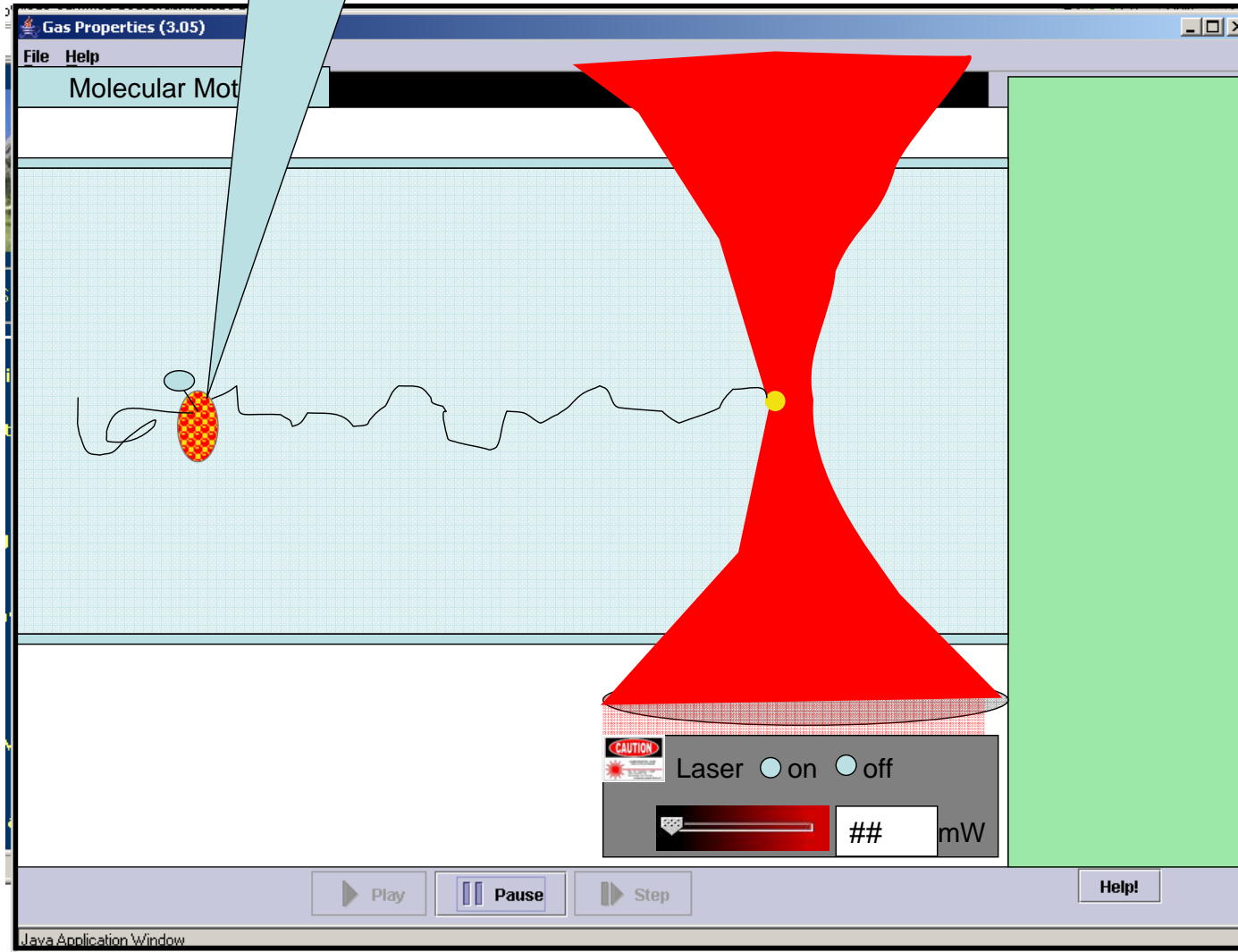


Basic idea:

- DNA with a bead on one end.
- Laser ON will trap bead.
- Can stretch DNA out ... it pulls back against F_{trap} on bead.
- If bead pops out of trap, see DNA recoil due to random walk.
- Same deal with viscous conditions, so $F_{\text{drag}} = \gamma \cdot v$
- Can manipulate bead directly with mouse, or by moving trap laser horizontally.

Molecular Motors: Panel Three

Some representation for an enzyme that is pinned down....



Basic idea:

- Similar to DNA panel, accept now:
- Enzyme pulls on DNA (walks it to left) if ATP (food) is present.
- Force that enzyme pulls with can be measured using laser trap.
- Can now set trap to “maintain constant force” so that it tracks RATE at which enzyme moves DNA along.