

CSU33081 Assignment 2

Instructions

- There are 10 Multiple Choice Questions in this assignment.
- Answer **ALL** questions by entering A, B, C, D or E on the **Answer Sheet** provided.
- Upload to Blackboard the filled out Answer Sheet with your **type written solutions as a .docx file**.
- **Submissions without fully worked solutions will receive zero marks.**

Q1.

Consider the following MATLAB program:

```
X=(1~=0)|(2>2)&(7<4)
```

What is the value of X?

- A. 1
- B. False
- C. True
- D. 0
- E. None of these

Q2.

What is approximately the value of r after the following Matlab code is executed?

```
p=[1 8 2];
```

```
r=roots(p);
```

- A. [8 2]
- B. [-4 -4]
- C. [-0.258 -7.742]
- D. $\begin{bmatrix} -0.258 \\ -7.742 \end{bmatrix}$
- E. None of these

Q3.

What is the value of e when the following code is executed?

`a=12/1*15/1; b=a/a*a; c=tand(30)+1/3; d=1+c; e=a-b*c+d`

- A. 0
- B. 1020
- C. 2010
- D. 2020
- E. None of these

Q4.

Apply the Power method to the following matrix and so determine approximately the largest in magnitude eigenvalue and the associated eigenvector.

$$A = \begin{bmatrix} -7 & 13 & -16 \\ 13 & -10 & 13 \\ -16 & 13 & -7 \end{bmatrix}$$

You may use $(1.0 \ -0.8 \ 0.9)^T$ as your initial guess for the eigenvector. You should perform 7 iterations. To a best approximation what is the largest in magnitude eigenvalue and the associated eigenvector? Choose your answer from the following:

- A. -32, $(1.6 \ 0.8 \ 0.9)^T$
- B. 34, $(1.0 \ -0.8 \ -1.0)^T$
- C. -36, $(1.0 \ -1.0 \ 1.0)^T$
- D. 32, $(1.2 \ -0.6 \ 0.1)^T$
- E. None of these

Q5.

Consider the following discrete data:

T_k	0	1	2	3	4	5	6	7
S_k	1.15	2.32	3.32	4.53	5.65	6.97	8.02	9.23

We expect that there is a linear relationship between T and S . That is:

$$S = aT + b; \quad a, b \in \mathbb{R}$$

Find the parameters a and b that give the line of best fit in a least squares sense. a and b are to a nearest approximation:

- A. 2.85379, 1.01676
- B. 1.54632, 1.55387
- C. 1.15630, 1.10167
- D. 2.83019, 1.13452
- E. None of these

Q6.

Given the experimental data:

(1, 5.12), (3, 3), (6, 2.48), (9, 2.34), (15, 2.18)

Find the parameters $\alpha, \beta \in \mathbb{R}$ that best fit the following function to the data in a least squares sense:

$$f(x) = \alpha e^{\beta x}$$

- A. 1.3980, -0.050601
- B. 1.3980, 0.050601
- C. -1.3980, 0.050601
- D. -1.3980, -0.050601
- E. None of these

Q7.

For the data in Q6. above, what are the values of α, β to a best approximation if we fit the following hyperbolic function, in a least square sense, to the data?

$$g(x) = \alpha + \frac{\beta}{x}$$

- A. 1.9681, 3.1468
- B. 3.1468, 1.9681
- C. 3.1468, -1.9681
- D. -3.1468, -1.9681
- E. None of these

Q8.

For the function $f(x) = \log_4(\cos(x))$ and the points $x_0 = 0.5$, $x_1 = 1.0$ and $x_2 = 1.5$ evaluate the Newtonian Divided Difference form of the quadratic interpolating polynomial $P_2(x)$ at the point $x = 1.3$

Choose your answer from the following:

- A. 0.38163
- B. 1.87312
- C. 0.01875
- D. -1.19004
- E. None of these

Q9.

For the function $f(x) = x^3 \log_2(x)$ and the points $x_0 = 2$, $x_1 = 3$ and $x_2 = 7$ evaluate, to a best approximation, the quadratic interpolating polynomial at the point $x = 5$.

- A. 26.67
- B. 42.76
- C. 76.17
- D. 55.81
- E. None of these

Q10. The upward velocity of a body is given as a function of time as:

$t \text{ (s)}$	9	15	20	22
$v \text{ (ms}^{-1}\text{)}$	21	32	48	11

To find the acceleration at $t = 18\text{s}$, a scientist finds a second order interpolating polynomial approximation for the velocity, and then differentiates it to find the acceleration. The estimate of the acceleration in ms^{-2} at $t = 18\text{s}$ is, to a best approximation:

- A. 4.060
- B. 4.200
- C. 8.157
- D. 8.498
- E. None of these

