

Article

Parallelized Inter-Image k-Means Clustering Algorithm for Unsupervised Classification of Series of Satellite Images

Soohee Han ^{1,*}  and Jeongho Lee ²

¹ Department of Geoinformatics Engineering, Kyungil University, 50, Gamasil-gil, Hayang-eup, Gyeongsan-si 38428, Republic of Korea

² Satellite Application Division, Satellite Operation & Application Center, Korea Aerospace Research Institute, Gwahak-ro, Yuseong-gu, Daejeon 34133, Republic of Korea; jeongho@kari.re.kr

* Correspondence: scivile2@gmail.com

Abstract: As the volume of satellite images increases rapidly, unsupervised classification can be utilized to swiftly investigate land cover distributions without prior knowledge and to generate training data for supervised (or deep learning-based) classification. In this study, an inter-image k-means clustering algorithm (IIkMC), as an improvement of the native k-means clustering algorithm (kMC), was introduced to obtain a single set of class signatures so that the classification results could be compatible among multiple images. Because IIkMC was a computationally intensive algorithm, parallelized approaches were deployed, using multi-cores of a central processing unit (CPU) and a graphics processing unit (GPU), to speed up the process. kMC and IIkMC were applied to a series of images acquired in a PlanetScope mission. In addition to the capability of the inter-image compatibility of the classification results, IIkMC could settle the problem of incomplete segmentation and class canceling revealed in kMC. Based on CPU parallelism, the speed of IIkMC improved, becoming up to 12.83 times better than sequential processing. When using a GPU, the speed improved up to 25.53 times, rising to 39.00 times with parallel reduction. From the results, it was confirmed IIkMC provided more reliable results than kMC, and its parallelism could facilitate the overall inspection of multiple images.

Keywords: unsupervised classification; k-means clustering; parallel processing; GPU; satellite image



Citation: Han, S.; Lee, J. Parallelized Inter-Image k-Means Clustering Algorithm for Unsupervised Classification of Series of Satellite Images. *Remote Sens.* **2024**, *16*, 102. <https://doi.org/10.3390/rs16010102>

Received: 14 November 2023

Revised: 14 December 2023

Accepted: 22 December 2023

Published: 26 December 2023



Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (<https://creativecommons.org/licenses/by/4.0/>).

1. Introduction

The volume of data obtained from satellites is increasing rapidly because of the development of satellite sensors and communication technologies. The geometric, spectral, and radiometric resolutions of satellite sensors are improving in tandem, and the size of scenes is increasing geometrically. As the speed of communication between satellites and ground stations improves, the volume of data received by ground stations grows. Moreover, nanosatellites (or cubesats) can capture more and more images with larger coverages and shorter revisit cycles, based on dense constellations and low altitude. For example, the PlanetScope mission involves more than 200 satellites, less than 4 m GSD, 400 square kilometer coverage, and a 90-min revisit cycle [1]. Because of the enhancing technologies and decreasing prices of storage media, there has been a steady rise in the size of the satellite images that could be stored in data warehouses. The development of computing power has led to an improvement in the conditions in which very large satellite images could be processed. However, it is not practically easy to process large satellite images via hardware improvements alone: corresponding software technologies should be developed and optimized for satellite image processing. As such, the advent of new and complex processing algorithms does not necessarily help to reduce processing times of larger satellite images, hindering their practical utilization. Therefore, there is an evident emerging need for research on reducing processing times.

Parallel processing is currently used for high-volume data processing and computationally intensive problem solving in a variety of fields, such as engineering, mathematics, and science. Parallel processing (or parallel computing) is a computing technology that divides complex problems into smaller parts and processes their data simultaneously on several computers. In the field of spatial informatics, large volumes of data are usually dealt with, and the complexity of processing methods is increasing considerably. As such, opportunities for using parallel processing in geographic information systems [2,3], remote sensing [4,5], and laser scanning [6,7] have steadily emerged. For example, in the field of remote sensing, parallelization was implemented in an optical real-time adaptive spectral identification system of which purpose was to analyze the endmembers of hyperspectral images [8]. In order to monitor and track wildfires in (near) real-time, another study focused on parallelizing classification algorithms based on automated morphological and self-organizing maps for hyperspectral images [9]. Endmember extraction (or pixel purity index) calculations for hyperspectral images were parallelized, and performance comparisons were performed on parallel processing hardware using various platforms [10–12]. Typically, relevant studies share a common aspect: they process hyperspectral images and parallelize various algorithms for classification and recognition.

Efforts have been made to develop parallel processing techniques that were suitable for new and affordable hardware. Starting from early 2010, there has been a trend toward parallel processing using graphics processing units (GPUs). They were applied, based on the compute unified device architecture (CUDA) of NVIDIA, to modulation transfer function compensation, cubic convolution interpolation, and discrete and wavelet inverse transformations [13]. CUDA was also used to apply the mean shift clustering algorithm to high-resolution remote sensing images [14]. Some researchers have developed GPU-based image mosaicking [15] and Sobel filtering [16]. However, the use of GPU-based approaches is not known ideal for very large image processing because of the limited capacity of GPU memory.

More recently, interest in cloud computing has grown rapidly, and there has been an increasing use of methods that allowed large satellite images to be processed using high-performance cloud servers. Cloud computing technology is a good candidate for processing large amounts of remote sensing data if the cost of high-performance computing implementations and technical usability is considered [17]. For example, maximum likelihood classification and Mahalanobis distance clustering algorithms have been implemented in a cloud computing environment [18]. However, the basic purpose of cloud computing is to make high-performance computing resources available to large quantities of clients through the Internet. When large satellite images are uploaded to cloud servers, the process of uploading itself can lead to inefficiencies, and the cloud resources cannot be reserved exclusively for the large projects. As an alternative, distributed computing decomposes data and processes them simultaneously. This concept can correspond to parallel processing; however, it is a loosely coupled method in which each node processes the data independently. Thus, it differs from tightly coupled parallel processing, which is based on computing nodes that share memory [5].

On the other hand, unsupervised classification is a preprocessing process implemented to investigate land cover distribution from satellite images without prior knowledge. Additionally, it is utilized to generate training data for supervised classification. Recently, the trend of satellite image classification has shifted to deep learning and a wide variety of pre-trained models were available for application to various landcovers and sensors [19], with studies being conducted to transfer and augment pre-trained models [20]. However, to train a new model for new objects and sensors, a large quantity of training data is still required, but acquisition cannot completely replace the use of human resources. Therefore, it is expected, for the time being, the unsupervised classification is applied to semi-automated training data collection in deep learning approaches.

Because unsupervised classification is generally assumed to be a preprocessing task, in some cases, when repeatedly performed using various parameters on multiple images,

it is strongly expected to require less processing time in a fully automatic method. However, computing-intensive methods are still likely to be relevant to the attainment of acceptable results. For example, k-means clustering, a de facto standard for unsupervised classification algorithms, is implemented in prevalent remote sensing software such as ENVI, Erdas Imagine, and SNAP. It is also implemented through extensions or plugins in GIS software such as QGIS and ArcGIS. Due to its simplicity and efficiency in clustering a large dataset, the k-means clustering algorithm is still popular and widely used in relevant studies in native and further modified forms [21–30]. K-means clustering is composed of multiple loops and may take hours depending on the volume of images and input parameters. Nevertheless, when applied to multiple images, resulting classes would not be compatible among the images because the method would lack pre-trained class signatures. Therefore, improvements are needed to increase processing speed and apply to series of images acquired from recent satellite missions.

The study aims at two objectives: (1) performing unsupervised classification to acquire consistent and compatible results from a series of satellite images and (2) improving computational efficiency by implementing parallel processing. For the objectives, the study improves the k-means clustering algorithm in two steps: firstly, it classifies a series of images attained by the PlanetScope mission and produces a single set of class signatures so the resulting images share consistent class IDs. The results generated by the proposed algorithm were compared with those obtained from the native version. Next, the algorithm is parallelized using multi-cores of a CPU and a GPU. The parallelism consists of concurrent processing of the main classification routines using numbers of computational units, followed by further optimization based on parallel reduction utilizing a GPU. The performance is compared between models with a sequential code (without parallel processing), a multi-core code, a GPU code, and a GPU code with parallel reduction.

2. Algorithm Development

2.1. Inter-Image k-Means Clustering Algorithm

The native k-means clustering algorithm (hereafter, kMC) segments points in N dimensions into k clusters so the within-cluster sum of squares of distances is minimized [31]. The k-means clustering algorithm, applied to the unsupervised classification of a satellite image, consists of the following steps in Figure 1:

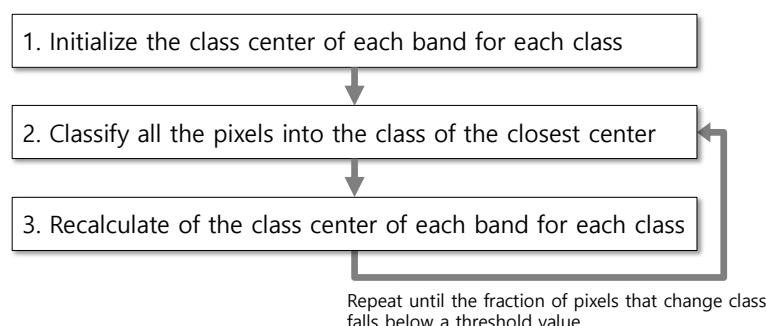


Figure 1. A general workflow of kMC.

In step 1, various kinds of methods have been developed to produce more accurate and unbiased centers and less iterations. Among these methods, a simple furthest-point heuristic can reduce the clustering error [32]. The method first sets a random center and then adds new centers using further points from newly-retrieved points. Therefore, if the computational cost of retrieving points is not that large, it is better to sweep all points and set class centers using the statistics of member points. Simply, the difference between the pixels' maximum and minimum values in each band is split into k segments, and the center of each segment is set as the initial center of the class (Algorithm 1).

Algorithm 1 Pseudocode for class initialization of kMC

```

1.   for (i = 1 to nRow * nColumn) //for all pixels
2.       for (j = 1 to nBand) //for all bands
3.           Min[j] = smaller(Min[j] vs. Pixel[i][j]) // retrieve the minimum value of band j
4.           Max[j] = larger(Min[j] vs. Pixel[i][j]) // retrieve the maximum value of band j
5.   for (i = 1 to nClass) //for all classes
6.       for (j = 1 to nBand) //for all bands
7.           interval = (Max[j] – Min[j])/nClass // set class interval
8.           Center[i][j] = Min[j] + interval/2 + interval * (i – 1) // set initial class centers

```

In step 2, Euclidean distances are calculated from each point to all the class centers, and a point is assigned to the closest class. In step 3, the average value is calculated for each band of each class and is set to a new class center (Algorithm 1). Equation (1) identifies the class \hat{j} into which a pixel P will be classified in a multispectral satellite image composed of N bands:

$$\begin{aligned} \hat{j} &= \operatorname{argmin}_j(\operatorname{dist}(P, j)) \\ \operatorname{dist}(P, j) &= \sqrt{\sum_{b=1}^N (P_b - C_b^j)^2} \end{aligned} \quad (1)$$

where $\operatorname{argmin}_j(\operatorname{dist}(P, j))$ stands for the class j that minimizes the argument $\operatorname{dist}(P, j)$, which denotes the distance from a pixel to each class center; P_b denotes the pixel value of band b of the pixel P ; and C_b^j denotes the center of band b of class j .

The pseudocode for steps 2 to 3 consists of four for-loops (Algorithm 2). The first for-loop iterates the entire classification process. The second for-loop retrieves all pixels. The third for-loop retrieves all classes, and the fourth for-loop does so for all the bands.

Algorithm 2 Pseudocode for main classification routine of kMC

```

1.   for (iter = 1 to nMaxIter) //iteration
2.       for (i = 1 to nRow * nColumn) //for all pixels
3.           for (j = 1 to nClass) //for all classes
4.               for (k = 1 to nBand) //for all bands
5.                   Dist[i][j] += (Pixel[i][k] – Center[j][k])2 //distance from pixel i to class
center j
6.               Class[i] = argmin_j(Dist[i][j]) //classify pixel i to the class j which minimizes the
distance
7.               if (isChanged(Class[i])) //if Pixel[i] is reclassified to a different class
8.                   nChanged++ //increase the number of reclassified pixels
9.                   nPixelClass[Class[i]]++ //increase the number of pixels of the class
10. ...
11.               Center[Class[i]] += Pixel[i][ ] //add the pixel values to the class
12. ...
13.   Center[ ][ ] = Center[ ][ ]/nPixelClass[ ][ ] //update class centers for all classes and bands when nPixelClass is not zero
14.   if (ChangedRatio < MaxChangedRatio) //iteration ending condition
15.       break

```

When k-means clustering is applied to multiple images, each image attains a different constitution of class signatures. Class ID is determined by chance, and an identical class ID among images does not indicate their land cover is the same. Unless it is necessary to attain separate class signatures for each image, integrated clustering of all images is the better choice for figuring out the landcover characteristics and their pixel value distribution through the entire images. In other words, if clustering is applied to continuously acquired images, it is better for a class ID to denote the same land cover through the images. In this study, a revised version of kMC is proposed, which is defined as inter-image

k-means clustering (hereafter, IIkMC), to segment entire images using a single set of class signatures (Figure 2).

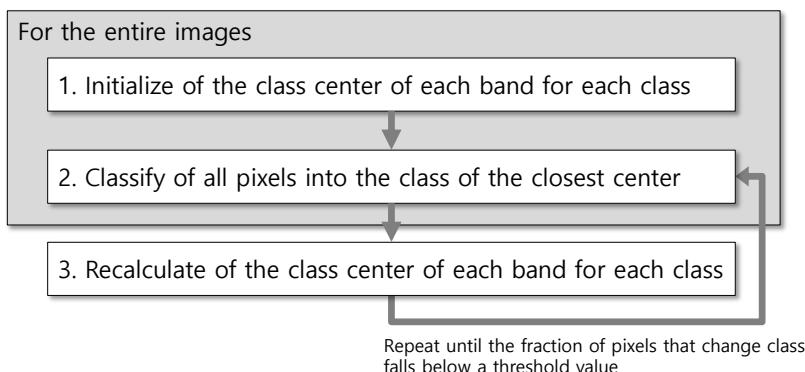


Figure 2. A workflow of IIkMC.

The pseudocode for IIkMC introduces an additional for-loop compared to the native code (Algorithm 3). The number of bands (*nBand*) is assumed to be the same because the same sensor is used. However, the dimension of an image (*nRow* and *nColumn*) is specified separately for each image as the effect of resampling in geo-rectification. All images are processed using a single set of (initial) class centers, which is updated using all the pixels of entire images through the classification process. In Algorithm 3, red text indicates changes from the native code, and blue text indicates variables that calculate a single set of class signatures.

As the revised algorithm includes five for-loops, time spent increases exponentially as the size of the image, the number of classes, and the number of images increase, necessitating the improvement of processing speed. Especially, as the third for-loop takes the longest iteration, it becomes the main target to be divided and processed concurrently.

Algorithm 3 Pseudocode for main classification routine of IIkMC

```

1.   for (iter = 1 to nMaxIter)//iteration
2.     for (img = 1 to nImage)//for all images
3.       for (i = 1 to nRowimg * nColumnimg)//for all pixels
4.         for (j = 1 to nClass)//for all classes
5.           for (k = 1 to nBand)//for all bands
6.             Dist[i][j] += (Pixel[img][i][k] - Center[j][k])2//distance from pixel i
      to class center j
7.             Class[img][i] = argminj(Dist[i][j])//classify pixel i to the class j which
      minimizes the distance
8.             if (isChanged(Class[img][i]))//if Pixel[i] is reclassified to a different class
9.               nChanged++//increase the number of reclassified pixels
10.              nPixelClass[Class[img][i]]++//increase the number of pixels of class j
11. ...
12.              Center[Class[img][i]][ ] += Pixel[i][ ]//add the pixel values to the class
13. ...
14.             Center[ ][ ] = Center[ ][ ]/nPixelClass[ ][ ]
      //update class centers for all classes and bands when nPixelClass is not zero
15.             if (ChangedRatio < MaxChangedRatio)//iteration ending condition
16.               break
  
```

Likewise, all pixels of all images should be swept when determining the initial class centers, which is the first step in Figure 1. The corresponding pseudocode is shown in Algorithm 4.

Algorithm 4 Pseudocode for class initialization of IIkMC

```

1. for (img = 1 to nImage) //for all images
2.   for (i = 1 to nRowimg * nColumnimg) //for all pixels
3.     for (j = 1 to nBand) //for all bands
4.       Min[j] = smaller(Min[j] vs. Pixel[img][i][j]) //retrieve the minimum value of
      band j
5.       Max[j] = larger(Min[j] vs. Pixel[img][i][j]) //retrieve the maximum value of
      band j
6.     for (i = 1 to nClass) //for all classes
7.       for (j = 1 to nBand) //for all bands
8.         ...
9.       Center[i][j] = Min[j] + interval/2 + interval * (i - 1) //set initial class centers

```

2.2. Parallel Processing of Inter-Image k-Means Clustering Algorithm

Parallel processing of kMC can be divided into intra-node parallel processing and inter-node parallel processing [33]. Intra-node parallel processing uses the multiple cores of a CPU and shared memory in a PC. OpenMP [34] programming can be used to control the multiple cores of a CPU, which all share data in the random access memory (RAM) and hard disk drive (HDD). Intra-node parallel processing can be favorably applied to the parallelization of the second loop (line 2) in Algorithm 2 because the loops constitute the worst bottleneck encountered throughout the procedures. Inter-node parallel processing uses multiple CPUs, each of which has its own OS and memory. MPI [35] programming is typically used to control CPUs in the nodes (PCs or workstations), transmitting data between the nodes through an external network (such as Ethernet). The inter-node parallelism can be implemented in a hybrid fashion with a PC cluster used to implement the inter-node method and the multiple cores of its nodes deployed to implement the intra-node method [33]. The third approach is based on general-purpose GPU. A typical GPU-based parallel implementation for kMC was applied to the second loop (line 2) in Algorithm 2 [36], in which lots of GPU cores were exploited to enormously accelerate Euclidian distance calculation. The fourth approach introduces MapReduce programming based on a Hadoop cluster for large data processing [37]. However, MapReduce programs are known to take a considerable time to process problems requiring many iterations, while OpenMP and GPU allow higher processing speed and more flexible control than MapReduce [38]. Hence, the present study develops parallel IIkMC based on the intra-node approach and the GPU method (Figure 3).

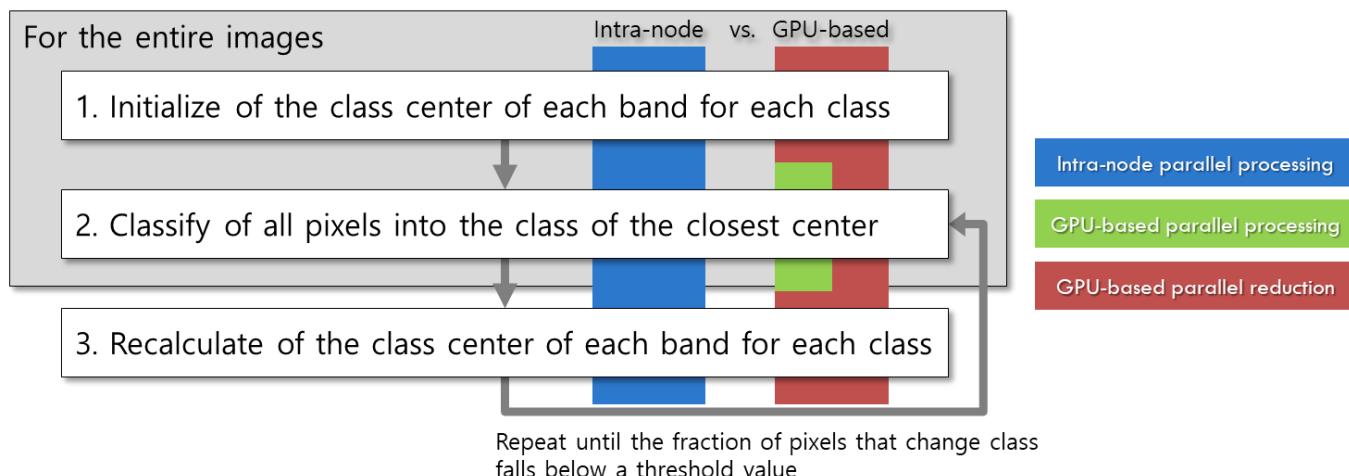


Figure 3. Procedures to which intra-node and GPU-based parallel processing is applicable.

2.2.1. Intra-Node Parallel Processing

Intra-node parallel processing is conducted by simultaneously processing N sub-images, each $1/N$ times the size of an entire image, using N cores in a CPU. This step is simply implemented by inserting an OpenMP clause **#pragma omp parallel for** before the third loop (line 3) in Algorithm 3.

Unfortunately, OpenMP is known to suffer from false sharing. If this problem is not resolved, the method consumes more time than when sequential (non-parallel) processing is used. False sharing is a phenomenon that occurs when different cores modify variables that are along the same cache line. Because the memory is forced to update to maintain cache consistency, the processing speed is greatly reduced [39]. This happens frequently when the contents of variables in a for-loop are changed almost simultaneously by different cores. To prevent false sharing, the variables with changed contents in each core must be placed in a **private()** construct, and **i**, **j**, and **k** should be defined as **private** after the **parallel for** clause. Variables that are placed in a **private()** construct are declared independently for each core and do not interfere with each other. A **reduction()** construct is used to sum up values without false sharing. The **nChanged** variable is used to count the total number of pixels with changed classes, and is defined as **reduction(+:nChanged)**. Therefore, the false sharing problem should not occur (Algorithm 5).

Algorithm 5 Implementation of intra-node parallel processing using OpenMP

```

1.   for (iter = 1 to nMaxIter) //iteration
2.     for (img = 1 to nImage) //for all images
3.       #pragma omp parallel for private(i, j, k) reduction(+:nChanged)
4.         for (i = 1 to nRowimg * nColumnimg) //for all pixels
5.           for (j = 1 to nClass) //for all classes
6.             for (k = 1 to nBand) //for all bands
7.               ...
8.               nChanged++ //increase the number of reclassified pixels
9.             ...

```

Despite these precautions, false sharing can still occur. **nPixelClass** and **Center** in Algorithm 3 are pointer arrays, which store the number of pixels classified in each class and the class center of each band. During classification, the values of **nPixelClass** or **Center** can be changed when accessed at the same time by different cores. When this happens, so does false sharing. To solve this problem, **nPixelClass** and **Center** are declared to be global variables, and **nPixel_local** and **Center_local** are declared to be local variables for each core, as illustrated in Figure 4. In each core, **Center** is shared during classification, but the numbers of pixels and pixel values for each class are accumulated in the local variables **nPixel_local** and **Center_local**. When classification is finished, all cores' local variables should be summed up to the global variables **Center** and **nPixelClass**, and the centers of each class are recalculated by averaging them. This method prevents false sharing, and the pseudocode is given in Algorithm 6.

Algorithm 6 Pseudocode for recalculation of class centers

```

1.   for (i = 0 to nClass) //through all classes
2.     for (j = 0 to nThread) //through all cores
3.       for (k = 0 to nBand) //for all bands
4.         ...
5.         Center[i][ ] += Center_local[i][ ] //update global center using local ones for all
   bands
6.         nPixelClass[i] += nPixel_local[i] //update global no. of pixels using local ones
7.         ...
8.         Center[i][ ] = Center[i][ ]/nPixelClass[i]
   //recalculate class centers for all classes and bands when nPixelClass is not zero

```

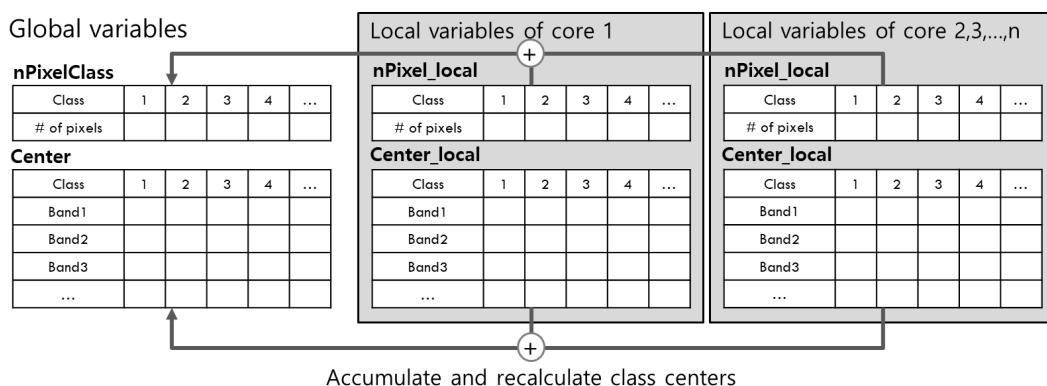


Figure 4. Global and local declarations of variables **nPixelClass** and **Center** (revised from [33]).

As shown in Algorithm 4, when initializing the class centers as the first step in Figure 1, there is a triple for-loops, and the speed can be improved by inserting an OpenMP clause **#pragma omp parallel for** before the second for-loop (line 2). Since this step also causes a false sharing problem in the **Min** and **Max** variables, local variables **Min_local** and **Max_local** should be declared for each core and integrated into the global variables **Min** and **Max**. Since this is relatively simple, a more detailed explanation is omitted.

2.2.2. GPU-Based Parallel Processing

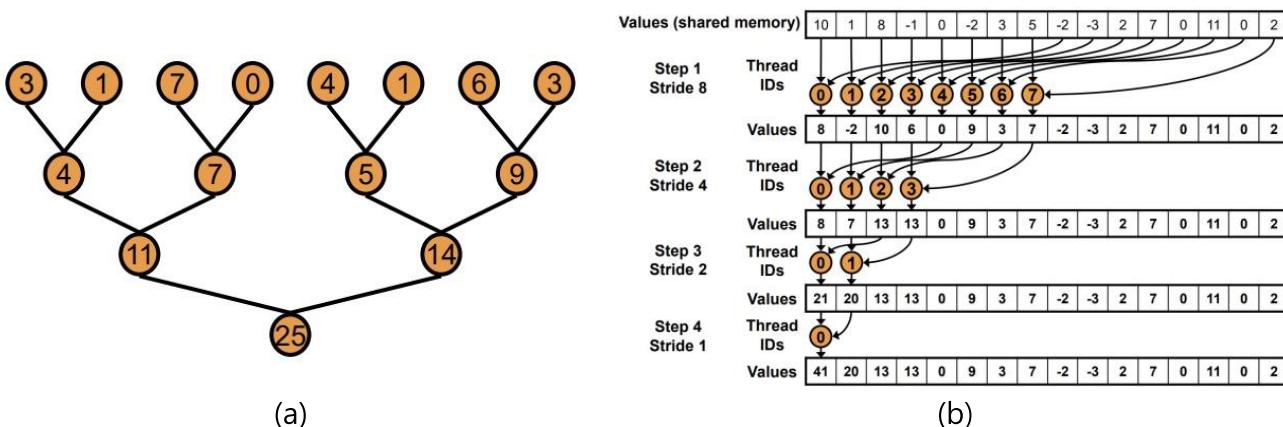
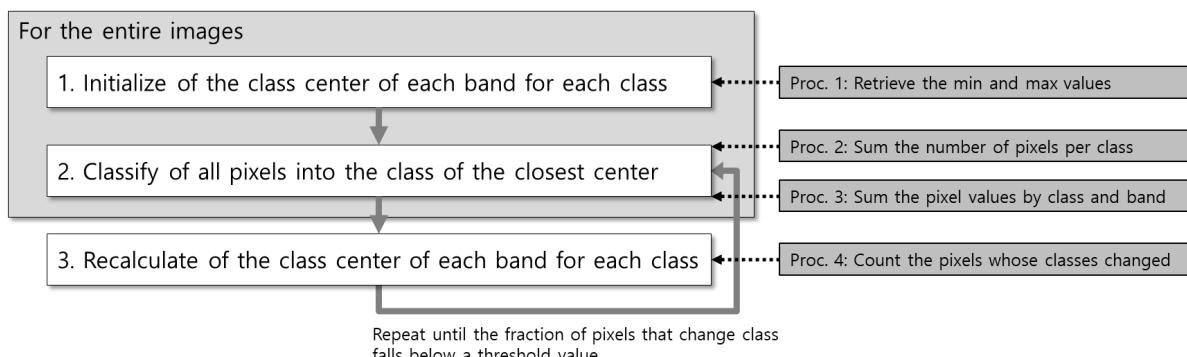
As a simple implementation method, the main classification routine (lines 2 to 7) in Algorithm 3 is divided into blocks and several blocks are concurrently processed using many arithmetic logic units (ALUs) in a GPU. In other words, a pixel of an image is assigned to an ALU, and the ALU calculates the distance to all class centers and designates the pixel to the shortest class. Thousands of ALUs concurrently conduct the same process for each pixel invoked by a kernel function. However, before the process, the class centers are initialized by a CPU and transferred to the GPU memory (hereafter, device memory), along with the image itself from main memory. The class information of each pixel, as the result of the main classification routine, is transmitted from the device memory to the main memory, and the class centers are updated by the CPU. In summary, the GPU is responsible for the distance calculation and classification of each pixel and the CPU is responsible for initializing and updating the class centers. Pseudocode for the GPU-based parallel processing is given in Algorithm 7.

Initializing and updating class centers requires more complex designs be used for GPU-based parallel processing. Initialization requires searching the minimum and maximum values of all pixels, and updating requires summing all pixel values for each band of each class along with the counts of the pixels in each class. This kind of operation utilizes an array of numerous values to produce a single output and is referred to as “reduction”. In the intra-node parallel processing, data can be divided into several sub-sections, and each section can be serially reduced by each CPU core. Here, a serial reduction is defined to iterate through the entire array, performing the reduction on pairs of elements, and updating the accumulator until the result is obtained. However, this approach is not well suited for the massively parallel architecture of a GPU. Because each ALUs is not fast as a CPU core, it should be applied to finer pieces of tasks. Thus, a parallel reduction is conducted in the fashion that each ALU performs a summation or logical operation for finer entities. This procedure is iteratively performed for the results until a single result is derived. However, as the iteration goes on, the number of ALUs participating in the operation decreases exponentially. It is important to make as many ALUs still participate in the reduction. Parallel reduction has been sufficiently studied to enhance procedural efficiency based on CUDA [40]. In this study, sequential addressing, a middle-optimized parallel reduction among the relevant approaches (Figure 5), was applied to the following procedures in Figure 6.

Algorithm 7 Pseudocode for GPU-based parallel processing of IIkMC

```

1. for (iter = 1 to nMaxIter)//iteration
2.     cudaMemcpy(devCenter, Center, ..., cudaMemcpyHostToDevice)
        //upload (initial) class centers to GPU
3.     for (img = 1 to nImage)//for all images
4.         cudaMemcpy(dev_Image, Image[img], ..., cudaMemcpyHostToDevice)
            //upload an image to GPU
5.         cudaMemcpy(devClass, Class[img], ..., cudaMemcpyHostToDevice)
            //upload (initial) class information of each pixel to GPU
6.         nBlock = (nRowimg *nColumnimg - 1)/nThread + 1//nThread is a multiple of 32
        or 64
7.         kmeansKernel<<<nBlock, nThread>>>(devImage, devClass, devCenter, ...)
        //invoke parallel classification
8.         cudaMemcpy(Class[img], devClass, ..., cudaMemcpyDeviceToHost)
            //download new pixel class from GPU
9.         for (i = 1 to nRowimg * nColumnimg)//for all pixels
10.            if (isChanged(Class[img][i]))//if Pixel[img][i] is reclassified to a different class
11.                nChanged++//increase the number of reclassified pixels
12.                nPixelClass[Class[img][i]]++//increase the number of pixels of class j
13. ...
14.            Center[Class[img][i]][ ] += Pixel[i][ ]//add the pixel values to the class
15. ...
16.         Center[ ][ ] = Center[ ]/nPixelClass[ ]
            //recalculate class centers for all classes and bands when nPixelClass is not zero
17.         if (ChangedRatio < MaxChangedRatio) //iteration ending condition
18.             break
    
```

**Figure 5.** Illustration of parallel reduction: (a) basic concept, (b) sequential addressing [40].**Figure 6.** Procedures to which parallel reduction is applicable.

Procedure 1 is implemented in initializing class centers, procedures 2 and 3 are applied to the main classification routine, and procedure 4 is used to update the class centers. Each step is executed with a pair of a kernel invocation function and a reduction function. The kernel invocation function organizes input data into an array compatible to parallel reduction and performs the first reduction. The reduction function iterates until a result is derived using a parallel reduction routine. In this way, IIkMC is fully parallelized using a GPU without any CPU implementations. The pseudocode is shown in Algorithm 8. Unlike line 7 in Algorithm 7, one more argument is given within <<< >>> in the kernel invocation in Algorithm 8. This dramatically improves the speed of the parallel reduction using cache memory (shared memory in CUDA) allocated to each ALU. However, the details of this are omitted in the manuscript.

Algorithm 8 Pseudocode for fully parallelized GPU-based IIkMC using parallel reduction

```

//Class center initialization
1.   for (img = 1 to nImage)//for all images
2.     ...
3.     minMaxKernel<<<nBlock, nThread, ...>>>(devImage, devClass, outArray, ...)
        //invoke parallel min, max retrieval
4.     reduce_minmax(outArray, minMaxArray)
        //reduce min and max values to minMaxArray
5.     ...
//Classification routine
7.   for (iter = 1 to nMaxIter)//iteration
8.     ...   for (img = 1 to nImage)//for all images
9.     ...
10.    kmeansKernel<<<nBlock, nThread, ...>>>(devImage, devClass, devCenter,
        outArray, ...)
        //invoke parallel classification
11.    reduce(outArray, nChanged)//reduce class-changed pixel counts to nChanged
12.    ...
13.    classPixelCountKernel <<<nBlock, nThread, ...>>>(devClass, outArray, ...)
        //invoke parallel pixel count
14.    reduce(outArray, nPixelClass)//reduce pixel counts to nPixelClass
15.    ...
16.    newCenterKernel<<<nBlock, nThread, ...>>>(devImage, devClass, outArray, ...)
        //invoke parallel pixel value summation
17.    reduce(outArray, Center)//reduce pixel values to Center
18.    ...
19.    Center[ ][ ] = Center[ ][ ]/nPixelClass[ ]
        //recalculate class centers for all bands when nPixelClass is not zero
20.    if (ChangedRatio < MaxChangedRatio)//iteration ending condition
21.      break

```

3. Evaluation and Discussions

3.1. Evaluation Method

A series of adjacent PlanetScope images were processed using kMC and IIkMC, and the classification results were compared. IIkMC was implemented in a sequential code (without parallel processing), an intra-node parallel code, a GPU-based parallel code, and a GPU-based parallel code using the parallel reduction. The performance of the parallel codes was compared to the sequential variant.

A total of twelve images were achieved over two days from 30 October 2018 to 31 October 2018 (Figure 7). Each image is composed of four multi-spectral bands (red, green, blue, and infra-red) and the file type is 16-bit geotiff. The dimension of each image is approximately $8.2\text{ k} \times 3.9\text{ k}$ and the average size in the uncompressed tiff is 244 MB. The computing system has an AMD Ryzen 9 CPU consisting of 16 cores for intra-node parallel

processing and an NVIDIA RTX 3090 Ti graphics card for GPU-based parallel processing (Table 1). The number of classes (k) is eight, and the iteration termination condition is 1.0% (Table 2).

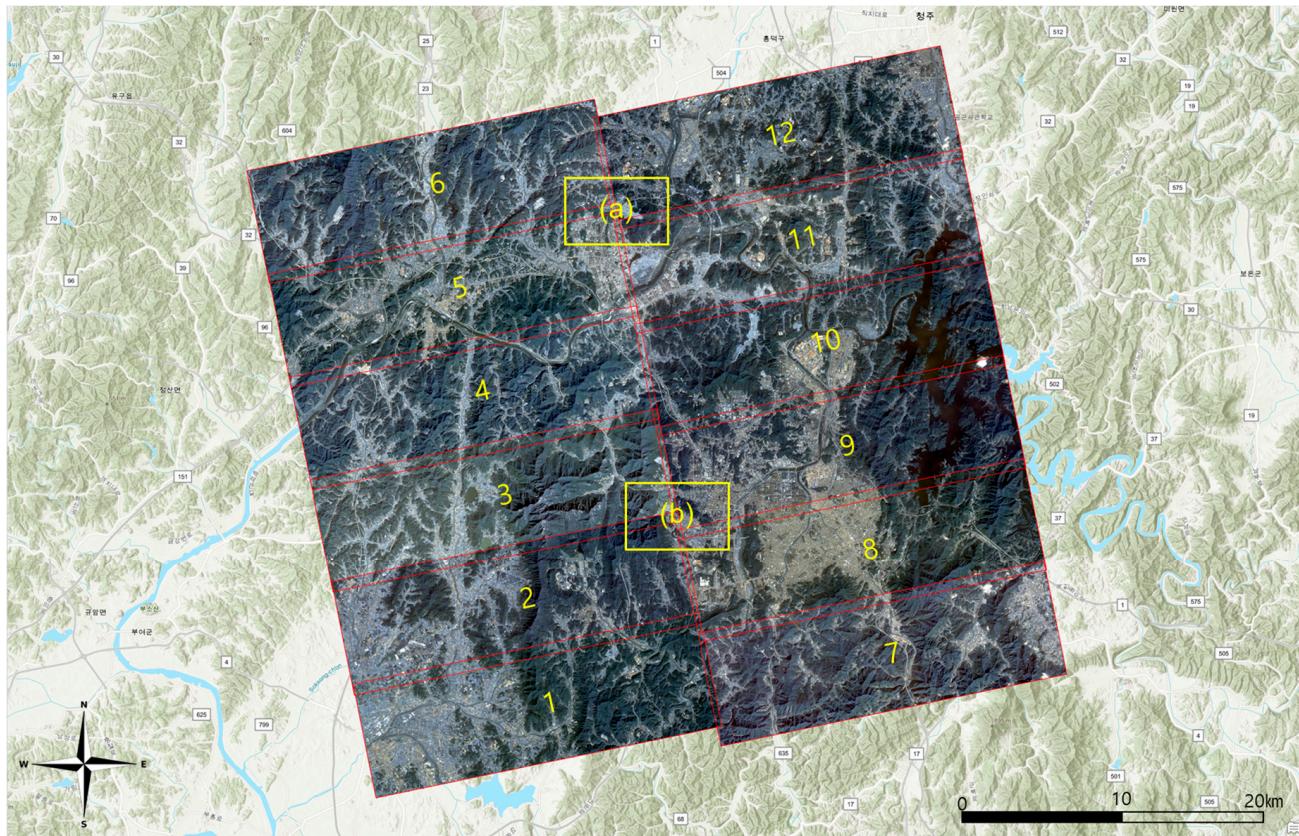


Figure 7. Placement of 12 PlanetScope images (Enlargements of (a) and (b) are in Appendix A, and location names are in local terms.)

Table 1. Specifications of the computing system.

CPU	GPU	RAM	SSD	OS	Library
AMD Ryzen 9 7950X 16-Core Processor 4.50 GHz	MSI Geforce RTX 3090 Ti 24 GB	Samsung DDR5 64 GB	Samsung SSD 980 pro 2 TB	Windows 11	CUDA Toolkit 12.2, gdal:x64-windows 3.7.2#1

Table 2. Parameters of k-means clustering.

Number of Classes (=k)	Maximum Number of Iterations	Iteration Termination Condition
8	100	Ratio of class-changed-pixels below 1.0%

3.2. Evaluation of Clustering Results

The results of the separate processing of each image using kMC are shown in Table 3 and Figure 8. A same-color map was applied to each result to match the same class ID with the same color. The number of iterations differed greatly, and image 3 was processed after three iterations, resulting in incomplete segmentation. With smaller termination condition, it would have produced different results, but it should be remarked 1.0% was not an unreasonable condition. One class was canceled in image 9, and two classes were canceled in image 11, which may have occurred accidentally due to the spectral characteristics of the initial and updated class centers. This problem might be solved by applying class-splitting step to the classification routine, which was not considered in this study.

Results 1 and 7 to 12 appear to have similar class signatures compatible among themselves; images 3, 4, and 6 also might, but the rest do not.

Table 3. Results of kMC (The numbers next to each class IDs are the numbers of entities and ratios of the pixels classified to the classes.).

Image	1	2	3	4
Date	30 October 2018	30 October 2018	30 October 2018	30 October 2018
Dim.(Size)	8146 × 3914 (243 MB)	8147 × 3917 (243 MB)	8157 × 3915 (244 MB)	8166 × 3916 (244 MB)
# of iter.	52	3	42	40
Class 1	4,928,065	24.8%	13,402,654	67.4%
Class 2	5,810,526	29.2%	6,187,532	31.1%
Class 3	3,387,364	17.0%	283,050	1.4%
Class 4	2,655,411	13.4%	15,046	0.1%
Class 5	2,448,135	12.3%	1610	0.0%
Class 6	93,745	0.5%	385	0.0%
Class 7	540,304	2.7%	86	0.0%
Class 8	15,364	0.1%	26	0.0%
Sum	9,878,914	100%	19,890,389	100%
30 October 2018				
8156 × 3916 (244 MB)	8155 × 3916 (244 MB)	8147 × 3932 (244 MB)	8164 × 3934 (245 MB)	8164 × 3934 (245 MB)
74	43	16	39	
Class 1	3,502,094	17.6%	4,068,726	20.4%
Class 2	5,179,392	26.0%	5,257,784	26.4%
Class 3	2,772,873	13.9%	6,329,473	31.8%
Class 4	4,009,512	20.1%	2,397,961	12.0%
Class 5	2,542,993	12.8%	1,484,225	7.5%
Class 6	1,525,131	7.7%	342,262	1.7%
Class 7	363,732	1.8%	28,155	0.1%
Class 8	17,147	0.1%	2662	0.0%
Sum	19,912,874	100%	9,911,248	100%
31 October 2018				
8172 × 3935 (245 MB)	8165 × 3937 (245 MB)	8156 × 3936 (245 MB)	8148 × 3934 (244 MB)	8148 × 3934 (244 MB)
15	27	32	57	
Class 1	6,699,672	33.8%	6,583,322	33.2%
Class 2	9,142,172	46.1%	8,092,120	40.8%
Class 3	3,053,169	15.4%	3,194,369	16.1%
Class 4	830,459	4.2%	1,691,523	8.5%
Class 5	102,337	0.5%	262,921	1.3%
Class 6	14,050	0.1%	26,349	0.1%
Class 7	669	0.0%	558	0.0%
Class 8	-	0.0%	42	0.0%
Sum	19,842,528	100%	9,851,204	100%
31 October 2018				
8172 × 3935 (245 MB)	8165 × 3937 (245 MB)	8156 × 3936 (245 MB)	8148 × 3934 (244 MB)	8148 × 3934 (244 MB)
15	27	32	57	
Class 1	6,699,672	33.8%	6,583,322	33.2%
Class 2	9,142,172	46.1%	8,092,120	40.8%
Class 3	3,053,169	15.4%	3,194,369	16.1%
Class 4	830,459	4.2%	1,691,523	8.5%
Class 5	102,337	0.5%	262,921	1.3%
Class 6	14,050	0.1%	26,349	0.1%
Class 7	669	0.0%	558	0.0%
Class 8	-	0.0%	42	0.0%
Sum	19,842,528	100%	9,851,204	100%

The result of concurrently processing the 12 images using IIkMC is shown in Table 4 and Figure 9. The result was derived after 55 iterations, and the class signatures appeared to be compatible throughout the results. From the enlarged image of Figure 7 (a) in Figure A1 and the corresponding results in Figures A2 and A3, it can be clearly seen IIkMC has better class compatibility among the results. From the enlarged image of Figure 7 (b) in Figure A4 and the corresponding results in Figures A5 and A6, it could be confirmed a complete result was obtained for image 2, which was not properly segmented by kMC. From the inspection, it was also confirmed none of the classes were canceled in the results of images 9 and 11.

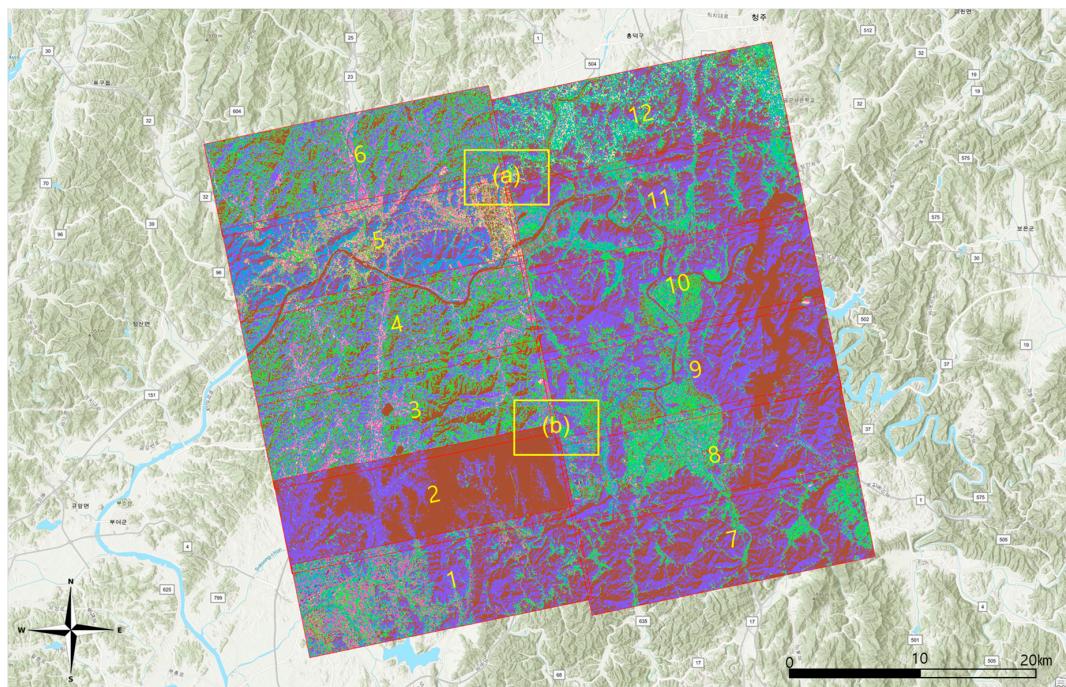


Figure 8. Results of kMC (Enlargements of (a) and (b) are in Appendix A, and location names are in local terms.)

Table 4. Results of IIkMC.

	Class 1	Class 2	Class 3	Class 4	Class 5	Class 6	Class 7	Class 8	Sum
# of pixels	43,484,072	52,010,051	68,692,476	35,446,580	27,183,058	1,682,832	9,736,596	170,283	238,405,948
Ratio	18.2%	21.8%	28.8%	14.9%	11.4%	0.7%	4.1%	0.1%	100%

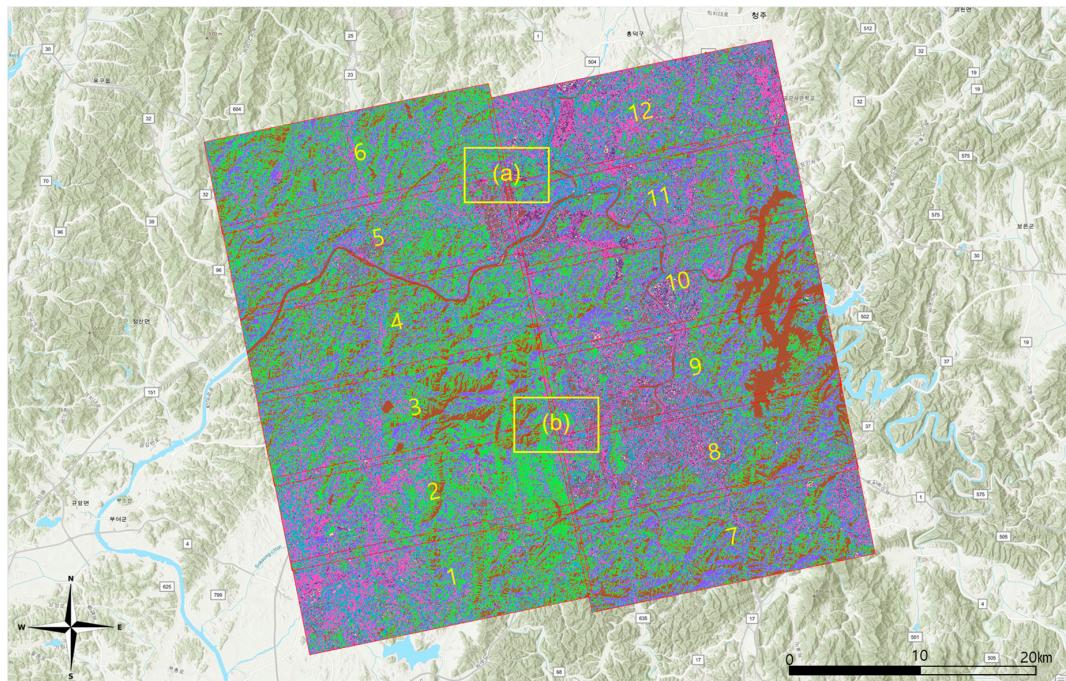


Figure 9. Results of IIkMC (Enlargements of (a) and (b) are in Appendix A, and location names are in local terms.)

However, from Figures A3 and A6, it could be remarked over-segmentation might have occurred in the results of IIkMC. The possible reason for this was acceptance of the spectral features from multiple images could have broadened the spectral distribution, and, as a result, separability among classes may have decreased. Separability can be better understood by inspecting the distribution of the center and standard deviation of each class in the spectral domain. In the results of kMC, the standard deviation starts in the mid 100 s (Table A1), while in IIkMC, it starts in the late 200 s (Table A2). A larger standard deviation can imply lower separability. Therefore, it will be necessary to reduce the spectral distribution by applying histogram matching among images before clustering.

Nevertheless, the standard deviation of kMC is very different for each image and band, and the large values exceed 3000. This is compared to the standard deviation of IIkMC, which does not exceed the early 2000 s. Therefore, it can be confirmed the result of IIkMC is more stable than that of kMC, even from the view of separability. Moreover, since it is challenging to identify a set of representative class signatures from KMC (i.e., widely distributed class centers and standard deviation among images), IIkMC is considered a better solution.

3.3. Evaluation of Parallel Processing Performance

Parallel processing performance is typically evaluated using two indices, efficiency and speedup, both of which are defined in terms of the processing time versus the number of cores or computing nodes involved (Equation (2)). In the ideal case, speedup is the same as the number of cores or computing nodes, and efficiency should be 1.0. This indicates the increase in execution speed is exactly proportional to the number of cores or computing nodes involved. However, according to Amdahl's law [41], this is not achievable in reality. Reasons for this include unequal workload among cores and nodes, as well as unparallelizable procedures. In addition, in some cases, the efficiency might exceed 1.0; this is called super-linearity. This can occur when processing an exceptional amount of data or when the complexity is beyond the ability of a single core or node [42]. Speedup S_p and efficiency E_p are defined as:

$$S_p = \frac{T_s}{T_p}, E_p = \frac{T_s}{p \cdot T_p} \quad (2)$$

where p is the number of cores (or computing nodes) and T_s and T_p denote the execution times for sequential and parallel processing, respectively.

The execution times were measured for the sequential code, the intra-node code, the GPU-based code, and the GPU-based code with parallel reduction for IIkMC. To calculate the speedup and the efficiency of the intra-node code, T_s was set as the execution time of the sequential code, and T_p was set as that of the intra-node code using all cores. However, since it is ambiguous to define p for the GPU-based code, the efficiency is not presented (Table 5).

Table 5. Execution time, speedup, and efficiency of parallel IIkMC.

Code	# of Cores	Execution Time	Speedup	Efficiency
Sequential	1	5765.18 s	-	-
Intra-node	16	449.27 s	12.83	0.80
GPU	-	225.83 s	25.53	-
GPU-reduction	-	174.37 s	39.00	-

The results are listed in Table 5. Processing with sequential code was very burdensome and required 5765.18 s (=1.6 h) to process 12 images (=2.86 GB). On the contrary, the intra-node code took 449.27 s (=7.5 min). This is about 13 times faster, meaning the task can be finished within an acceptable time. The GPU-based code processed the data 25.53 times faster than sequential code and 2.00 times faster than intra-node code. Furthermore, the GPU-based code with parallel reduction processed 1.53 times faster than the GPU-based code. In this study, sequential addressing, a middle-optimized parallel reduction approach,

was applied. With more optimized reduction approaches, the processing speed will be further improved. Additionally, it can be predicted the speed can be maximized by using multi-GPUs.

Finally, this study verified whether the results obtained using the sequential, intra-node, and GPU-based codes with and without parallel reduction, matched. The class centers of each band and the classified number of pixels of the results were compared. No discrepancy was detected among the results, confirming they matched completely.

3.4. Discussion

Applying kMC and IIkMC to 12 planetscope images revealed quite different results. In the results of kMC, using 12 consecutively acquired images that might constitute similar land cover, the number of iterations was significantly different, some images were not clustered appropriately, and some classes were canceled during iteration. Class signatures of kMC proved challenging because choosing a representative one among images would take a lot of work. On the other hand, IIkMC conducted stable clustering while assigning consistent classes to all the images. Although the standard deviations were estimated to be slightly larger, the results were expected to provide a comprehensive result by delivering a single set of class signatures for all images.

Because of its efficiency, kMC is still widely used for unsupervised classification of satellite images. Nevertheless, as the capacity or quantity of images increases, the processing time of IIkMC increases exponentially. The intra-node parallel processing and GPU-based parallel processing succeeded in increasing the speed of IIkMC several times faster than sequential processing. In addition, the performance is further improved with the introduction of parallel reduction and is expected to be enhanced by optimizing parallel reduction and utilizing multi-GPU. Therefore, it will be possible to process data acquired in a more extensive range of areas, including satellite and drone images ranging from hundreds to thousands.

4. Conclusions

In this study, IIkMC was introduced for the unsupervised classification of satellite images acquired in series. The results can be summarized in three points as follows:

- derived a single set of class signatures for multiple satellite images;
- performed complete classification of all images, granting consistent class IDs;
- implemented intra-node and GPU-base parallel processing.

A single set of class signatures was derived, and each image was consistently classified so the classification results were compatible between the images. In addition, some images were completely processed could not be correctly segmented by kMC. However, IIkMC also revealed the possibility the separability among classes could be weakened because wider spectral features from multiple images were merged into each class. Nevertheless, it should be remarked IIkMC provides more reliable results, potentially facilitating overall inspection of multiple images and training data generation for supervised classification or deep learning.

kMC is a computationally intensive algorithm, making it burdensome to apply to large images, which is also the case for IIkMC. With the parallelized IIkMC using multi-cores of a CPU and a GPU, the processing speed could be dramatically improved. Thus, large volumes of satellite images acquired from an extensive range of areas are expected to be plausibly inspected prior to intensive analysis or supervised classification.

For better performance of IIkMC, future works aim to improve the class center management and enhance class separability. The former includes class center initialization along with class separation and integration based on data characteristics, similar to ISODATA clustering. The latter will be achieved by normalizing the radiometric distributions among images. GPU-based approaches will be improved by implementing further optimized parallel reduction, manipulating high-performance operations introduced in cuBLAS [43], and modifying parallel code to fit using multi-GPUs.

Author Contributions: Conceptualization, S.H.; methodology, S.H.; software, S.H.; data curation, J.L.; writing—original draft preparation, S.H.; supervision, S.H.; project administration, J.L. All authors have read and agreed to the published version of the manuscript.

Funding: This research was supported by the consigned research project funded by Korea Aerospace Research Institute, grant number FR22H00W02.

Data Availability Statement: No new data were created or analyzed in this study. Data sharing is not applicable to this article.

Conflicts of Interest: The authors declare no conflicts of interest.

Appendix A

Table A1. Class centers and standard deviations produced by kMC.

Image ID	1		2		3		4		5		6	
	Center	Std. dev.										
Class 1												
Band 1	3281	198	3453	252	3151	171	3229	167	3357	212	3241	152
Band 2	2697	210	2931	285	2535	195	2617	186	2744	229	2636	166
Band 3	1921	230	2193	338	1752	197	1812	203	1919	239	1851	194
Band 4	2862	599	3812	899	2325	499	2412	504	2337	520	2608	467
Class 2												
Band 1	3494	183	4561	475	3495	167	3525	165	3424	145	3538	168
Band 2	3019	205	4164	442	3050	185	3088	187	2892	163	3091	195
Band 3	2301	244	3636	524	2366	245	2401	245	2129	203	2417	264
Band 4	4544	595	4364	759	5048	499	5070	491	3810	387	5022	450
Class 3												
Band 1	4156	306	6701	821	3350	137	3364	125	4091	263	3394	131
Band 2	3656	278	6215	758	2822	147	2835	139	3594	239	2869	143
Band 3	2989	305	5513	824	2095	195	2091	184	2902	255	2139	193
Band 4	3455	396	4894	740	3740	398	3775	386	3357	475	3859	356
Class 4												
Band 1	4326	224	10,072	1130	4053	253	3980	217	3616	203	4066	243
Band 2	3961	224	9576	979	3590	234	3509	205	3175	230	3607	227
Band 3	3462	314	8808	1018	2963	265	2874	248	2466	280	2996	270
Band 4	4494	502	7198	1432	3798	487	3659	461	5024	501	3758	482
Class 5												
Band 1	5061	331	13,581	1378	4602	313	4467	267	4512	285	4638	324
Band 2	4619	246	12,970	941	4215	245	4065	222	4097	241	4261	265
Band 3	4065	369	12,892	1184	3701	301	3539	278	3528	289	3780	329
Band 4	4162	550	11,029	2099	4383	567	4203	493	4100	516	4361	532
Class 6												
Band 1	8127	842	17,241	1815	5503	464	5291	373	5359	365	5694	517
Band 2	7597	750	14,967	828	5046	342	4833	284	4907	296	5238	406
Band 3	6754	842	16,878	1484	4466	416	4232	367	4288	370	4632	475
Band 4	5764	1043	13,809	2638	4428	618	4158	567	4030	593	4409	607
Class 7												
Band 1	6150	580	20,635	1493	7465	840	8833	1262	6655	641	7863	1024
Band 2	5606	428	15,570	1058	6913	749	8261	1068	6196	569	7289	943
Band 3	4858	520	19,338	1590	6159	824	7424	1098	5537	637	6474	1045
Band 4	4525	616	18,004	1866	5385	923	5477	761	4530	582	5179	805
Class 8												
Band 1	11,536	1969	19,443	2192	11,215	1650	6590	570	10,538	1946	15,141	3121
Band 2	11,066	1517	14,170	1030	10,759	1404	6077	478	9924	1753	12,943	1219
Band 3	10,633	2014	18,900	1635	10,407	1773	5355	609	9275	2128	13,824	3245
Band 4	9115	1938	26,417	2234	9123	1895	4585	567	6666	1819	10,612	2478
Image ID	7		8		9		10		11		12	
	Center	Std. dev.										
Class 1												
Band 1	3826	191	3862	219	3887	210	3870	235	3955	198	4031	197
Band 2	3063	214	3079	225	3093	225	3063	246	3191	214	3283	207
Band 3	2114	246	2074	223	2064	242	2016	248	2186	244	2288	230
Band 4	2835	617	2540	657	2365	746	2147	691	2736	699	2994	612

Table A1. *Cont.*

	Class 2											
Band 1	4079	191	4122	244	4108	214	4086	241	4155	195	4256	230
Band 2	3453	214	3480	267	3460	243	3428	278	3519	224	3627	258
Band 3	2607	271	2592	314	2543	288	2500	328	2584	267	2698	308
Band 4	4747	690	4574	688	4528	749	4453	737	4664	659	4765	618
	Class 3											
Band 1	4975	385	4867	312	5179	417	5050	364	4794	276	4686	257
Band 2	4313	355	4137	294	4533	375	4348	339	4161	272	4021	239
Band 3	3456	387	3075	291	3658	422	3359	358	3333	320	3148	266
Band 4	3836	569	2922	479	3865	704	3350	669	3809	536	3552	453
	Class 4											
Band 1	6335	601	5543	369	6491	668	6023	544	5585	357	5245	292
Band 2	5637	519	4851	311	5840	533	5340	448	5011	296	4644	233
Band 3	4746	579	3886	327	4925	644	4395	461	4292	361	3873	273
Band 4	4436	650	3676	620	4427	676	4091	734	4188	571	4057	518
	Class 5											
Band 1	8772	941	6590	515	9018	1164	8044	895	6713	594	9691	1210
Band 2	8017	822	5861	403	8272	955	7342	801	6122	478	9001	1096
Band 3	6960	811	4887	483	7086	1013	6376	900	5376	569	7955	1144
Band 4	5742	988	4145	639	5596	931	5029	912	4559	591	6105	955
	Class 6											
Band 1	12,599	1158	8187	796	14,179	1804	12,563	1876	9361	1489	5956	408
Band 2	11,630	1069	7556	691	13,058	1597	11,595	1735	8693	1352	5371	296
Band 3	10,148	1049	6723	875	11,505	1588	10,171	1635	7794	1392	4635	370
Band 4	7064	1227	5192	856	8182	1518	7232	1538	5843	1136	4397	577
	Class 7											
Band 1	19,047	2628	11,795	1463	19,464	2214	19,536	3024	N/A	N/A	7268	633
Band 2	16,634	1030	11,451	1476	14,886	785	15,930	925	N/A	N/A	6634	503
Band 3	16,940	2590	10,686	1527	18,196	1760	17,435	3092	N/A	N/A	5776	665
Band 4	11,956	1760	7526	1227	15,681	3574	12,068	5175	N/A	N/A	4928	683
	Class 8											
Band 1	22,716	2927	20,948	2854	N/A	N/A	6921	2375	N/A	N/A	20,006	4133
Band 2	16,680	1941	15,563	1294	N/A	N/A	6438	2466	N/A	N/A	14,954	1298
Band 3	20,584	2917	19,057	2716	N/A	N/A	5441	3098	N/A	N/A	17,699	3775
Band 4	5940	1393	16,343	6137	N/A	N/A	22,647	6216	N/A	N/A	8690	6287

Table A2. Class centers and standard deviations produced by IIkMC

		Class 1	Class 2	Class 3	Class 4	Class 5	Class 6	Class 7	Class 8
Band 1	Center	3571	3883	3605	4428	5082	7850	6125	12,043
	Std. dev.	361	343	292	318	373	856	485	2250
Band 2	Center	2853	3365	3011	3838	4552	7227	5510	11,206
	Std. dev.	296	306	230	262	277	733	371	1717
Band 3	Center	1929	2585	2196	3044	3858	6348	4688	10,279
	Std. dev.	240	323	220	301	343	833	477	2171
Band 4	Center	2253	5058	3757	3553	4135	5167	4224	7644
	Std. dev.	526	538	422	554	637	841	641	2075

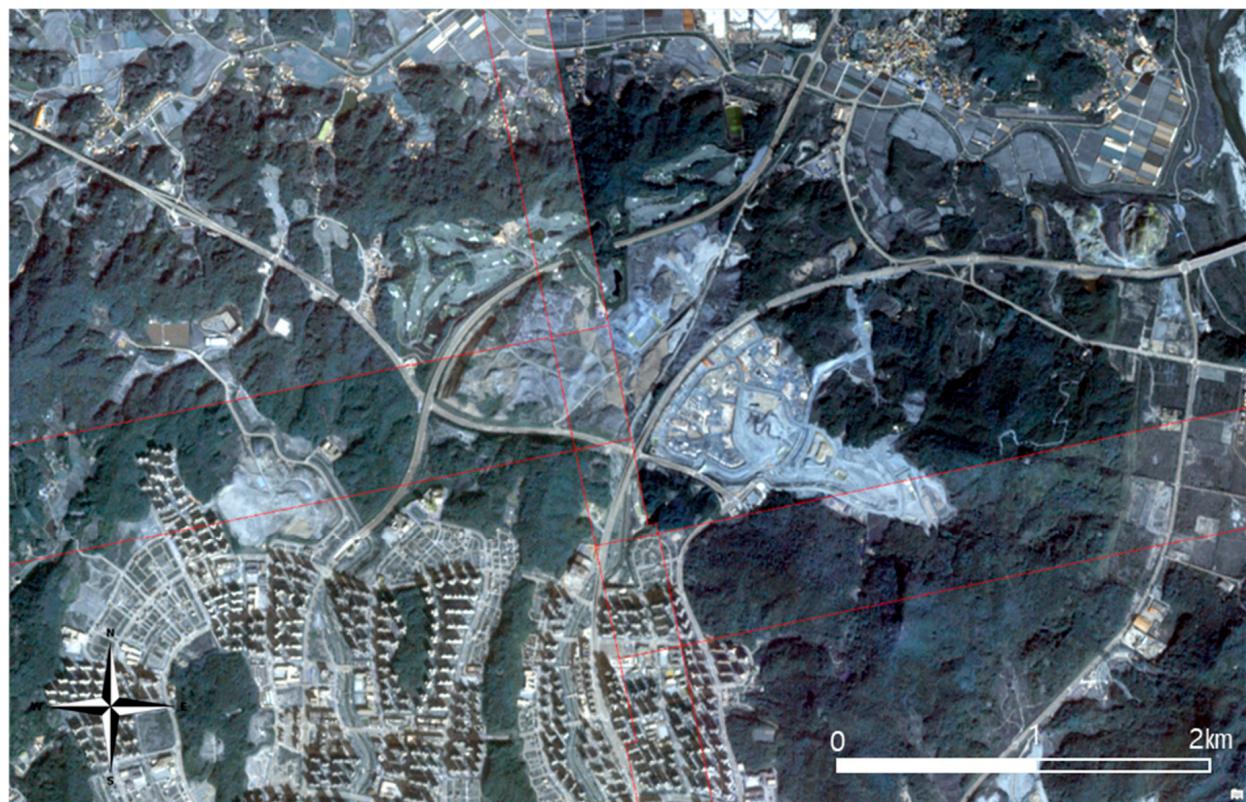


Figure A1. Enlarged view of Figure 7 (a).

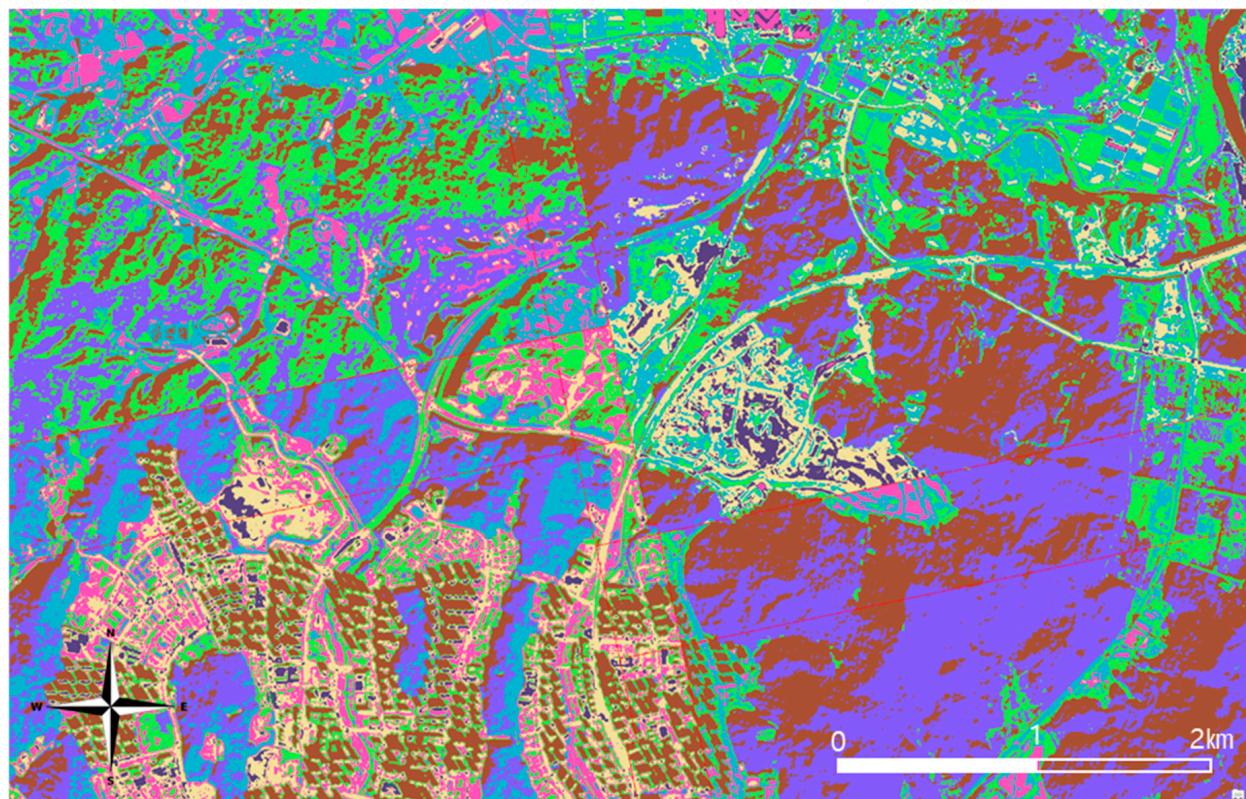


Figure A2. Results of kMC (enlarged view of Figure 8 (a)).

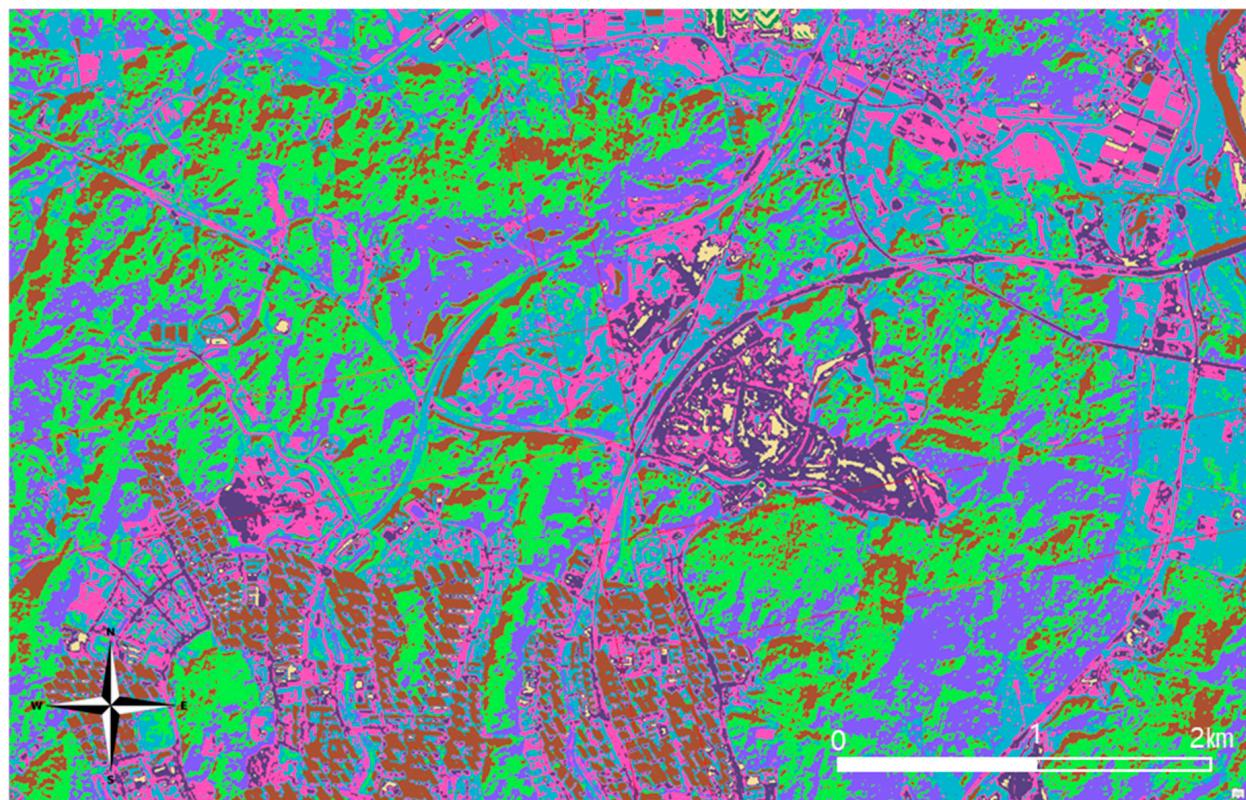


Figure A3. Results of IIkMC (enlarged view of Figure 9 (a)).

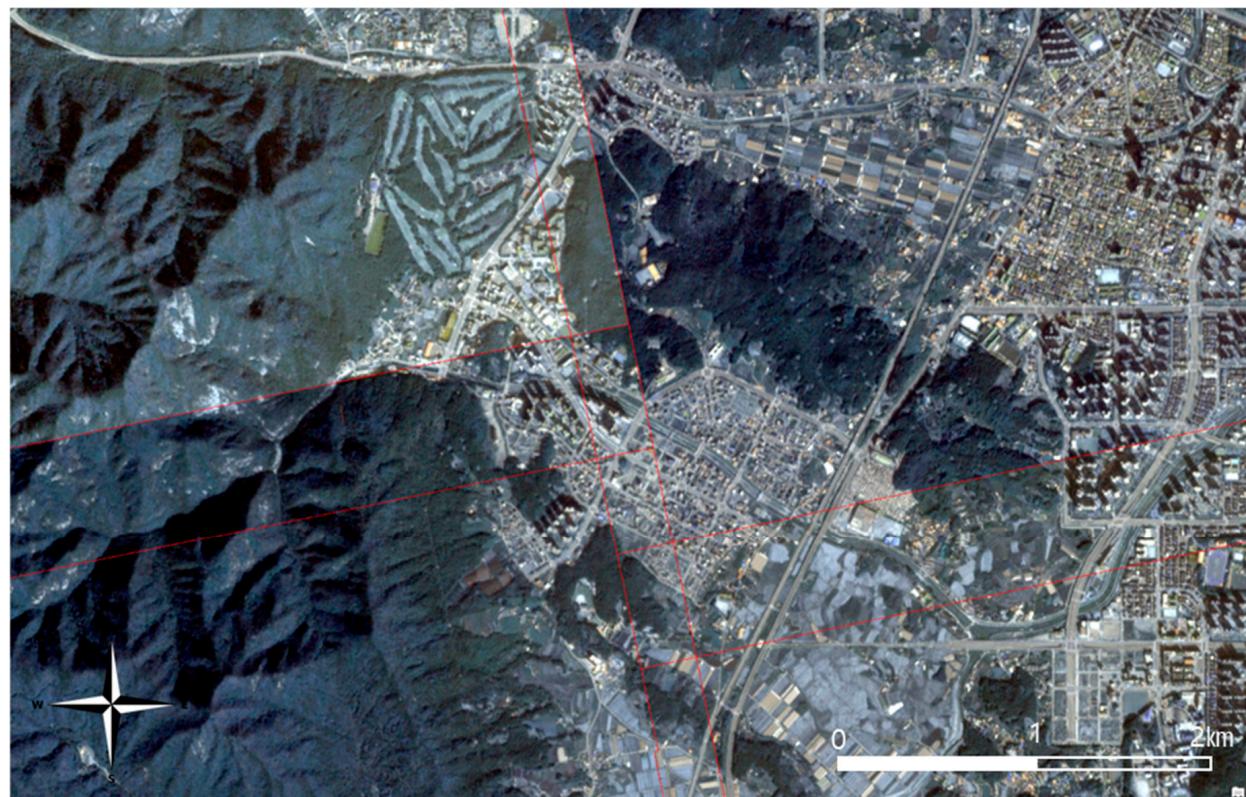


Figure A4. Enlarged view of Figure 7 (b).

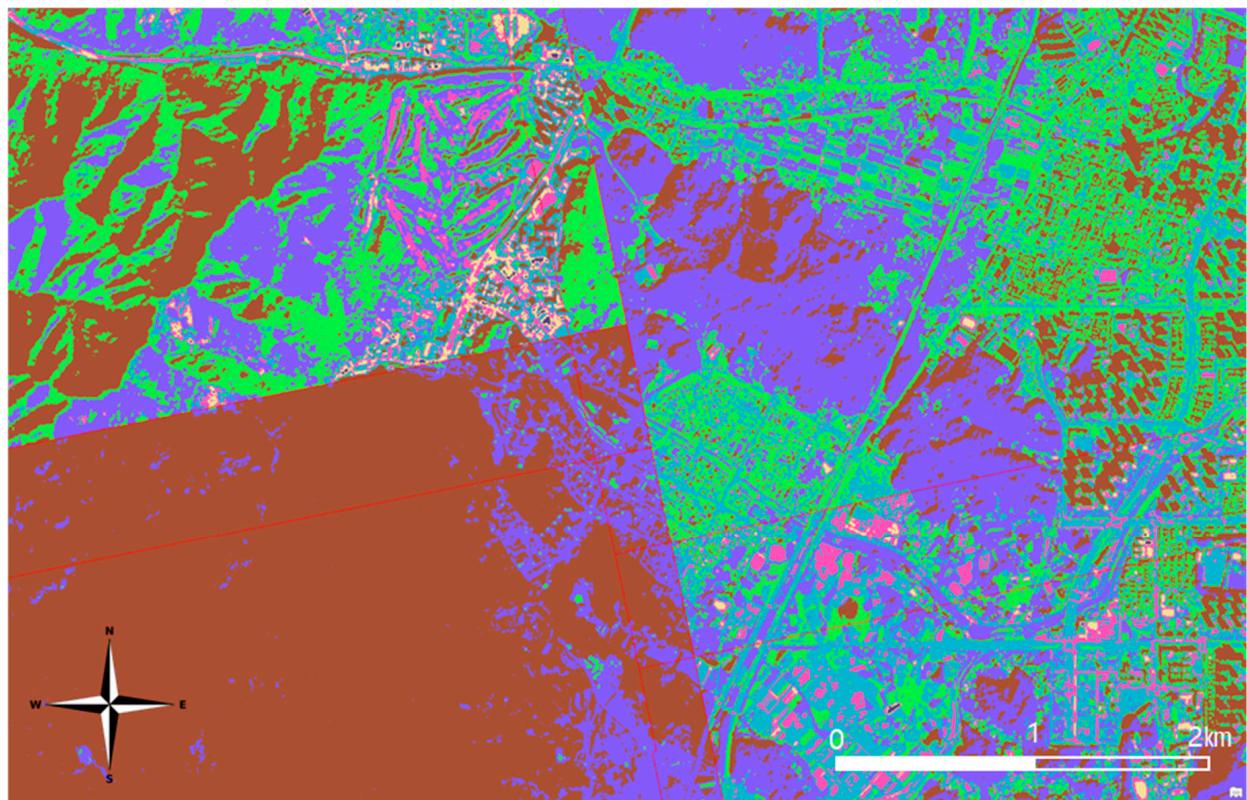


Figure A5. Results of kMC (enlarged view of Figure 8 (b)).

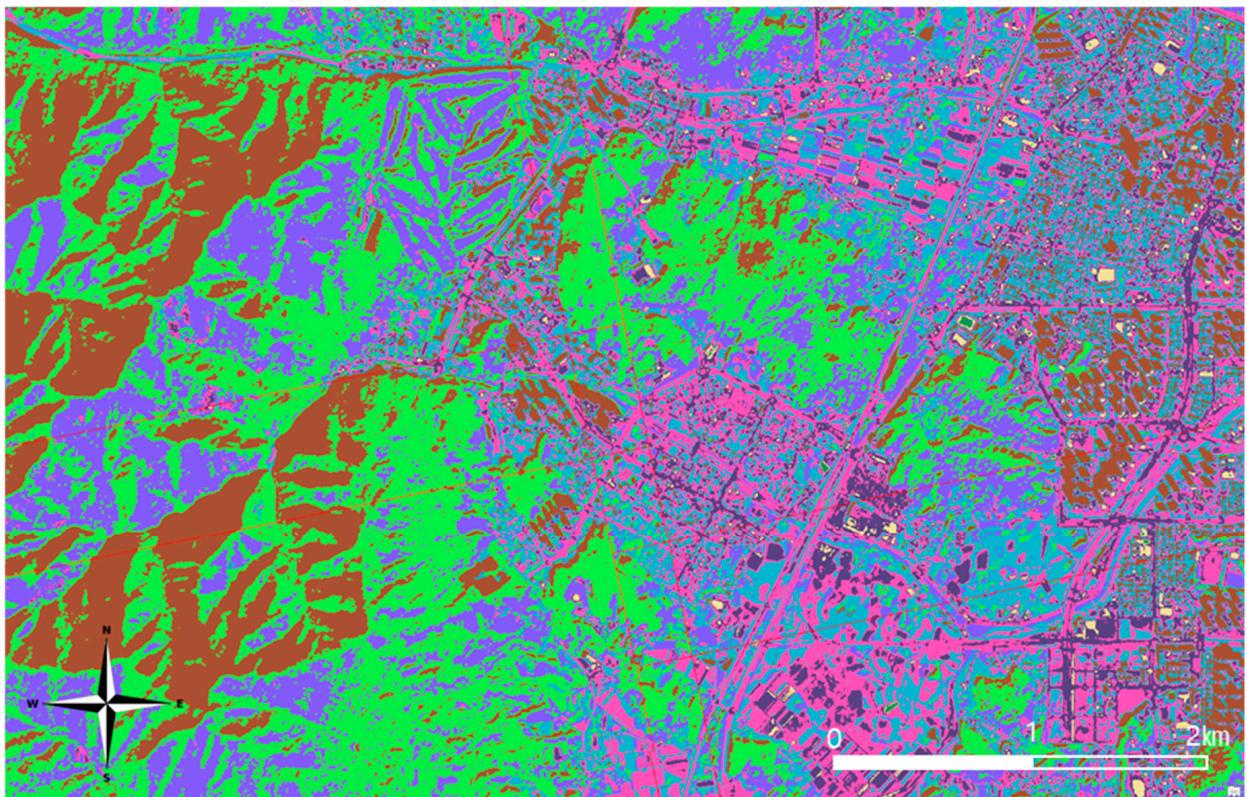


Figure A6. Results of IIkMC (enlarged view of Figure 9 (b)).

References

1. The European Space Agency PlanetScope Overview—Earth Online. Available online: <https://earth.esa.int/eogateway/missions/planetscope/description> (accessed on 11 November 2023).
2. Healey, R.G.; Minetar, M.J.; Dowers, S. (Eds.). *Parallel Processing Algorithms for GIS*; Taylor & Francis Ltd.: London, UK, 1997; ISBN 0-7484-0508-9.
3. Zhao, L.; Chen, L.; Ranjan, R.; Choo, K.-K.R.; He, J. Geographical Information System Parallelization for Spatial Big Data Processing: A Review. *Clust. Comput.* **2016**, *19*, 139–152. [[CrossRef](#)]
4. Plaza, A.J.; Chang, C.-I. *High Performance Computing in Remote Sensing*; Chapman & Hall/CRC: Boca Raton, FL, USA, 2007; ISBN 1-58488-662-5.
5. Bhojne, M.; Chakravarti, A.; Pallav, A.; Sivakumar, V. High Performance Computing for Satellite Image Processing and Analyzing—A Review. *Int. J. Comput. Appl. Technol. Res.* **2013**, *2*, 424–430. [[CrossRef](#)]
6. Cao, V.; Chu, K.; Le-Khac, N.; Kechadi, M.; Laefer, D.; Truong-Hong, L. Toward a New Approach for Massive LiDAR Data Processing. In Proceedings of the 2015 2nd IEEE International Conference on Spatial Data Mining and Geographical Knowledge Services (ICSDM), Fuzhou, China, 8–10 July 2015; Institute of Electrical and Electronics Engineers: Piscataway, NJ, USA; pp. 135–140.
7. Han, S.H.; Heo, J.; Sohn, H.G.; Yu, K. Parallel Processing Method for Airborne Laser Scanning Data Using a PC Cluster and a Virtual Grid. *Sensors* **2009**, *9*, 2555–2573. [[CrossRef](#)] [[PubMed](#)]
8. Gillis, D.; Bowles, J.H.; Bowles, J.H. Parallel Implementation of the ORASIS Algorithm for Remote Sensing Data Analysis. In *High Performance Computing in Remote Sensing*; Chapman & Hall/CRC: Boca Raton, FL, USA, 2007; p. 69.
9. Valencia, D.; Martínez, P.; Plaza, A.; Plaza, J. Parallel Wildland Fire Monitoring and Tracking Using Remotely Sensed Data. In *High Performance Computing in Remote Sensing*; Chapman & Hall/CRC: Boca Raton, FL, USA, 2007; p. 151.
10. González, C.; Resano, J.; Mozos, D.; Plaza, A.; Valencia, D. FPGA Implementation of the Pixel Purity Index Algorithm for Remotely Sensed Hyperspectral Image Analysis. *EURASIP J. Adv. Signal Process.* **2010**, *2010*, 969806. [[CrossRef](#)]
11. Plaza, A.; Valencia, D.; Plaza, J.; Martinez, P. Commodity Cluster-Based Parallel Processing of Hyperspectral Imagery. *J. Parallel Distrib. Comput.* **2006**, *66*, 345–358. [[CrossRef](#)]
12. Sánchez, S.; Plaza, A. GPU Implementation of the Pixel Purity Index Algorithm for Hyperspectral Image Analysis. In Proceedings of the 2010 IEEE International Conference on Cluster Computing Workshops and Posters (CLUSTER WORKSHOPS), Heraklion, Greece, 20–24 September 2010; Institute of Electrical and Electronics Engineers: Piscataway, NJ, USA; pp. 1–7.
13. Koo, I.H. High-Speed Processing of Satellite Image Using GPU. Master’s Thesis, Chungnam National University, Daejeon, Republic of Korea, 2012.
14. Sun, X.; Li, M.; Liu, Y.; Tan, L.; Liu, W. Accelerated Segmentation Approach with CUDA for High Spatial Resolution Remotely Sensed Imagery Based on Improved Mean Shift. In Proceedings of the 2009 Joint Urban Remote Sensing Event, Shanghai, China, 20–22 May 2009; Institute of Electrical and Electronics Engineers: Piscataway, NJ, USA; pp. 1–6.
15. Lu, Y.; Gao, Q.; Chen, S.; Sun, D.; Xia, Y.; Peng, X. Fast Implementation of Image Mosaicing on GPU. In Proceedings of the 2017 10th International Congress on Image and Signal Processing, BioMedical Engineering and Informatics (CISP-BMEI), Shanghai, China, 14–16 October 2017; Institute of Electrical and Electronics Engineers: Piscataway, NJ, USA; pp. 1–5.
16. Fredj, H.B.; Ltaif, M.; Ammar, A.; Souani, C. Parallel Implementation of Sobel Filter Using CUDA. In Proceedings of the 2017 International Conference on Control, Automation and Diagnosis (ICCAD), Hammamet, Tunisia, 19–21 January 2017; Institute of Electrical and Electronics Engineers: Piscataway, NJ, USA; pp. 209–212.
17. Sugumaran, R.; Hegeman, J.W.; Sardeshmukh, V.B.; Armstrong, M.P.; Hegeman, J.W.; Sardeshmukh, V.B.; Armstrong, M.P. Processing Remote-Sensing Data in Cloud Computing Environments. In *Remote Sensing Handbook—Three Volume Set*; CRC Press: Boca Raton, FL, USA, 2018.
18. Wang, P.; Wang, J.; Chen, Y.; Ni, G. Rapid Processing of Remote Sensing Images Based on Cloud Computing. *Future Gener. Comput. Syst.* **2013**, *29*, 1963–1968. [[CrossRef](#)]
19. Mishra, B.; Dahal, A.; Luintel, N.; Shahi, T.B.; Panthi, S.; Pariyar, S.; Ghimire, B.R. Methods in the Spatial Deep Learning: Current Status and Future Direction. *Spat. Inf. Res.* **2022**, *30*, 215–232. [[CrossRef](#)]
20. Alzubaidi, L.; Zhang, J.; Humaidi, A.J.; Al-Dujaili, A.; Duan, Y.; Al-Shamma, O.; Santamaría, J.; Fadhel, M.A.; Al-Amidie, M.; Farhan, L. Review of Deep Learning: Concepts, CNN Architectures, Challenges, Applications, Future Directions. *J. Big Data* **2021**, *8*, 53. [[CrossRef](#)] [[PubMed](#)]
21. Haroun, F.M.E.; Deros, S.N.M.; Din, N.M. Detection and Monitoring of Power Line Corridor From Satellite Imagery Using RetinaNet and K-Mean Clustering. *IEEE Access* **2021**, *9*, 116720–116730. [[CrossRef](#)]
22. Ali, I.; Rehman, A.U.; Khan, D.M.; Khan, Z.; Shafiq, M.; Choi, J.-G. Model Selection Using K-Means Clustering Algorithm for the Symmetrical Segmentation of Remote Sensing Datasets. *Symmetry* **2022**, *14*, 1149. [[CrossRef](#)]
23. Pugazhenthi, A.; Kumar, L.S. Cloud Extraction from INSAT-3D Satellite Image by K-Means and Fuzzy C-Means Clustering Algorithms. In Proceedings of the 2020 International Conference on System, Computation, Automation and Networking (ICSCAN), Pondicherry, India, 3–4 July 2020; pp. 1–4.
24. Guo, W.; Zhang, W.; Zhang, Z.; Tang, P.; Gao, S. Deep Temporal Iterative Clustering for Satellite Image Time Series Land Cover Analysis. *Remote Sens.* **2022**, *14*, 3635. [[CrossRef](#)]

25. Lemenkova, P.; Debeir, O. R Libraries for Remote Sensing Data Classification by K-Means Clustering and NDVI Computation in Congo River Basin, DRC. *Appl. Sci.* **2022**, *12*, 12554. [[CrossRef](#)]
26. Venkata Dasu, M.; Reddy, P.V.N.; Chandra Mohan Reddy, S. Classification of Remote Sensing Images Based on K-Means Clustering and Artificial Bee Colony Optimization. In *Advances in Cybernetics, Cognition, and Machine Learning for Communication Technologies*; Gunjan, V.K., Senatore, S., Kumar, A., Gao, X.-Z., Merugu, S., Eds.; Lecture Notes in Electrical Engineering; Springer: Singapore, 2020; pp. 57–65. ISBN 9789811531255.
27. Shahrin, F.; Zahin, L.; Rahman, R.; Hossain, A.J.; Kaf, A.H.; Abdul Malek Azad, A.K.M. Agricultural Analysis and Crop Yield Prediction of Habiganj Using Multispectral Bands of Satellite Imagery with Machine Learning. In Proceedings of the 2020 11th International Conference on Electrical and Computer Engineering (ICECE), Dhaka, Bangladesh, 17–19 December 2020; pp. 21–24.
28. Waleed, M.; Um, T.-W.; Khan, A.; Khan, U. Automatic Detection System of Olive Trees Using Improved K-Means Algorithm. *Remote Sens.* **2020**, *12*, 760. [[CrossRef](#)]
29. Gaikwad, S.V.; Vibhute, A.D.; Kale, K.V.; Mane, A.V. Vegetation Cover Classification Using Sentinel-2 Time-Series Images and K-Means Clustering. In Proceedings of the 2021 IEEE Bombay Section Signature Conference (IBSSC), Gwalior, India, 18–20 November 2021; pp. 1–6.
30. Nga, P.T.T.; Ha, P.T.; Hang, V.T. Satellite-Based Regionalization of Solar Irradiation in Vietnam by k-Means Clustering. *J. Appl. Meteorol. Climatol.* **2021**, *60*, 391–402. [[CrossRef](#)]
31. Hartigan, J.A.; Wong, M.A. Algorithm AS 136: A k-Means Clustering Algorithm. *J. R. Stat. Soc. Ser. C Appl. Stat.* **1979**, *28*, 100–108. [[CrossRef](#)]
32. Fräntti, P.; Sieranoja, S. How Much Can K-Means Be Improved by Using Better Initialization and Repeats? *Pattern Recognit.* **2019**, *93*, 95–112. [[CrossRef](#)]
33. Han, S. Parallel Processing of K-means Clustering Algorithm for Unsupervised Classification of Large Satellite Imagery. *J. Korean Soc. Surv. Geod. Photogramm. Cartogr.* **2017**, *35*, 187–194. [[CrossRef](#)]
34. OpenMP OpenMP API Specification: Version 5.0. 2018. Available online: <https://www.openmp.org/spec-html/5.0/openmp.html> (accessed on 11 November 2023).
35. Argonne National Laboratory the Message Passing Interface (MPI) Standard. Available online: <https://www.mcs.anl.gov/research/projects/mpi/> (accessed on 11 November 2023).
36. Farivar, R.; Rebollo, D.; Chan, E.; Campbell, R.H. A Parallel Implementation of K-Means Clustering on GPUs. In Proceedings of the 2008 International Conference on Parallel and Distributed Processing Techniques and Applications, PDPTA 2008, Las Vegas, NV, USA, 14–17 July 2008; CSREA Press: Red Hook, NY, USA, 2008; pp. 340–345.
37. Zhao, W.; Ma, H.; He, Q. Parallel K-Means Clustering Based on MapReduce. In Proceedings of the IEEE International Conference on Cloud Computing, Beijing, China, 1–4 December 2009; Jaatun, M.G., Zhao, G., Rong, C., Eds.; Springer: Berlin/Heidelberg, Germany, 2009; pp. 674–679.
38. Kang, S.J.; Lee, S.Y.; Lee, K.M. Performance Comparison of OpenMP, MPI, and MapReduce in Practical Problems. *Adv. Multimed.* **2015**, *2015*, 9. [[CrossRef](#)]
39. Intel Avoiding and Identifying False Sharing Among Threads. Available online: <https://www.intel.com/content/www/us/en/developer/topic-technology/data-center/overview.html> (accessed on 11 November 2023).
40. Harris, M. Optimizing Parallel Reduction in CUDA. Available online: <https://developer.download.nvidia.com/assets/cuda/files/reduction.pdf> (accessed on 11 November 2023).
41. Gustafson, J.L. Amdahl's Law. In *Encyclopedia of Parallel Computing*; Padua, D., Ed.; Springer US: Boston, MA, USA, 2011; pp. 53–60. ISBN 978-0-387-09766-4.
42. Ristov, S.; Prodan, R.; Gusev, M.; Skala, K. *Superlinear Speedup in HPC Systems: Why and When?* Institute of Electrical and Electronics Engineers: Piscataway, NJ, USA, 2016; pp. 889–898.
43. NVIDIA Developer cuBLAS. Available online: <https://developer.nvidia.com/cublas> (accessed on 11 December 2023).

Disclaimer/Publisher's Note: The statements, opinions and data contained in all publications are solely those of the individual author(s) and contributor(s) and not of MDPI and/or the editor(s). MDPI and/or the editor(s) disclaim responsibility for any injury to people or property resulting from any ideas, methods, instructions or products referred to in the content.