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Subject: glacier model
Date: January 30, 2008 1:24:06 AM MST
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 1 Attachment, 7.1 KB [Save](#)

Chris,

Here is a model for the variables you need now (on the basic panel). In the end, I had to give up on making the true model work, so instead this is a way to get decent results without a physically accurate glacial model behind the scenes. Hopefully your design will include the possibility to change some of the numerical values later (within reason), if need be.

In the development of the stuff below, I wrote some python code to make sure things work. I have attached it, just in case you care.

Please let me know when questions arise about this. I will continue to work on the climate change user interface and model. I'll try harder to get those done before you need them.

I'm terribly sorry for the long delay. My big bad.

-Archie

Note: x**y means 'x to the power of y'

1. temperature control:
 - range from -15 to 10 (cold to warm)
 - call this variable 'ref_temp' for reference temperature
 - initial default ref_temp=0
2. snowfall control:
 - range from 1e-3 to 1e-4 (little snowfall to lots)
 - call this variable 'snowfall_lapse_rate'
 - initial default snowfall_lapse_rate=5e-4
3. temperature gauge:
 - given the ref_temp, the temperature as a function of elevation (z, in meters) is
 - $20. + \text{ref_temp} - 6.5 * z / 1e3$
4. accumulation:
 - given
 - (a) the constant snowfall_max=2.0, and
 - (b) the snowfall_lapse_rate,
 - the accumulation as a function of elevation (z) is
 - $z * \text{snowfall_lapse_rate}$,
 - clipped to a minimum of 0 and a max of snowfall_max
5. ablation:
 - given
 - (a) the constant melt_v_elev=-0.011,

(b) the constant $\text{melt_v_temp}=1.3$,
 (c) the constant $\text{melt_temp0}=45.0$,
 (d) the ref_temp ,
 the ablation as a function of elevation (z) is
 $\text{melt_v_elev} \cdot z + \text{melt_temp0} + \text{melt_v_temp} \cdot \text{ref_temp}$,
 clipped to a minimum of 0

6. mass_balance:

given

(a) accumulation as a function of z,

(b) ablation as a function of z,

the mass_balance as a function of elevation (z) is

accumulation – ablation

note this is also called the 'glacial budget';

note the mass_balance as a function of x can be found as follows:

given

(a) the unchanging valley floor elevation, F:

$$F = 4e3 - x/30. + \exp(-(x-5e3)/1e3)$$

(b) mass_balance as a function of z

the mass_balance as a function of x is

mass_balance(F(x))

7. ELA:

given the mass_balance as a function of z,

ELA = elevation at which mass_balance=0

note: ELA stands for equilibrium line altitude; it is
 the elevation of the equilibrium line

8. ice volume flux (Q):

given

(a) the unchanging valley width, W:

$$W = 1e3 + 5e3 \cdot \exp(-((x-5e3)/2e3)**2)$$

(b) the mass_balance as a function of x

the ice volume flux as a function of X is

integral (from 0 to X) of W * mass_balance,

clipped to a minimum of 0

call this variable 'Q'

9. the length of the glacier (x_terminus):

given the ice volume flux, Q

the length of the glacier is the x-coordinate at which Q
 becomes 0

call this variable 'x_terminus'

10. ice thickness at steady state (H):

given

(a) the constant max_thickness=500.0,

(b) the ice volume flux, Q

(c) the maximum value of Q, max_Q

(d) the length of the glacier, x_terminus

(e) the constant length of valley, x_max=80e3

the steady state (or equilibrium) glacier thickness as a
 function of x is

$$Q * (\text{max_thickness}/\text{max_Q}) * (x_terminus/x_max)$$

call this variable 'H'

11. vertically-averaged deformation ice velocity ($u_{\text{deform_ave}}$):
given

- (a) the variable $u_{0\text{ave}}$ which is the average of H^2 ,
where the average is over the nonzero of H ,
the vertically-averaged deformation ice velocity as a
function of x is

$$H^2 * 20 / u_{0\text{ave}}$$

call this variable ' $u_{\text{deform_ave}}$ '

12. vertically-averaged total ice velocity (u_{ave}):
given

- (a) the constant $u_{\text{slide}}=20$
 - (b) the variable $u_{\text{deform_ave}}$ as a function of x
- the vertically-averaged total ice velocity as a function
of x is

$$u_{\text{deform_ave}} + u_{\text{slide}}$$

call this variable ' u_{ave} '

13. vertical velocity profile
given

- (a) the variable zz which varies from 0 at the base
of the glacier (rock-ice interface) to 1 at the
top of the glacier (air-ice interface)
- (b) the vertically-averaged ice deformation
velocity, $u_{\text{deform_ave}}$
- (c) the point X (within the domain of x) at which to
measure the vertical velocity profile
- (d) the constant $u_{\text{slide}}=20$

the vertical velocity profile (as a function of zz) is

$$u_{\text{slide}} + u_{\text{deform_ave}}[X] * 5. * (zz - 1.5 * zz^2 + zz^3 - 0.25 * zz^4)$$

note that $u_{\text{deform_ave}}[X]$ means $u_{\text{deform_ave}}$ evaluated
at the position $x=X$

14. climate change timescale

given an ELA, the climate change timescale is

$$-35.7/300. * \text{ELA} + 484.6,$$

clipped to a minimum of 20 and a max of 50

call this variable ' timescale '

15. model for simple time-dependence

In the basic panel, when a control is changed, the
time-dependence between the original climate (call it
 climate_0) and the new climate (call it climate_1) can
be computed as follows

- (a) calculate the ELA for climate_0
- (b) calculate the ELA for climate_1
- (c) calculate the climate change timescale for climate_0
- (d) calculate the climate change timescale for climate_1
- (e) calculate the average of these two timescales, call
it T
- (f) calculate a new glacier thickness, H , for climate_1
- (g) evolve each point in the glacier from the original
thickness to the new thickness with an exponentially
decaying time-dependence of characteristic time T ;

for example, going from H0 (for climate_0) to H1
(for climate_1) looks like
$$H(t) = H_0 + (H_1 - H_0) * (1 - \exp(-t/T))$$

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[model.py \(7.1 KB\)](#)