NLP: N-Grams

Dan Garrette dhg@cs.utexas.edu

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1 Language Modeling Tasks

- Language idenfication / Authorship identification
- Machine Translation
- Speech recognition
- Optical character recognition (OCR)
- Context-sensitive spelling correction
- Predictive text (text messaging clients, search engines, etc)
- Generating spam
- Code-breaking (e.g. decipherment)

2 Kinds of Language Models

- Bag of words
- Sequences of words
- Sequences of tagged words
- Grammars
- Topic models

3 Language as a sequence of words

- What is the probability of seeing a particular sequence of words?
- Simplified model of language: words in order
- p(some words in sequence)

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p("an interesting story")?
p("a interesting story")?
p("a story interesting")?
p(next | some sequence of previous words)
p("austin" | "university of texas at")?
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-p("dallas" | "university of texas at") ? -p("giraffe" | "university of texas at") ?

Use as a language model

- Language ID: This sequence is most likely to be seen in what language?
- Authorship ID: What is the most likely person to have produced this sequence of words?
- Machine Translation: Which sentence (word choices, ordering) seems most like the target language?
- Text Prediction: What's the most likely next word in the sequence

Notation

- Probability of a sequence is a joint probability of words
- But the order of the words matters, so each gets its own feature
- $p(\text{"an interesting story"}) = p(w_1 = an, w_2 = interesting, w_3 = story)$
- $p(\text{"austin"} \mid \text{"university of texas at"})$ = $p(w_0 = austin \mid w_{-4} = university, w_{-3} = of, w_{-2} = texas, w_{-1} = at)$
- So w_0 means "current word" and w_{-1} is "the previous word".
- We will typically use the short-hand

4 Counting Words

- Terminology:
 - **Type:** Distinct word

Token: Particular occurrence of a word

- "the man saw the saw": 3 types, 5 tokens

What is a word? What do we count?

• Punctuation? Separate from neighboring words? Keep it at all?

- Stopwords?
- Lowercase everything?
- Distinct numbers vs. $\langle number \rangle$
- Hyphenated words?
- Lemmas only?
- Disfluencies? (um, uh)

5 Estimating Sequence Probabilities

- To build a statistical model, we need to set parameters.
- Our parameters: probabilities of various sequences of text
- Maximum Likelihood Estimate (MLE): of all the sequences of length N, what proportion are the relevant sequence?
- p(university of texas at austin)= $p(w_1 = \text{university}, w_2 = \text{of}, w_3 = \text{texas}, w_4 = \text{at}, w_5 = \text{austin})$ = $\frac{C(\text{"university of texas at austin"})}{C(\text{all 5-word sequences})} = \frac{3}{25,000,000}$
- $p(a \text{ bank}) = \frac{C(\text{``a bank''})}{C(\text{all 2-word sequences})} = \frac{609}{50,000,000}$
- $p(\text{in the}) = \frac{C(\text{"in the"})}{C(\text{all 2-word sequences})} = \frac{312,776}{50,000,000}$
- Long sequences are unlikely to have any counts: $p(\text{the university of texas football team started the season off right by scoring a touchdown in the final seconds of play to secure a stunning victory over the out-of-town challengers) = <math>\frac{C(\dots \text{ that sentence } \dots)}{C(\text{all } 30\text{-word sequences})} = \mathbf{0.0}$
- Even shorter sentences may not have counts, even if they make sense, are perfectly grammatical, and not improbable that someone might say them:
 - "university of texas in amarillo"
- We need a way of estimating the probability of a long sequence, even though counts will be low.

Make a "naïve" assumption?

- With naïve Bayes, we dealt with this problem by assuming that all features were independent.
- $p(w_1 = university, w_2 = of, w_3 = texas, w_4 = in, w_5 = amarillo) = p(w = university) \cdot p(w = of) \cdot p(w = texas) \cdot p(w = in) \cdot p(w = amarillo)$

- But this loses the difference between "university of texas in amarillo", which seems likely, and "university texas amarillo in of", which does not
- This amounts to a "bag of words" model

Use Chain Rule?

- Long sequences are sparse, short sequences are less so
- Break down long sequences using the chain rule
- $p(university \ of \ texas \ in \ amarillo) = p(university) \cdot p(of \mid university) \cdot p(texas \mid university \ of) \cdot p(in \mid university \ of \ texas) \cdot p(amarillo \mid university \ of \ texas \ in)$
- "p(seeing 'university') times p(seeing 'of' given that the previous word was 'university') times p(seeing 'texas' given that the previous two words were 'university of') ..."
- $p(\text{university}) = \frac{C(\text{university})}{\sum_x C(x)} = \frac{C(\text{university})}{C(all\ words)};$ easy to estimate $p(\text{of} \mid \text{university}) = \frac{C(\text{university of})}{\sum_w C(\text{university }x)} = \frac{C(\text{university of})}{C(\text{university of})};$ easy to estimate $p(\text{texas} \mid \text{university of}) = \frac{C(\text{university of texas})}{\sum_w C(\text{university of texas})} = \frac{C(\text{university of texas})}{C(\text{university of texas in})};$ easy to estimate $p(\text{in} \mid \text{university of texas}) = \frac{C(\text{university of texas in})}{\sum_w C(\text{university of texas in})} = \frac{C(\text{university of texas in})}{C(\text{university of texas in amarillo})};$ easy to estimate $p(\text{amarillo} \mid \text{university of texas in}) = \frac{C(\text{university of texas in amarillo})}{\sum_w C(\text{university of texas in amarillo})} = \frac{C(\text{university of texas in amarillo})}{C(\text{university of texas in amarillo})};$ same problem
- So this doesn't help us at all.

6 N-Grams

- We don't necessarily want a "fully naïve" solution
 - Partial independence: limit how far back we look
- "Markov assumption": future behavior depends only on recent history
 - $-k^{th}$ -order Markov model: depend only on k most recent states
- **n-gram**: sequence of n words
- n-gram model: statistical model of word sequences using n-grams.
- p(university of texas in amarillo)
 - 5+ -gram: $p(university) \cdot p(of \mid university) \cdot p(texas \mid university \mid of) \cdot p(in \mid university \mid of \mid texas)$ $\cdot p(amarillo \mid university \mid of \mid texas \mid in)$
 - 3-gram (trigram): $p(university) \cdot p(of \mid university) \cdot p(texas \mid university \ of) \cdot p(in \mid of \ texas) \cdot p(amarillo \mid texas \ in)$

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- 2-gram (bigram): p(university) \cdot p(of \mid university) \cdot p(texas \mid of) \cdot p(in \mid texas) \cdot p(amarillo \mid in)
- 1-gram (unigram) / bag-of-words model / full independence: p(university) \cdot p(of) \cdot p(texas) \cdot p(in) \cdot p(amarillo)
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- Idea: reduce necessary probabilities to an estimatble size.
- Estimating trigrams:

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\begin{split} &p(\text{university}) \cdot p(\text{of} \mid \text{university}) \cdot p(\text{texas} \mid \text{university of}) \cdot p(\text{in} \mid \text{of texas}) \\ & \cdot p(\text{amarillo} \mid \text{texas in}) \end{split} &= \frac{C(\text{university})}{\sum_{x} C(x)} \cdot \frac{C(\text{university of})}{\sum_{x} C(\text{university of})} \cdot \frac{C(\text{university of texas})}{\sum_{x} C(\text{university of } x)} \cdot \frac{C(\text{of texas in})}{\sum_{x} C(\text{of texas in})} \cdot \frac{C(\text{texas in amarillio})}{\sum_{x} C(\text{texas in } x)} \\ &= \frac{C(\text{university})}{C(\text{all words})} \cdot \frac{C(\text{university of})}{C(\text{university})} \cdot \frac{C(\text{university of texas})}{C(\text{university of})} \cdot \frac{C(\text{of texas in})}{C(\text{of texas in})} \cdot \frac{C(\text{texas in amarillio})}{C(\text{texas in})} \end{split}
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• All of these should be easy to estimate!

7 N-Gram Model of Sentences

- Sentences are sequences of words, but with starts and ends.
- We also want to model the likelihood of words being at the beginning/end of a sentence.
- Append special "words" to the sentence
 - -n-1 ' $\langle b \rangle$ ' symbols to beginning
 - only one ' $\langle b \rangle$ ' to then end needed
 - * $p(\langle b \rangle \mid . \langle b \rangle) = 1.0$ since $\langle b \rangle$ would always be followed by $\langle b \rangle$.
- "the man walks the dog ." (trigrams)
 - Becomes " $\langle b \rangle \langle b \rangle$ the man walks the dog. $\langle b \rangle$ "
 - $-p(\langle b \rangle \langle b \rangle \text{ the man walks the dog . } \langle \backslash b \rangle) = p(\text{the } | \langle b \rangle \langle b \rangle) \\ \cdot p(\text{man } | \langle b \rangle \text{ the}) \\ \cdot p(\text{walks } | \text{ the man}) \\ \cdot p(\text{the } | \text{ man walks}) \\ \cdot p(\text{dog } | \text{ walks the}) \\ \cdot p(. | \text{ the dog}) \\ \cdot p(\langle \backslash b \rangle | \text{dog .})$
- Can be generalized to model longer texts: paragraphs, documents, etc:
 - Good: can model ngrams that cross sentences (e.g. $p(w_0 \mid .)$ or $p(w_0 \mid ?)$)
 - Bad: more sparsity on $\langle b \rangle$ and $\langle b \rangle$

8 Sentence Likelihood Examples

Example dataset:

Sentence Likelihood with Bigrams:

$$\begin{split} p(\langle b \rangle \text{ the dog walks . } \langle \backslash b \rangle) \\ &= p(\text{the } | \langle b \rangle) \cdot p(\text{dog } | \text{ the}) \cdot p(\text{walks } | \text{dog}) \cdot p(. | \text{ walks}) \cdot p(\langle \backslash b \rangle | .) \\ &= \frac{C(\langle b \rangle \text{ the})}{\sum_{x} C(\langle b \rangle x)} \cdot \frac{C(\text{the dog})}{\sum_{x} C(\text{the } x)} \cdot \frac{C(\text{dog walks})}{\sum_{x} C(\text{dog } x)} \cdot \frac{C(\text{walks } .)}{\sum_{x} C(\text{walks } x)} \cdot \frac{C(. \langle \backslash b \rangle)}{\sum_{x} C(. x)} \\ &= \frac{C(\langle b \rangle \text{ the})}{C(\langle b \rangle)} \cdot \frac{C(\text{the dog})}{C(\text{the})} \cdot \frac{C(\text{dog walks})}{C(\text{dog})} \cdot \frac{C(\text{walks } .)}{C(\text{walks } .)} \cdot \frac{C(. \langle \backslash b \rangle)}{C(.)} \\ &= \frac{5}{6} \cdot \frac{4}{7} \cdot \frac{1}{4} \cdot \frac{3}{4} \cdot \frac{6}{6} = 0.83 \cdot 0.57 \cdot 0.25 \cdot 0.75 \cdot 1.0 = \mathbf{0.089} \end{split}$$

 $p(\langle b \rangle)$ the cat walks the dog . $\langle b \rangle$

$$= p(\text{the} \mid \langle b \rangle) \cdot p(\text{cat} \mid \text{the}) \cdot p(\text{walks} \mid \text{cat}) \cdot p(\text{the} \mid \text{walks}) \cdot p(\text{dog} \mid \text{the}) \cdot p(\cdot \mid \text{dog}) \cdot p(\langle b \rangle \mid \cdot)$$

$$= \frac{C(\langle b \rangle \text{ the})}{\sum_{x} C(\langle b \rangle x)} \cdot \frac{C(\text{the cat})}{\sum_{x} C(\text{the } x)} \cdot \frac{C(\text{cat walks})}{\sum_{x} C(\text{cat } x)} \cdot \frac{C(\text{walks the})}{\sum_{x} C(\text{walks } x)} \cdot \frac{C(\text{the dog})}{\sum_{x} C(\text{the } x)} \cdot \frac{C(\text{dog } \cdot)}{\sum_{x} C(\text{dog } x)} \cdot \frac{C(\cdot \langle b \rangle)}{\sum_{x} C(\cdot x)}$$

$$= \frac{C(\langle b \rangle \text{ the})}{C(\langle b \rangle)} \cdot \frac{C(\text{the cat})}{C(\text{the})} \cdot \frac{C(\text{cat walks})}{C(\text{cat})} \cdot \frac{C(\text{walks the})}{C(\text{walks})} \cdot \frac{C(\text{the dog})}{C(\text{the})} \cdot \frac{C(\text{dog } \cdot)}{C(\text{dog})} \cdot \frac{C(\cdot \langle b \rangle)}{C(\cdot x)}$$

$$= \frac{5}{6} \cdot \frac{1}{7} \cdot \frac{1}{1} \cdot \frac{1}{4} \cdot \frac{4}{7} \cdot \frac{1}{4} \cdot \frac{6}{6} = 0.83 \cdot 0.14 \cdot 1.0 \cdot 0.25 \cdot 0.57 \cdot 0.25 \cdot 1.0 = \mathbf{0.004}$$

$$\begin{split} p(\langle b \rangle \text{ the cat runs . } \langle \backslash b \rangle) &= p(\text{the } | \langle b \rangle) \cdot p(\text{cat } | \text{ the}) \cdot p(\text{runs } | \text{ cat}) \cdot p(. | \text{ runs}) \cdot p(\langle \backslash b \rangle | .) \\ &= \frac{C(\langle b \rangle \text{ the})}{\sum_x C(\langle b \rangle x)} \cdot \frac{C(\text{the cat})}{\sum_x C(\text{the } x)} \cdot \frac{C(\text{cat runs})}{\sum_x C(\text{cat } x)} \cdot \frac{C(\text{runs } .)}{\sum_x C(\text{runs } x)} \cdot \frac{C(. \langle \backslash b \rangle)}{\sum_x C(. x)} \\ &= \frac{C(\langle b \rangle \text{ the})}{C(\langle b \rangle)} \cdot \frac{C(\text{the cat})}{C(\text{the})} \cdot \frac{C(\text{cat runs})}{C(\text{cat})} \cdot \frac{C(\text{runs } .)}{C(\text{runs})} \cdot \frac{C(. \langle \backslash b \rangle)}{C(.)} \\ &= \frac{5}{6} \cdot \frac{1}{7} \cdot \frac{\mathbf{0}}{1} \cdot \frac{1}{1} \cdot \frac{6}{6} = 0.83 \cdot 0.14 \cdot \mathbf{0.0} \cdot 1.0 \cdot 1.0 = \mathbf{0.000} \end{split}$$

- Longer sentences have lower likelihoods.
 - This makes sense because longer sequences are harder to match exactly.
- Zeros happen when an n-gram isn't seen.

9 Handling Sparsity

How big of a problem is sparsity?

- Alice's Adventures in Wonderland
 - Vocabulary (all word types) size: V = 3,569
 - Distinct bigrams: 17,149; $\frac{17,149}{|V|^2},$ or 99.8% of possible bigrams unseen
 - Distinct trigrams: 28,540; $\frac{17,149}{|V|^3}$, or 99.999994% of possible trigrams unseen
- If a sequence contains an unseen ngram, it will have likelihood zero: an impossible sequence.
- Many legitimate ngrams will simply be absent from the corpus.
- This does not mean they are impossible.
- Even ungrammatical/nonsense ngrams should not cause an entire sequence's likelihood to be zero
- Many others will be too infrequent to estimate well.

Add- λ Smoothing

- Add some constant λ to every count, including unseen ngrams

$$\bullet \ p(w_0 \mid w_{1-n} \dots w_{-1}) = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{\sum_x (C(w_{1-n} \dots w_{-1} \ x) + 1)} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{(\sum_x C(w_{1-n} \dots w_{-1} \ x)) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_{-1} \ w_0) + 1}{C(w_{1-n} \dots w_{-1}) + |V|} = \frac{C(w_{1-n} \dots w_0) + 1}{C(w_{1-n} \dots w_0) + 1}$$

- Add |V| to the denominator to account for the fact that there is an extra count for every x
- In practice it over-smoothes, even when $\lambda < 1$

Good-Turing Smoothing

- Estimate counts of things you haven't seen from counts of things you have
- Estimate probability of things which occur c times with the probability of things which occur c+1 times

•
$$c^* = (c+1)\frac{N_{c+1}}{N_c}$$

 $p^*_{GT}(things\ with\ freq\ \theta) = \frac{N_1}{N}$

•
$$p_{GT}(w_0 \mid w_{1-n} \dots w_{-1}) = \frac{C^*(w_{1-n} \dots w_{-1} w_0)}{C^*(w_{1-n} \dots w_{-1})}$$

Stupid Backoff

• If p(n-gram)=0, use p((n-1)-gram)

• Works shockingly well for huge datasets

Interpolation

• Mix n-gram probability with probabilities from lower-order models

$$\hat{p}(w_0 \mid w_{-2} \mid w_{-1}) = \lambda_3 \cdot p(w_0 \mid w_{-2} \mid w_{-1}) + \lambda_2 \cdot p(w_0 \mid w_{-1}) + \lambda_1 \cdot p(w_0)$$

- λ_i terms used to decide how much to smooth
- $\sum_{i} \lambda_{i} = 1$, because they are proportions
- Use dev dataset to tune λ hyperparameters
- Also useful for combining models trained on different data:
 - Can interpolate "customized" models with "general" models
 - Baseline English + regional English + user-specific English
 - Little in-domain data, lots of out-of-domain

Knesser-Ney Smoothing

- Intuition: interpolate based on "openness" of the context
- Words seen in more contexts are more likely to appear in others
- Even if we haven't seen w_0 following the context, if the context is "open" (supports a wide variety of "next words"), then it is more likely to support w_0
- Boost counts based on $|\{x: C(w_{1-n} \dots w_{-1} x) > 0\}|$, the number of different "next words" seen after $w_{1-n} \dots w_{-1}$

10 Out-of-Vocabulary Words (OOV)

$Add-\lambda$

- If ngram contains OOV item, assume count of λ , just like for all other ngrams.
- Probability distributions become invalid. We can't know the full vocabulary size, so we can't normalize counts correctly.

$\langle unk \rangle$

- Create special token $\langle unk \rangle$
- \bullet Create a fixed lexicon L

- All types in some subset of training data?
- All types appearing more than k times?
- $V = L + \langle unk \rangle$, |V| = |L| + 1
- Before training, change any word not in L to $\langle unk \rangle$
- Then train as usual as if $\langle unk \rangle$ was a normal word
- For new sentence, again replace words not in L with $\langle unk \rangle$ before using model
- Probabilities containing $\langle unk \rangle$ measure likelihood with some rare word
- Problem: the "rare" word is no longer rare since there are many $\langle unk \rangle$ tokens
 - Ngrams with $\langle unk \rangle$ will have higher probabilities than those with any particular rare word
 - Not so bad when comparing same sequence under multiple models. All will have inflated probabilities.
 - More problematic when comparing probabilities of different sequences under the same model
 - * p(i totes know) < p(i totally know) < p(i $\langle unk \rangle$ know)

11 Evaluation

Extrinsic

- Use the model in some larger task. See if it helps.
- More realistic
- Harder

Intrinsic

- Evaluate on a test corpus
- Easier

Perplexity

- Intrinsic measure of model quality
- How well does the model "fit" the test data?
- How "perplexed" is the model whe it sees the test data?
- Measure the probability of the test corpus, normalize for number of words.
- $\bullet \ PP(W) = \sqrt[|W|]{\frac{1}{p(w_1 \ w_2 \ \dots \ w_{|W|})}}$

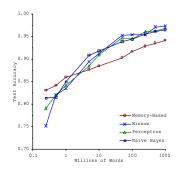
12 How much data?

Choosing n

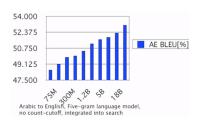
- Large n
 - More context for probabilities: p(phone) vs $p(\text{phone} \mid \text{cell})$ vs $p(\text{phone} \mid \text{your cell})$ vs $p(\text{phone} \mid \text{off your cell})$ vs $p(\text{phone} \mid \text{turn off your cell})$
 - Long-range dependencies
- Small n
 - Better generalization
 - Better estimates
 - Long-range dependencies

How much training data?

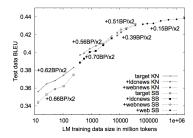
- As much as possible.
- More data means better estimates
- Google N-Gram corpus uses 10-grams



(a) Data size matters more than algorithm (Banko and Brill, 2001)



(b) Results keep improving with more data (Norvig: Unreasonable ...)



(c) With enough data, stupid backoff approaches Knesser-Ney accuracy (Brants et al., 2007)

13 Generative Models

- Generative models are designed to model how the data could have been generated.
- The best parameters are those that would most likely generate the data.

- MLE maximizes that likelihood that the training data was generated by the model.
- As such, we can actually generate data from a model.
- Trigram model:
 - General:

For each sequence:

- 1. Sample a word w_0 according to $w_0 \sim p(w_0)$
- 2. Sample a second word w_1 according to $w_1 \sim p(w_1 \mid w_0)$
- 3. Sample a next word w_k according to $w_k \sim p(w_k \mid w_{k-2} \mid w_{k-1})$
- 4. Repeat step 3 until you feel like stopping.
- Sentences:

For each sentence:

- 1. Sample a word w_0 according to $w_0 \sim p(w_0 \mid \langle b \rangle \mid \langle b \rangle)$
- 2. Sample a second word w_1 according to $w_1 \sim p(w_1 \mid w_0 \langle b \rangle)$
- 3. Sample a next word w_k according to $w_k \sim p(w_k \mid w_{k-2} \mid w_{k-1})$
- 4. Repeat until $\langle b \rangle$ is drawn.
- \bullet Longer n generates more coherent text
- Too-large n just ends up generating sentences from the training data because most counts will be 1 (no choice of next word).
- Naïve Bayes was a generative model too!

For each instance:

- 1. Sample a label l according to $l \sim p(Label = l)$
- 2. For each feature F: sample a value v according to $v \sim p(F = v \mid Label = l)$
- We will see many more generative models throughout this course

14 Citations

Some content adapted from:

• http://courses.washington.edu/ling570/gina_fall11/slides/ling570_class8_smoothing.pdf