

# Recent Developments in Pyrocar and MechElastic

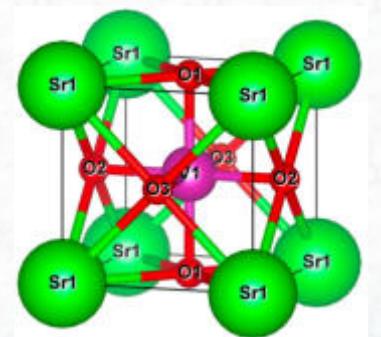
## Pyrocar Contributors

Uthpala Herath, Pedram Tavadze, Xu He, Eric Bousquet, Sobhit Singh, Reese Boucher, Logan Lang, Freddy Farah, Francisco Muñoz and Aldo H. Romero

## MechElastic Contributors

Logan Lang , Sobhit Singh, Viviana Dovale-Farelo, Uthpala Herath, Pedram Tavazohi, François-Xavier Coudert, Aldo H. Romero

# Pyprocarn



DFT



Numerical data



Li<sub>3</sub>Mn<sub>10</sub>5

- Simple, single line commands

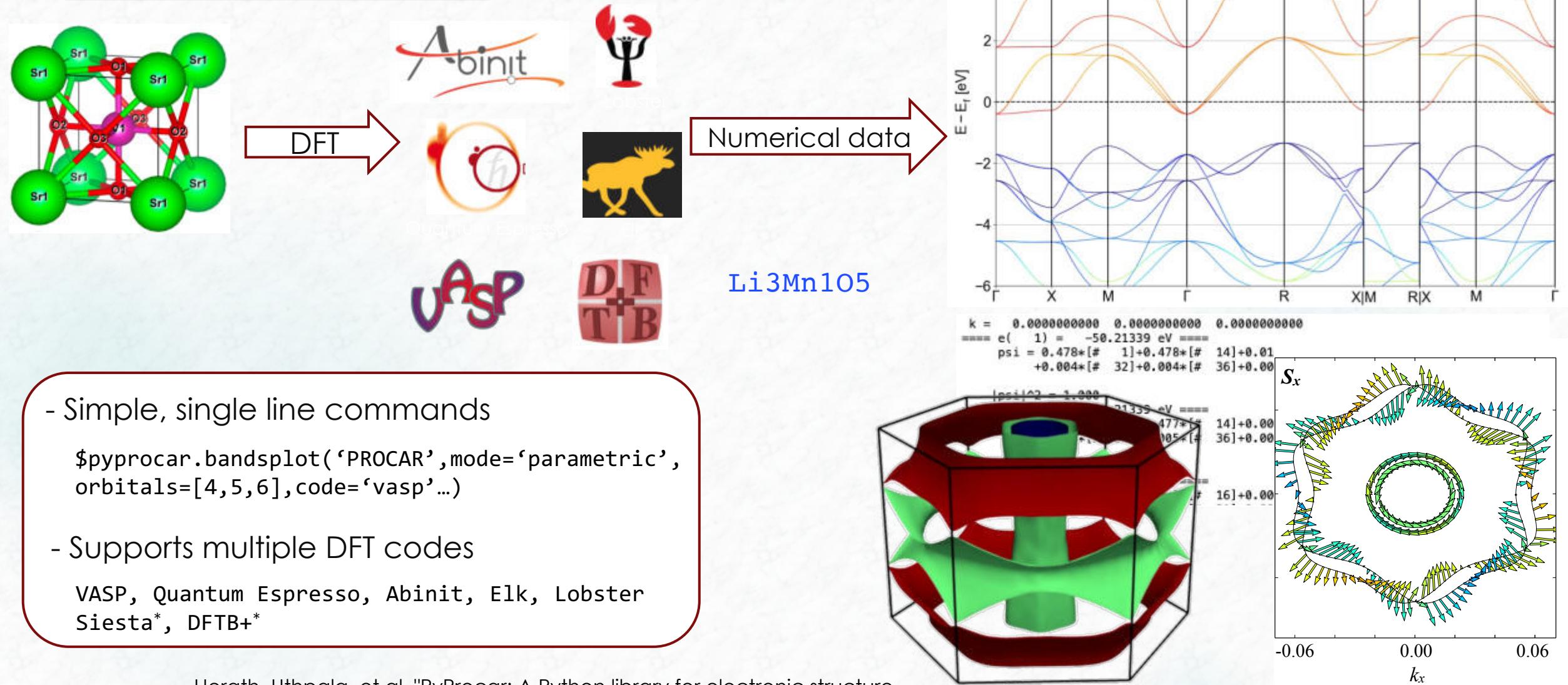
```
$pyprocarn.bandsplot('PROCAR', mode='parametric',  
                     orbitals=[4,5,6], code='vasp'...)
```

- Supports multiple DFT codes

VASP, Quantum Espresso, Abinit, Elk, Lobster  
Siesta\*, DFTB+\*

```
PROCAR lm decomposed  
# of k-points: 200      # of bands: 48      # of ions: 5  
  
k-point    1 :  0.000000000 0.000000000 0.000000000      weight = 0.005000000  
  
band      1 # energy -29.05690371 # occ.  2.000000000  
  
ion      s   py   pz   px   dxy   dyz   dz2   dxz   x2-y2   tot  
1  0.972  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.972  
2  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  
3  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  
4  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  
5  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  
tot  0.974  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.000  0.974  
  
0.000000000  1.203497247  0.000000  0.000000  0.000000  0.000000  0.000215  0.  
0.7213197256E-01  1.206644141  0.029906  0.000944  0.000000  0.000944  0.007378  0.  
0.1442639451  1.215535536  0.014263  0.001967  0.000000  0.001967  0.007869  0.  
0.2163959177  1.2226439061  0.004364  0.002027  0.000000  0.002027  0.008587  0.  
0.2885278902  1.235537941  0.000056  0.001289  0.000000  0.001289  0.010137  0.  
0.3606598628  1.233460228  0.002649  0.000051  0.000000  0.000051  0.003660  0.  
0.4327918353  1.228146745  0.000000  0.000002  0.000000  0.000002  0.000000  0.  
0.5049238879  1.206604221  0.000000  0.000011  0.000000  0.000011  0.000086  0.  
0.5770557805  1.195644770  0.000000  0.000000  0.019435  0.000000  0.000000  0.  
0.6491877530  1.198648720  0.000000  0.004414  0.000000  0.004414  0.035955  0.  
0.7213197256  1.172068978  0.000000  0.001263  0.000000  0.001263  0.017216  0.  
0.7934516981  1.143774531  0.000000  0.000369  0.000000  0.000369  0.016328  0.  
0.8655836787  1.139814551  0.000000  0.000000  0.000000  0.000000  0.000000  0.  
  
k =  0.0000000000  0.0000000000  0.0000000000  
==== e( 1) = -50.21339 eV ====  
psi = 0.478*[# 1]+0.478*[# 14]+0.010*[# 2]+0.010*[# 15]+0.004*[# 28]  
+0.004*[# 32]+0.004*[# 36]+0.004*[# 40]+0.002*[# 9]+0.002*[# 22]  
  
|psi|^2 = 1.000  
==== e( 2) = -50.21339 eV ====  
psi = 0.477*[# 1]+0.477*[# 14]+0.009*[# 2]+0.009*[# 15]+0.005*[# 28]  
+0.005*[# 32]+0.005*[# 36]+0.005*[# 40]+0.002*[# 9]+0.002*[# 22]  
  
|psi|^2 = 1.000  
==== e( 3) = -24.41820 eV ====  
psi = 0.485*[# 3]+0.485*[# 16]+0.006*[# 6]+0.006*[# 19]+0.002*[# 27]
```

# Pyprocarn



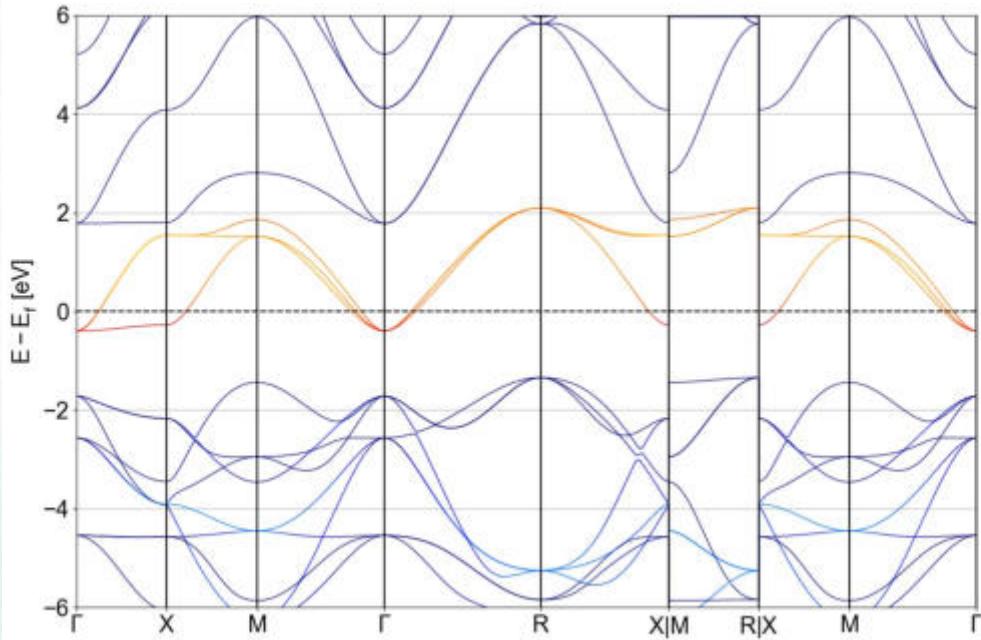
- Simple, single line commands

```
$pyprocarn.bandsplot('PROCAR', mode='parametric',
                      orbitals=[4,5,6], code='vasp'...)
```

- Supports multiple DFT codes

VASP, Quantum Espresso, Abinit, Elk, Lobster  
Siesta\*, DFTB+\*

# Plotting band structures



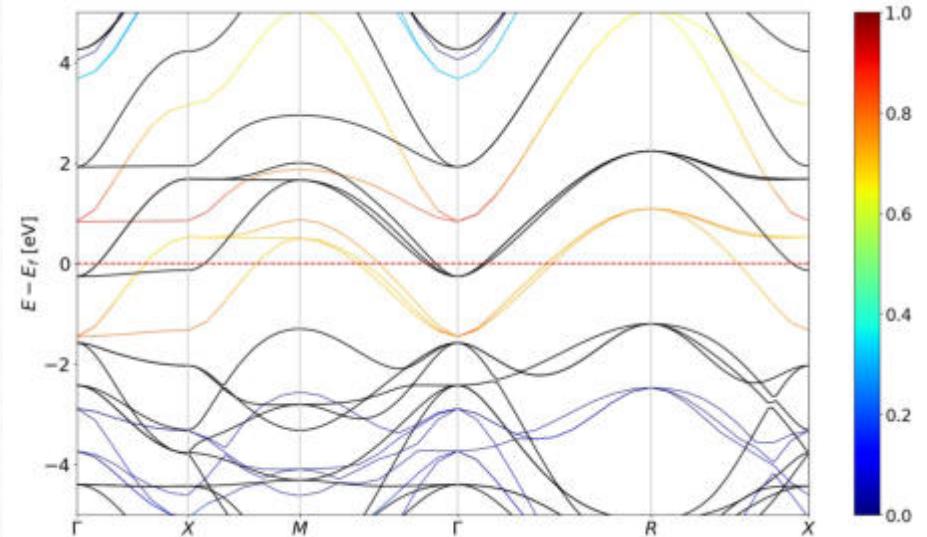
Export plots as matplotlib objects for further processing

```
ax=pyprocar.bandsplot(..,mode='plain',code='elk')
pyprocar.bandsplot(..,mode='parametric',code='vasp',ax=ax)
```

Perform a combination of one or more projections.

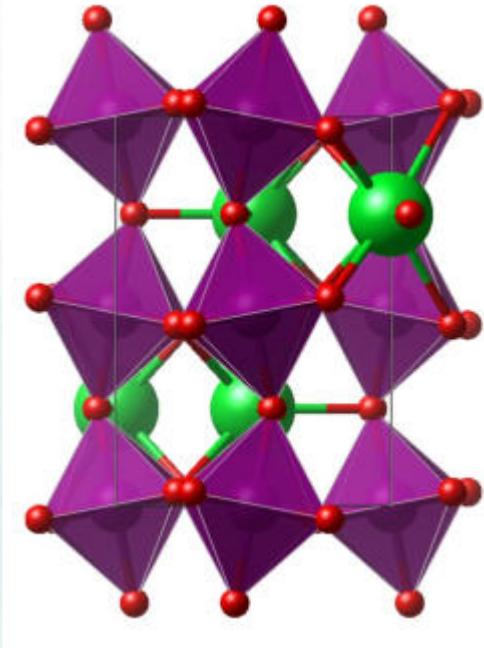
V -  $d_{t_2g}$

```
pyprocar.bandsplot(..,mode='parametric',atoms=[1],
                   orbitals=[4,5,7])
```

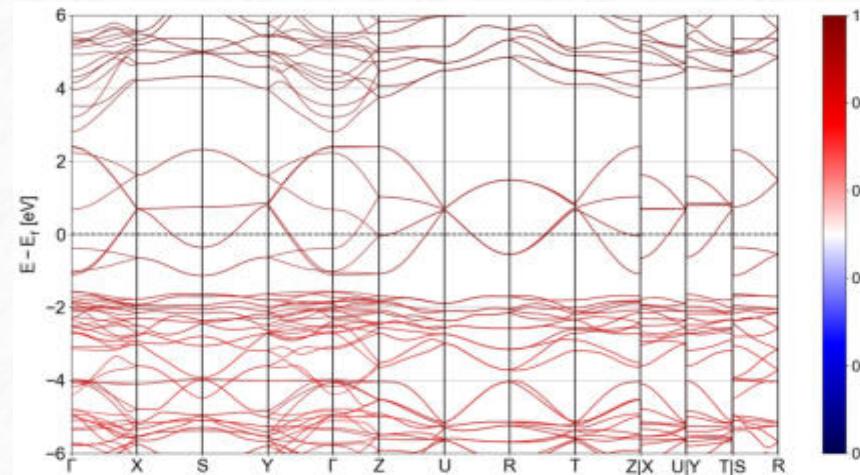


# Plotting band structures

Collinear spin calculations

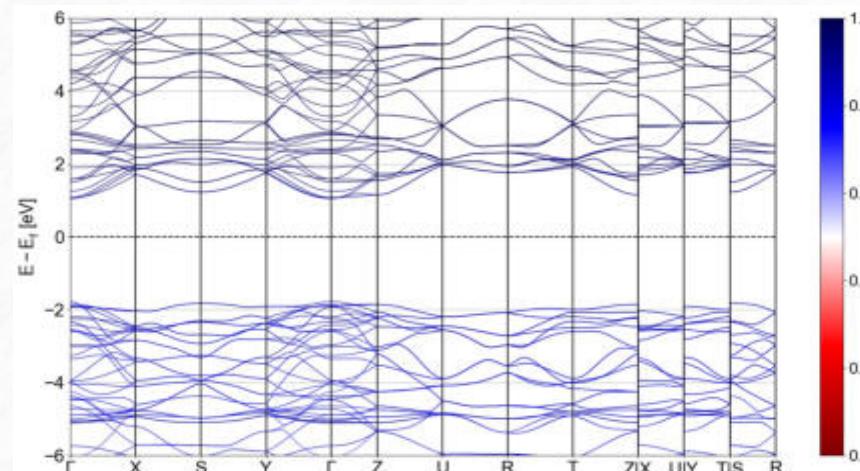


$\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$



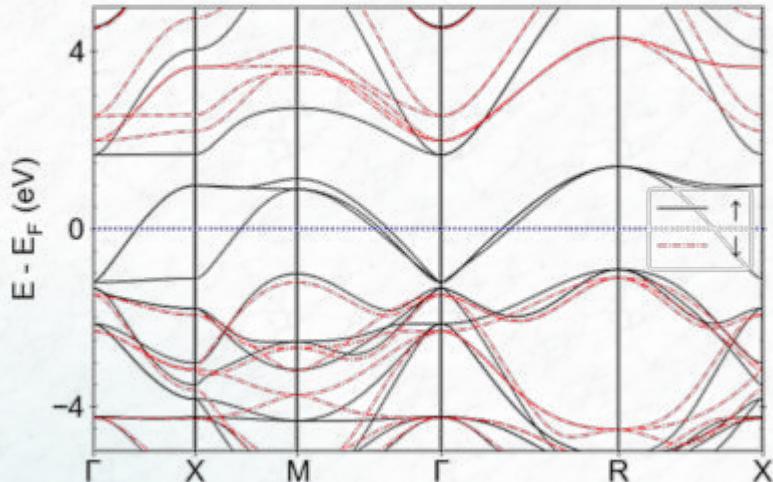
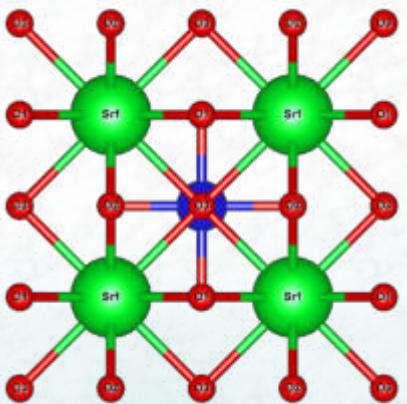
Spin up

`pyprocar.bandsplot(..., spin=1, separate=True)`

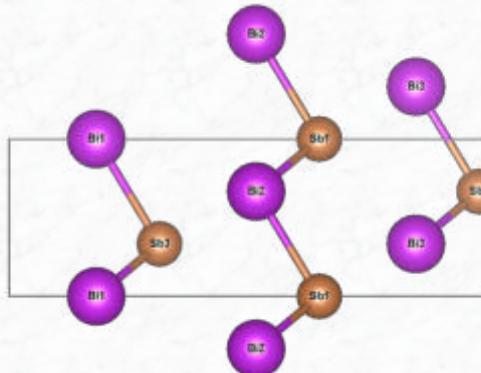


Spin down

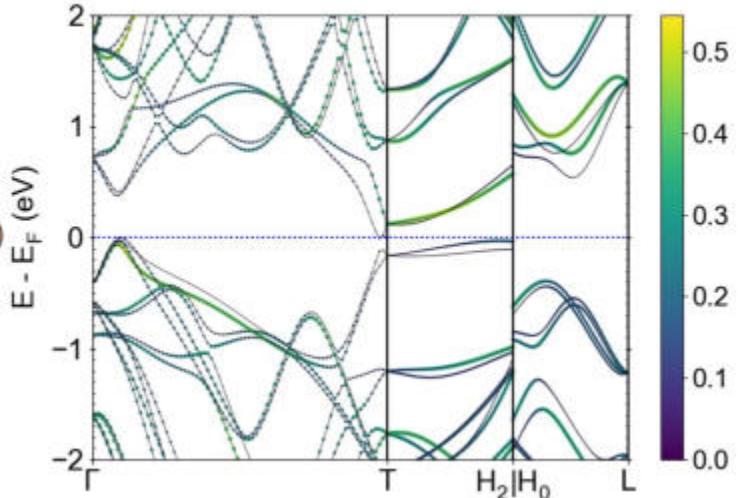
# Plotting band structures



```
pyprocar.bandsplot(mode='plain',
    linestyles=['solid', 'dashdot'],
    colors=["black", "red"],
    elimit=[-5, 5],
    savefig="SrVO3-spin-pol.png",
    show=True,
    legend=True,
)
```

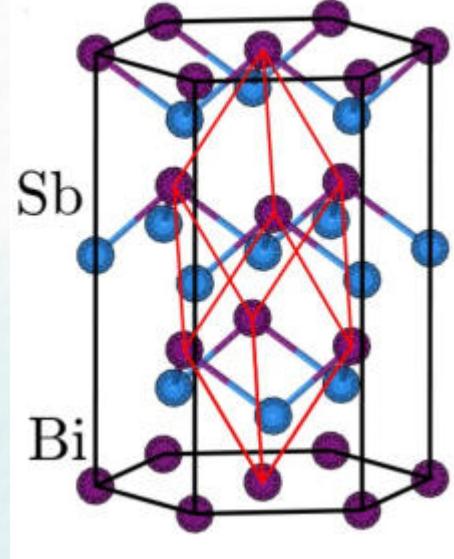


```
ebs_plot = pyprocar.bandsplot(mode='scatter',
    legend=False,
    spins=[0, 1],
    orbitals=['p'],
    atoms=['Bi'],
    weighted_color=True,
    weighted_width=True,
    elimit=[-2,2]
)
pyprocar.bandsplot(mode='plain',
    legend=False,
    opacities=[0.5],
    elimit=[-2,2],
    ax=ebs_plot.ax)
```

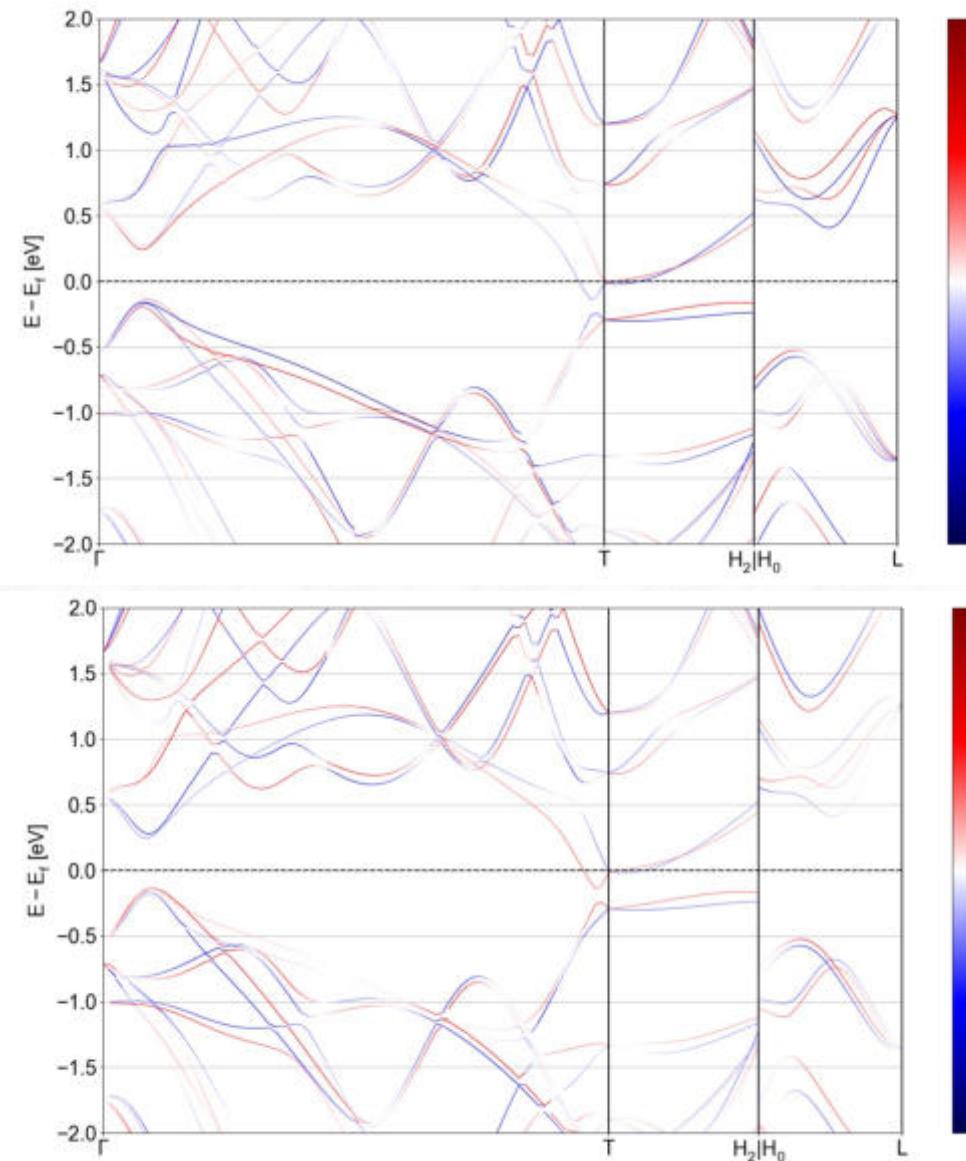


# Plotting band structures

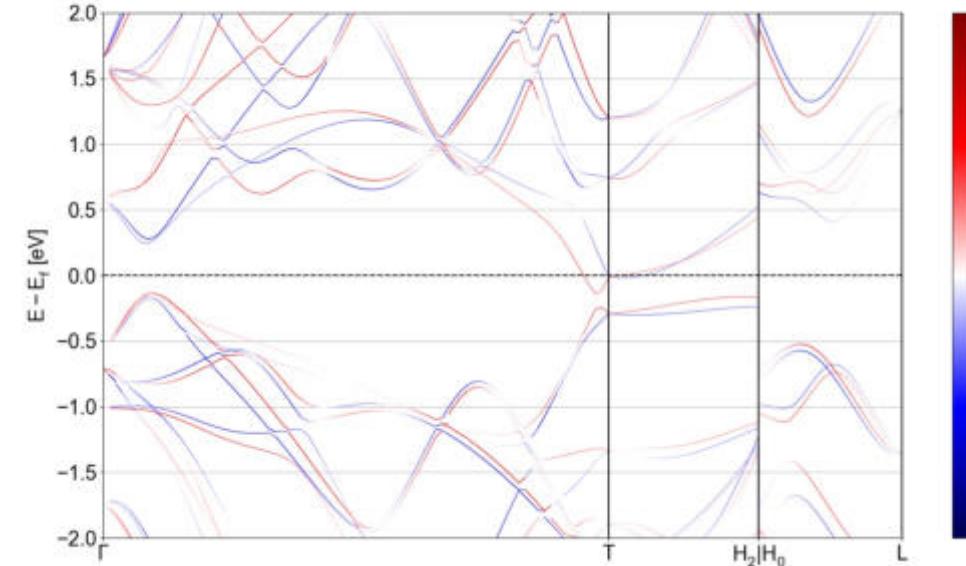
Non-collinear spin calculations



BiSb

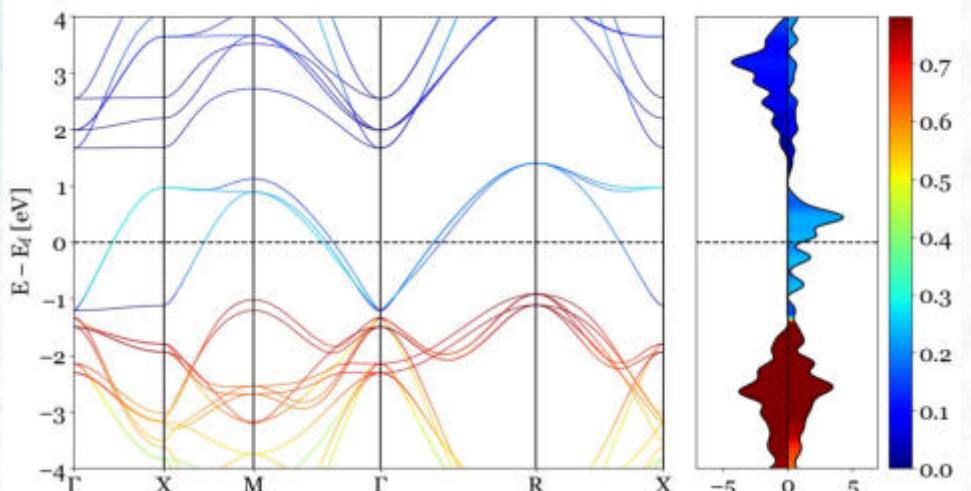
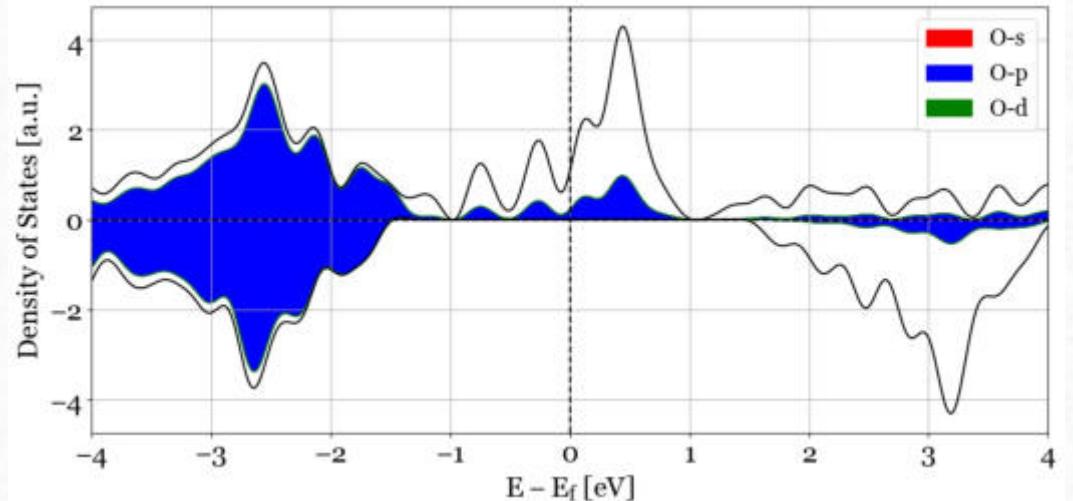
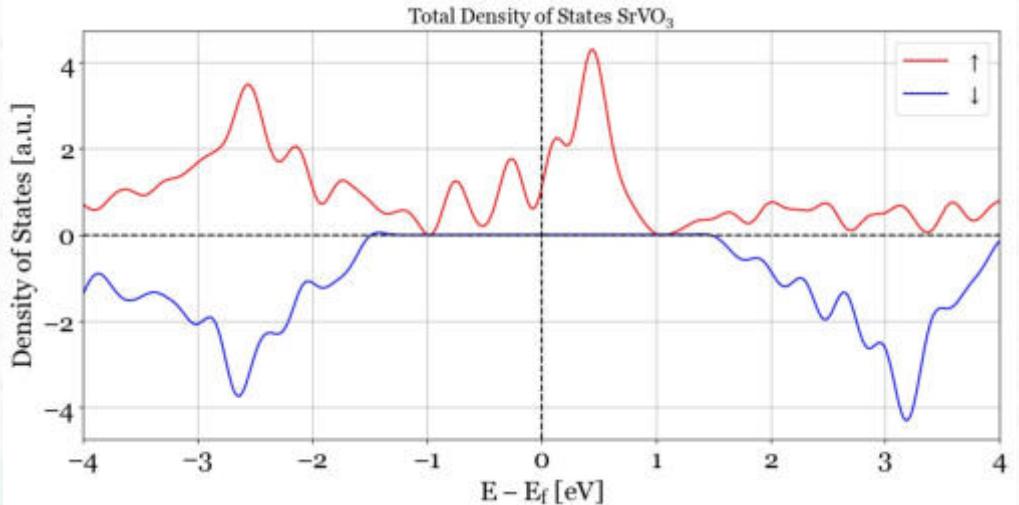


$S_x$   
`pyprocar.bandsplot(..., spin=1)`



$S_y$   
`pyprocar.bandsplot(..., spin=2)`

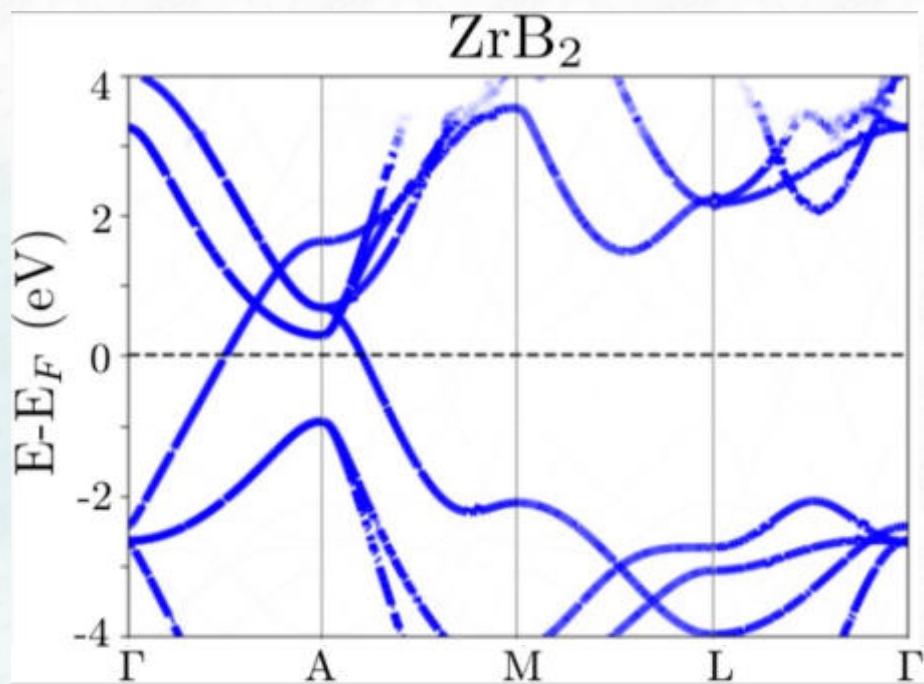
# Density of States



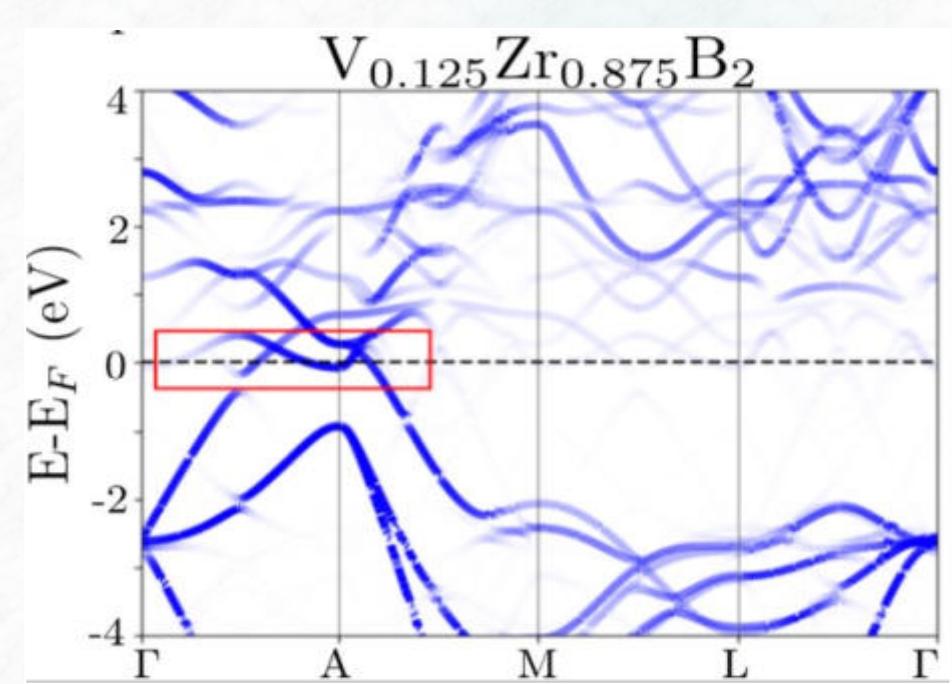
Partial Density of States + Band structure  
pyprocar.bandsdosplot(vasprunfile='vasprun.xml',  
bands\_file='PROCAR', bands\_mode='parametric', dos\_mode='parametric',  
orbitals=[1,2,3], atoms=[2,3,4], ...)

# Band unfolding

- Useful to unfold bands from supercells to compare with primitive cell.  
E.g. - 10% of V doping can induce superconductivity in ZrB<sub>2</sub>. A 2 × 2 × 2 supercell was used to see the changes in the electronic structure.



Primitive cell band structure



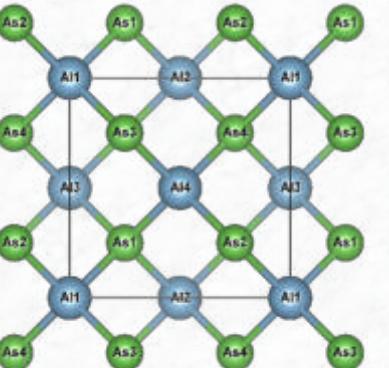
Unfolded band structure of supercell

```
pyprocar.unfold( fname='PROCAR', supercell_matrix=np.diag([2, 2, 2]), ispin=None, show_band=True, width=4, ...)
```



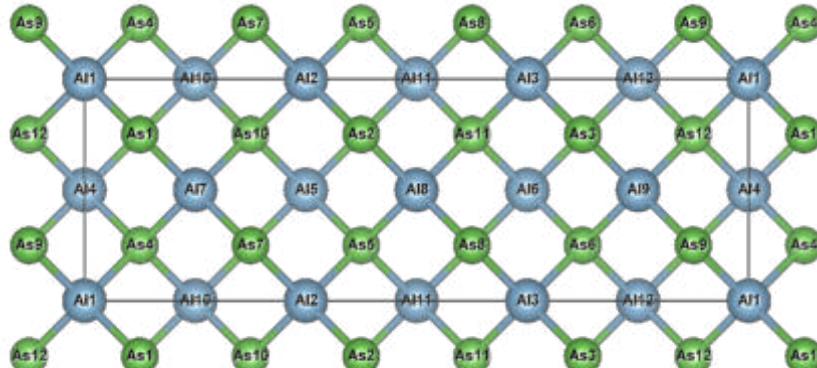
Primitive

$$[[-1, 1, 1], [1, -1, 1], [1, 1, -1]]$$

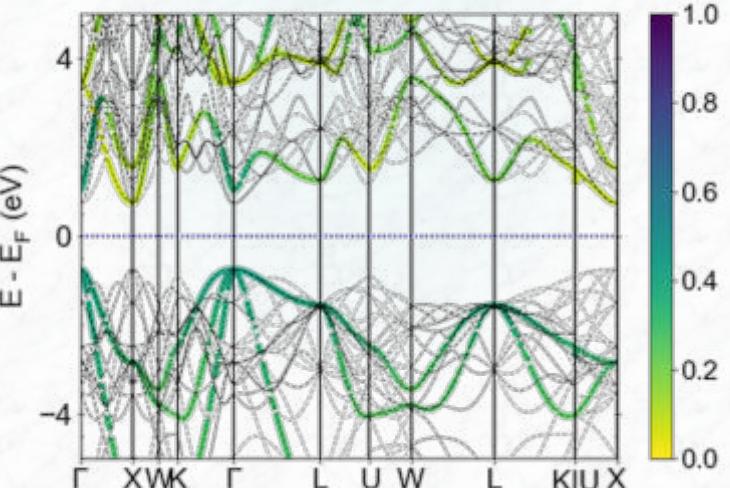
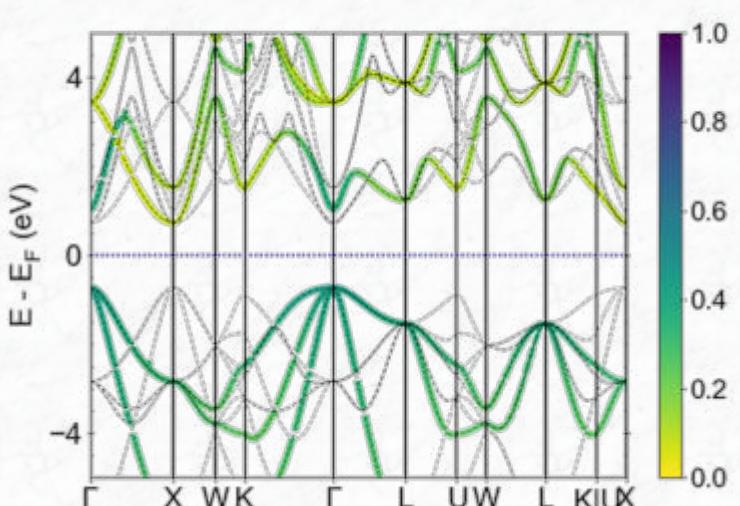
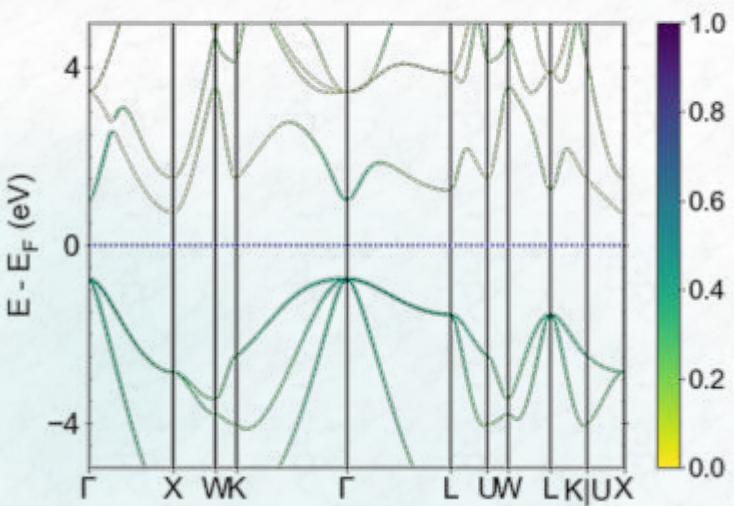


Conventional

$$[[1, 0, 0], [0, 1, 0], [0, 0, 3]]$$



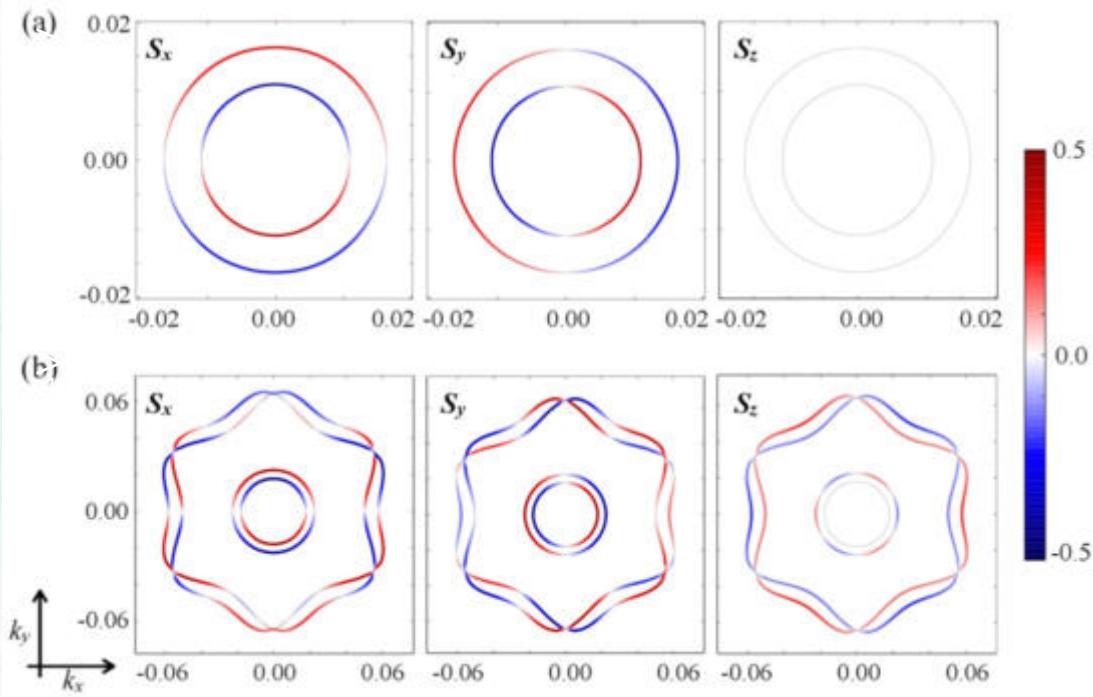
Conventional 1x1x3



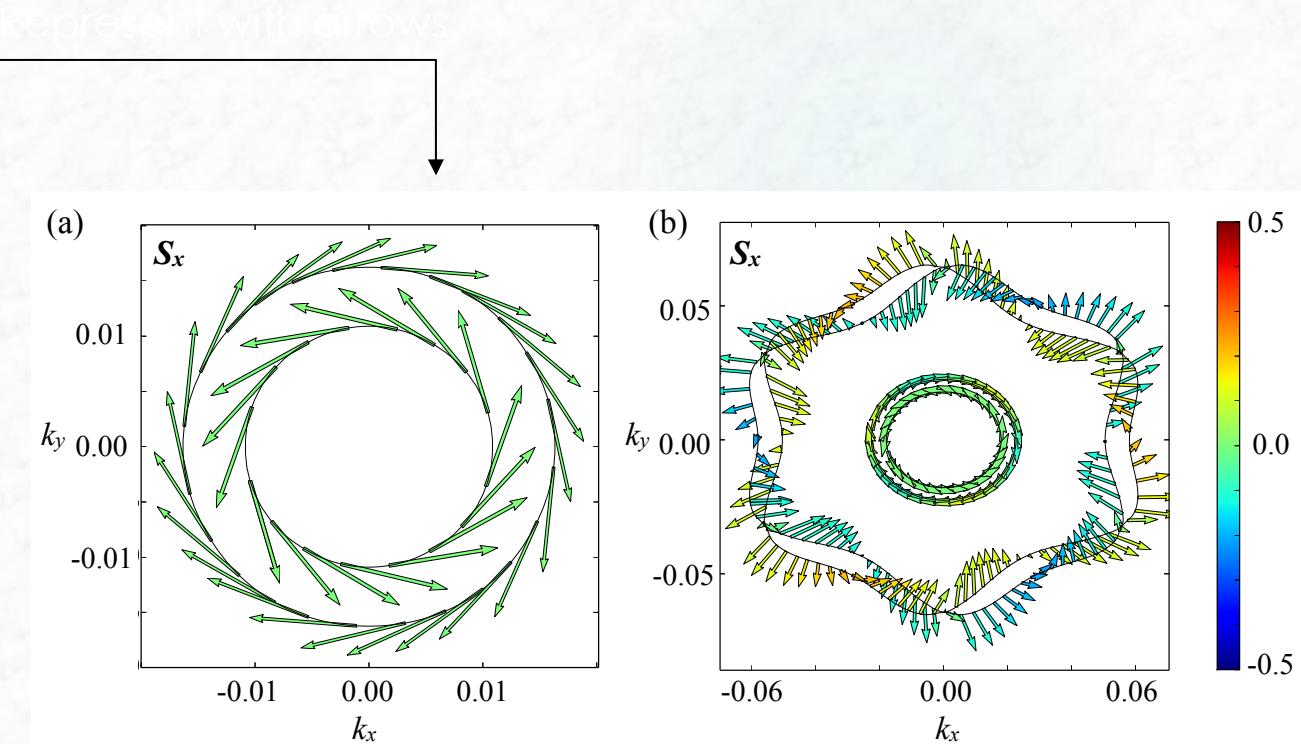
```
ebs_plot = pyprocarr.bandsplot(procar="PROCAR", poscar="POSCAR", outcar="OUTCAR", kpoints="KPOINTS",
                                mode='parametric',
                                atoms=['As'],
                                unfold_mode=unfolding_mode,
                                transformation_matrix= np.dot(np.diag([1, 1, 3]),M),
                                weighted_width=True,
```

# 2D spin texture

- Visualize the constant energy surface spin textures in a system.
- Spin texture in BiSb monolayer. Useful to investigate Rashba and Dresselhaus type spin-splitting effects.

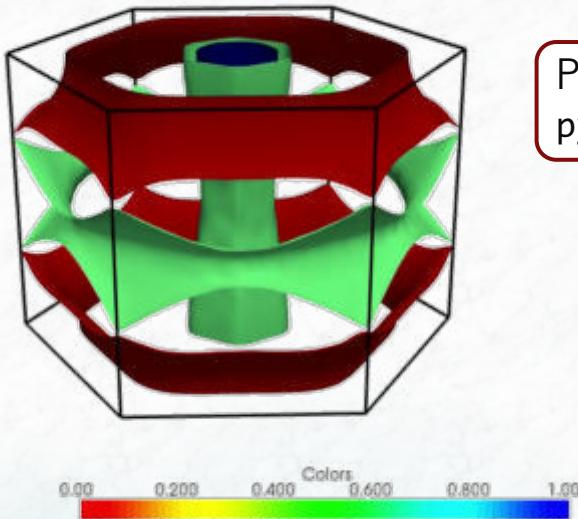


```
pyprocar.fermi2D('PROCAR',st=True,energy=1,  
spin=1,noarrow=True)
```

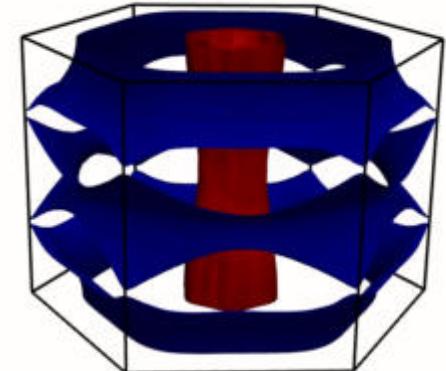


```
pyprocar.fermi2D('PROCAR',st=True,energy=1,  
spin=1,noarrow=False)
```

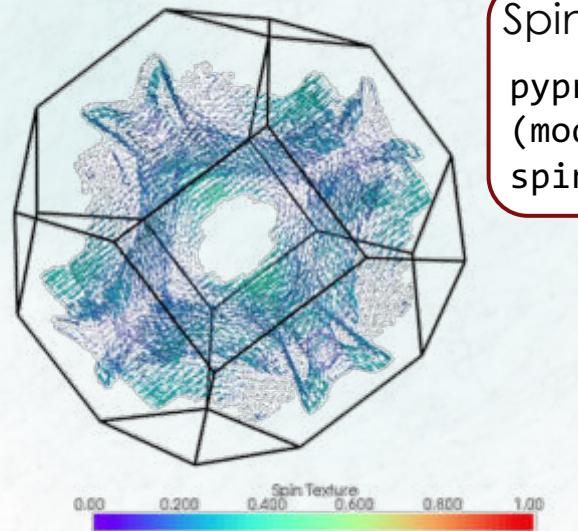
# 3D Fermi surface



Plain Fermi surface – MgB<sub>2</sub>  
`pyprocar.fermi3D(mode='plain'...)`



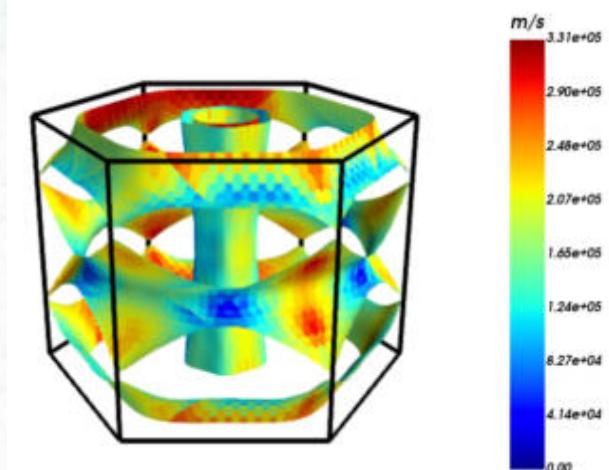
Orbital projected Fermi surface- MgB<sub>2</sub>: B-p<sub>z</sub>  
`pyprocar.fermi3D(mode='parametric',  
orbitals=[3],atoms=[1,2])`



Spin texture surface- BiSb  
`pyprocar.fermi3D  
(mode='parametric',  
spin_texture=True)`

Plotting from external data:  
Fermi velocity projection  
`pyprocar.fermi3D(mode='external',  
color_file='data.dat'...)`

other: effective mass, electron-phonon coupling



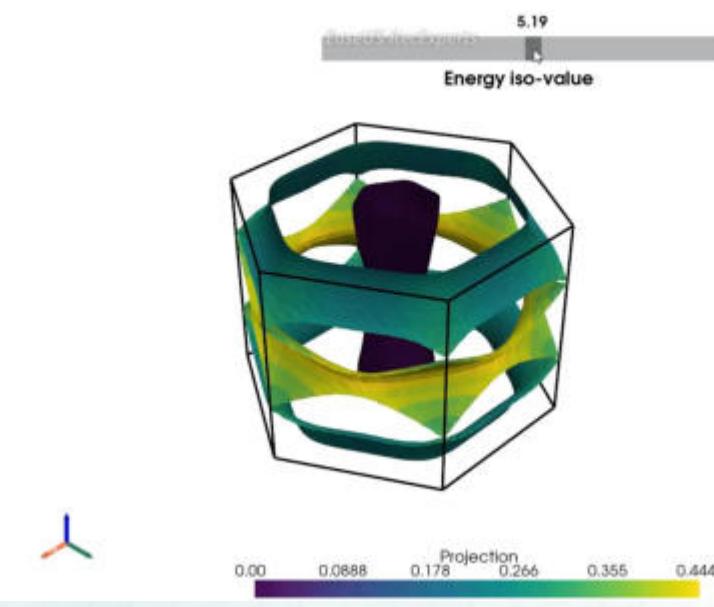
## Input formats

- PROCAR format
- bxsf format

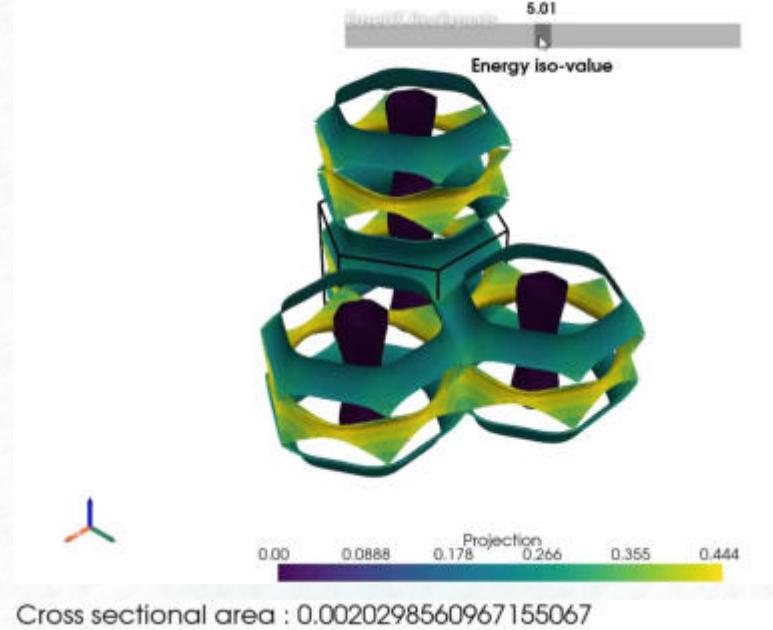
## Export formats

- 2D : png, pdf, ps, ...
- 3D : obj, ply, glb, xml...
- other : gif, mp4

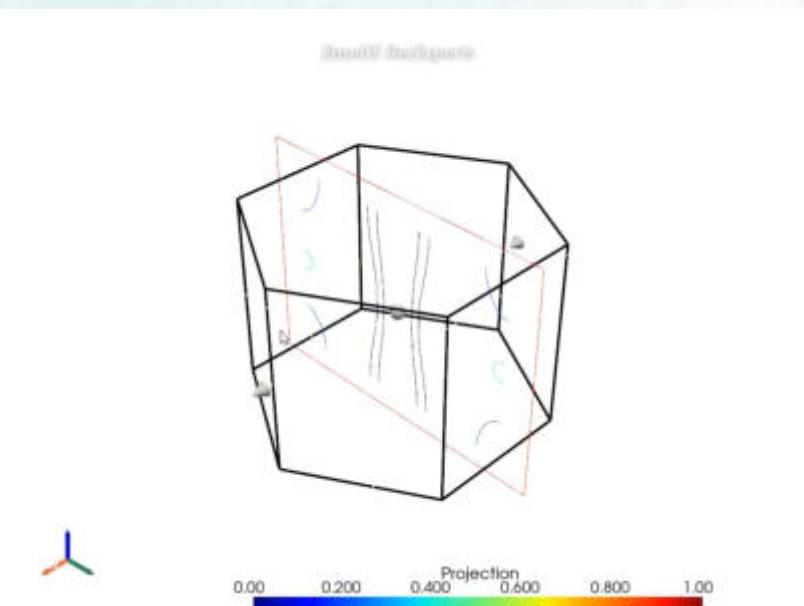
# 3D Fermi surface



```
pyprocar.fermi3D(...,  
    iso_slider = True,  
    iso_range = 5,  
    iso_surfaces = 5,)
```

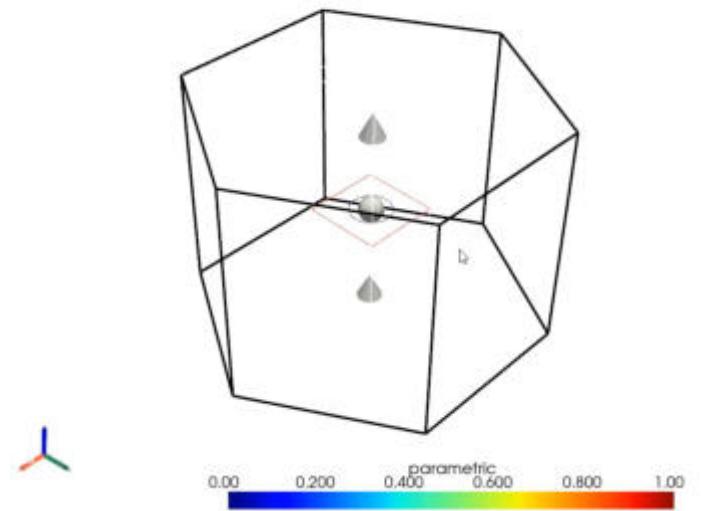


```
pyprocar.fermi3D(...,  
    extended_zone_directions=  
    [[1,0,0],[0,1,0],[0,0,1]])
```



```
pyprocar.fermi3D(...,  
    show_slice=True,  
    slice_origin = (0,0,0)  
    slice_normal = (1,0,0))
```

```
pyprocar.fermi3D(...  
    bands = [5],  
    show_slice=True,  
    slice_normal = (0,0,1),  
    slice_origin = (0,0,0),  
    show_cross_section_area= True)
```



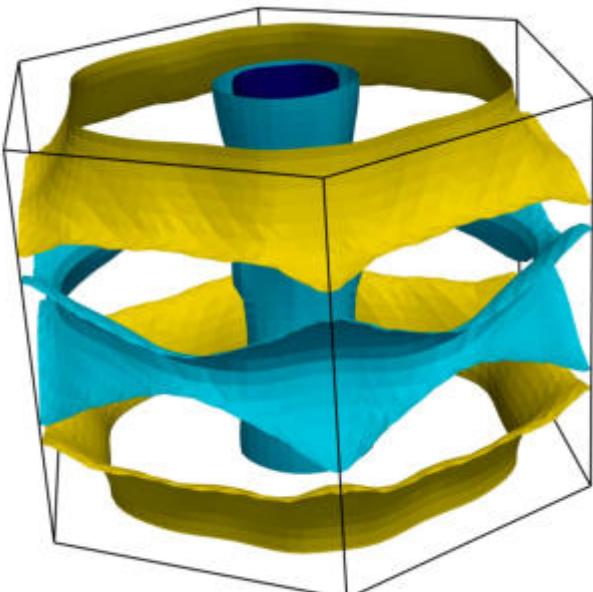
# Fermi Surface - Abinit

```
pyprocar.fermi3D(  
    "PROCAR",  
    abinit_output="abinit.out",  
    code="abinit",  
    mode="plain",  
    interpolation_factor=4,
```

With Abinit v9+ PROCAR is generated when prtproc is set in the .in file.

However, due to parallelization, the PROCAR is split into multiple files. To fix this:

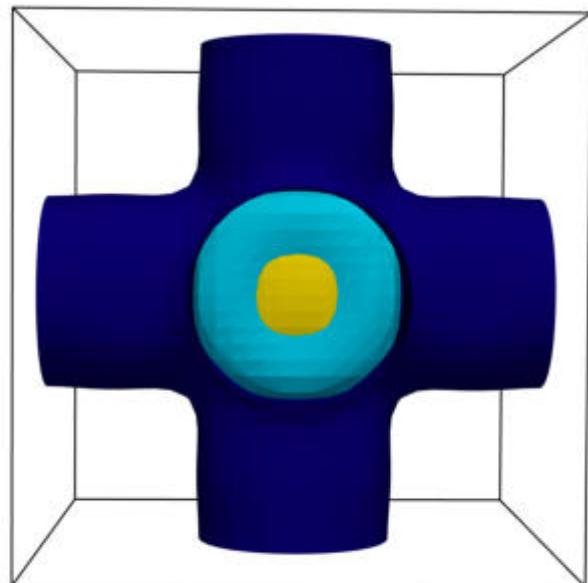
Pyproc.cat(mergeparallel=True, code="abinit") in the directory where the PROCAR\_ files are. In a future release this step will be automated.



MgB<sub>2</sub> Fermi surface

Another option:

Subtract Fermi  
surface of  
different spin  
polarizations



SrVO<sub>3</sub> Fermi surface

# MechElastic



Quantum Espresso



- Simple, single line commands

```
mechelastic.calculate_elastic(code="vasp",
                               dim="3D",
                               infile="OUTCAR-Si_bulk")
```

- Supports multiple DFT codes

VASP, Quantum Espresso, Abinit,

- Elastic constants and EOS

Numerical data

```
Elastic Tensor (GPa units)
553.138 56.794 56.794 0.000 0.000 0.000
56.794 153.138 56.794 -0.000 -0.000 0.000
56.794 56.794 153.138 -0.000 0.000 0.000
0.000 -0.000 -0.000 74.717 -0.000 0.000
0.000 -0.000 0.000 -0.000 74.717 0.000
0.000 -0.000 0.000 0.000 0.000 74.717

This matrix was computed from vasp
Note: for VASP users this is the pressure-corrected matrix

Elastic Tensor Eigen Values (GPa units)
[95.110, 388.718, 96.535, 74.717, 74.717, 74.717]

Mechanical Stability Tests

WARNING: crystal symmetry class was not provided by user, it will be taken from the OUTCAR
One of the following was expected as the second argument:
'cubic', 'hexagonal', 'tetragonal', 'rhombohedral-1', 'rhombohedral-2', 'orthorhombic', 'monoclinic'
From OUTCAR the crystal type is = cubic
Cubic crystal system

More stability criteria for the stability of cubic system one: Ref.[1]
(I) C11 - C12 > 0; (II) C11 + 2C12 > 0; (III) C44 > 0
Condition (I) satisfied,
Condition (II) satisfied,
Condition (III) satisfied.

Elastic Moduli

          Voigt    Reuss   Average
Bulk modulus (GPa) 88.986 88.986 88.986
Shear modulus (GPa) 64.088 61.220 62.659
Young's modulus (GPa) 155.035 149.374 152.284
Poisson's ratio 0.209 0.220 0.215
P-wave modulus (GPa) 174.369 170.532 172.451
Bulk/Shear ratio 1.387 1.452 1.419 (brittle)

Elastic parameters

Lame's first and second parameter; Ref.[3]
Lambda (GPa) = 47.138
Mu (GPa) = 62.652

Bonding information

Kleinman's parameter; Ref.[4,5]
NOTE: K = 0 (I) bending (stretching) would dominate
K = 0.63391

Cauchy's Pressure calculated from the relation : CP = C_12 - C_44
CP > 0 (+ve) indicates that ionic bonding dominates
CP < 0 (-ve) indicates that covalent bonding dominates
CP (GPa) = -17.923
Bonding is mainly covalent

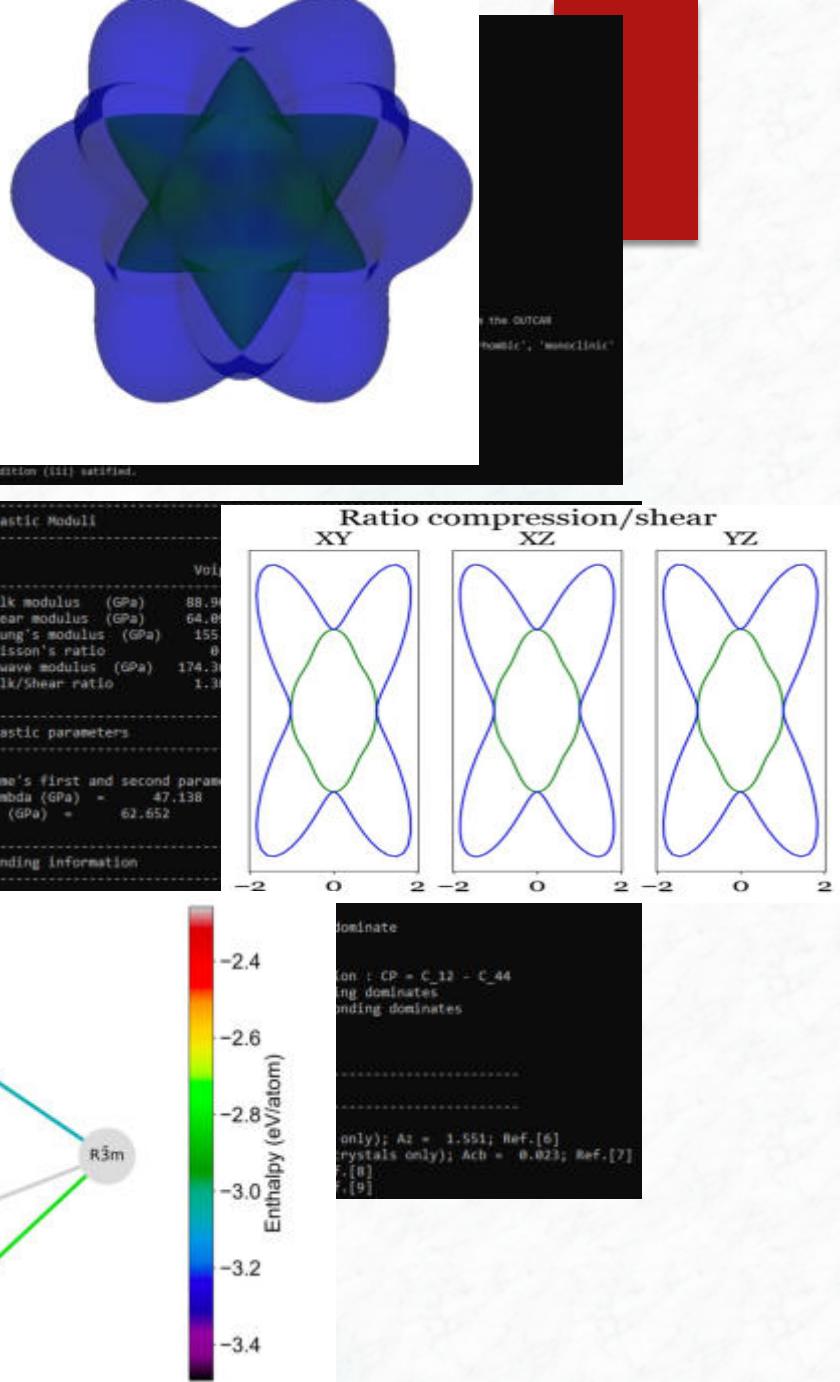
Elastic Anisotropy

Zener's anisotropy (true for cubic crystals only); Az = 1.551; Ref.[6]
Chung-Buessem's anisotropy (true for cubic crystals only); Acb = 0.023; Ref.[7]
Universal anisotropy index; Au = 0.235; Ref.[8]
Log-Euclidean's anisotropy; Al = 0.303; Ref.[9]
```

# MechElastic



Numerical data →



- Simple, single line commands

```
mechelastic.calculate_elastic(code="vasp",
                               dim="3D",
                               infile="OUTCAR-Si_bulk")
```

- Supports multiple DFT codes

VASP, Quantum Espresso, Abinit,

- Elastic constants and EOS

# MechElastic 3D Analysis

```
mechelastic.calculate_elastic(code="vasp",
                               dim="3D",
                               infile="OUTCAR-Si_bulk")
```

## Elastic Tensor (GPa units)

153.130	56.794	56.794	0.000	0.000	-0.000
56.794	153.130	56.794	-0.000	-0.000	-0.000
56.794	56.794	153.130	-0.000	0.000	0.000
0.000	-0.000	-0.000	74.717	-0.000	0.000
0.000	-0.000	0.000	-0.000	74.717	0.000
-0.000	-0.000	0.000	0.000	0.000	74.717

This matrix was computed from vasp

Note: For VASP users this is the pressure-corrected matrix

## Elastic Tensor Eigen Values (GPa units)

```
[96.335, 266.718, 96.335, 74.717, 74.717, 74.717]
```

## Mechanical Stability Tests

WARNING: crystal symmetry class was not provided by user, it will be taken from the OUTCAR  
One of the following was expected as the second argument:  
'cubic', 'hexagonal', 'tetragonal', 'rhombohedral-1', 'rhombohedral-2', 'orthorhombic', 'monoclinic'  
From OUTCAR the crystal type is = cubic  
Cubic crystal system

Born stability criteria for the stability of cubic system are: Ref.[1]

(i) C11 - C12 > 0; (ii) C11 + 2C12 > 0; (iii) C44 > 0

Condition (i) satisfied.

Condition (ii) satisfied.

Condition (iii) satisfied.

# MechElastic 3D Analysis

## Elastic Moduli

	Voigt	Reuss	Average
Bulk modulus (GPa)	88.906	88.906	88.906
Shear modulus (GPa)	64.098	61.220	62.659
Young's modulus (GPa)	155.035	149.374	152.204
Poisson's ratio	0.209	0.220	0.215
P-wave modulus (GPa)	174.369	170.532	172.451
Bulk/Shear ratio	1.387	1.452	1.419 (brittle)

## Elastic parameters

Lame's first and second parameter; Ref.[3]

Lambda (GPa) = 47.138

Mu (GPa) = 62.652

## Bonding information

Kleinman's parameter; Ref.[4,5]

NOTE: K = 0 (1) bending (stretching) would dominate

K = 0.63391

Cauchy's Pressure calculated from the relation : CP = C\_12 - C\_44

CP > 0 (+ve) indicates that ionic bonding dominates

CP < 0 (-ve) indicates that covalent bonding dominates

CP (GPa) = -17.923

Bonding is mainly covalent

## Elastic Anisotropy

Zener's anisotropy (true for cubic crystals only); Az = 1.551; Ref.[6]

Chung-Buessem's anisotropy (true for cubic crystals only); Acb = 0.023; Ref.[7]

Universal anisotropy index; Au = 0.235; Ref.[8]

Log-Euclidean's anisotropy; AL = 0.103; Ref.[9]

## Elastic Wave Velocities and Debye Temperature

Longitudinal wave velocity (vl) : 8694.638 m/s; Ref.[10]

Transverse wave velocity (vt) : 5240.943 m/s; Ref.[10]

Average wave velocity (vm) : 5795.129 m/s; Ref.[10]

Debye temperature : 630.982 K; Ref.[10]

WARNING: The Debye model for the atomic displacement is based on a monoatomic crystal approximation.  
Here we consider an averaged mass, in case your crystal has several species.

## Melting Temperature

Melting temperature calculated from the empirical relation: Tm = 607 + 9.3\*Kvrh \pm 555 (in K); Ref.[11]  
Tm = 1433.825 K (plus-minus 555 K)

WARNING: This is a crude approximation and its validity needs to be checked!

## Hardness Analysis

Hardness (H1a) = 9.24 GPa; Ref.[12]

Hardness (H1b) = 9.24 GPa; Ref.[12]

Hardness (H2) = 8.19 GPa; Ref.[13]

Hardness (H3) = 9.66 GPa; Ref.[14]

Hardness (H4) = 6.96 GPa; Ref.[15]

Hardness (H5) = 11.94 GPa; Ref.[16]

## Hardness recommendation model:

\*\*\*\*\* Cubic Hexagonal Orthorhombic Rhombohedral General \*\*\*\*\*

\*\*\*\*\* Insulator H2 H1b H2 H2 H2

Semiconductor H5 H1b, H3 H2 H5

Metal H1a H4 H4 H4 H4

\*\*\*\*\*

Insulator : bandgap > 2 eV

Semiconductor : bandgap < 2 eV

Metal : bandgap = 0

# The MechElastic 2D Analysis

```
import mechelastic
mechelastic.calculate_elastic(code="vasp",
                                dim="2D",
                                infile="OUTCAR-graphene"
                                lattice_type = 'hexagonal')
```

```
Elastic tensor for two-dimensional system in N/m units
334.1501    89.8781    0.8525   -0.0015   -0.0169    0.0009
 89.8781    334.2872    0.8606    0.0018    0.0115    0.0013
  0.8525    0.8606   -0.7386    0.0170   -0.0437   -0.0004
 -0.0015    0.0018    0.0170   -1.6537    0.0009   -0.0073
 -0.0169    0.0115   -0.0437    0.0009   -0.4477   -0.0042
  0.0009    0.0013   -0.0004   -0.0073   -0.0042   122.0850

Mechanical Stability Test
Hexagonal lattice
Stability criteria for the stability of hexagonal system are:
(i) C11 + C12 > 0;    (ii) C11 - C12 > 0;
Condition (i) satisfied.
Condition (ii) satisfied.

Elastic properties in two-dimensions
[Useful refs. Andrew et al.; Phys. Rev. B 85, 125428 (2012), Peng et al., Acta Mechanica 223 (2012), 2591-2596; Comput. Mater. Sci. 68, 320 (2013); Mech. Mater. 64, 135 (2013) ]
-----
2D layer modulus (N/m) : 212.048
2D Young's modulus Y[10] (N/m) : 309.985
2D Young's modulus Y[01] (N/m) : 310.112
2D Shear modulus G (N/m) : 122.085
2D Poisson ratio v[10] : 0.269
2D Poisson ratio v[01] : 0.269
-----
```

# EOS module

## Enthalpy Curves

$$H=U+PV$$

```
eos_object = EOS()
```

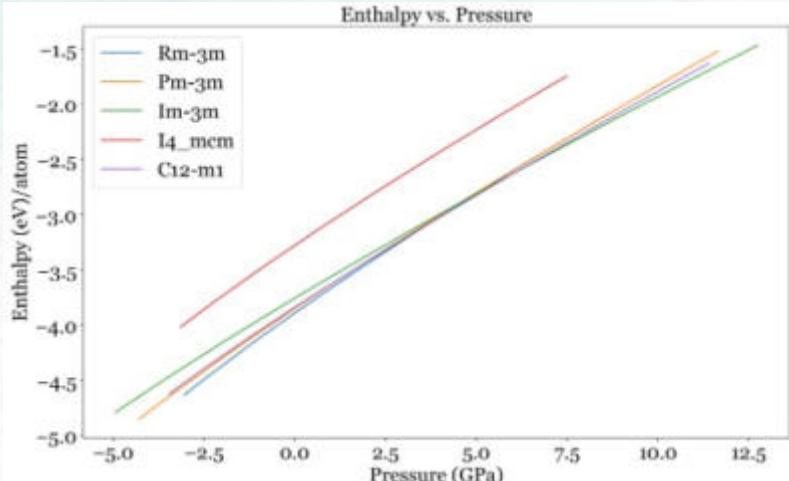
```
infiles = ["Rm-3m", "Pm-3m",
```

```
    "Im-3m", "I4_mcm",
```

```
    "C12-m1"]
```

```
natoms = [6, 1, 2, 9, 4]
```

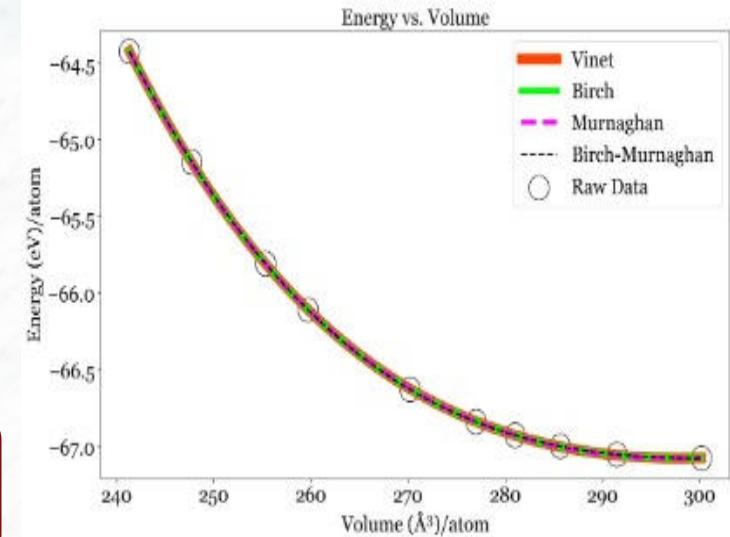
```
 eos_object.plot_enthalpy_curves(infiles,  
 eostype = 'energy', natoms, au=False)
```



## EvsV.dat

```
300.21 -67.07549985  
291.50 -67.05105419  
285.67 -66.99700837  
281.02 -66.92530138  
277.00 -66.83788211  
270.22 -66.62790736  
259.71 -66.10926114  
255.34 -65.80844965  
247.75 -65.14777164  
241.31 -64.42659671
```

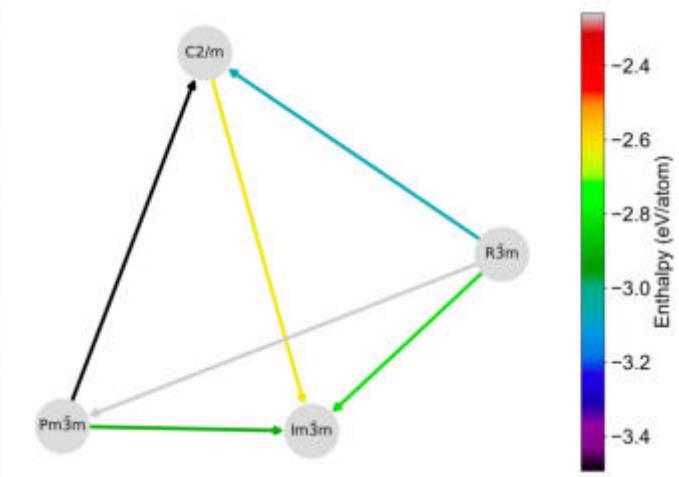
## Curve Fitting



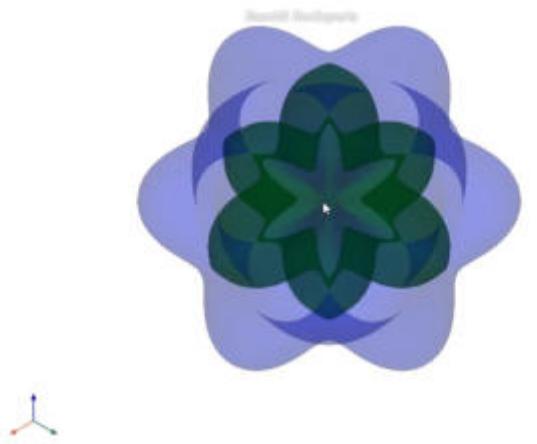
```
 eos = EOS("EvsV.dat")  
 eos.plot_eos(au=False)
```

## Phase transition paths

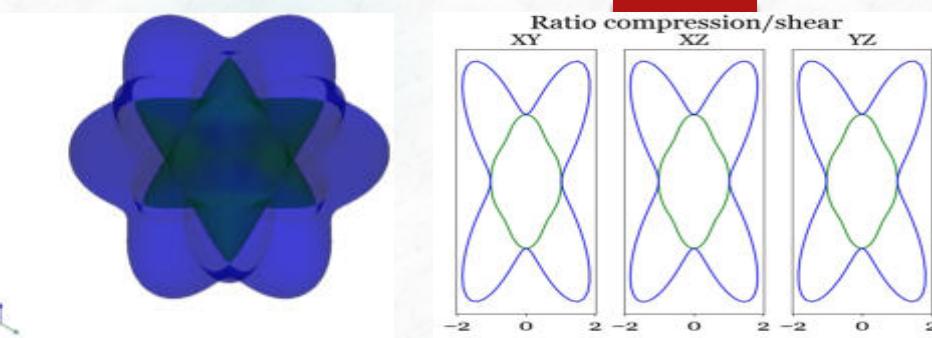
A network plot of the phase transition paths for different phases of Bi. The color of the arrows represents the relative enthalpy for different phase transitions.



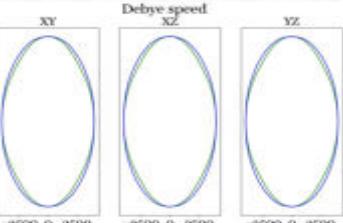
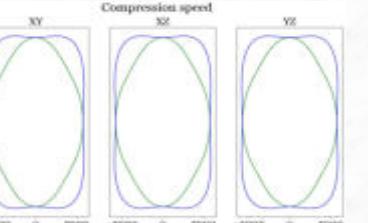
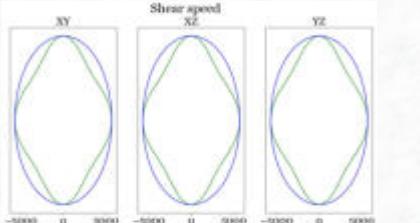
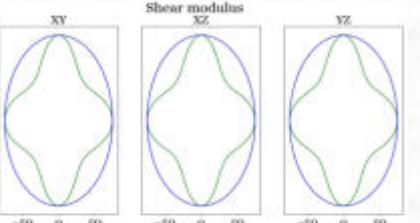
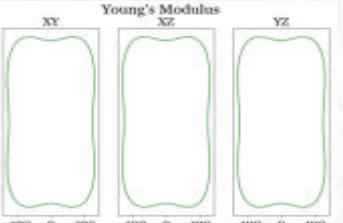
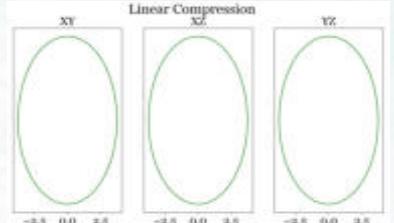
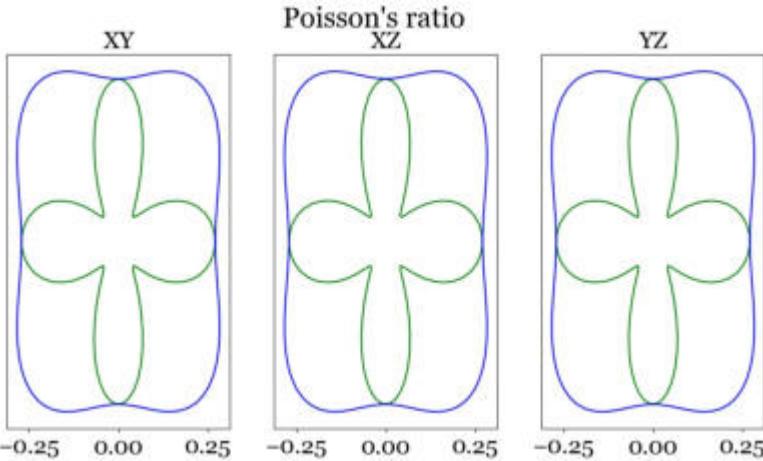
# 2D and 3D Visualizations of Elastic Properties



```
Output1, meshes= mechelastic.calculate_elastic(...,  
plot= "3D"  
elastic_calc= "POISSON"  
show = True)
```



```
Output2,fig = mechelastic.calculate_elastic(... ,  
plot= "2D"  
elastic_calc= "POISSON"  
show=True )
```



# Perspectives

Development of two packages to perform electronic structure and elastic analysis of electronic structure calculations.

Perspectives:

Improve the Fermi surface topology.

Correlate Fermi area cross section with the De Haas-van Alphen Effect (Verstraete).

Compute the Gyrotropic Magnetic Effect (we need extra terms, Fermi curvature).

Extend the package to perform Wavefunction or density analysis.

Some ideas from the community are also considered.