

Q1)



The image shows a MATLAB interface. At the top, a script editor displays the code `X=(1~=0) | (2>2)&(7<4)`. Below it, the Command Window shows the execution of `>> Ass2Q1`, resulting in `X = logical 1`. At the bottom, the Variable Explorer shows a table with two columns: 'Name' and 'Value'. The first row contains a checked checkbox, the variable name 'X', and the value '1'.

Name	Value
<input checked="" type="checkbox"/> X	1

A ~= B returns a logical array with elements set to logical 1 (true) where arrays A and B

are not equal; otherwise, the element is logical 0 (false). The test compares both real

and imaginary parts of numeric arrays. ne returns logical 1 (true) where A or B

have NaN or undefined categorical elements and that's why the answer is logical 1 = true but here it asks about the value

of X which is 1

Q2)

```
1 p=[1 8 2];  
2 r=roots(p);
```

Command Window

```
>> Ass2Q2
```

```
r =
```

```
-7.7417
```

```
-0.2583
```

$r = \text{roots}(p)$ return the roots of the polynomial represented by p as a column vector.

Input p is a vector containing $n+1$ polynomial coefficients, starting with the coefficient of x^n .

A coefficient of 0 indicates an intermediate power that is not present in the equation.






For example, $p = [1 \ 8 \ 2]$ represents the polynomial $x^2 + 8x - 2$

Q3)

```
1 a=12/1*15/1;  
2 b=a/a*a;  
3 c=tand(30)+1/3;  
4 d=1+c;  
5 e=a-b*c+d
```

Command Window

```
>> AssQ3m  
  
e =  
  
17.9876
```

Name ▲	Value	
 a	180	
 b	180	
 c	0.9107	
 d	1.9107	
 e	17.9876	

It is basically variables and were substitutes in an equation to get the value of e

As $a = 180$, $b = 180$, $c =$ which is the tangent of (30) added by 1 divided by 3 as `tand(X)` returns the tangent of the elements of X, which are expressed in degrees which is 0.9107 and then d is $1 + c$ (0.9107) = 1.9107 and then e which we substitute the values $e = (180) - (180)*0.9107+1.9107 = 17.9876$

Q.4. $A = \begin{bmatrix} -7 & 13 & -16 \\ 13 & -10 & 13 \\ -16 & 13 & -7 \end{bmatrix}$

Initial vector $n = x_i = [1.0 \quad -0.8 \quad 0.9]^T$

Formula:

$$x_{i+1} = Ax_i$$

For first iteration: $i = 0$

$$\begin{aligned} x_1 = Ax_0 &= \begin{bmatrix} -7 & 13 & -16 \\ 13 & -10 & 13 \\ -16 & 13 & -7 \end{bmatrix} \begin{bmatrix} 1.0 \\ -0.8 \\ 0.9 \end{bmatrix} \\ &= \begin{bmatrix} -31.8 \\ 32.7 \\ -32.7 \end{bmatrix} \\ &= 32.7 \begin{bmatrix} -0.9725 \\ 1 \\ -1 \end{bmatrix} \end{aligned}$$

For 2nd iteration:

$$\begin{aligned} x_2 = Ax_1 &= \begin{bmatrix} -7 & 13 & -16 \\ 13 & -10 & 13 \\ -16 & 13 & -7 \end{bmatrix} \begin{bmatrix} -0.9725 \\ 1 \\ -1 \end{bmatrix} \\ &= \begin{bmatrix} 35.8075 \\ -35.6425 \\ 35.56 \end{bmatrix} \\ &= 35.8075 \begin{bmatrix} 1 \\ -0.9954 \\ 0.9931 \end{bmatrix} \end{aligned}$$

For 3rd iteration:

$$x_3 = Ax_2 = \begin{bmatrix} -7 & 13 & -16 \\ 13 & -10 & 13 \\ -16 & 13 & -7 \end{bmatrix} \begin{bmatrix} 1 \\ -0.9954 \\ 0.9931 \end{bmatrix}$$

$$\begin{aligned}
&= \begin{bmatrix} -35.8298 \\ 35.8643 \\ -35.8919 \end{bmatrix} \\
&= 35.8643 \begin{bmatrix} -0.9990 \\ 1 \\ -1.0008 \end{bmatrix}
\end{aligned}$$

For 4th iteration:

$$\begin{aligned}
x_4 = Ax_3 &= \begin{bmatrix} -7 & 13 & -16 \\ 13 & -10 & 13 \\ -16 & 13 & -7 \end{bmatrix} \begin{bmatrix} -0.9990 \\ 1 \\ -1.0008 \end{bmatrix} \\
&= \begin{bmatrix} 36.0058 \\ -35.9974 \\ 35.9896 \end{bmatrix} \\
&= 36.0058 \begin{bmatrix} 1 \\ -0.9998 \\ 0.9996 \end{bmatrix}
\end{aligned}$$

For 5th iteration:

$$\begin{aligned}
x_5 = Ax_4 &= \begin{bmatrix} -7 & 13 & -16 \\ 13 & -10 & 13 \\ -16 & 13 & -7 \end{bmatrix} \begin{bmatrix} 1 \\ -0.9998 \\ 0.9996 \end{bmatrix} \\
&= \begin{bmatrix} -35.991 \\ 35.9928 \\ -35.9946 \end{bmatrix} \\
&= 35.9928 \begin{bmatrix} -0.9999 \\ 1 \\ -1.0001 \end{bmatrix}
\end{aligned}$$

For 6th iteration:

$$\begin{aligned}
x_6 = Ax_5 &= \begin{bmatrix} -7 & 13 & -16 \\ 13 & -10 & 13 \\ -16 & 13 & -7 \end{bmatrix} \begin{bmatrix} -0.9999 \\ 1 \\ -1.0001 \end{bmatrix} \\
&= \begin{bmatrix} 36.0009 \\ -36 \\ 35.9991 \end{bmatrix} \\
&= 36.0009 \begin{bmatrix} 1 \\ -1 \\ 1 \end{bmatrix}
\end{aligned}$$

For 7th iteration:

$$\begin{aligned}
 x_7 &= Ax_6 = \begin{bmatrix} -7 & 13 & -16 \\ 13 & -10 & 13 \\ -16 & 13 & -7 \end{bmatrix} \begin{bmatrix} 1 \\ -1 \\ 1 \end{bmatrix} \\
 &= \begin{bmatrix} -36 \\ 36 \\ -36 \end{bmatrix} \\
 &= -36 \begin{bmatrix} 1 \\ -1 \\ 1 \end{bmatrix}
 \end{aligned}$$

Q5)

Denote the variable T_k as X , and S_k as Y

Then the linear equation that fits the data can be given by

$$Y = aX + b$$

Where,

$$a = \text{Slope} = a = \frac{N \sum(xy) - \sum x \sum y}{N \sum(x^2) - (\sum x)^2}$$

$$b = \text{Intercept} = \frac{(\sum Y) - a \sum X}{N}$$

Here, N = Total Number of Observation (data point)

Construct a table of value as shown below:

	$T_k (X)$	$S_k (Y)$	XY	$(X)^2$
	0	1.15	0.00	0
	1	2.32	2.32	1
	2	3.32	6.64	4
	3	4.53	13.59	9
	4	5.56	22.60	16

	5	6.97	34.85	25
	6	8.02	48.12	36
	7	9.23	64.61	49
SUM	28	41.19	192.73	140

From the table;

$$N = 8$$

$$\sum X = 28$$

$$\sum Y = 41.19$$

$$\sum XY = 192.73$$

$$\sum X^2 = 140$$

Use the table values to obtain the values of **a** and **b**.

So,

$$a = \text{Slope} = \frac{(8 \times 192.73) - 28 \times 41.19}{8 \times (140) - (28)^2}$$

$$\Rightarrow a = \frac{388.52}{336} = 1.15631$$

And

$$b = \text{Intercept} = \frac{(41.19) - (1.15631) \times 28}{8}$$

$$\Rightarrow b = \frac{8.81332}{8} = 1.10167$$

Required line of best fit will be:

$$S = (1.15631)T + 1.10167$$

Where,

$$a = 1.15631 \approx 1.15630$$

$$b = 1.10167$$

So, option (C) gives the nearest approximation.

Q6

X	Y
1	5.12
3	3
6	2.48
9	2.34
15	2.18

$$y = ae^{\beta x}$$

$$\ln(y) = \ln(a) + \beta x \ln(e)$$

$$Y = A + Bx$$

When $Y = \ln(y)$

$$A = \ln(a)$$

$$B = \ln(e)$$

Corresponding normal equation we.

$$\sum Y = NA + B \sum x$$

$$\sum XY = A \sum x + B \sum x^2$$

X	y	$Y = \ln(y)$	x^2	$x.Y$
1	5.122	1.6332	1	1.6332
3	3	1.0986	9	3.2958
6	2.48	0.9083	36	5.4498
9	2.34	0.8502	81	7.6518
15	2.18	0.7793	225	11.6895
$\sum x = 34$	$\sum y = 15.12$	$\sum Y = 5.2696$	$\sum x^2 = 352$	$\sum x.y = 29.7201$

$$\text{Slope formula } \beta = \frac{n \sum(XY) - \sum X \sum Y}{n \sum(X^2) - (\sum X)^2}$$

$$\beta = \frac{5(29.7201) - (34)(5.2696)}{5(352) - (34)^2}$$

$$= -0.05061$$

$$\text{Intercept formula} = \frac{(\sum X^2) \sum y - \sum(XY) \sum x}{n \sum(x^2) - (\sum x)^2}$$

$$= \frac{5.2696 - (-0.05061)(34)}{5}$$

$$= 1.3981$$

$$= \ln(x)$$

$$1.3980 = \ln(a)$$

$$a = 4.04709$$

$$y = 4.047 e^{-0.0506x}$$

Q7):

Given equation $\Rightarrow g(x) = a + \frac{\beta}{x}$

We can write as:

$$y = mx + c$$

$$y = a + \frac{1}{x}\beta$$

x	$Y = y$	$X = \frac{1}{x}$	XY	X^2
1	5.12	1	5.12	1
3	3	0.33	1	0.111
6	2.48	0.166	0.4133	0.0277
9	2.34	0.111	0.26	0.0123
12	2.18	0.0666	0.14533	0.0044
	15.12	1.677	6.93866	1.1557

$$\beta = \frac{5(6.93866) - (1.677)(15.12)}{5(1.1557) - (1.677)^2}$$

$$= 3.14828$$

$$a = \frac{(15.12) - (3.14828)(1.677)}{5} = 1.9681$$

Q8)

Given

$$f(x) = \log_4(\cos(x))$$

x	0.5	1	1.5
$f(x)$	-0.09420	-0.44408	-1.91069

Construct a divided difference table as shown below:

x	$f(x)$	First Order	Second Order
0.5	-0.09420		
		-0.69976	
1	-0.44408		-2.23346
		-2.93322	
1.5	-1.91069		

Now, the Newton's divided difference formula is:

$$f(x) = f(x_0) + (x - x_0)f(x_0, x_1) + (x - x_1)f(x_0, x_1, x_2)$$

Here,

$$x_0 = 0.5 \Rightarrow f(x_0) = \log_4(\cos(0.5)) = -0.09420$$

$$x_1 = 1 \Rightarrow f(x_1) = \log_4(\cos(1)) = -0.44408$$

$$x_2 = 1.5 \Rightarrow f(x_2) = \log_4(\cos(1.5)) = -1.191069$$

$$f(x_0, x_1) = \frac{f(x_1) - f(x_0)}{(x_1 - x_0)} = \frac{-0.44408 - (-0.09420)}{(1 - 0.5)} = -0.69976$$

$$f(x_1, x_2) = \frac{f(x_2) - f(x_1)}{(x_2 - x_1)} = \frac{-1.191069 - (-0.44408)}{(1.5 - 1)} = -2.93322$$

$$f(x_0, x_1, x_2) = \frac{f(x_1, x_2) - f(x_0, x_1)}{(x_2 - x_0)} = \frac{-2.93322 - (-0.69976)}{1.5 - 0.5} = -2.23346$$

Thus, for $x = 1.3$

$$\begin{aligned} f(1.3) &= -0.09420 + (1.3 - 0.5)(-0.69976) + (1.3 - 0.5)(1.3 - 1)(-2.23346) \\ &= -0.09420 - 0.55981 - 0.53603 \\ &= -1.19004 \end{aligned}$$

Thus, $f(1.3) = -1.19004$

Q9)

Using langrage's interpolation:

$$f(x) = x^3 \log_2(x)$$

$$x_0 = 2, f(x_0) = 8 \log_2(2) = 8$$

$$x_1 = 3, f(x_1) = 27 \log_2(3) = 42.72$$

$$x_2 = 7, f(x_2) = 343 \log_2(7) = 962.90$$

	x	y
x_0	2	8
x_1	3	42.79399
x_2	7	962.9227

Using larynges, inter pollution formula

$$\begin{aligned} f(x) &= \frac{(x-x_1)(x-x_2)-f(x_0)}{(x_0-x_1)(x_0-x_2)} + \frac{(x-x_0)(x-x_2)-f(x_1)}{(x_1-x_0)(x_1-x_2)} \\ &+ \frac{(x-x_0)(x-x_1)-f(x_2)}{(x_2-x_0)(x_2-x_1)} \\ &= \frac{(x-3)(x-7)}{(2-3)(2-7)} 8 + \frac{(x-2)(x-7)}{(3-2)(3-7)} 42.793 \\ &- \frac{(x-2)(x-3)}{(2-3)(2-7)} 962.9227 \end{aligned}$$

For $x = 5$

$$\begin{aligned} &= \frac{(5-3)(5-7)}{(2-3)(2-7)} 8 + \frac{(5-2)(5-7)}{(3-2)(3-7)} 42.793 \\ &- \frac{(5-2)(5-3)}{(2-3)(2-7)} 962.9227 \end{aligned}$$

$$= -6.4 + 64.1895 + 288.87681$$

$$f(5) = 346.661$$

Q10)

Solution: we choose first 3 points to find velocity approximation that close to 18s.

$$\begin{array}{c|c|c} x/t & 9 & 15 & 20 \\ \hline v & 21 & 32 & 48 \end{array}$$

Using langrage's interpolation

$$v = \frac{(x - x_1)(x - x_2)}{(x_0 - x_1)(x_0 - x_2)} v_0 + \frac{(x - x_0)(x - x_2)}{(x_1 - x_0)(x_1 - x_2)} v_1$$

$$+ \frac{(x - x_0)(x - x_1)}{(x_2 - x_0)(x_2 - x_1)} \times v_2$$

$$= \frac{(x-15)(x-20)}{(9-15)(9-20)} \times 21 + \frac{(x-9)(x-20)}{(15-9)(15-20)} \times 32$$

$$+ \frac{(x - 9)(x - 15)}{(20 - 9)(20 - 15)} \times 48$$

$$= (x^2 - 35x + 300) \times 0.3182 + (x^2 - 29x + 180) \times (-1.0667)$$

$$+ (x^2 - 24x + 135) \times 0.8727$$

$$v = 0.1242x^2 - 1.1485x + 21.2727$$

$$\frac{dv}{dt} = a = 0.1242 \times 2x - 1.1485$$

$$= 0.2484x - 1.1485$$

At $x/t = 18$

$$a = 0.2484 \times 18 - 1.1485$$

$$= \mathbf{3.3227 \frac{m}{s^2}}$$