



United International University

School of Science and Engineering

Final Assessment Trimester: Fall-2020

Course Title: Probability and Statistics

Course Code: Stat 205 Marks: 25 Time: 1 Hour 15 Mins

There are 3 questions. Answer question no. 1 and any one from 2 and 3.

1. a) Consider the following frequency distribution table.

[10]

Class	61-65	66-70	71-75	76-80
Frequency	9	13	21	7

- (i) **Sketch** the cumulative frequency polygon and find the median from it.
 (ii) **Find** mode and mean-deviation from mode.
 (iii) **Find** the first four raw moments about $A = 75$; **convert** them to the central moments. Also, **find** the co-efficient of skewness and kurtosis. **Make comments** about the distribution.

$$m_2 = m'_2 - m'_1{}^2; \quad m_3 = m'_3 - 3m'_2m'_1 + 2m'_1{}^3;$$

$$m_4 = m'_4 - 4m'_3m'_1 + 6m'_2m'_1{}^2 - 3m'_1{}^4$$

- b) If the correlation coefficient of two variables is **0.5** and regression coefficient of x on y is **0.8**. Also, $\bar{x} = 31.5$ and $\bar{y} = 42.75$. **Find** and **sketch** the regression line of y on x . **Predict** the value of y when x is **40** and **verify** it graphically. [5]

2. a) Let $Y_1 < Y_2 < Y_3 < Y_4$ be the order statistics of four independent observations X_1, X_2, X_3, X_4 each from the distribution with pdf $f(x) = \frac{1}{4}x^3; 0 < x < 2$. **Find** $P\left(Y_3 \leq \frac{3}{2}\right)$ and the pdf of the order statistics. Also, **find** $\mu_3(y)$. [4]

$$G_r(y) = \sum_{k=r}^n \binom{n}{k} [F(y)]^k [1 - F(y)]^{n-k}$$

$$g_r(y) = \frac{n!}{(n-r)!(r-1)!} [F(y)]^{r-1} [1 - F(y)]^{n-r} f(y)$$

- b) Let X equal the daily sell of foods in **kg** by the super shops. Suppose the variance of X is **25 kg**. To estimate the mean μ of X , an agency took a random sample of **15** super shops and found they sold in a total of **750 kg** of foods in a day. **Find** an approximate **80%** confidence interval for μ . [2.5]

- c) The breaking strengths of cables produced by a manufacturer have a mean of **2500** pounds and standard deviation of **100** pounds. By a new technique in the manufacturing process, it is claimed that the breaking strength can be increased. To test the claim, a sample of **100** cables is tested and it is found that the mean breaking strength is **2575** pounds. Construct a hypothesis test. Can we support the claim at the **0.1** significance level? [3.5]
3. a) Consider **1009, 999, 1013, 998, 1001, 995, 1011, 1005, 993 & 1003** grams are the weights of soap in a “**1000-gram**” bottle, defined by the random variable **X** . Order them increasingly and find the **mode, median, D_9 , and P_{45}** . [4]
- b) In a forest **100** crocodiles are infected by viral disease, **half** of the crocodiles are brought to a zoo. If **30** of the crocodiles survived in the zoo, **find** the confidence interval of the proportion with **10%** significance level. Is the transfer process effective? [2.5]
- c) **ABC** company produces machineries with the average lifetime is **30** years and the standard deviation **5** years. It is claimed that, in a new process the mean life time can be increased. [3.5]
- (i) If the estimated average life time for **40** samples is **31.5** years, find the **p** –value of the claim of the producer.
 - (ii) If the new process has increase the mean life time to **32** years. Find **α** and **β** for the estimated mean **31.25** years for **35** samples.

STANDARD NORMAL DISTRIBUTION: Table Values Represent AREA to the LEFT of the Z score.

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.9	.00005	.00005	.00004	.00004	.00004	.00004	.00004	.00004	.00003	.00003
-3.8	.00007	.00007	.00007	.00006	.00006	.00006	.00006	.00005	.00005	.00005
-3.7	.00011	.00010	.00010	.00010	.00009	.00009	.00008	.00008	.00008	.00008
-3.6	.00016	.00015	.00015	.00014	.00014	.00013	.00013	.00012	.00012	.00011
-3.5	.00023	.00022	.00022	.00021	.00020	.00019	.00019	.00018	.00017	.00017
-3.4	.00034	.00032	.00031	.00030	.00029	.00028	.00027	.00026	.00025	.00024
-3.3	.00048	.00047	.00045	.00043	.00042	.00040	.00039	.00038	.00036	.00035
-3.2	.00069	.00066	.00064	.00062	.00060	.00058	.00056	.00054	.00052	.00050
-3.1	.00097	.00094	.00090	.00087	.00084	.00082	.00079	.00076	.00074	.00071
-3.0	.00135	.00131	.00126	.00122	.00118	.00114	.00111	.00107	.00104	.00100
-2.9	.00187	.00181	.00175	.00169	.00164	.00159	.00154	.00149	.00144	.00139
-2.8	.00256	.00248	.00240	.00233	.00226	.00219	.00212	.00205	.00199	.00193
-2.7	.00347	.00336	.00326	.00317	.00307	.00298	.00289	.00280	.00272	.00264
-2.6	.00466	.00453	.00440	.00427	.00415	.00402	.00391	.00379	.00368	.00357
-2.5	.00621	.00604	.00587	.00570	.00554	.00539	.00523	.00508	.00494	.00480
-2.4	.00820	.00798	.00776	.00755	.00734	.00714	.00695	.00676	.00657	.00639
-2.3	.01072	.01044	.01017	.00990	.00964	.00939	.00914	.00889	.00866	.00842
-2.2	.01390	.01355	.01321	.01287	.01255	.01222	.01191	.01160	.01130	.01101
-2.1	.01786	.01743	.01700	.01659	.01618	.01578	.01539	.01500	.01463	.01426
-2.0	.02275	.02222	.02169	.02118	.02068	.02018	.01970	.01923	.01876	.01831
-1.9	.02872	.02807	.02743	.02680	.02619	.02559	.02500	.02442	.02385	.02330
-1.8	.03593	.03515	.03438	.03362	.03288	.03216	.03144	.03074	.03005	.02938
-1.7	.04457	.04363	.04272	.04182	.04093	.04006	.03920	.03836	.03754	.03673
-1.6	.05480	.05370	.05262	.05155	.05050	.04947	.04846	.04746	.04648	.04551
-1.5	.06681	.06552	.06426	.06301	.06178	.06057	.05938	.05821	.05705	.05592
-1.4	.08076	.07927	.07780	.07636	.07493	.07353	.07215	.07078	.06944	.06811
-1.3	.09680	.09510	.09342	.09176	.09012	.08851	.08691	.08534	.08379	.08226
-1.2	.11507	.11314	.11123	.10935	.10749	.10565	.10383	.10204	.10027	.09853
-1.1	.13567	.13350	.13136	.12924	.12714	.12507	.12302	.12100	.11900	.11702
-1.0	.15866	.15625	.15386	.15151	.14917	.14686	.14457	.14231	.14007	.13786
-0.9	.18406	.18141	.17879	.17619	.17361	.17106	.16853	.16602	.16354	.16109
-0.8	.21186	.20897	.20611	.20327	.20045	.19766	.19489	.19215	.18943	.18673
-0.7	.24196	.23885	.23576	.23270	.22965	.22663	.22363	.22065	.21770	.21476
-0.6	.27425	.27093	.26763	.26435	.26109	.25785	.25463	.25143	.24825	.24510
-0.5	.30854	.30503	.30153	.29806	.29460	.29116	.28774	.28434	.28096	.27760
-0.4	.34458	.34090	.33724	.33360	.32997	.32636	.32276	.31918	.31561	.31207
-0.3	.38209	.37828	.37448	.37070	.36693	.36317	.35942	.35569	.35197	.34827
-0.2	.42074	.41683	.41294	.40905	.40517	.40129	.39743	.39358	.38974	.38591
-0.1	.46017	.45620	.45224	.44828	.44433	.44038	.43644	.43251	.42858	.42465
-0.0	.50000	.49601	.49202	.48803	.48405	.48006	.47608	.47210	.46812	.46414

