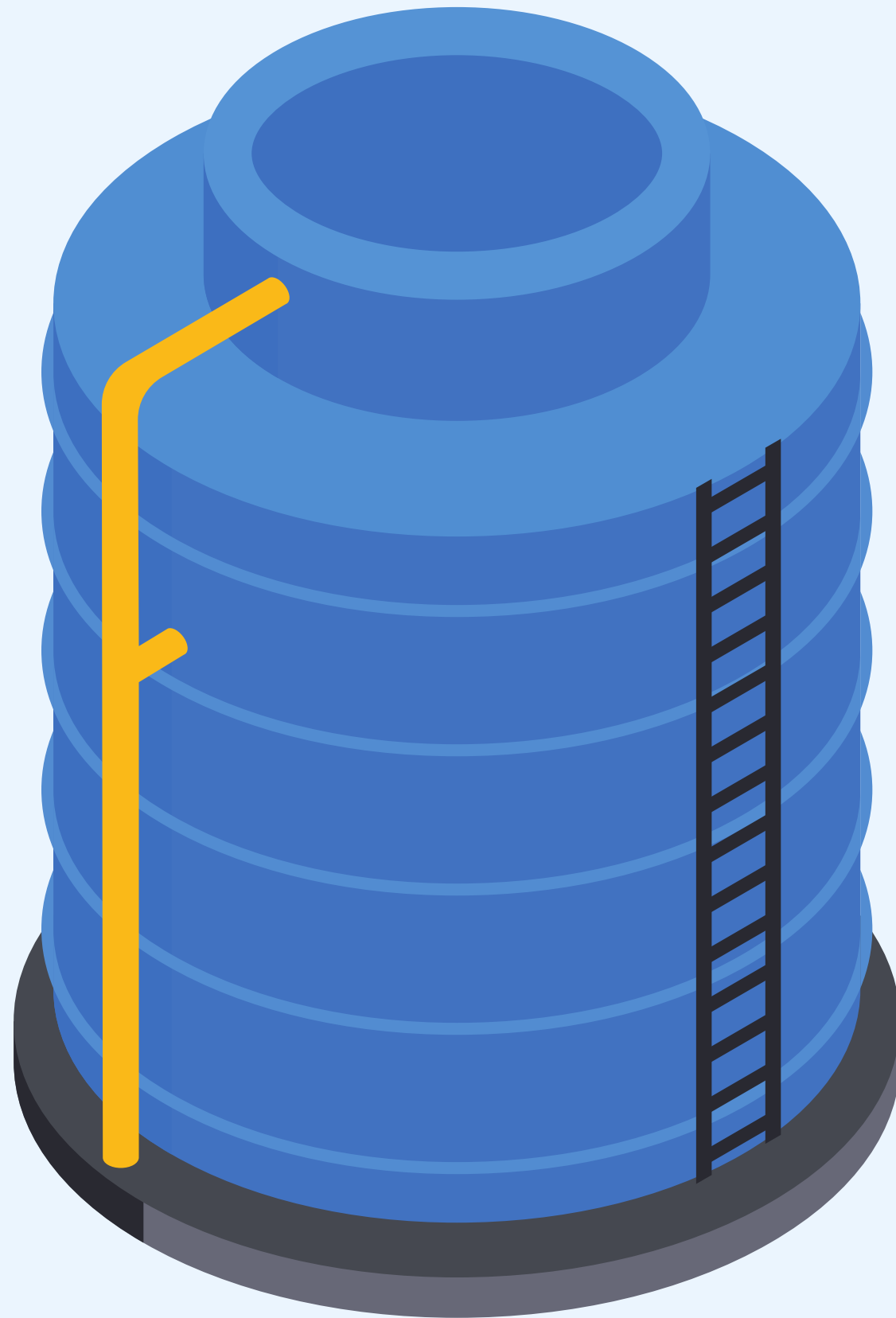


MCTA4362

MACHINE LEARNING - MINI PROJECT

WATER LEVEL CONTROL IN TANK



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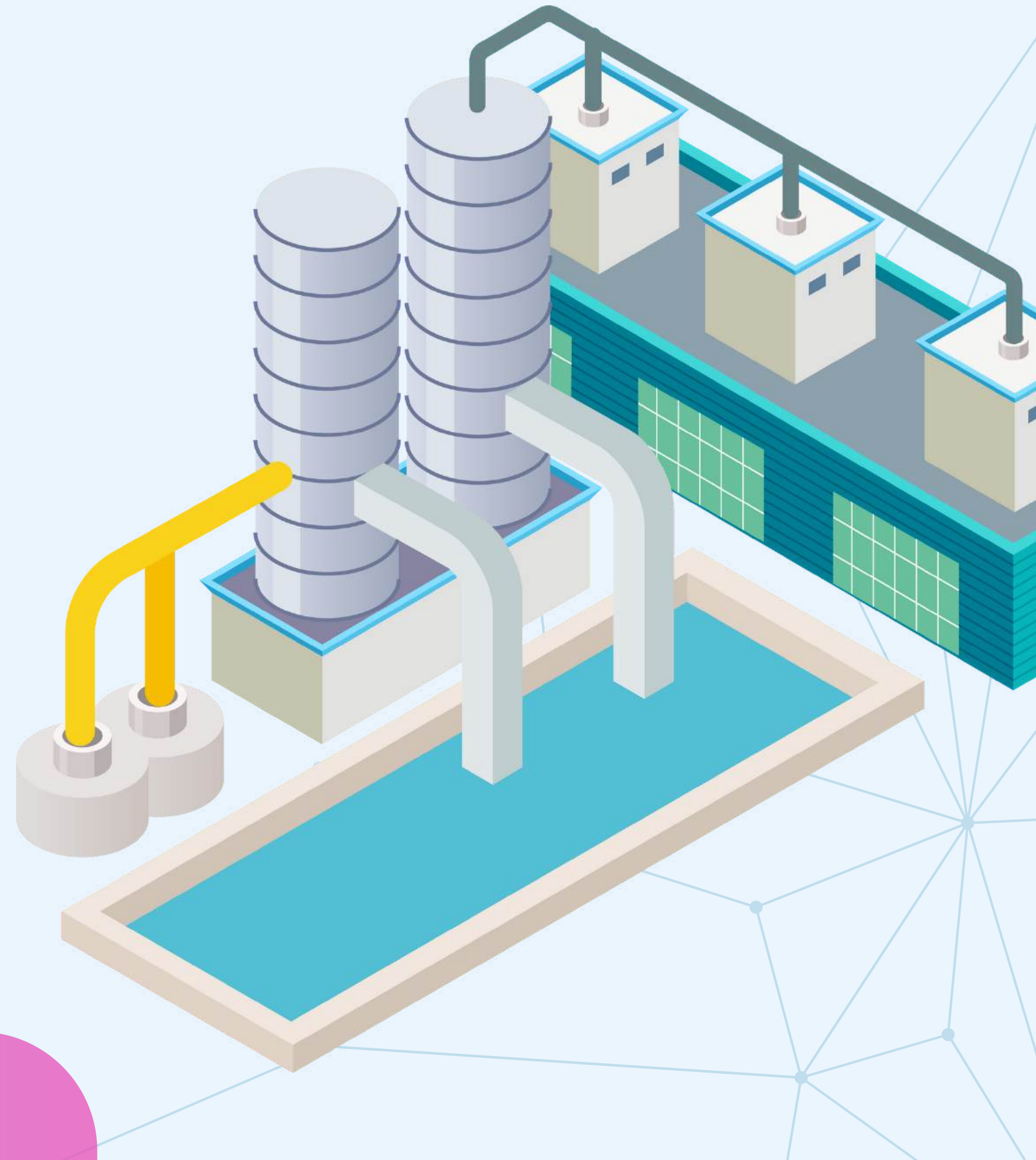


Maisara
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Problem Statement

The nonlinear nature of water flow and dynamics in a tank system makes it difficult for **conventional PID controllers** to maintain accurate water level regulation under varying conditions .

To solve this problem, we aim to implement a **reinforcement learning-based controller** for a nonlinear water tank level system and evaluate its performance against a traditional PID controller.



System Modelling

- Simulates a water tank with controlled inflow and gravity-driven outflow.
- Commonly used in fluid level control problems (chemical plants, irrigation, etc.).
- Nonlinearity introduced by outflow being proportional to \sqrt{H} (Torricelli's law).
- Serves as a benchmark system for comparing PID and Reinforcement Learning controllers.
- Implemented in Simulink for real-time simulation and control analysis.

Mathematical Model

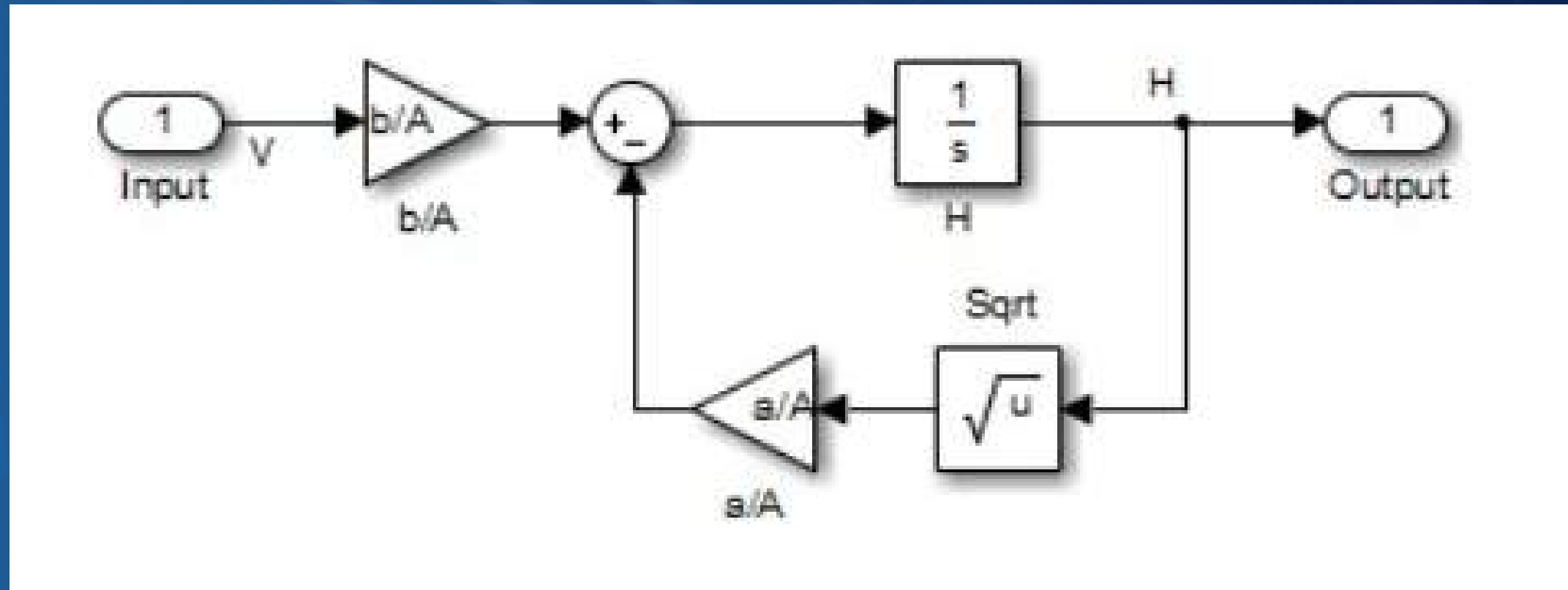
$$\frac{dH(t)}{dt} = \frac{1}{A} \left(V(t) - a\sqrt{H(t)} \right)$$

FIRST ORDER NONLINEAR DIFFERENTIAL EQUATION

- $H(t)$: Tank water level (output)
- $V(t)$: Inflow (control input)
- A : Tank cross-sectional area
- a : Outflow coefficient (gravity-driven)
- Captures balance between controlled inflow and nonlinear outflow



Simulation Block Diagram



- In1 (Input): Receives control input $V(t)$ from the controller (e.g. PID or RL)
- Gain (b/A): Scales the inflow according to the tank's cross-sectional area
- Sum (+ -): Computes net flow: inflow – outflow
- Integrator: Integrates net flow to calculate water level $H(t)$
- Sqrt: Calculates \sqrt{H} to model gravity-driven outflow (Torricelli's law)
- Gain (a/A): Scales the outflow rate using outflow coefficient a
- Out1 (Output): Outputs the current water level for feedback or display



Control Objectives

- To implement and tune a PID controller
- To train an RL agent for adaptive control
- To evaluate and compare their performance. Use key metrics like rise time, overshoot, and settling time

Assumptions & Parameters

- Ideal actuator and sensor (no delay/noise)
- No leakage or external disturbances
- Constant fluid properties (incompressible water)
- Vertical tank with constant area
- Tank area $A=4.0 \text{ m}^2$
- Outflow coefficient $a=0.4$
- Inflow gain $b=1.0$
- $b/A=0.25$, $a/A=0.1$, and initial level $H_0=0$
- These values help simulate realistic yet controllable water level behavior

PI Controller

- The tank dynamics include a square-root relationship in the outflow, introducing nonlinearity that complicates analytical control.
- PI controller was selected to regulate the water level in a nonlinear tank system.

Controller: Form:

Time domain:
☒ Continuous-time
☐ Discrete-time

Discrete-time settings
Sample time (-1 for inherited):

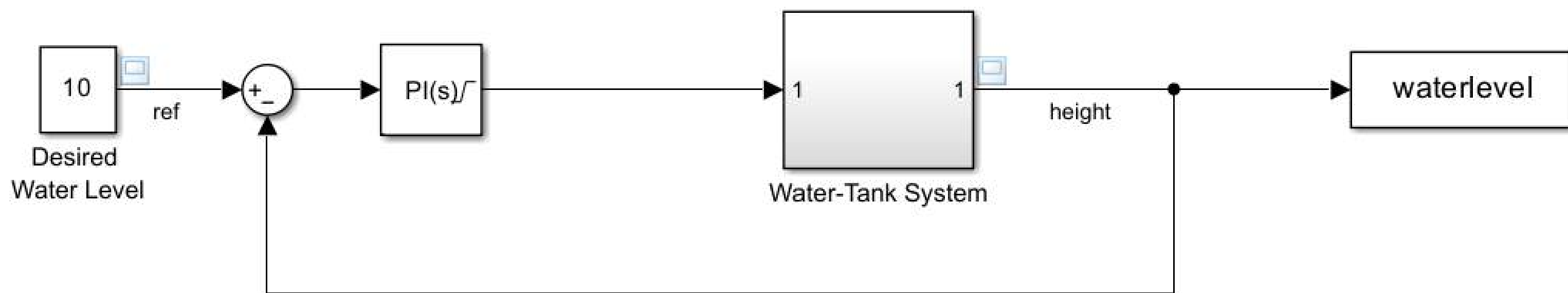
Compensator formula
$$P + I \frac{1}{s}$$

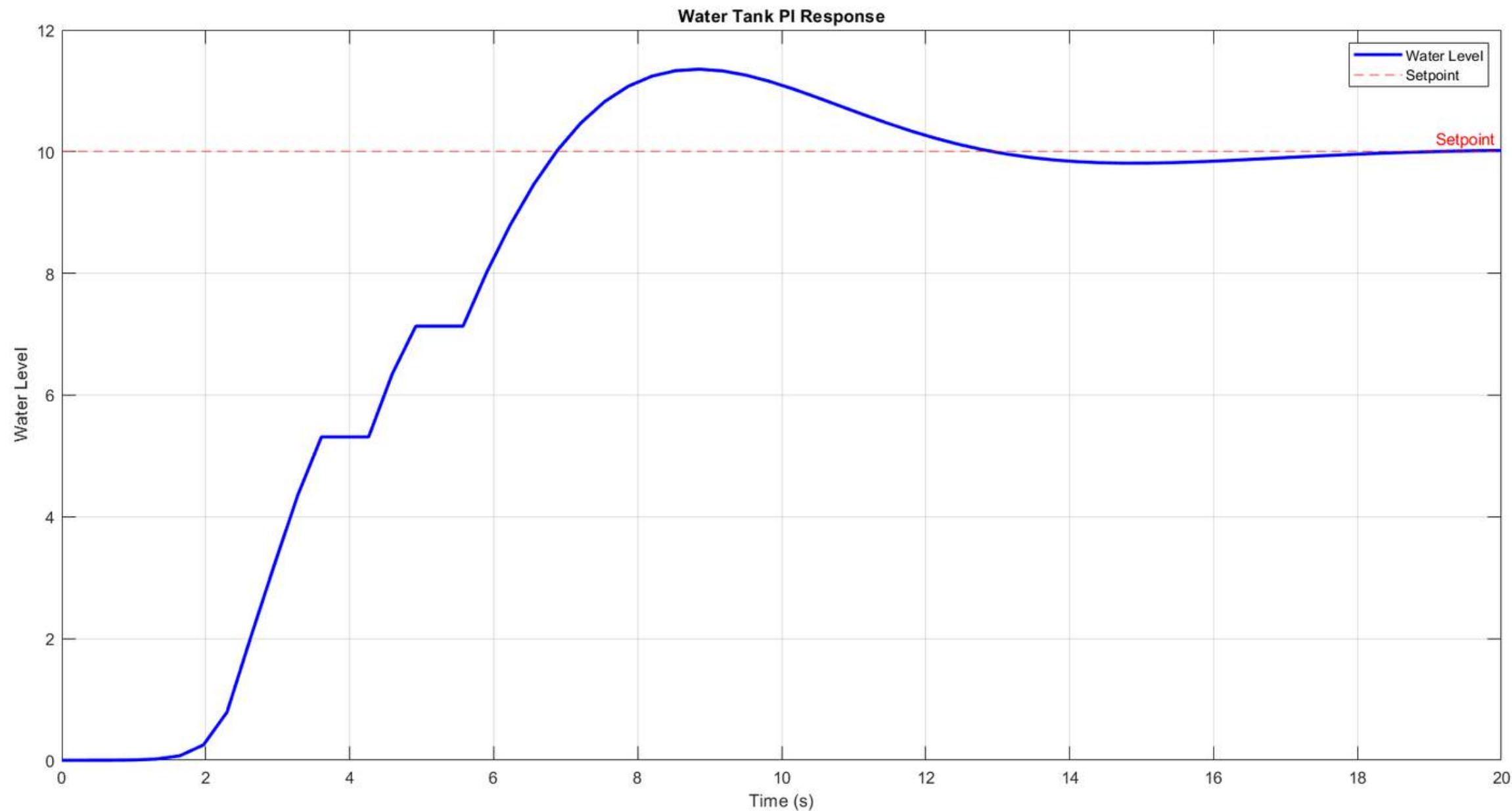
Main Initialization Saturation Data Types State Attributes

Controller parameters
Source:

Proportional (P):

Integral (I): ☐ Use I*Ts (optimal for codegen)





Command Window

```
>> watertank_pi_metrics  
Performance Metrics:  
Rise Time: 3.9791 seconds  
Settling Time: 12.2020 seconds  
Overshoot: 13.55 %  
Peak Time: 8.8525 seconds  
Mean Squared Error (MSE): 16.846315  
fx >>
```

**Plot showing water tank
PI controller response**

**Metrics
performance**

RL Controller for Water Tank System using DDPG



Objective: Design a controller to regulate water level in a tank using RL

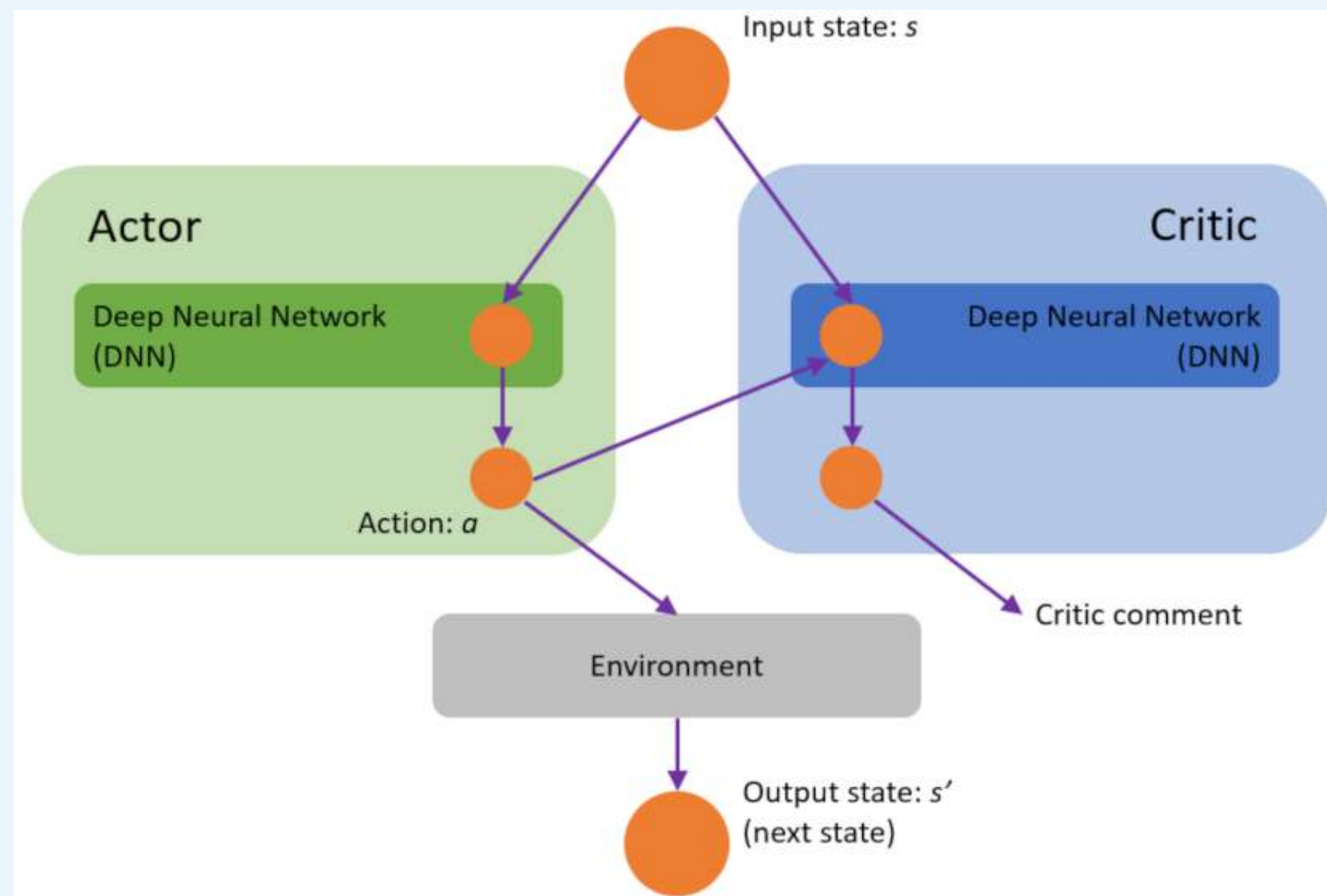
Approach: Implement Deep Deterministic Policy Gradient DDPG in Simulink environment

Key Components:

- RL Agent Design
- Reward Engineering
- Simulation and Training
- Performance Evaluation

Why DDPG and Environment Design

Deep Deterministic Policy Gradient (DDPG) architecture



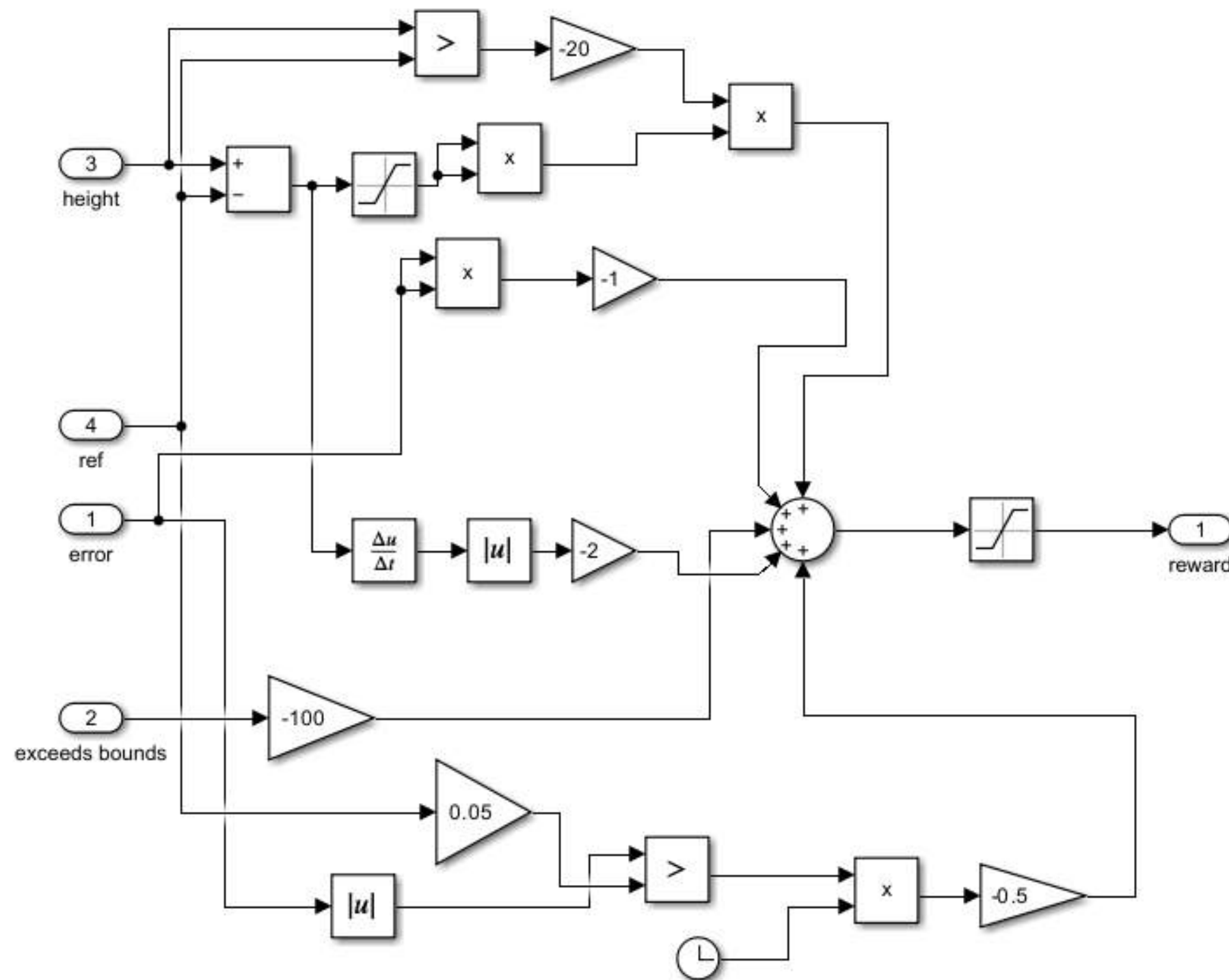
Why Deep Deterministic Policy Gradient (DDPG):

- Suitable for continuous state/action spaces
- Proven in physical control tasks
- Supported by MATLAB RL Toolbox

Environment Design:

- **State Space:**
 - Water height
 - Error from reference
 - Derivative of error
 - Boolean: within $\pm 5\%$ tolerance
- **Action space**
 - Valve opening: continuous scalar $[0,1]$

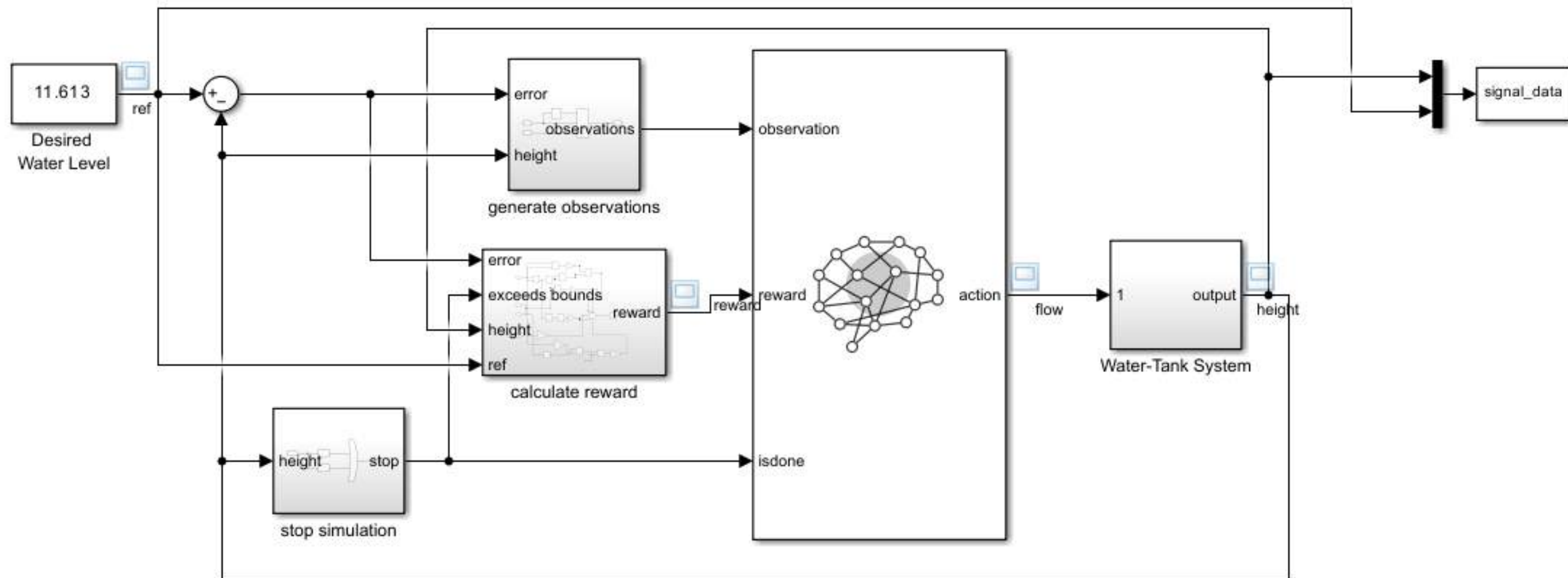
Reward Design



- Accurate reference tracking
- Penalize
 - Overshoot
 - Oscillation
 - Settling time delay
 - Exceeding bounds

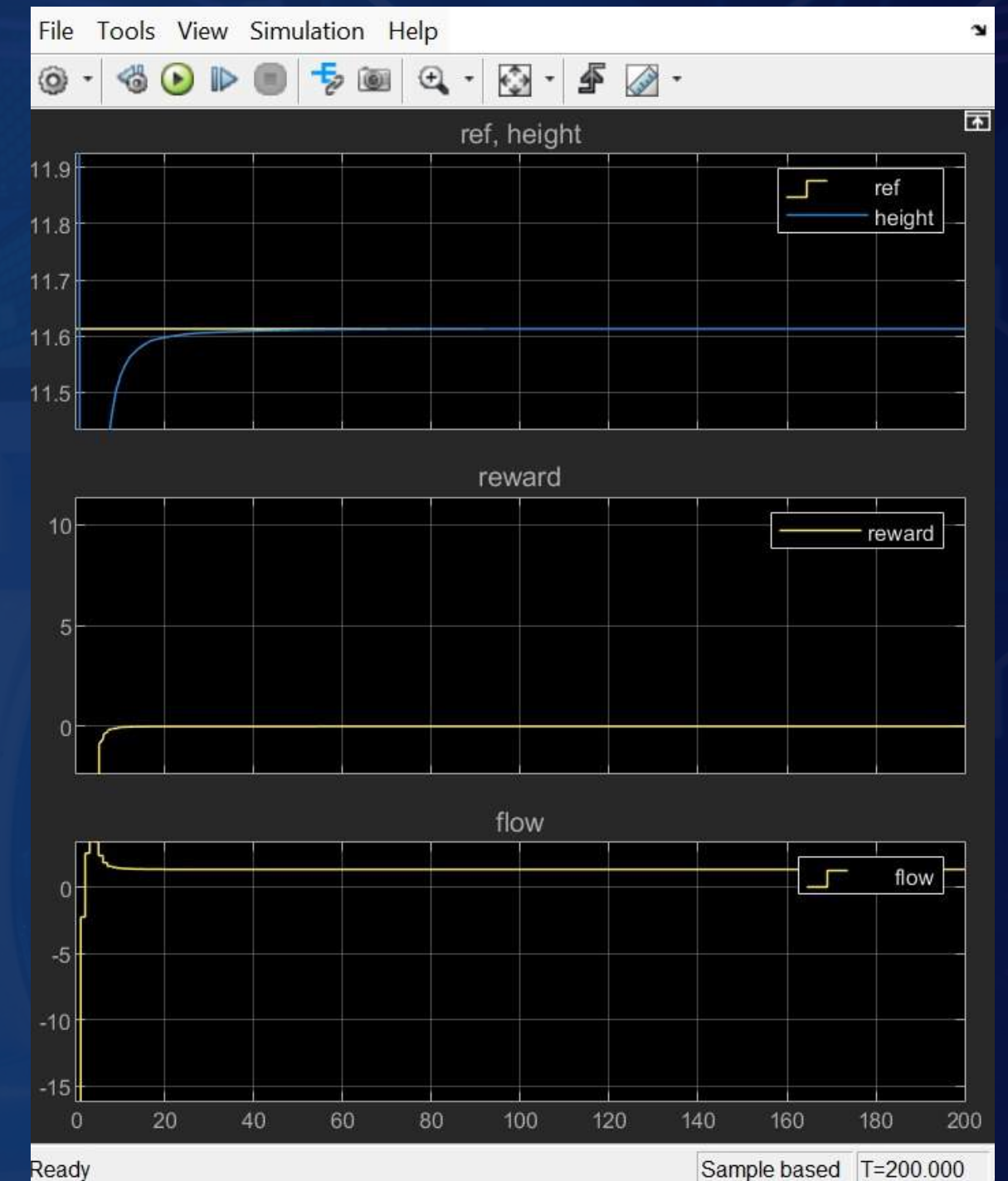
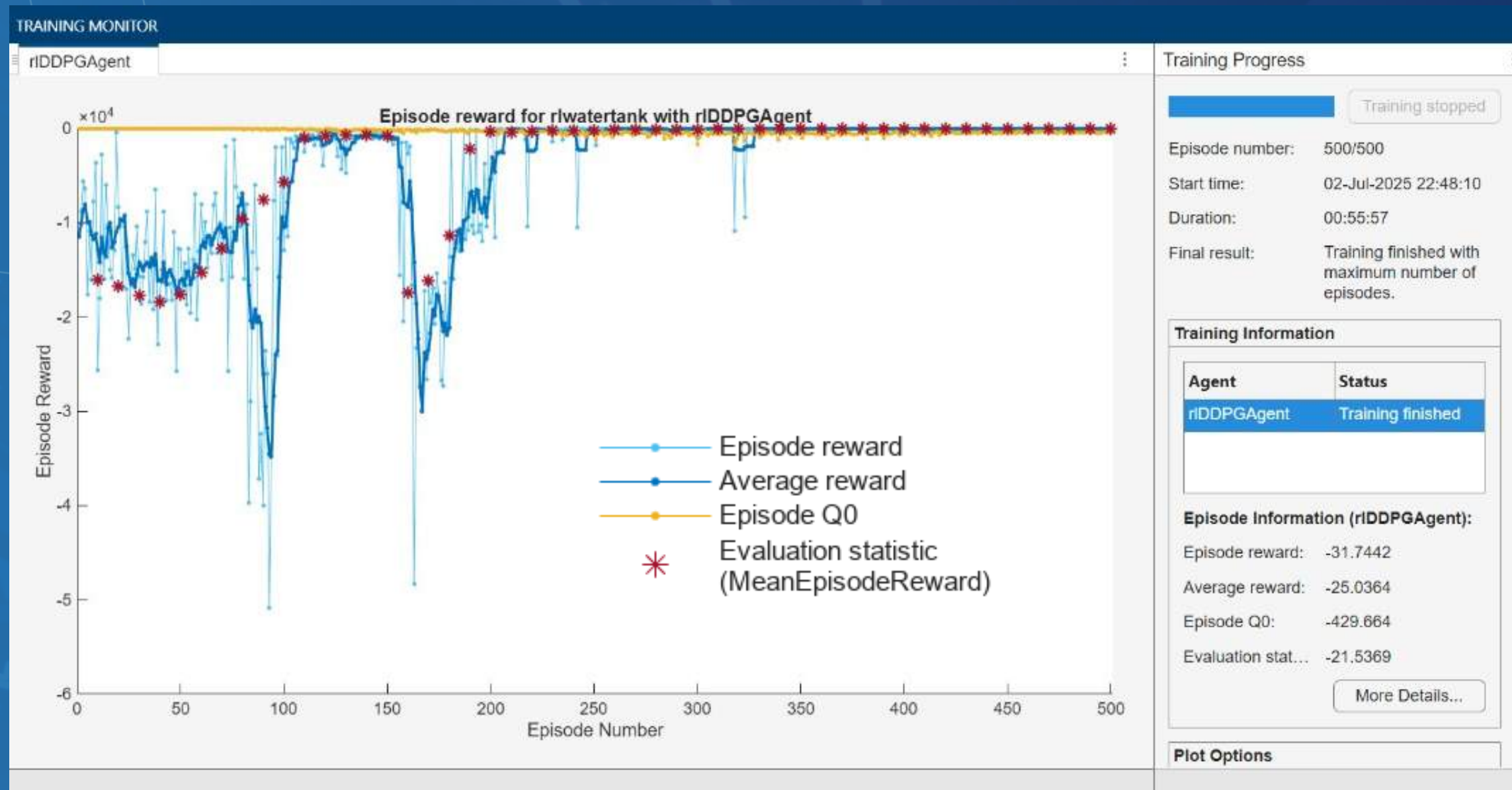
• Reward Formula:
$$R = -[(h - h_{ref})^2 + \alpha u^2 + \beta(\text{overshoot})^2 + \gamma(\text{dError})^2 + \delta t \times \text{unsettled} + \text{hard penalty}]$$

Training Setup



- RL Agent Block
 - contains actor and critic networks
 - input: observation, reward, isdone
 - output: action (flow rate)
- Generate observations
- Desired water level
- Calculate Reward
- stop simulation
- water-tank system

Simulation and Learning Process



Performance metric

Performance Metrics (RL Controller):

- Rise Time : 0.00 seconds
- Settling Time : 200.00 seconds
- Overshoot : 54.96 %
- Undershoot : 11.39 %
- MSE : 0.1909

PI vs RL

Testing phase

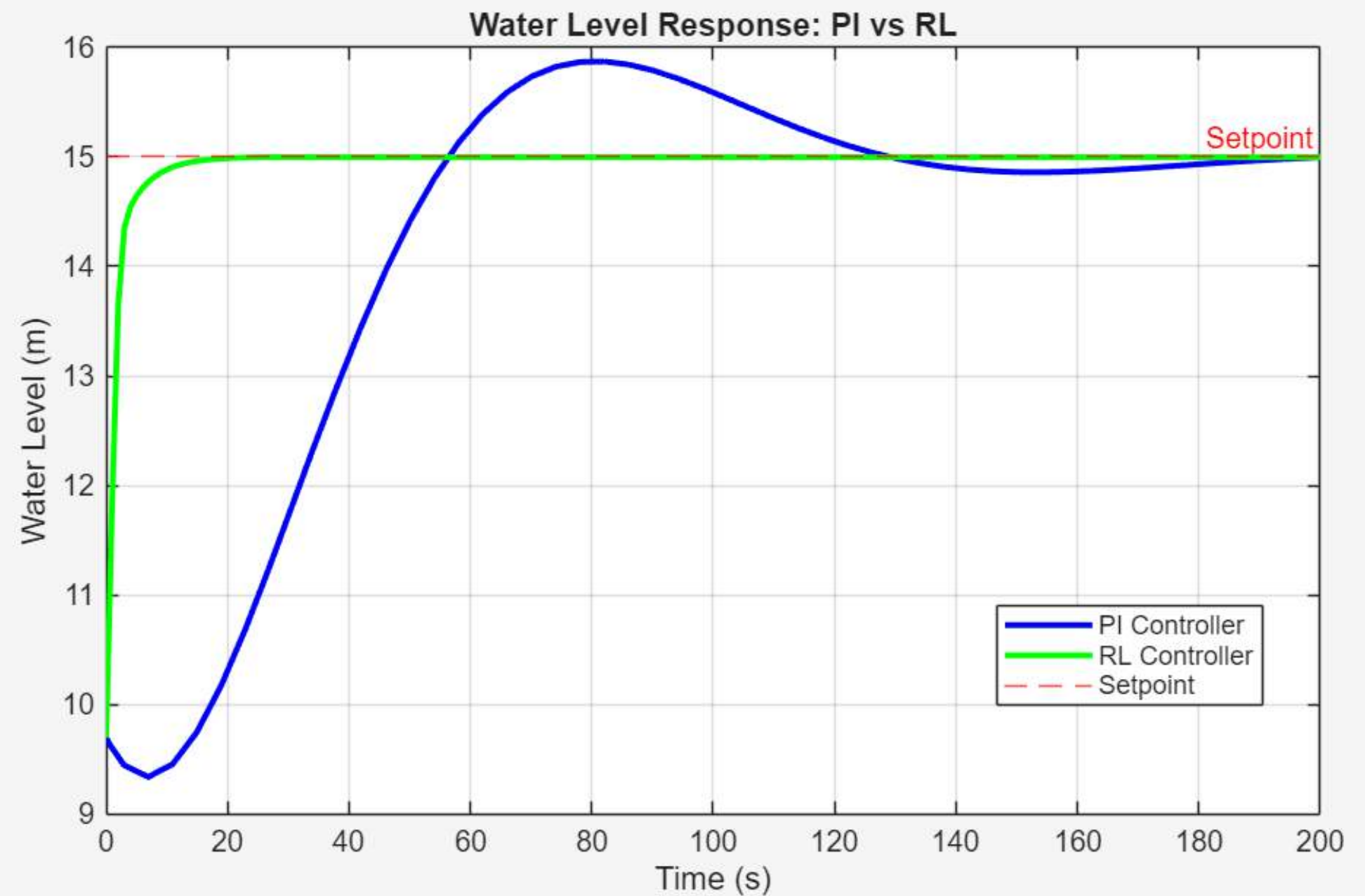
- Comparing between PI and RL controller in a controlled environment
- Desired Water Level : 15 m
- Initial Water Level : 9.5 m

Output:

Performance Metrics Comparison:

Metric	PI	RL
Rise Time (s)	NaN	NaN
Settling Time (s)	110.08	5.00
Overshoot (%)	5.81	-0.02
Mean Squared Error	6.17	0.20

>>



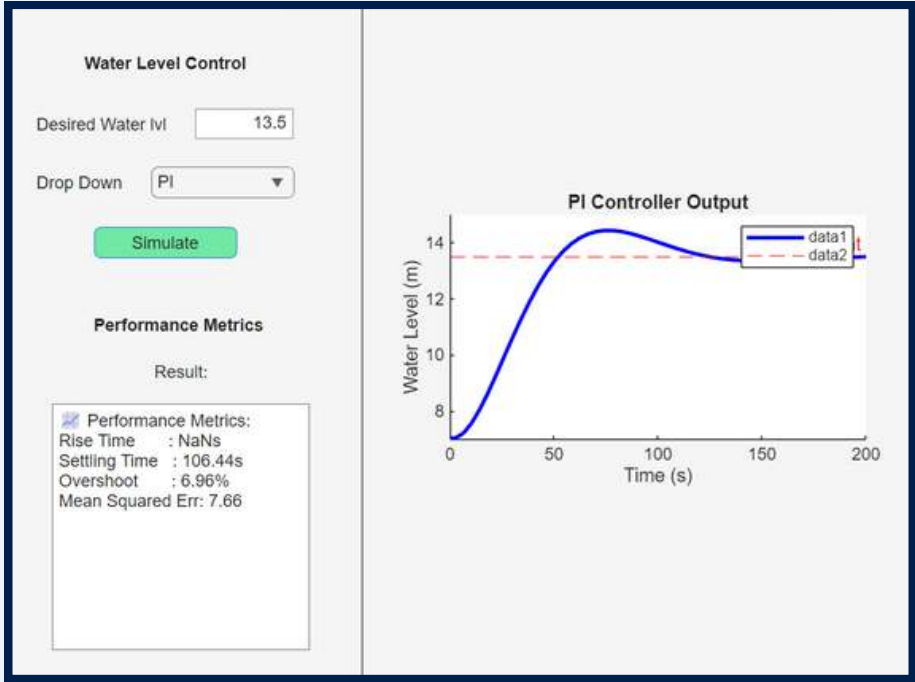
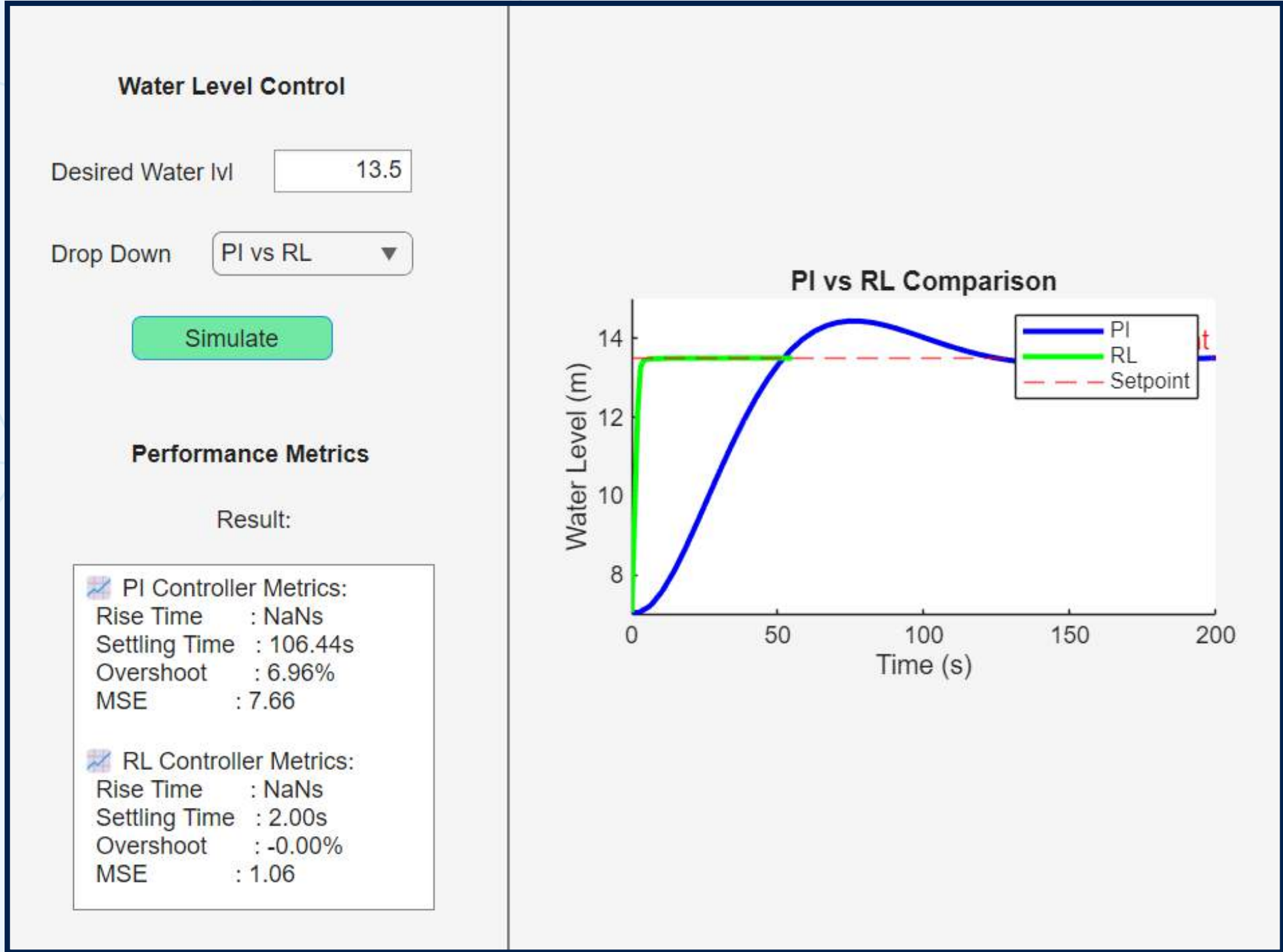
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Comparison between RL and PI Controller

Controller	Advantages	Disadvantages
PI Controller	<ul style="list-style-type: none">- Simple to design and tune- Predictable behaviour- Low overshoot	<ul style="list-style-type: none">- Very slow response- Higher average error (MSE)- Not adaptive to changes in dynamics
RL Controller	<ul style="list-style-type: none">- Fast and accurate tracking- Extremely low MSE- Adaptive to environment	<ul style="list-style-type: none">- Requires extensive training-Complex to design and tune-Less explainable logic

- PI Controller: Reliable and easy to implement, but responds slowly and has higher error due to limited adaptability.
- RL Controller: Delivers fast, precise, and adaptive control with minimal error, but requires complex setup, long training, and careful design to ensure safe performance.

GUI Simulation Result - via MATLAB app





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THANK YOU!

gulduck final!