

# Finite State Verification

CSE 4495 - Lecture 9 - 10/09/2022

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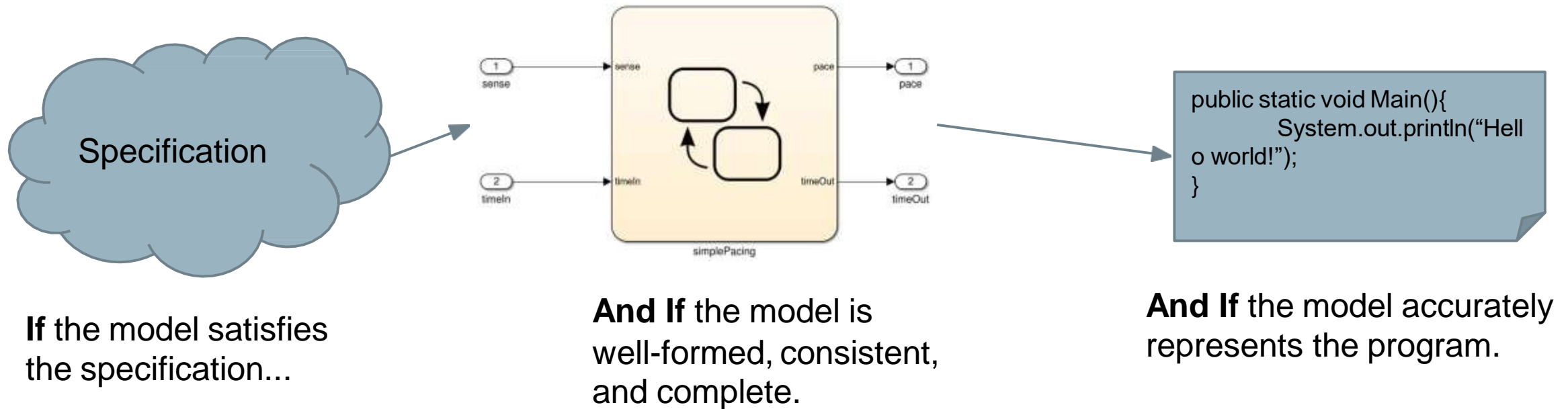
# So, You Want to Perform Verification...

- You have a requirement the program must obey.
- Great! Let's write some tests!
- **Does testing guarantee the requirement is met?**
  - Not quite...
    - Testing can only make a **statistical** argument.

# What About a Model?

- We have previously used models to create tests.
  - Models are simpler than the real program.
  - By abstracting away unnecessary details, we can learn important insights.
- Models can be used to verify full programs.
  - Can see if properties hold exhaustively over a model.

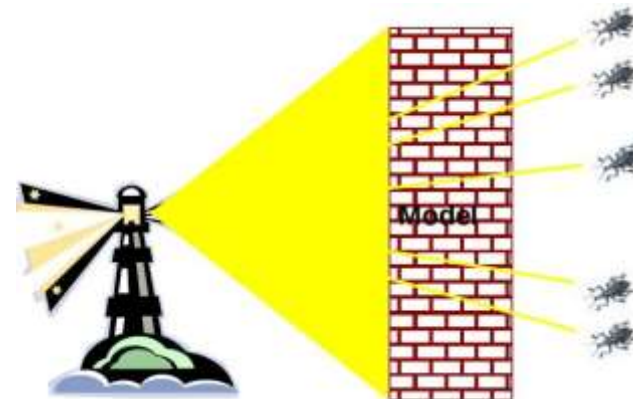
# What Can We Do With This Model?



If we can show that the model satisfies the requirement, then the program should as well.

# Finite State Verification

- Express requirements as Boolean formulae.
- Exhaustively search state space of the model for violations of those properties.
- If the property holds - proof of correctness
- Contrast with testing - no violation might mean bad tests.



# Today's Goals

- Formulating requirements as logical expressions.
  - Introduction to temporal logic.
- Building behavioral models in NuSMV.
- Performing finite-state verification over the model.
  - Exhaustive search algorithms.

# Expressing Requirements in Temporal Logic

# Expressing Properties

- Properties expressed in a formal logic.
  - Temporal logic ensures that properties hold over execution paths, not just at a single point in time.
- Safety Properties
  - System **never** reaches bad state.
  - **Always** in some good state.
    - “If the traffic light is red, it will always turn green within 10 seconds.”
    - “If an emergency vehicle arrives at a red light, it must turn green in the next time step.”



# Expressing Properties

- Liveness Properties
  - **Eventually** useful things happen.
  - **Fairness** criteria.
  - Reason over paths of unknown length.
    - “If the light is red, it must eventually become green.”
    - “If the package is shipped, it must eventually arrive.”
    - “If Player A is taking a turn, Player B must be allowed a turn at some time in the future.”

# Temporal Logic

- Represents propositions qualified over time.
- Linear Time Logic (LTL)
  - Reason about events over a single timeline.
- Computation Tree Logic (CTL)
  - Branching logic that can reason about multiple timelines.
- Each can express properties that the other cannot.

# Linear Time Logic Formulae

Formulae written with boolean predicates, logical operators (and, or, not, implication), and operators:

hunger = “I am hungry”

burger = “I eat a burger”

|                     |                 |  |
|---------------------|-----------------|--|
| <b>X (next)</b>     | X hunger        | In the next state, I will be hungry.   |
| <b>G (globally)</b> | G hunger        | In all future states, I will be hungry.  |
| <b>F (finally)</b>  | F hunger        | Eventually, there will be a state where I am hungry.   |
| <b>U (until)</b>    | hunger U burger | I will be hungry until I start to eat a burger. (hunger does not need to be true once burger becomes true)                                       |
| <b>R (release)</b>  | hunger R burger | I will cease to be hungry after I eat a burger. (hunger and burger are true at the same time for at least one state before hunger becomes false) |

# LTL Examples

- **X (next)** - This operator provides a constraint on the next moment in time.
  - $(\text{sad} \ \&\& \ !\text{rich}) \rightarrow X(\text{sad})$
  - $(\text{hungry} \ \&\& \ \text{haveMoney}) \rightarrow X(\text{orderedPizza})$
- **F (finally)** - At some point in the future, this property will be true.
  - $(\text{funny} \ \&\& \ \text{ownCamera}) \rightarrow F(\text{famous})$
  - $\text{sad} \rightarrow F(\text{happy})$
  - $\text{send} \rightarrow F(\text{receive})$

# LTL Examples

- **G (globally)** - This property must be true forever.
  - `winLottery -> G(rich)`
- **U (until)** - One property must be true until the second becomes true.
  - `startLecture -> (talk U endLecture)`
  - `born -> (alive U dead)`
  - `request -> (!reply U acknowledgement)`

# More LTL Examples

- $G (\text{requested} \rightarrow F (\text{received}))$
- $G (\text{received} \rightarrow X (\text{processed}))$
- $G (\text{processed} \rightarrow F (G (\text{done})))$
- If all three above are true, can this be true?
  - $G (\text{requested} \rightarrow G (!\text{done}))$

requested = action requested  
received = request received  
processed = request processed  
done = action completed

# Computation Tree Logic Formulae

Combines all-path quantifiers with path-specific quantifiers:

|                   |          |  |
|-------------------|----------|--|
| <b>A (all)</b>    | A hunger | Starting from the current state, I must be hungry on <b>all paths</b> .              |
| <b>E (exists)</b> | E hunger | There must be <b>some path</b> , starting from the current state, where I am hungry. |

|                       |                 |   |
|-----------------------|-----------------|---|
| <b>X (next)</b>       | X hunger        | In the next state on this path, I will be hungry.   |
| <b>G (globally)</b>   | G hunger        | In all future states on this path, I will be hungry.  |
| <b>F (finally)</b>    | F hunger        | Eventually on this path, there will be a state where I am hungry.   |
| <b>U (until)</b>      | hunger U burger | On this path, I will be hungry until I start to eat a burger. (I must eventually eat a burger)            |
| <b>W (weak until)</b> | hunger W burger | On this path, I will be hungry until I start to eat a burger. (There is no guarantee that I eat a burger) |

# CTL Examples

**coffee** = "*I like coffee.*" **warm** = "*It is warm.*"

- AG coffee
- EF coffee
- AF (EG coffee)
- EG (AF coffee)
- AG (coffee U warm)
- EF ((EX coffee) U (AG warm))



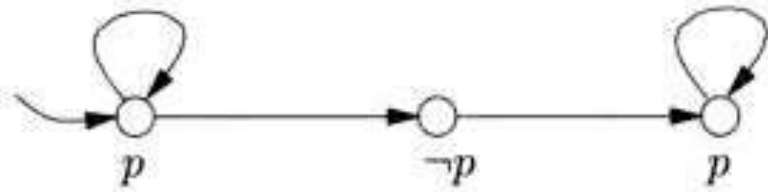
# Examples

- **requested**: a request has been made
- **acknowledged**: request has been acknowledged.
  - CTL: AG (**requested**  $\rightarrow$  AF **acknowledged**)
    - On all paths (A) from an initial state, at every state in the path (G), if **requested** holds true, then ( $\rightarrow$ ) for all paths (A) from that state, eventually (F) at some other state, **acknowledge** holds true.
  - LTL: G (**requested**  $\rightarrow$  F **acknowledged**)
    - On all paths from an initial state, at every state in the path (G), if **requested** holds true, then ( $\rightarrow$ ) eventually (F) at some other state, **acknowledge** holds true.

# Examples

- It is always possible (AG) to reach a state (EF) where we can reset.

- **AG (EF reset)**
- Is LTL formula **G (F reset)** the same expression?



- Eventually (F), the system will reach a state where P will be true forever (G).

- **F (G P)**
- Is CTL formula **AF (AG P)** the same?

# Building Models

# Building Models

- Many different modeling languages.
- Most verification tools use their own language.
- Most map to finite state machines.
  - Define list of variables.
  - Describe how values are calculated.
  - Each “time step”, recalculate values of these variables.
  - State is the current values of all variables.

# Building Models in NuSMV

- NuSMV is a symbolic model checker.
  - Models written in a basic language, represented using Binary Decision Diagrams (BDDs).
    - BDDs translate concrete states into compact summary states.
    - Allows large models to be processed efficiently.
  - Properties may be expressed in CTL or LTL.
  - If a model may be falsified, it provides a concrete counterexample demonstrating how it was falsified.

# A Basic NuSMV Model

MODULE main      Models consist of one or more modules, which execute in parallel.

VAR      The state of the model is the current value of all variables.

request: boolean;

status: {ready, busy};

ASSIGN      Expressions define how the state of each variable can change.

init(status) := ready;

next(status) :=

“request” is set randomly. This represents an environmental factor out of our control.

case

status=ready & request: busy;

status=ready & !request : ready;

TRUE: {ready, busy};

esac;

SPEC AG(request -> AF (status = busy))

Property we wish to prove over the model.

# Checking Properties

- Execute from command line:  
NuSMV <model name>
- Properties that are true are indicated as true.
- If property is false, a counter-example is shown (input violating the property).

```
C19ZRM:bin ggay$ ./NuSMV main.smv
*** This is NuSMV 2.6.0 (compiled on Wed Oct 14 15:32:58 2015)
*** Enabled addons are: compass
*** For more information on NuSMV see <http://nusmv.fbk.eu>
*** or email to <nusmv-users@list.fbk.eu>.
*** Please report bugs to <Please report bugs to <nusmv-users@fbk.eu>>

*** Copyright (c) 2010-2014, Fondazione Bruno Kessler

*** This version of NuSMV is linked to the CUDD library version 2.4.1
*** Copyright (c) 1995-2004, Regents of the University of Colorado

*** This version of NuSMV is linked to the MiniSat SAT solver.
*** See http://minisat.se/MiniSat.html
*** Copyright (c) 2003-2006, Niklas Een, Niklas Sorensson
*** Copyright (c) 2007-2010, Niklas Sorensson

-- specification AG (request -> AF status = busy) is true
```

# Checking Properties

- New property: AG (status = ready)
- (Obviously not true - we set it randomly in the absence of a request)
- Counterexample:
  - In first state, request = false, status = ready.
  - We set status randomly for second state (because request was false). It is set to busy, violating property.

```
-- specification AG status = ready is false
-- as demonstrated by the following execution sequence
Trace Description: CTL Counterexample
Trace Type: Counterexample
-> State: 1.1 <-
    request = FALSE
    status = ready
-> State: 1.2 <-
    status = busy
```



```
MODULE main
```

```
VAR  
  traffic_light: {RED, YELLOW, GREEN}; ped_light:  
  {WAIT, WALK, FLASH}; button: {RESET, SET};
```

```
ASSIGN
```

```
  init(traffic_light) := RED;
```

```
  next(traffic_light) := case
```

```
    traffic_light=RED & button=RESET:
```

```
      GREEN;
```

```
    traffic_light=RED: RED;
```

```
    traffic_light=GREEN & button=SET:  
      {GREEN, YELLOW};
```

```
    traffic_light=GREEN: GREEN;
```

```
    traffic_light=YELLOW:  
      {YELLOW, RED};
```

```
    TRUE: {RED};
```

```
  esac;
```

```
  init(ped_light) := WAIT;
```

```
  next(ped_light) := case
```

```
    ped_light=WAIT &
```

```
      traffic_light=RED: WALK;
```

```
    ped_light=WAIT: WAIT;
```

```
    ped_light=WALK: {WALK, FLASH};
```

```
    ped_light=FLASH: {FLASH, WAIT};
```

```
    TRUE: {WAIT};
```

```
  esac;
```

```
  next(button) := case
```

```
    button=SET & ped_light=WALK: RESET;
```

```
    button=SET: SET;
```

```
    button=RESET & traffic_light=GREEN:  
      {RESET, SET};
```

```
    button=RESET: RESET;
```

```
    TRUE: {RESET};
```

```
  esac;
```

**Let's Take a Break**

- Describe a safety property (something does or does not happen at a specific time) and formulate in CTL.
- Describe a liveness property (something eventually happens) and formulate in LTL.

```
MODULE main
```

```
VAR
```

```
  traffic_light: {RED, YELLOW, GREEN}; ped_light:
  {WAIT, WALK, FLASH};  button: {RESET, SET};
```

```
ASSIGN
```

```
  init(traffic_light) := RED;
```

```
  next(traffic_light) := case
```

```
    traffic_light=RED & button=RESET:
      GREEN;
```

```
    traffic_light=RED: RED;
```

```
    traffic_light=GREEN & button=SET:
      {GREEN, YELLOW};
```

```
    traffic_light=GREEN: GREEN;
```

```
    traffic_light=YELLOW:
      {YELLOW, RED};
```

```
    TRUE: {RED};
```

```
  esac;
```

```
  init(ped_light) := WAIT;
```

```
  next(ped_light) := case
```

```
    ped_light=WAIT &
      traffic_light=RED: WALK;
```

```
    ped_light=WAIT: WAIT;
```

```
    ped_light=WALK: {WALK, FLASH};
```

```
    ped_light=FLASH: {FLASH, WAIT};
```

```
    TRUE: {WAIT};
```

```
  esac;
```

```
  next(button) := case
```

```
    button=SET & ped_light=WALK: RESET;
```

```
    button=SET: SET;
```

```
    button=RESET & traffic_light=GREEN:
      {RESET, SET};
```

```
    button=RESET: RESET;
```

```
    TRUE: {RESET};
```

```
  esac;
```

# Activity - Potential Solutions

- Safety Property
  - A bad thing never happens, or a good thing happens at a specific time.
- AG (pedestrian\_light = walk -> traffic\_light != green)
  - The pedestrian light cannot indicate that I should walk when the traffic light is green.
  - This is a safety property. We are saying that this should NEVER happen.

# Activity - Potential Solutions

- Liveness Property
  - **Eventually** useful things happen.
- $G (\text{traffic\_light} = \text{RED} \ \& \ \text{button} = \text{RESET} \rightarrow F (\text{traffic\_light} = \text{green}))$ 
  - If the light is red, and the button is reset, then eventually, the light will turn green.
  - This is a liveness property, as we assert that something will eventually happen.

# Proving Properties Over Models

# Proving Properties

- Search state space for property violations.
- Violations give us counter-examples
  - Path that demonstrates the violation.
  - (useful test case)
- Implications of counter-example:
  - Property is incorrect.
  - Model does not reflect expected behavior.
  - Real issue found in the system being designed.

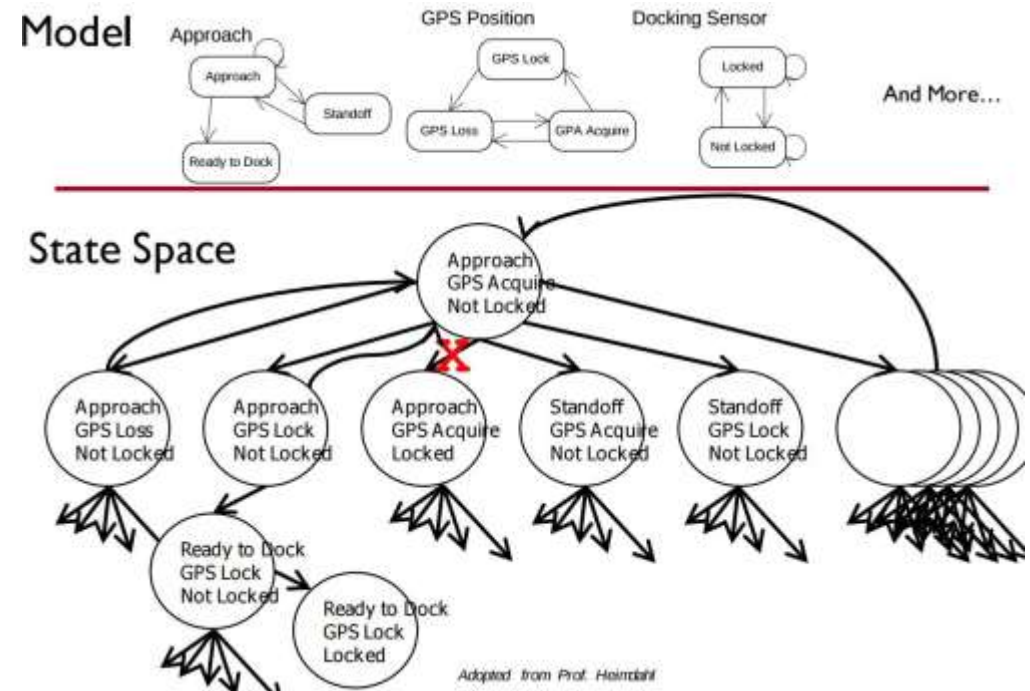
# Test Generation from FS Verification

- We can also take properties and **negate** them.
  - Called a “trap property” - we assert that a property can never be met.
- Shows one way the property can be met.
- Can be used as a test for the real system.
  - Demonstrate that final system meets specification.



# Exhaustive Search

- Algorithms examine all execution paths through the state space.
- Major limitation - state space explosion.
  - Limit number of variables and possible values to control state space size.



# Search Based on SAT

- Express properties in **conjunctive normal form**:
  - $f = (!x_2 \vee x_5) \wedge (x_1 \vee !x_3 \vee x_4) \wedge (x_4 \vee !x_5) \wedge (x_1 \vee x_2)$
- Examine reachable states and choose a transition based on how it affects the CNF expression.
  - If we want  $x_2$  to be false, choose a transition that imposes that change.
- Continue until CNF expression is satisfied.

# Boolean Satisfiability (SAT)

- Find assignments to Boolean variables  $X_1, X_2, \dots, X_n$  that results in expression  $\varphi$  evaluating to true.
- Defined over expressions written in **conjunctive normal form**.
  - $\varphi = (X_1 \vee \neg X_2) \wedge (\neg X_1 \vee X_2)$
  - $(X_1 \vee \neg X_2)$  is a **clause**, made of variables,  $\neg$ ,  $\vee$
  - Clauses are joined with  $\wedge$

# Boolean Satisfiability

- Find assignment to  $X_1, X_2, X_3, X_4, X_5$  to solve
  - $(\neg X_2 \vee X_5) \wedge (X_1 \vee \neg X_3 \vee X_4) \wedge (X_4 \vee \neg X_5) \wedge (X_1 \vee X_2)$
- One solution: 1, 0, 1, 1, 1
  - $(\neg X_2 \vee X_5) \wedge (X_1 \vee \neg X_3 \vee X_4) \wedge (X_4 \vee \neg X_5) \wedge (X_1 \vee X_2)$
  - $(\neg 0 \vee 1) \wedge (1 \vee \neg 1 \vee 1) \wedge (1 \vee \neg 1) \wedge (1 \vee 0)$
  - $(1) \wedge (1) \wedge (1) \wedge (1)$
  - 1

# Branch & Bound Algorithm

- Set variable to true or false.
- Apply that value.
- Does value satisfy the clauses that it appears in?
  - If so, assign a value to the next variable.
  - If not, backtrack (bound) and apply the other value.
- Prunes branches of the boolean decision tree as values are applied.

# Branch & Bound Algorithm

$$\varphi = (\neg x_2 \vee x_5) \wedge (x_1 \vee \neg x_3 \vee x_4) \wedge (x_4 \vee \neg x_5) \wedge (x_1 \vee x_2)$$

**1. Set  $x_1$  to false.**

$$\varphi = (\neg x_2 \vee x_5) \wedge (0 \vee \neg x_3 \vee x_4) \wedge (x_4 \vee \neg x_5) \wedge (0 \vee x_2)$$

**2. Set  $x_2$  to false.**

$$\varphi = (1 \vee x_5) \wedge (0 \vee \neg x_3 \vee x_4) \wedge (x_4 \vee \neg x_5) \wedge (0 \vee 0)$$

**3. Backtrack and set  $x_2$  to true.**

$$\varphi = (0 \vee x_5) \wedge (0 \vee \neg x_3 \vee x_4) \wedge (x_4 \vee \neg x_5) \wedge (0 \vee 1)$$

# DPLL Algorithm

- Set a variable to true/false.
  - Apply that value to the expression.
  - Remove all satisfied clauses.
  - If assignment does not satisfy a clause, then remove that variable from that clause.
  - If this leaves any **unit clauses** (single variable clauses), assign a value that removes those next.
- Repeat until a solution is found.

# DPLL Algorithm

$$\varphi = (\neg x_2 \vee x_5) \wedge (x_1 \vee \neg x_3 \vee x_4) \wedge (x_4 \vee \neg x_5) \wedge (x_1 \vee x_2)$$

1. Set  $x_2$  to false.

$$\varphi = (\neg \mathbf{0} \vee x_5) \wedge (x_1 \vee \neg x_3 \vee x_4) \wedge (x_4 \vee \neg x_5) \wedge (x_1 \vee \mathbf{0})$$

$$\varphi = (x_1 \vee \neg x_3 \vee x_4) \wedge (x_4 \vee \neg x_5) \wedge (x_1)$$

2. Set  $x_1$  to true.

$$\varphi = (\mathbf{1} \vee \neg x_3 \vee x_4) \wedge (x_4 \vee \neg x_5) \wedge (\mathbf{1})$$

$$\varphi = (x_4 \vee \neg x_5)$$

3. Set  $x_4$  to false, then  $x_5$  to false.

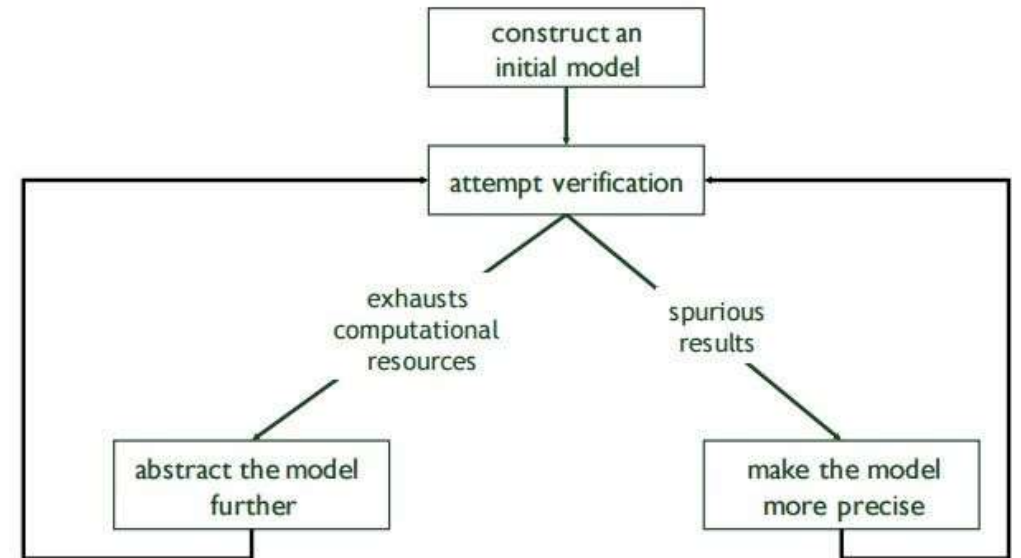
$$\varphi = (\mathbf{0} \vee \neg x_5)$$

$$\varphi = (\neg \mathbf{0})$$



# Model Refinement

- Must balance precision with efficiency.
  - Models that are too simple introduce failure paths that may not be in the real system.
  - Complex models may be infeasible due to resource exhaustion.



# Who Uses This Stuff?

- Used heavily in **safety-critical** development.
  - Verifies certain complex, critical functions.
  - Used extensively in automotive, aerospace, medical development domains.
- Used to verify security policies, stateful behaviors.
  - Uses at Amazon Web Services to verify cloud security.
- Not used for all functionality.
  - Time-consuming, requires additional effort.

# We Have Learned

- We can perform verification by creating models of function behavior and proving that the requirements hold over the model.
  - To do so, express requirements as logical formulae written in a temporal logic.
  - Finite state verification exhaustively searches the state space for violations of properties.
  - Presents counter-examples showing properties are violated.

# We Have Learned

- By performing this process, we can gain confidence that the system will meet the specifications.
- Can also generate test cases to demonstrate that properties hold over the final system.
  - Negate a property, the counter-example shows that the property can be met.
  - Execute the input from the counter-example on the real system - should give the same result!

# Next Time

- Exercise Session: Finite-State Verification

**Thank You**