Following examples showing graphical methods to find different locations of Quartiles, Deciles and Percentiles with appropriate data values.

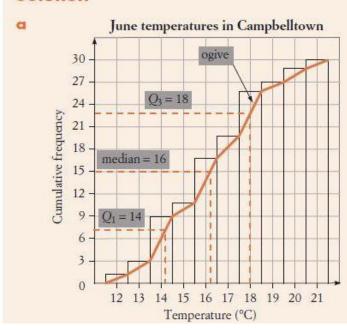
EXAMPLE 14

The maximum daily temperatures (in °C) in Campbelltown in June were recorded and grouped into the frequency table shown.

- Draw a cumulative frequency histogram and polygon for the data.
- Use the frequency polygon to find the median and calculate the interquartile range.

| Temperature (°C) | Frequency | Cumulative frequency |
|------------------|-----------|----------------------|
| 12 | 1 | 1 |
| 13 | 2 | 3 |
| 14 | 6 | 9 |
| 15 | 2 | 11 |
| 16 | 6 | 17 |
| 17 | 3 | 20 |
| 18 | 6 | 26 |
| 19 | 1 | 27 |
| 20 | 2 | 29 |
| 21 | 1 | 30 |

Solution



The ogive (polygon) is always inside the columns.

b Draw a horizontal line from the halfway mark (15) on the cumulative frequency axis to where it meets the ogive. The median is the corresponding value on the 'Temperature' axis.

Median = 16

To find Q_1 , draw a horizontal line from the quarter mark $(\frac{1}{4} \times 30 = 7.5)$ on the cumulative frequency axis to where it meets the ogive, then read the temperature value.

$$Q_1 = 14$$

To find Q_3 , draw a horizontal line from the three-quarter mark $(\frac{3}{4} \times 30 = 22.5)$ on the cumulative frequency axis.

$$Q_3 = 18$$

Interquartile range = $Q_3 - Q_1$ = 18 - 14= 4

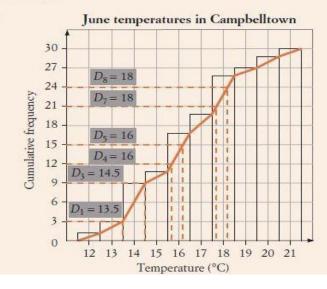
EXAMPLE 15

Use the cumulative frequency graph from Example 14 to answer the following questions.

- g Find:
 - i the 4th decile, D_4
 - ii the 7th decile, D_7 .
- b What value cuts off the top 20% of temperatures?
- Between which two deciles would you find a temperature of 14°C?

Solution

-



The deciles are marked at intervals of three units on the cumulative frequency axis.

- $D_4 = 16$
- $D_7 = 18$
- **b** D_8 cuts off the top 20% of temperatures, so the value is 18.
- Between D_1 and D_3 .

EXAMPLE 16

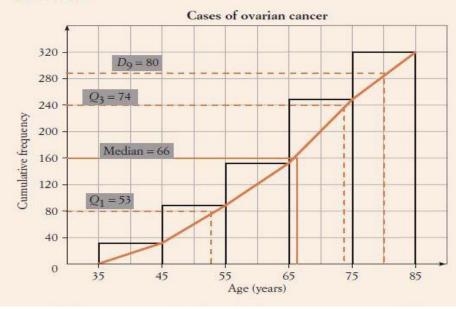
The number of cases of ovarian cancer in women from various age groups is shown below.

| Age (years) | Class centre | Frequency | Cumulative frequency |
|----------------|--------------|-----------|----------------------|
| 35-<45 | 40 | 28 | 28 |
| 45-<55 | 50 | 61 | 89 |
| 55-<65 | 60 | 65 | 154 |
| 65-<75 | 70 | 92 | 246 |
| 75-<85 | 80 | 74 | 320 |

Draw an ogive for this data and use it to find an estimate for:

- a the median
- b the 3rd quartile
- the 9th decile
- d the interquartile range.

Solution



All these values are estimates because the

- Halfway point on the 'Cumulative frequency' axis = 160 data has into class
 - data has been grouped into class intervals.
- b The three-quarter point on the 'Cumulative frequency' axis = $\frac{3}{4}$ × 320 = 240 $Q_3 \approx 74$
- \circ 90% point on the 'Cumulative frequency' axis = 0.9×320

$$= 288$$

$$D_9 \approx 80$$

d Quarter point on the 'Cumulative frequency' axis = $\frac{1}{4} \times 320$

$$= 80$$

$$Q_1 \approx 53$$

Interquartile range =
$$Q_3 - Q_1 = 74 - 53$$

$$= 21$$

