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তারিখ :

Qnn : 2

$$y_{1,2} = A \cos\left(\frac{2}{3} kx \pm \omega t\right)$$

$$y_1 = A \cos\left(\frac{2}{3} kx - \omega t\right) \quad \text{--- (1)}$$

$$y_2 = A \cos\left(\frac{2}{3} kx + \omega t\right) \quad \text{--- (2)}$$

$k \rightarrow$ wave number

$\omega \rightarrow$ angular frequency.

$$y = y_1 + y_2$$

$$= A \cos\left(\frac{2}{3} kx - \omega t\right) + A \cos\left(\frac{2}{3} kx + \omega t\right)$$

$$= A \left[\cos\left(\frac{2}{3} kx - \omega t\right) + \cos\left(\frac{2}{3} kx + \omega t\right) \right] \quad \text{--- (3)}$$

Again

$$\cos A + \cos B = 2 \cos\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right)$$

From eqn 3

$$y = A \cdot 2 \cos \left(\frac{\frac{2}{3} kx - \omega t + \frac{2}{3} kx + \omega t}{2} \right)$$

$$\cos \left(\frac{\frac{2}{3} kx - \omega t - \frac{2}{3} kx + \omega t}{2} \right)$$

$$= 2A \cos \frac{\frac{4}{3} kx}{2} \cos \left(\frac{-\omega t}{2} \right)$$

$$= 2A \cos \frac{2}{3} kx \cos \omega t$$

$$y = A_0 \cos \omega t$$

$A_0 \rightarrow$ resultant amplitude

$$A_0 = 2A \cos \frac{2}{3} kx$$

P.T.O

Node point: (for minimum amplitude displacement)

$$\cos \frac{2}{3} kx = 0$$

$$\textcircled{a} \frac{2}{3} \cos kx = \cos(0) \quad A \sin =$$

$$\frac{2}{3} kx = 1 \quad A \sin =$$

$$kx = \frac{3}{2} \quad A \sin =$$

$$\textcircled{b} \frac{2}{3} kx = \pi \quad A \sin =$$

$$kx = \frac{3\pi}{2} \quad A \sin =$$

Nodes are separated by $\frac{\lambda}{2}$

and

Antinode point:

$$\cos \frac{2}{3} kn = \pm 1 \quad \text{--- Harmonic = 1}$$

$$\frac{2}{3} \cos \left(\frac{kn}{2} \right) = \cos \left(\frac{\pi}{2} \right)$$

$$\therefore \frac{2}{3} \left(\frac{kn}{2} \right) = \frac{\pi}{2} \quad \text{--- (1)}$$

$$kn = \frac{3\pi}{4}$$

$$= (2n+1) \frac{3\pi}{4}$$

$$n = \frac{(2n+1) \frac{3\pi}{4}}{k}$$

$$= \frac{(2n+1) \frac{3\pi}{4}}{\frac{2\pi}{\lambda}}$$

$$= 2n+1 \cdot \frac{3\pi}{4} \times \frac{\lambda}{2\pi}$$

$$= (2n+1) \frac{\lambda}{4}$$

$\therefore n =$

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$$n = \frac{2n+1}{2} \times \frac{\lambda}{2}$$

$$n = \frac{2n+1}{2} \times \frac{\lambda}{2}$$

$$\therefore n = n + \frac{1}{2}$$

$$n = \left(n + \frac{1}{2}\right) \times \frac{\lambda}{2}$$

Antinodes are separated by $\frac{\lambda}{2}$

Ans:

Qn 4

$$R = 20 \Omega$$

$$L = 10 \text{ mH} = 10 \times 10^{-3} = 0.01 \text{ H}$$

$$\text{voltage amplitude} = 169.7 \text{ V.}$$

1) ~~Resonant frequency~~
resonance.

$$I = \frac{V_m}{R}$$

$$= \frac{169.7}{20}$$

$$= 8.485 \text{ A}$$

$$\omega_0 = 15 \text{ kHz} = \frac{2\pi f}{1}$$

$$= 15000 \text{ Hz}$$

ii) The bandwidth $\Delta \omega = \omega_2 - \omega_1$

$$B = \frac{R}{L} \quad \omega_0 = \frac{1}{\sqrt{LC}}$$

$$= \frac{20}{1} \quad \sqrt{LC} = \frac{1}{\omega_0}$$

$$= 20 \text{ krad/s} \quad LC = \frac{1}{\omega_0^2}$$

$$C = \frac{1}{L \omega_0^2}$$

The quality factor

$$Q = \frac{\omega_0}{B}$$

$$= \frac{15000}{20} = 750$$

$$\omega_0 = 8.165 \times 10^3$$

$$\text{iii) } \omega_1 = -\frac{R}{2L} + \sqrt{\left(\frac{R}{2L}\right)^2 + \frac{1}{LC}}$$

$$= -\frac{20}{2} + \sqrt{\left(\frac{20}{2}\right)^2 + \frac{1}{8.165 \times 10^{-3}}}$$

$$= -10 + \sqrt{100 + 1.225 \times 10^4}$$

$$= 6.125 \times 10^{-6} \text{ krad/s}$$

$$\omega_2 = 10 + \sqrt{100 + 1.225 \times 10^{-4}} \quad (ii)$$

$$= 20 \text{ krad/s} = 4$$

$$\omega_1 = 3.7 \quad \text{Ans}$$

$$(iv) \quad \omega = \omega_0$$

$$I = \frac{V_m}{R} = \frac{169.7}{20}$$

$$= 8.485 \text{ A}$$

At.

$$\omega = \omega_1, \omega_2$$

$$I = \frac{V_m}{\sqrt{2} R}$$

$$169.7$$

$$\sqrt{2} \cdot 20$$

$$= 11.999 \text{ A}$$

Ans

Qnn 3

$$y = 10 \sin 0.79 \frac{\pi}{3} (3600t + 18\pi)$$

$$y = A \sin \frac{2\pi}{\lambda} (\omega t + \pi)$$

$$y = 10 \sin 0.79 \frac{\pi}{3} \times 18 \left(\frac{3600}{18} t + \pi \right)$$

$$y = 10 \sin \frac{19}{100} \times \frac{\pi}{3} \times 18 (2000t + \pi)$$

$$= 10 \sin \frac{2\pi}{0.422} (-2000t + \pi)$$

i) $A = 10 \text{ m}$

ii) $v = 2000 \text{ ms}^{-1}$

iii) $\frac{2\pi}{\lambda} = 14.9$

~~20~~
 $\lambda = 0.422 \text{ m}$

$$iv) v = \lambda f$$

$$\frac{v}{\lambda} = f$$

$$f = \frac{2000}{0.422}$$

$$f = 4739.34 \text{ Hz}$$

$$v) T = \frac{1}{f}$$

$$= \frac{1}{4739.34}$$

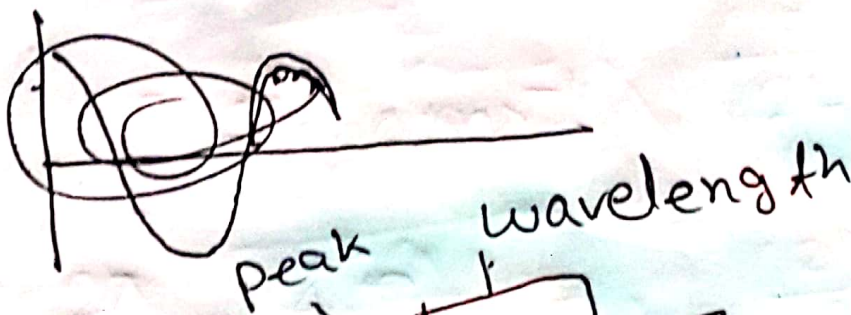
$$= 2.11 \times 10^{-4} \text{ s}$$

Qnn: 1

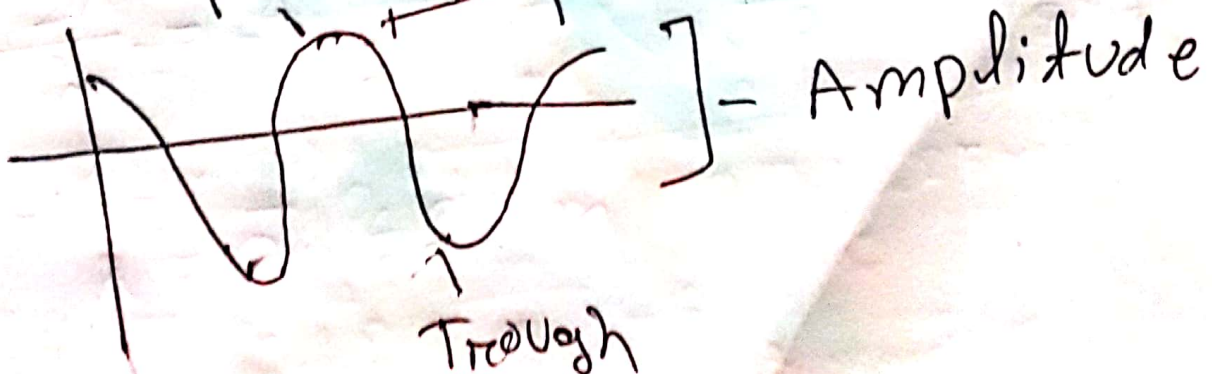
A wave which generally travels continuously in a medium of the same direction without the change in its amplitude is known as **progressive wave**

$$y = A \cos(\omega t - kx)$$

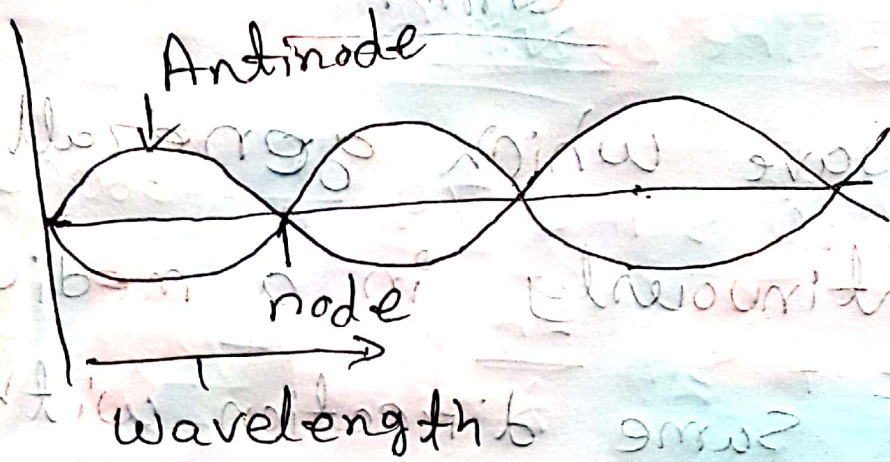
i)



ii



iii)



$$A = \mu$$

$$y = A \sin(kx - \omega t)$$

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