Introducing Convolutional Neural Networks



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Overview

Intuition behind Convolutional Neural Networks (CNNs)

Convolution layers and feature maps

Pooling layers to subsample inputs

Typical CNN architecture

How Do We See?



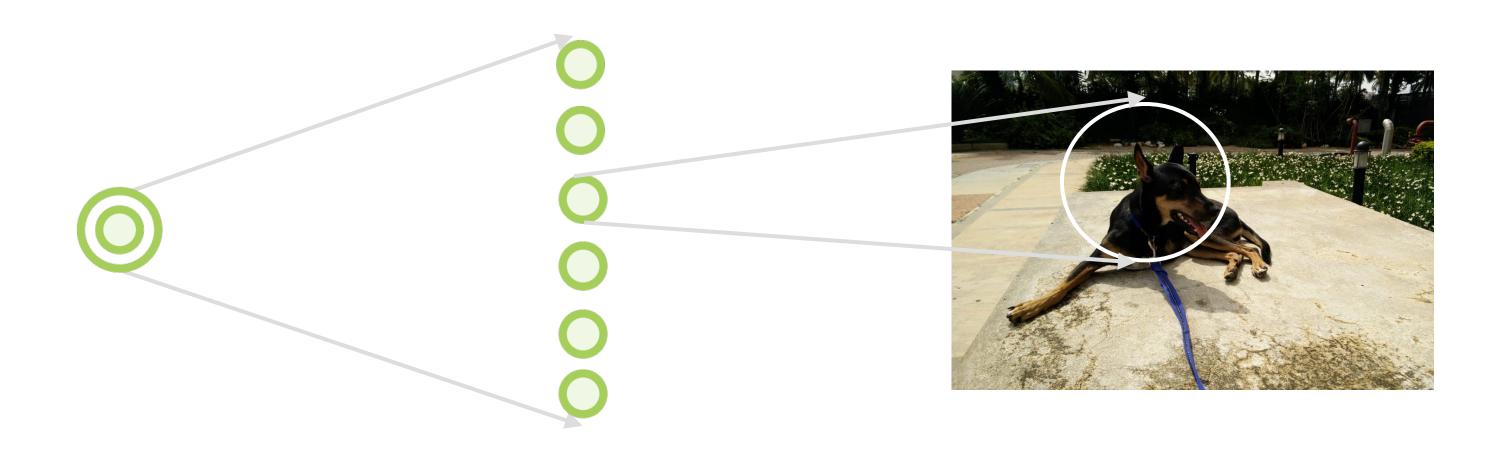
All neurons in the eye don't see the entire image



Each neuron has its own local receptive field

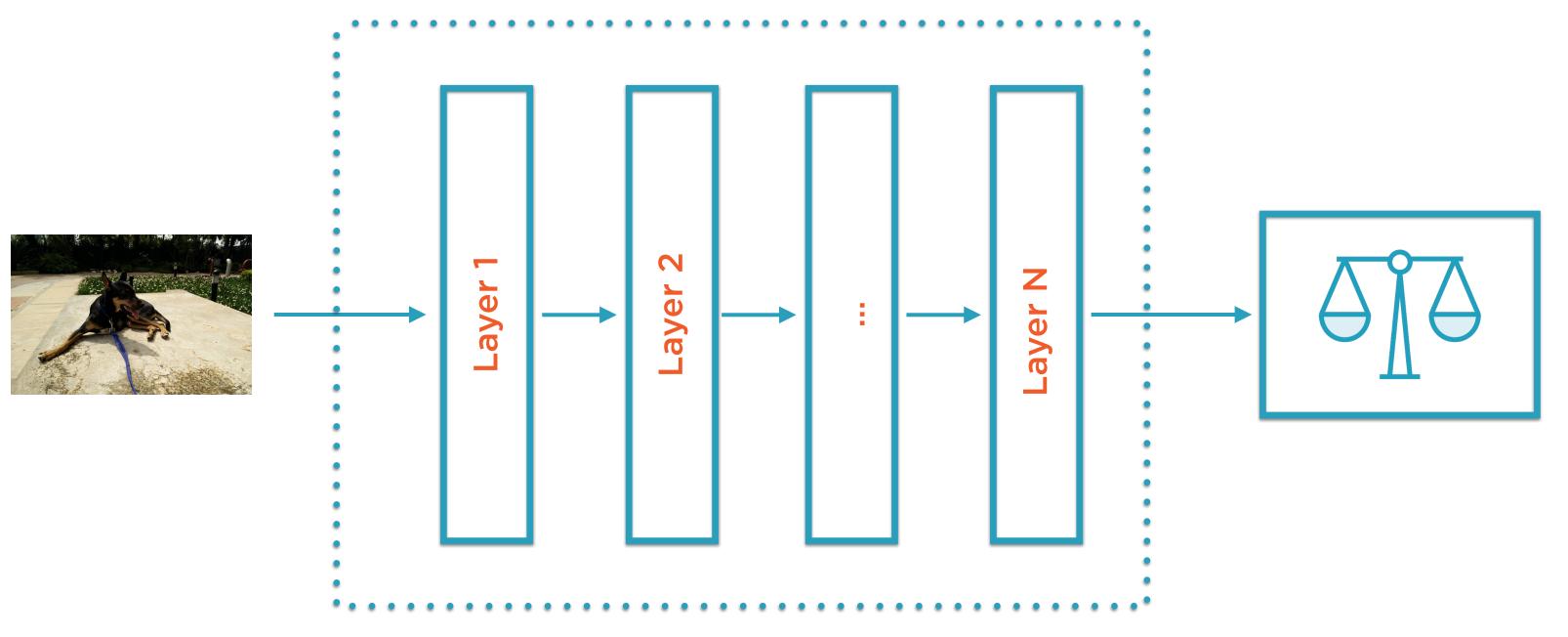


It reacts only to visual stimuli located in its receptive field



Some neurons react to more complex patterns that are combinations of lower level patterns

Neural Networks



Sounds like a classic neural network problem

Two Kinds of Layers in CNNs

Convolution

Local receptive field

Pooling

Subsampling of inputs

Two Kinds of Layers in CNNs

Convolution

Local receptive field

Pooling

Subsampling of inputs

In this context, a sliding window function applied to a matrix

In this context, a sliding window function applied to

a matrix

e.g. a matrix of pixels representing an image

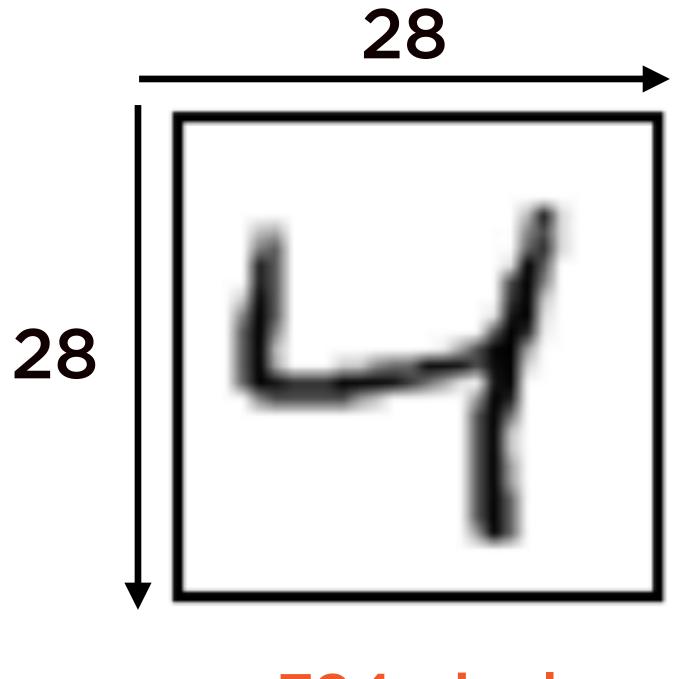
In this context, a sliding window function applied to a matrix

Often called a kernel or filter

In this context, a sliding window function applied to a matrix

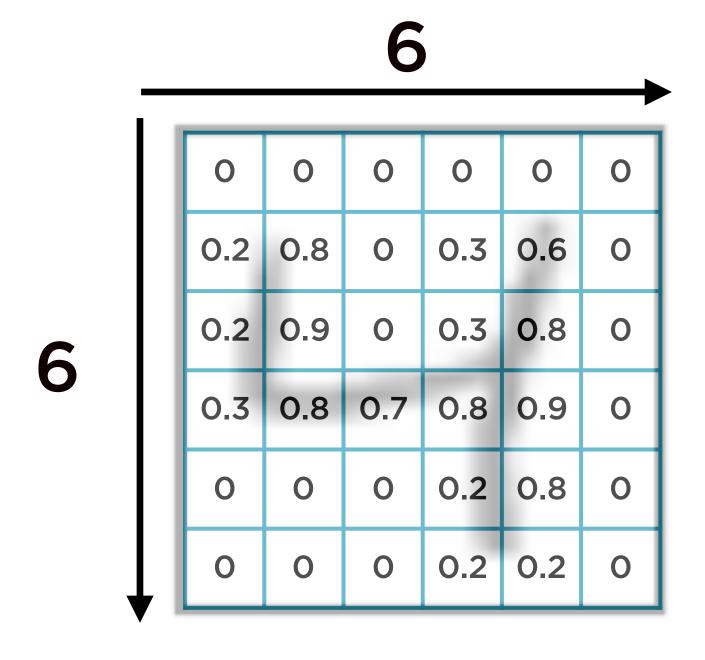
Kernel is applied element-wise in sliding-window fashion

Representing Images as Matrices



= 784 pixels

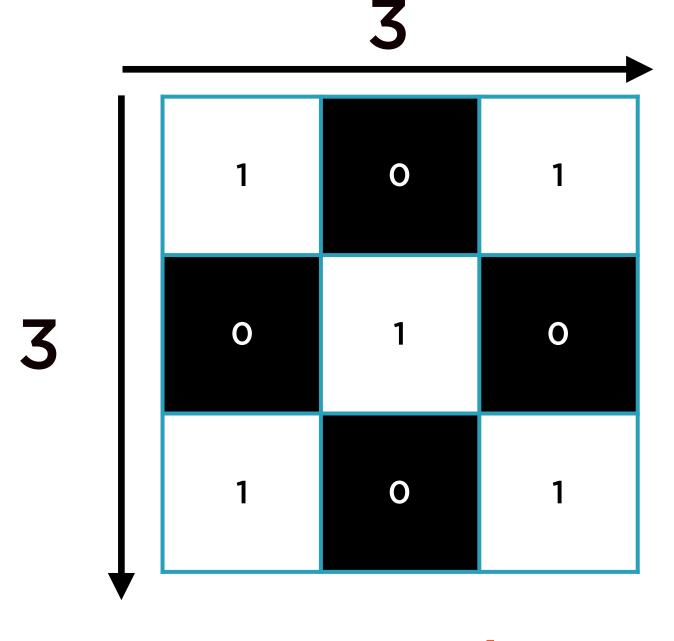
Representing Images as Matrices



= 36 pixels

Representing Images

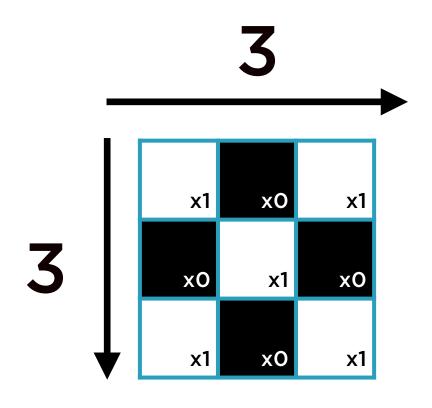
0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	0	0.3	0.8	0
0.3	0.8	0.7	0.8	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0



Matrix

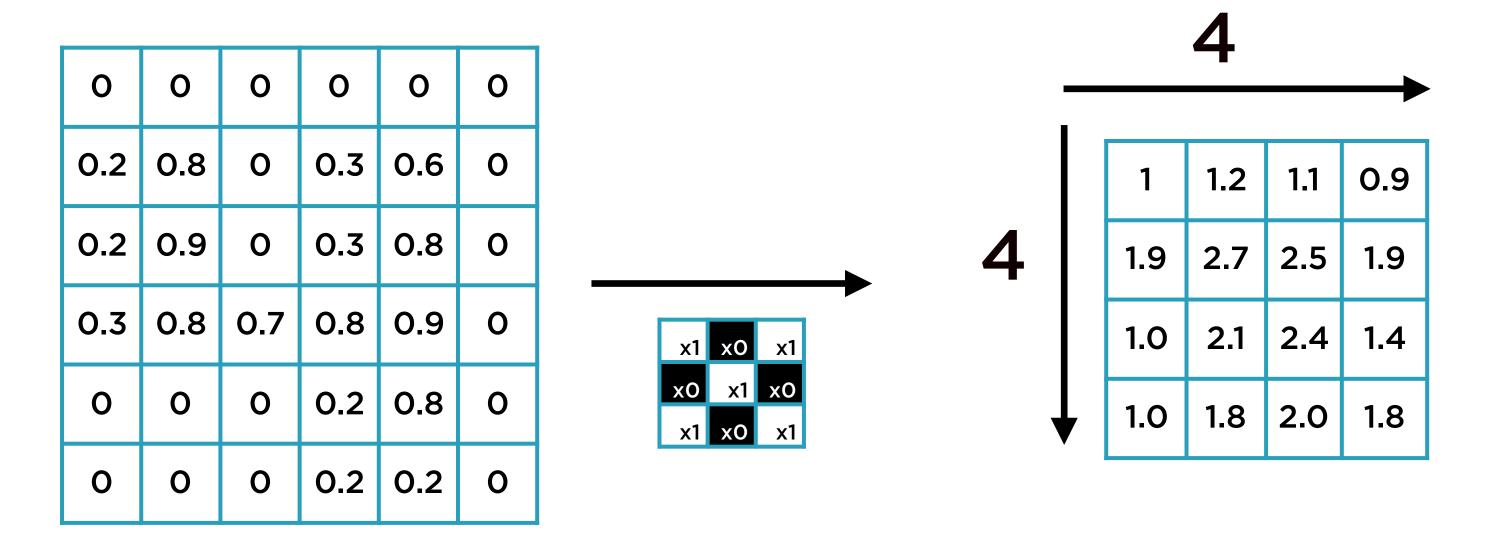
Kernel

0	0	0	0	0	0
0.2	8.0	0	0.3	0.6	0
0.2	0.9	0	0.3	0.8	0
0.3	0.8	0.7	0.8	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

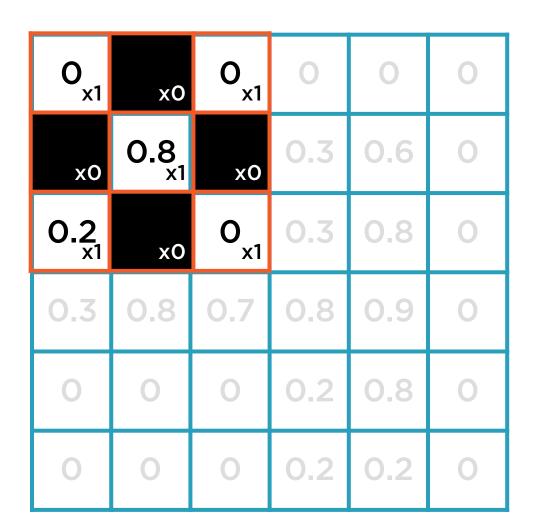


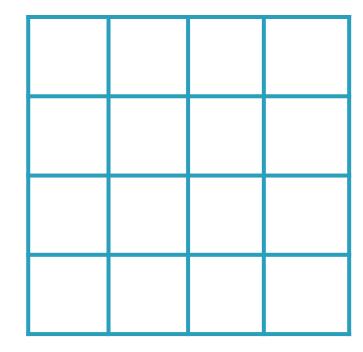
Matrix

Kernel



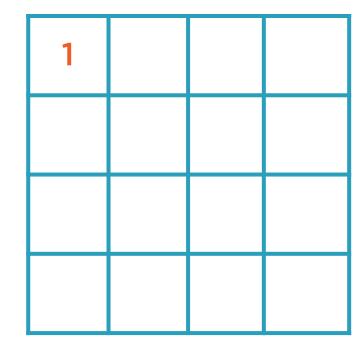
Matrix





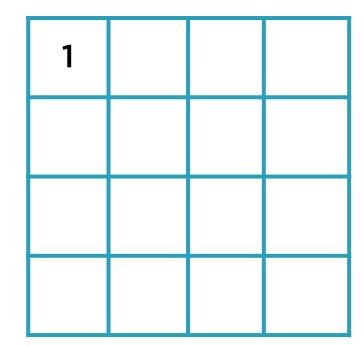
Matrix

O _{x1}	хO	O _{x1}	0	0	0
хО	0.8 _{x1}	хО	0.3	0.6	0
0.2 x1	хO	O _{x1}	0.3	0.8	0
0.3	0.8	0.7	0.8	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0



Matrix

0	O _{x1}	хO	O _{x1}	0	0
0.2	хO	O _{x1}	хО	0.6	0
0.2	0.9 x1	хO	0.3 x1	0.8	0
0.3	0.8	0.7	0.8	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0



Matrix

0	O _{x1}	хO	O _{x1}	0	0
0.2	хO	O _{x1}	хО	0.6	0
0.2	0.9 x1	хO	0.3 x1	0.8	0
0.3	0.8	0.7	0.8	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	

Matrix

0	0	O _{x1}	хO	O _{x1}	0
0.2	0.8	хO	0.3 x1	хО	0
0.2	0.9	O _{×1}	хO	0.8 _{×1}	0
0.3	0.8	0.7	0.8	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	

Matrix

0	0	O _{x1}	хO	O _{x1}	0
0.2	0.8	хО	0.3	хО	0
0.2	0.9	O _{x1}	хO	0.8 x1	0
0.3	0.8	0.7	0.8	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	

Matrix

0	0	0	O _{x1}	хO	O _{x1}
0.2	0.8	0	хО	0.6 x1	хO
0.2	0.9	0	0.3 _{×1}	хО	O _{x1}
0.3	0.8	0.7	0.8	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	

Matrix

0	0	0	O _{x1}	хO	O _{x1}
0.2	0.8	0	хО	0.6 x1	хO
0.2	0.9	0	0.3 _{×1}	хО	O _{x1}
0.3	0.8	0.7	0.8	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9

Matrix

0	0	0	0	0	0
0.2 ×1	хO	O _{x1}	0.3	0.6	0
хО	0.9 x1	хО	0.3	0.8	0
0.3 x1	хО	0.7 ×1	0.8	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9

Matrix

0	0	0	0	0	0
0.2 x1	хO	O _{x1}	0.3	0.6	0
хО	0.9 x1	хO	0.3	0.8	0
0.3 x1	хO	0.7 x1	0.8	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9			

Matrix

0	0	0	0	0	0
0.2	0.8 x1	хO	0.3 x1	0.6	0
0.2	хО	O _{x1}	хO	0.8	0
0.3	0.8 x1	хО	0.8 x1	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9			

Matrix

0	0	0	0	0	0
0.2	0.8 x1	хO	0.3 x1	0.6	0
0.2	хО	O _{x1}	хO	0.8	0
0.3	0.8 x1	хО	0.8 x1	0.9	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7		

Matrix

0	0	0	0	0	0
0.2	0.8	O _{x1}	хО	0.6 x1	0
0.2	0.9	хО	0.3 x1	хО	0
0.3	0.8	0.7 ×1	хO	0.9 x1	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7		

Matrix

0	0	0	0	0	0
0.2	0.8	O _{x1}	хO	0.6 x1	0
0.2	0.9	хО	0.3 x1	хO	0
0.3	0.8	0.7 ×1	хО	0.9 x1	0
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7	2.5	

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3 x1	хO	O _{x1}
0.2	0.9	0	хО	0.8 x1	хO
0.3	0.8	0.7	0.8 x1	хO	O _{x1}
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7	2.5	

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3 x1	хO	O _{x1}
0.2	0.9	0	хО	0.8 x1	хO
0.3	0.8	0.7	0.8 x1	хО	O _{x1}
0	0	0	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2 ×1	хО	O _{×1}	0.3	0.8	0
хO	0.8 _{x1}	хO	0.8	0.9	0
O _{x1}	хO	O _{×1}	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2 ×1	хО	O _{x1}	0.3	0.8	0
хО	0.8 _{×1}	хO	0.8	0.9	0
O _{x1}	хО	O _{x1}	0.2	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0			

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9 x1	хО	0.3 x1	0.8	0
0.3	хО	0.7 x1	хО	0.9	0
0	O _{x1}	хО	0.2 x1	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0			

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9 x1	хО	0.3 x1	0.8	0
0.3	хО	0.7 x1	хО	0.9	0
0	O _{x1}	хО	0.2 x1	0.8	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1		

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	O _{x1}	хO	0.8 _{x1}	0
0.3	0.8	хО	0.8 _{x1}	хO	0
0	0	O _{x1}	хO	0.8 _{x1}	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1		

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	O _{×1}	хО	0.8 _{x1}	0
0.3	0.8	хО	0.8 _{x1}	хO	0
0	0	O _{x1}	хO	0.8 _{x1}	0
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1	2.4	

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	0	0.3 x1	хО	O _{x1}
0.3	0.8	0.7	хO	0.9 x1	хO
0	0	0	0.2 x1	хO	O _{x1}
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1	2.4	

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	0	0.3 x1	хO	O _{x1}
0.3	0.8	0.7	хO	0.9 x1	хO
0	0	0	0.2 x1	хO	O _{x1}
0	0	0	0.2	0.2	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1	2.4	1.4

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	0	0.3	0.8	0
0.3 x1	хО	0.7 x1	0.8	0.9	0
	O _{x1}	хО	0.2	0.8	0
хO	71.				

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1	2.4	1.4

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	0	0.3	0.8	0
0.3 x1	хО	0.7 x1	0.8	0.9	0
хO	O x1	хO	0.2	0.8	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1	2.4	1.4
1.0			

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	0	0.3	0.8	0
0.3	0.8 x1	хО	0.8 x1	0.9	0
0.3	0.8 x1	x0 O x1	0.8 x1	0.9	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1	2.4	1.4
1.0			

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	0	0.3	0.8	0
0.3	0.8 x1	хO	0.8 x1	0.9	0
0.3	0.8 x1	x0 O x1	0.8 x1	0.9	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1	2.4	1.4
1.0	1.8		

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	0	0.3	0.8	0
0.3	0.8	0.7 x1	хО	0.9 x1	0
0.3	0.8	O.7 x1	x0 O.2 x1	0.9 x1	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1	2.4	1.4
1.0	1.8		

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	0	0.3	0.8	0
0.3	0.8	O.7 x1	хO	0.9 x1	0
0.3	0.8	O.7 x1	x0 O.2 x1	0.9 x1	0

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1	2.4	1.4
1.0	1.8	2.0	

Matrix

0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	0	0.3	0.8	0
0.3	0.8	0.7	0.8 x1	хO	O x1
0.3	0.8	0.7	0.8 x1	x0 O.8 x1	

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1	2.4	1.4
1.0	1.8	2.0	

Matrix

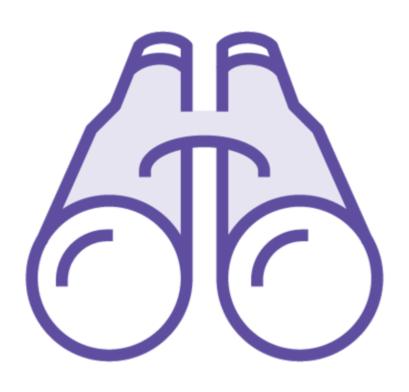
0	0	0	0	0	0
0.2	0.8	0	0.3	0.6	0
0.2	0.9	0	0.3	0.8	0
0.3	0.8	0.7	0.8 x1	хO	O x1
0.3	0.8	0.7	0.8 x1	0.8 x1	_

1	1.2	1.1	0.9
1.9	2.7	2.5	1.9
1.0	2.1	2.4	1.4
1.0	1.8	2.0	1.8

Matrix

Convolutional Layers

Convolutional Layers

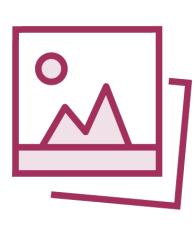


Convolution layers - zoom in on specific bits of input

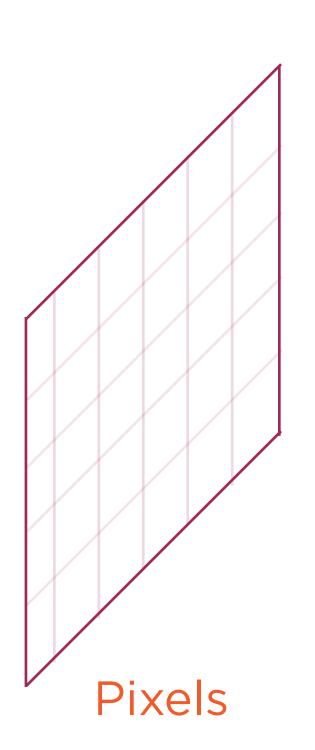
Extract structure and features in the input image

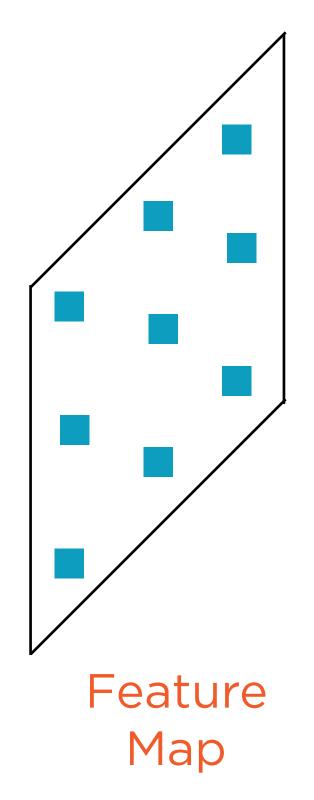
Successive layers aggregate inputs into higher level features

Pixels >> Lines >> Edges >> Object

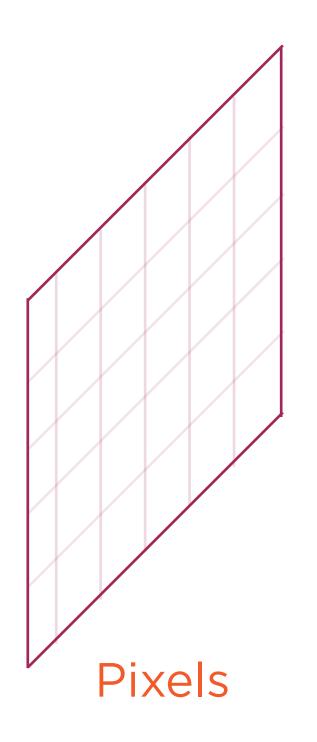


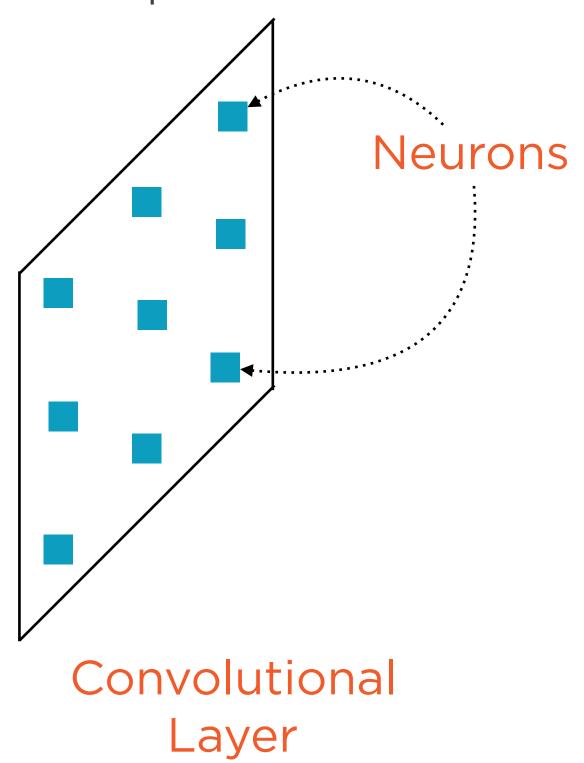
Image

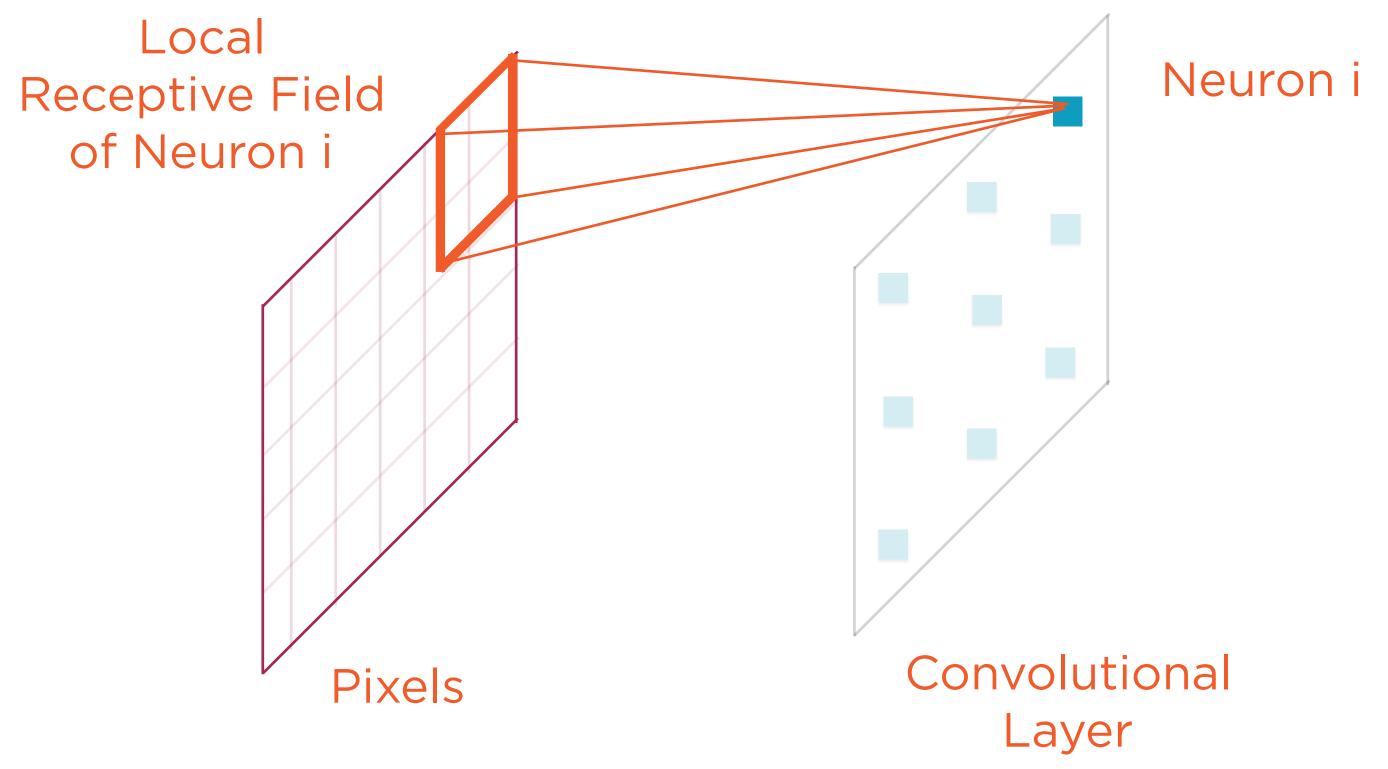


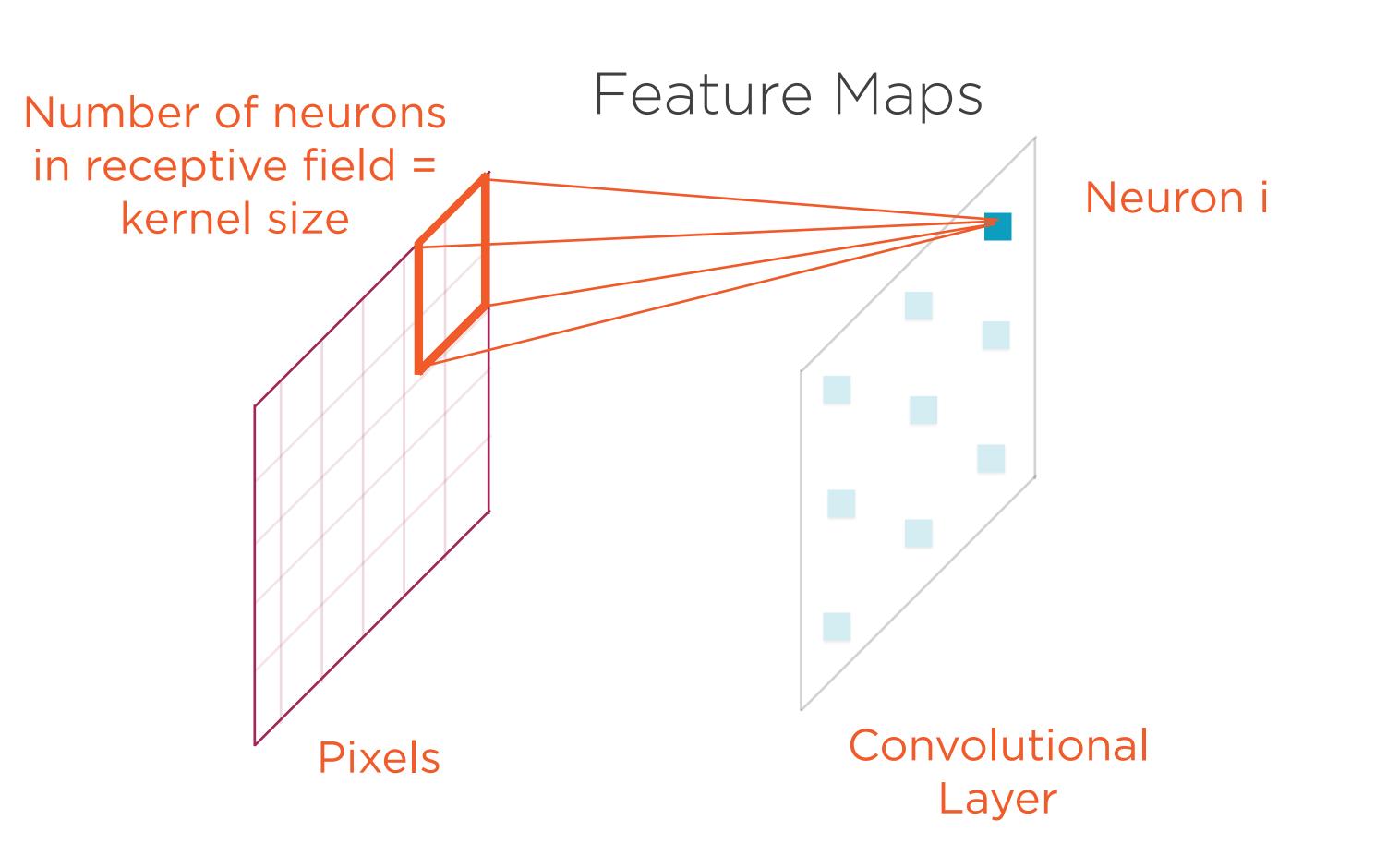


Feature maps are convolutional layers generated by applying a convolutional kernel to the input

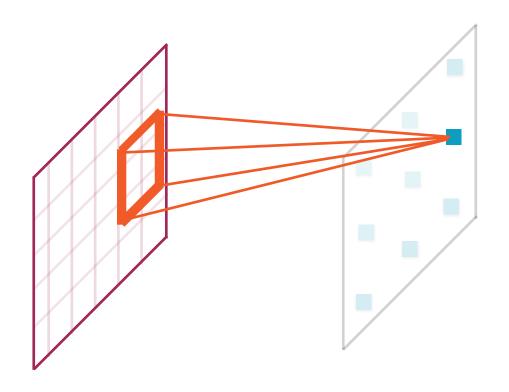








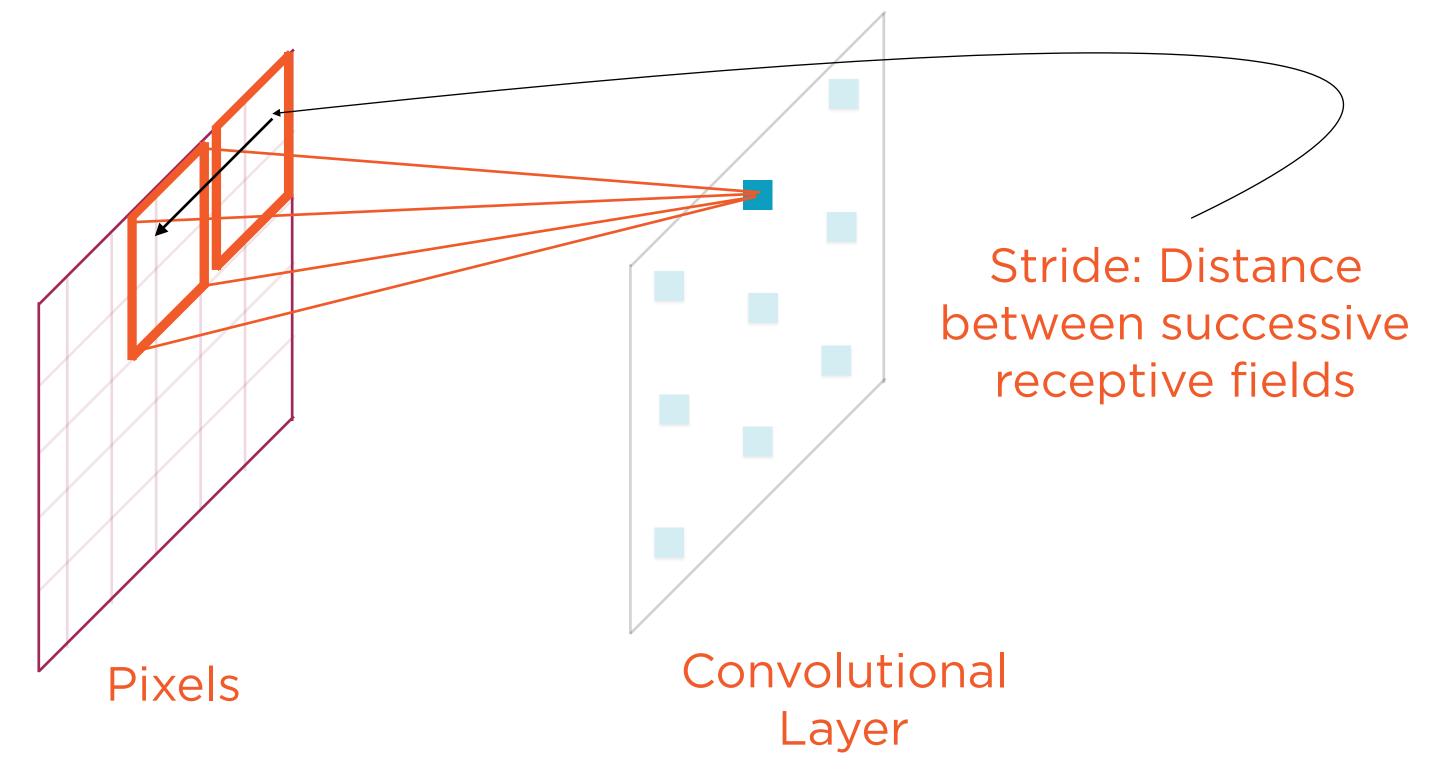
Kernel Size

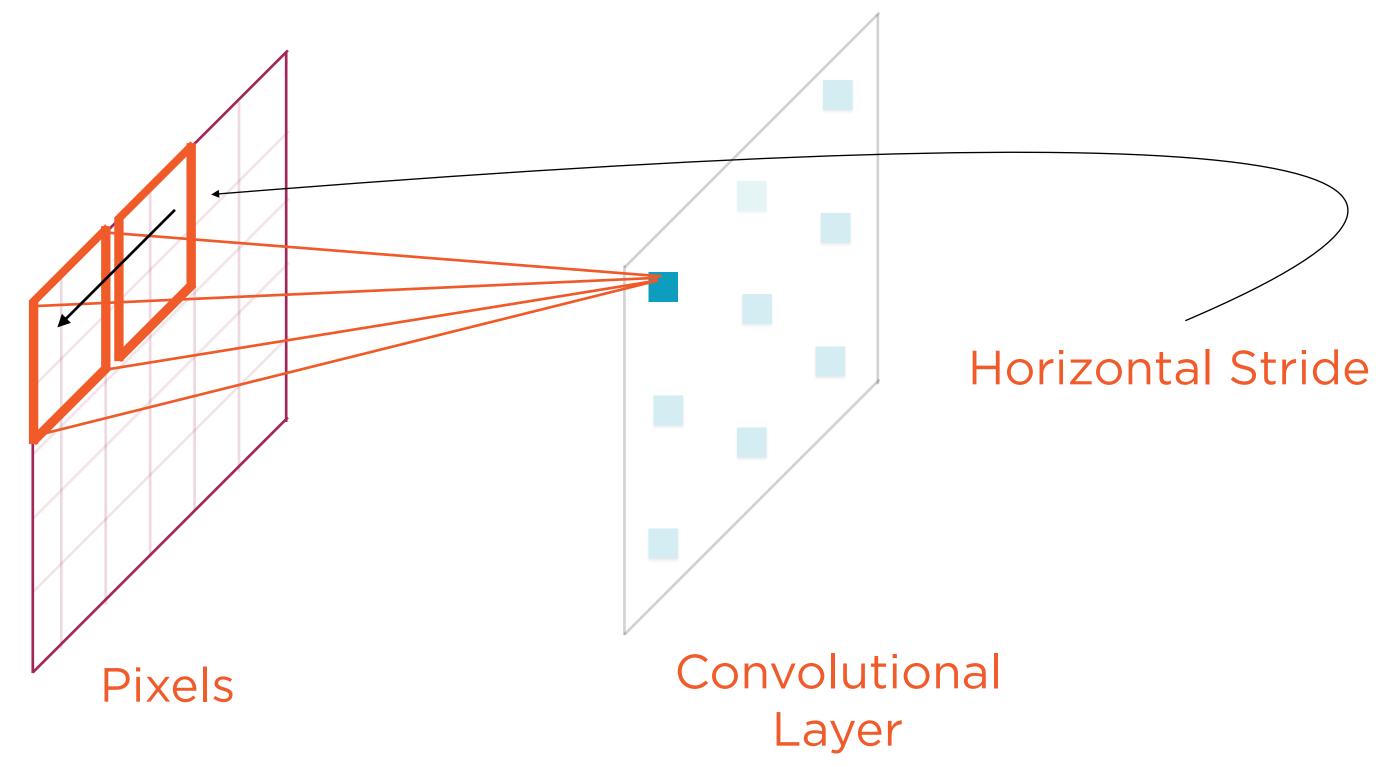


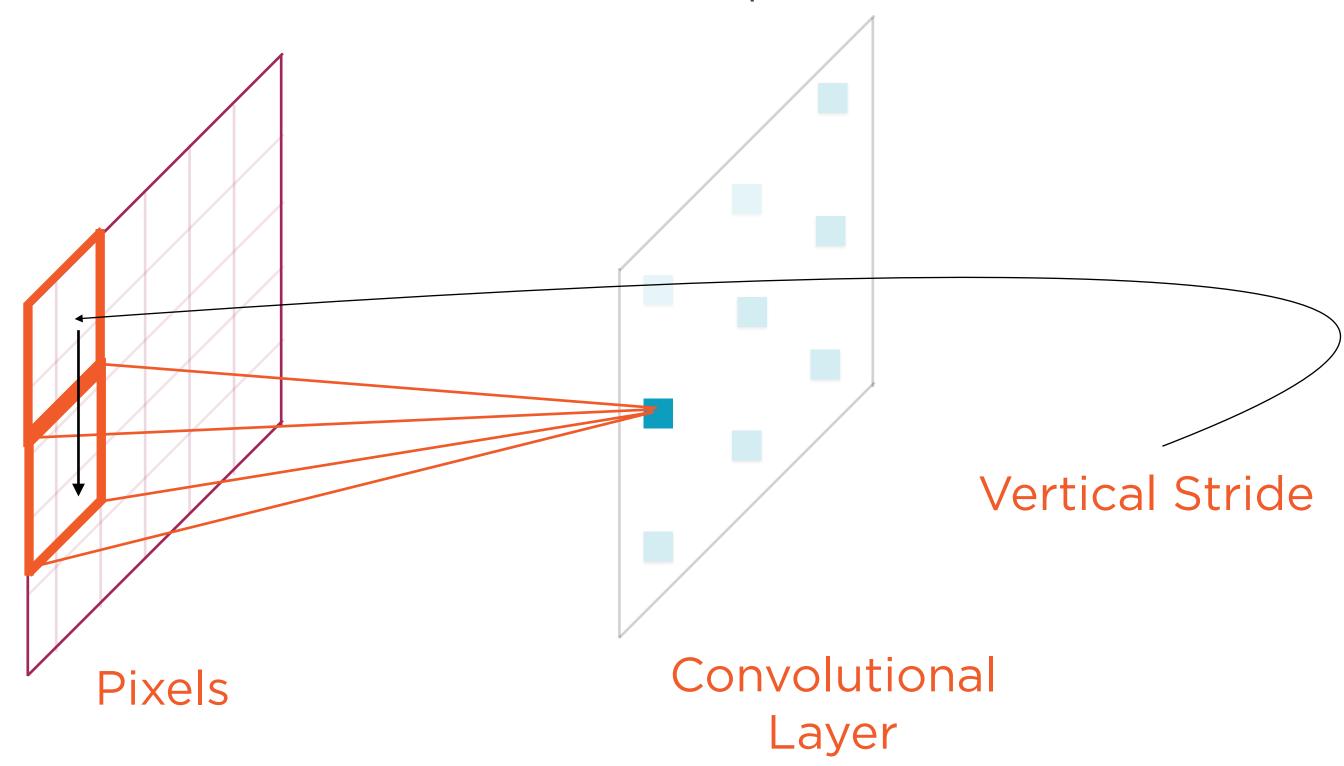
Convolutional kernel size usually expressed in terms of width and height of receptive area

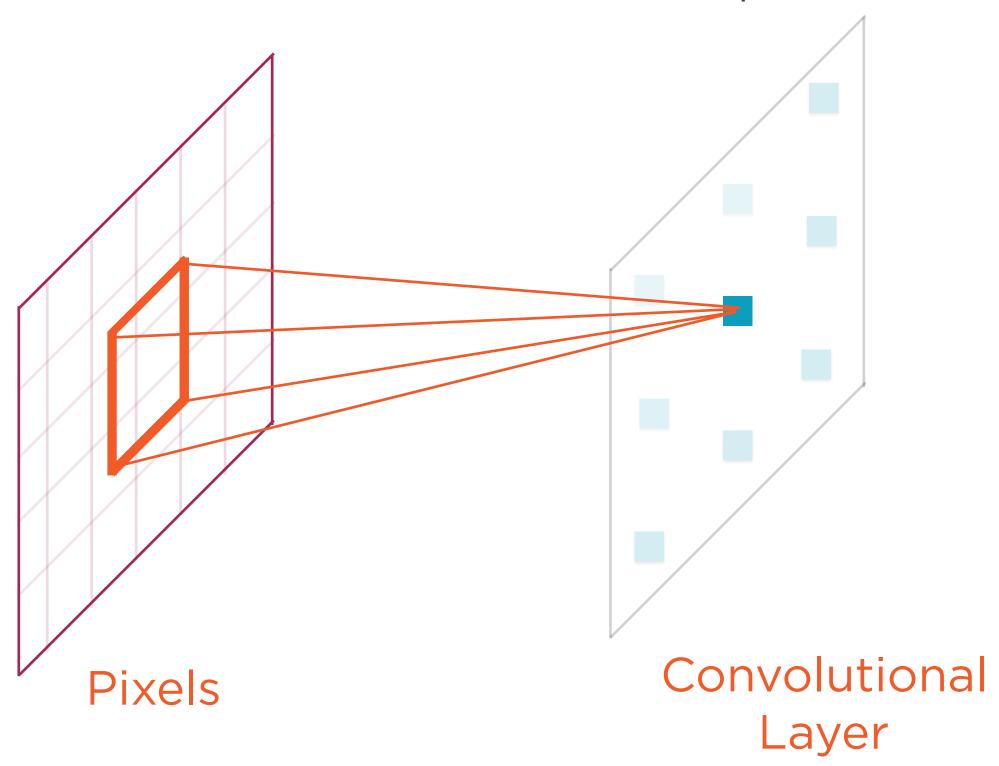
Use small convolutional kernels, more efficient

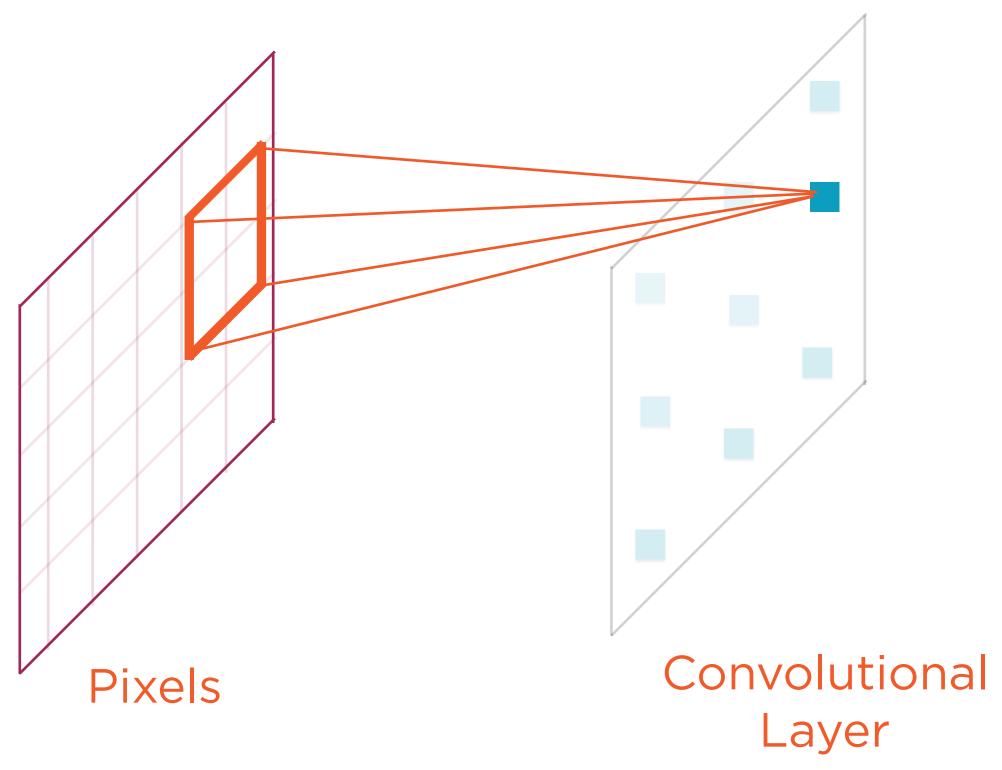
Stacking two 3x3 kernels is preferable to one 9x9 kernel

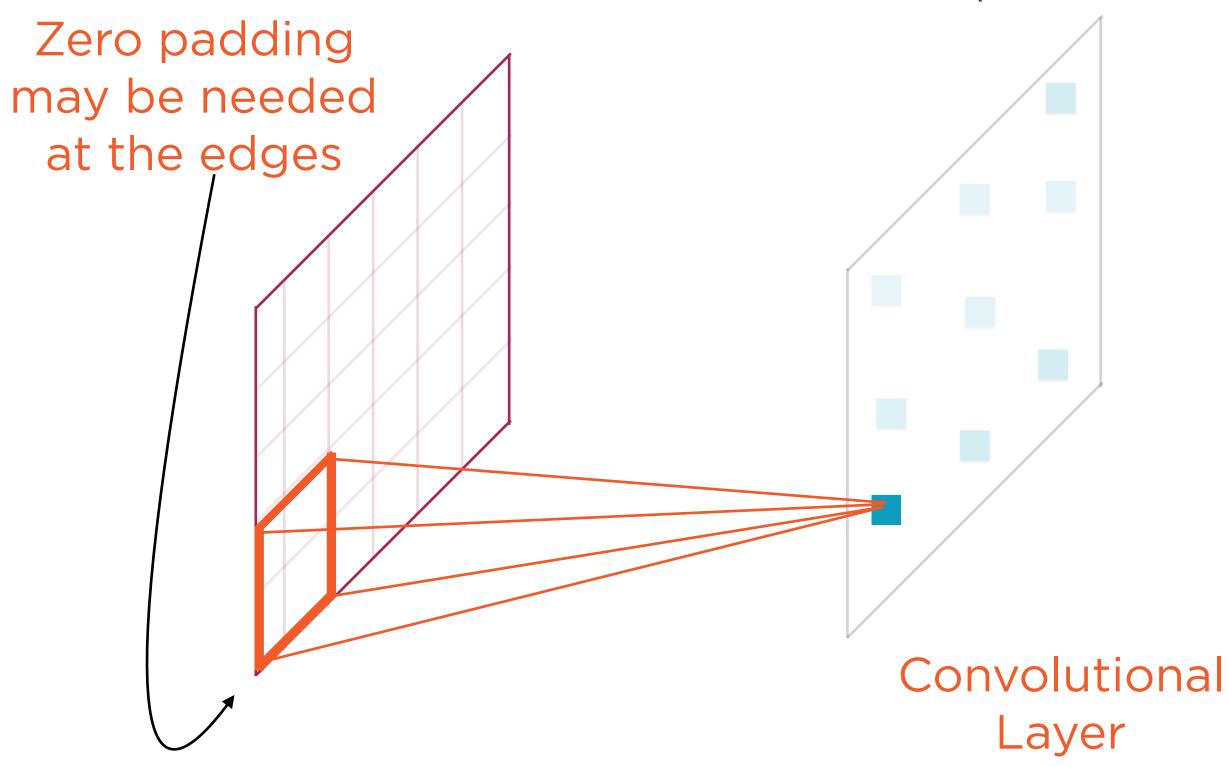


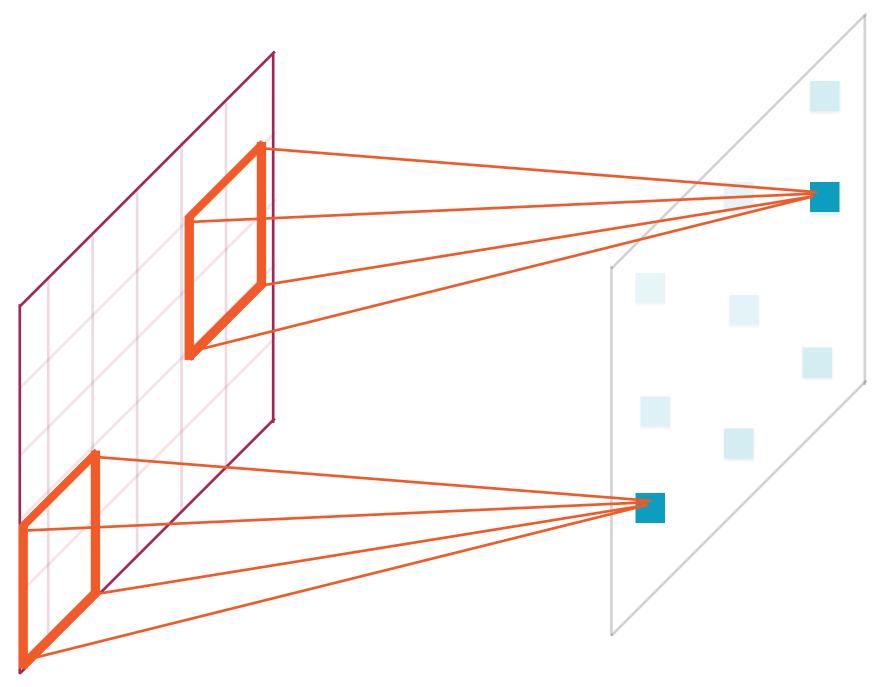




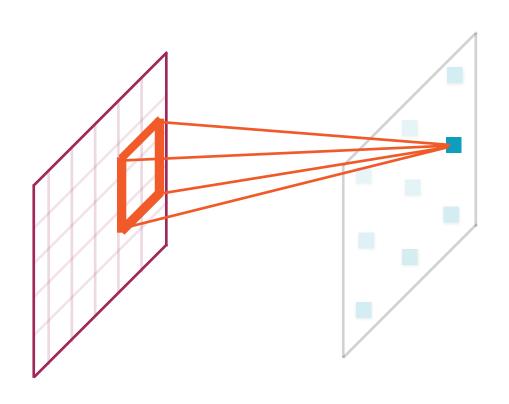






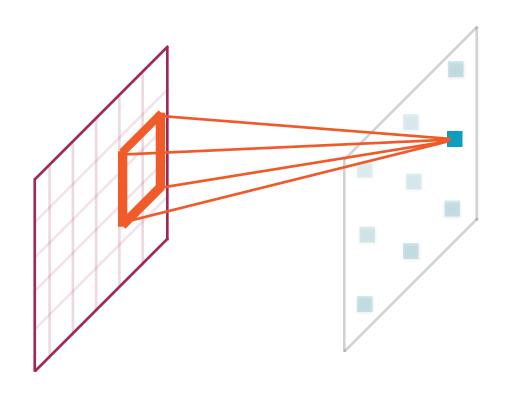


Sparse, not Dense



Notice also that neurons are not connected to all pixels

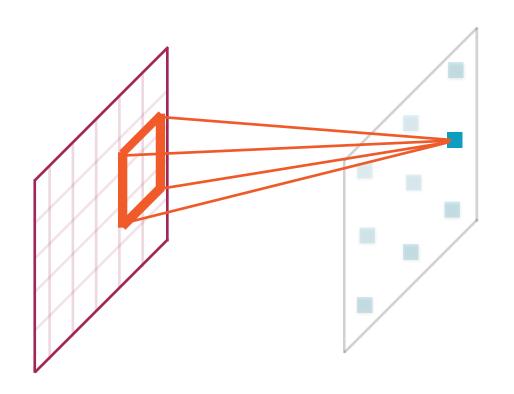
CNNs are sparse neural networks



All neurons in a feature map have the same weights and biases

Two big advantages over DNNs

- Dramatically fewer parameters to train
- CNN can recognize feature patterns independent of location

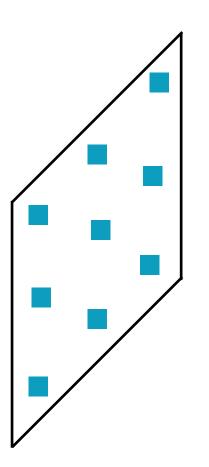


The parameters of all neurons in a feature map are collectively called the filter

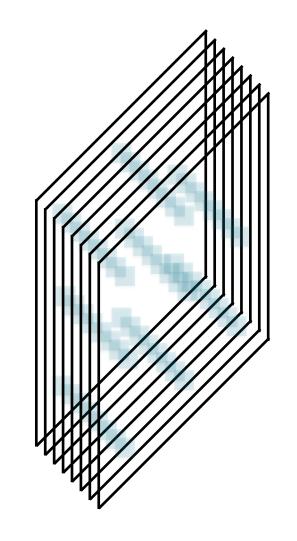
Why filter?

Because weights highlight (filter) specific patterns from the input pixels

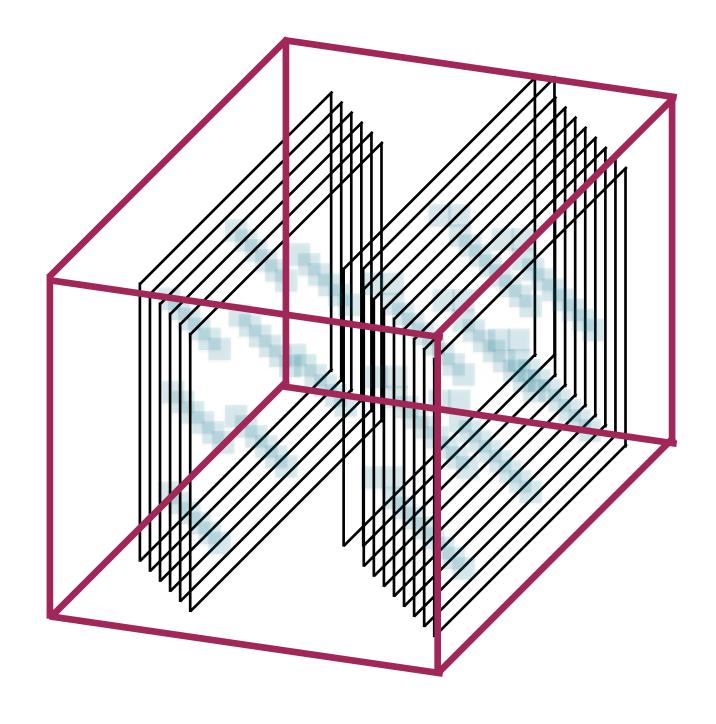
CNNs



Feature Map

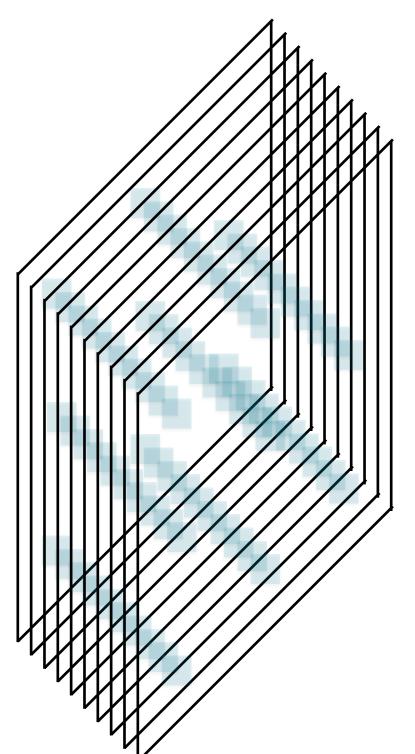


Convolutional Layer



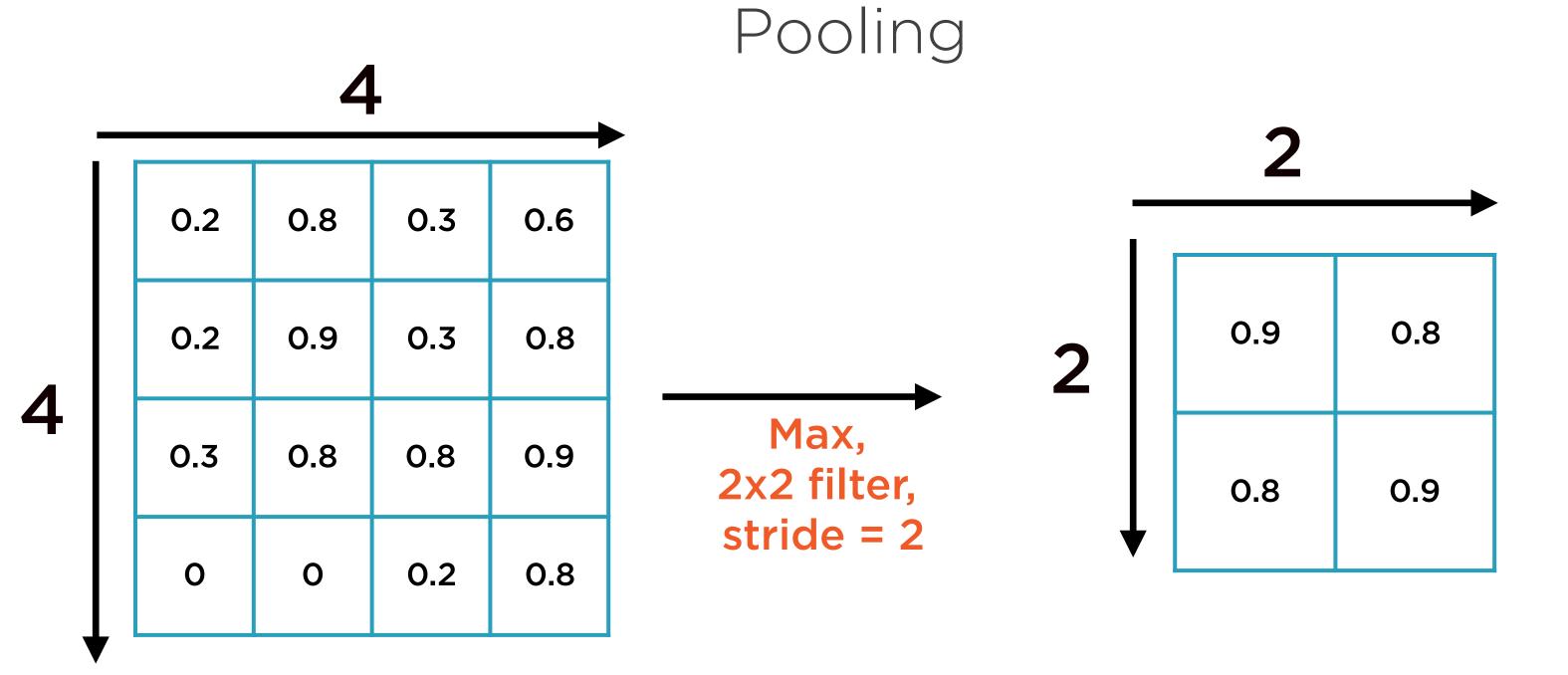
CNN

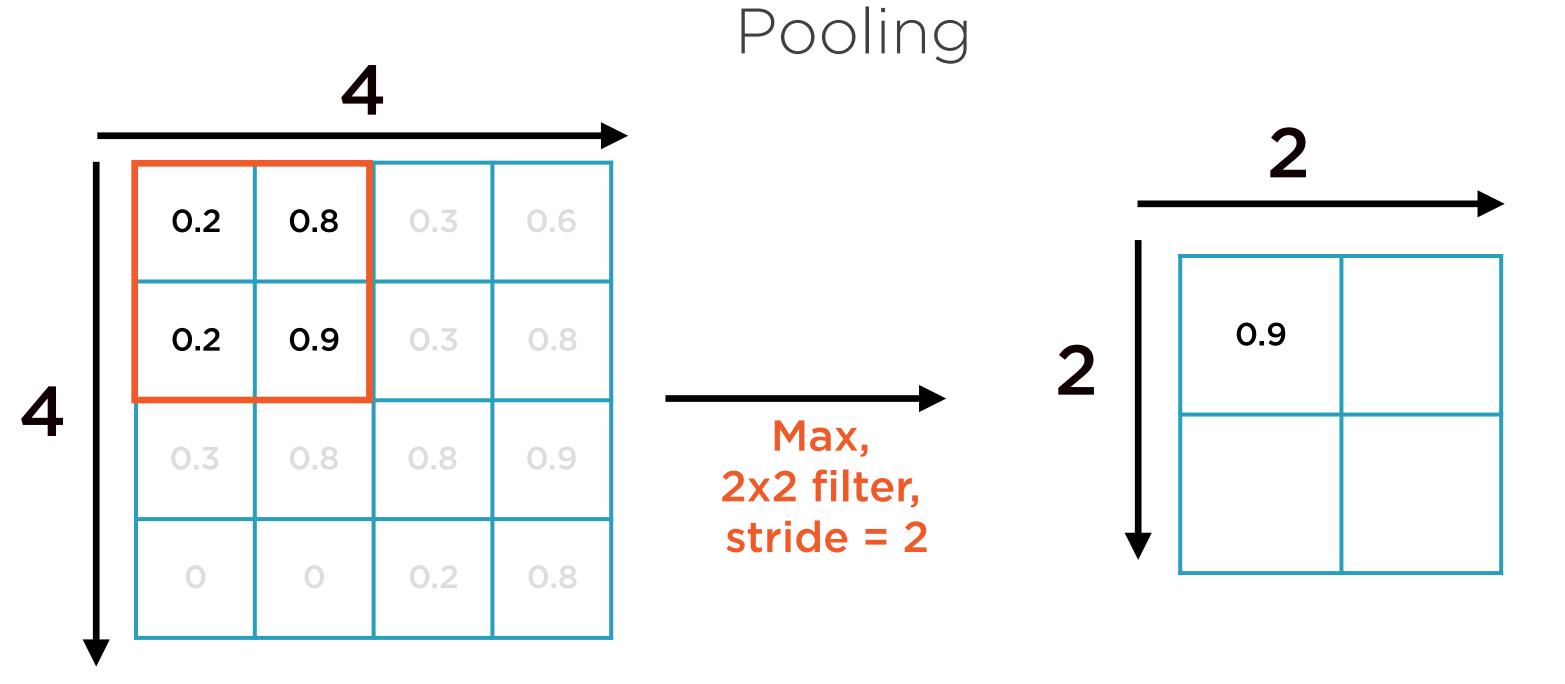


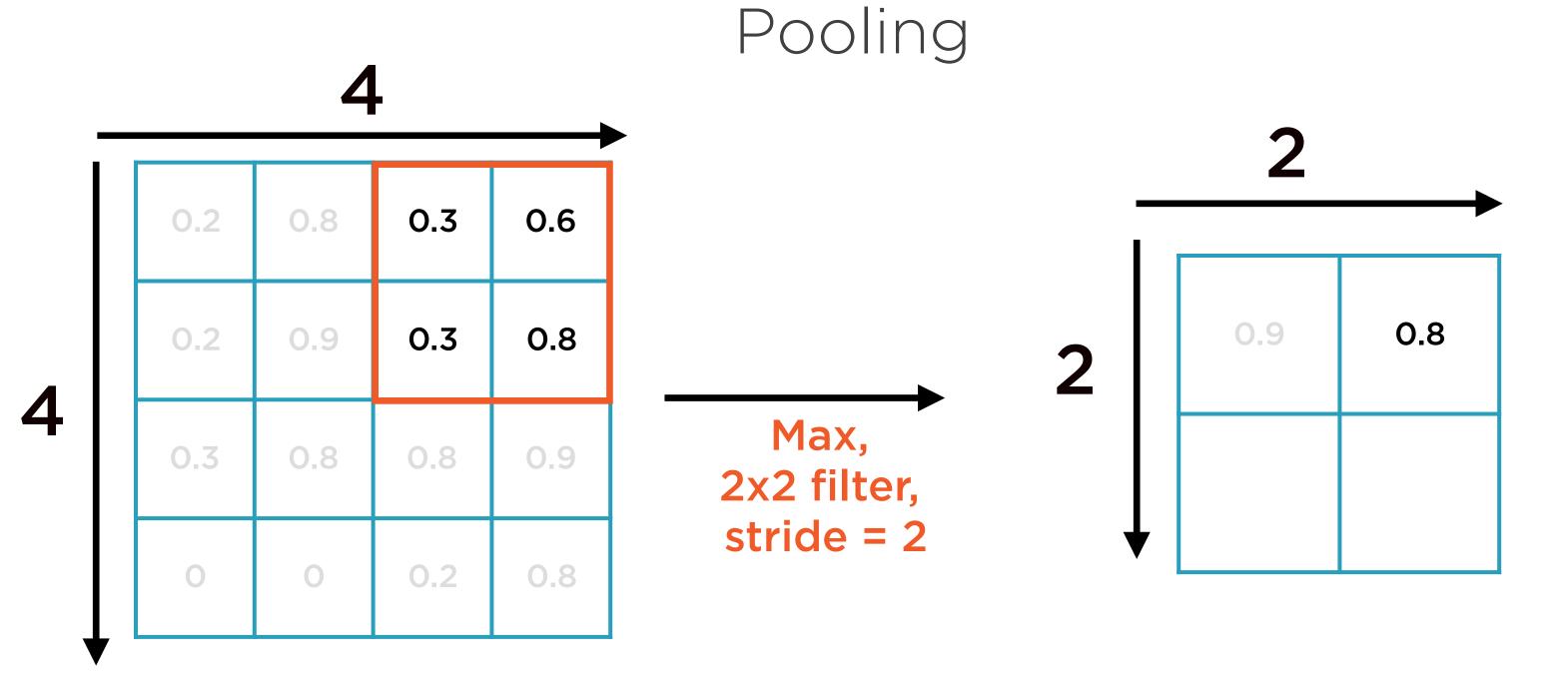


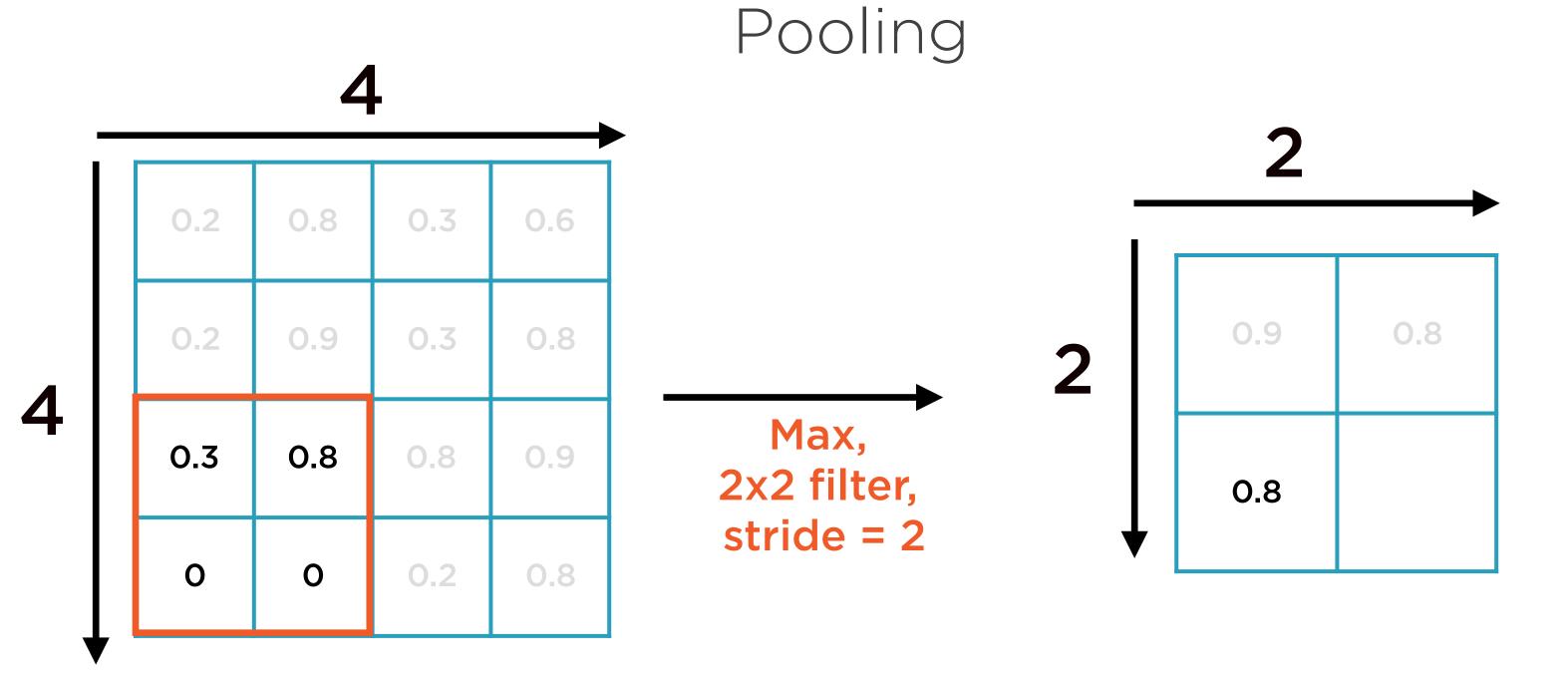
Each convolutional layer consists of several feature maps of equal sizes

The different feature maps have different parameters



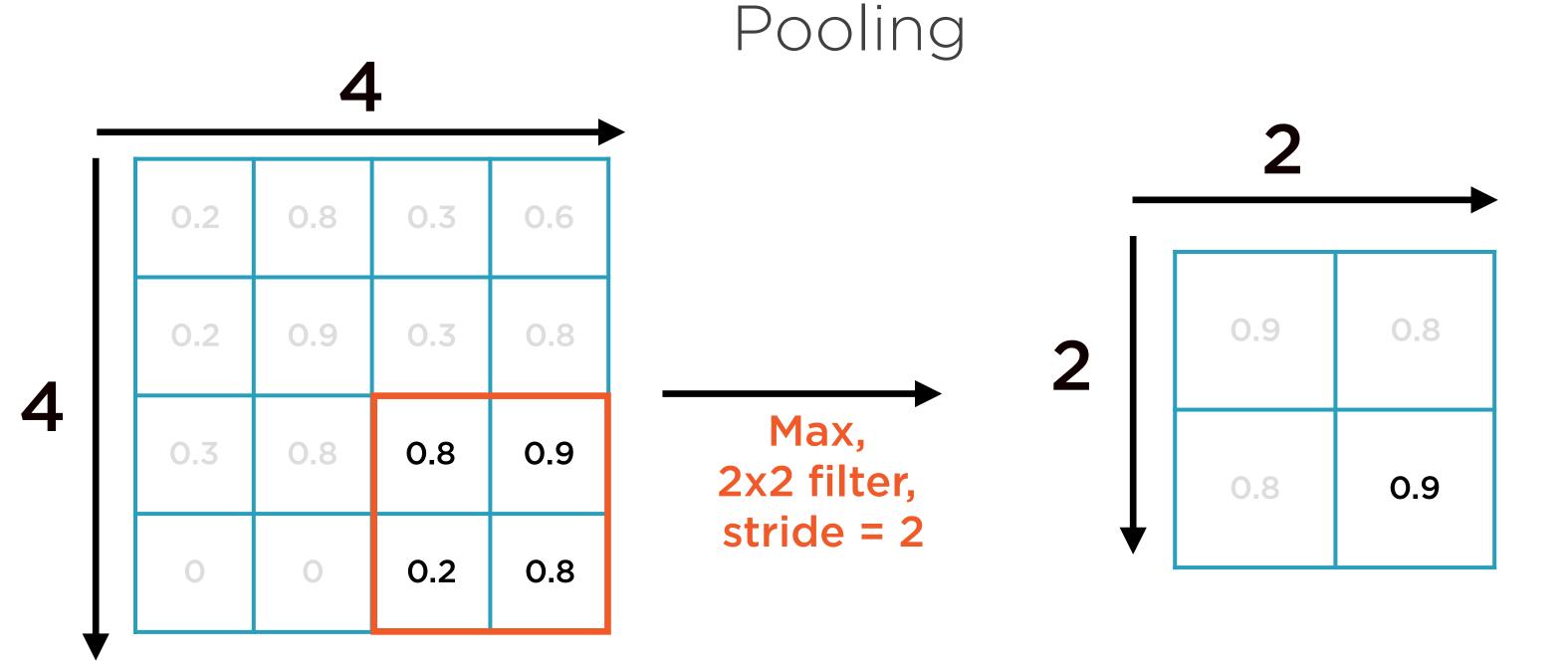


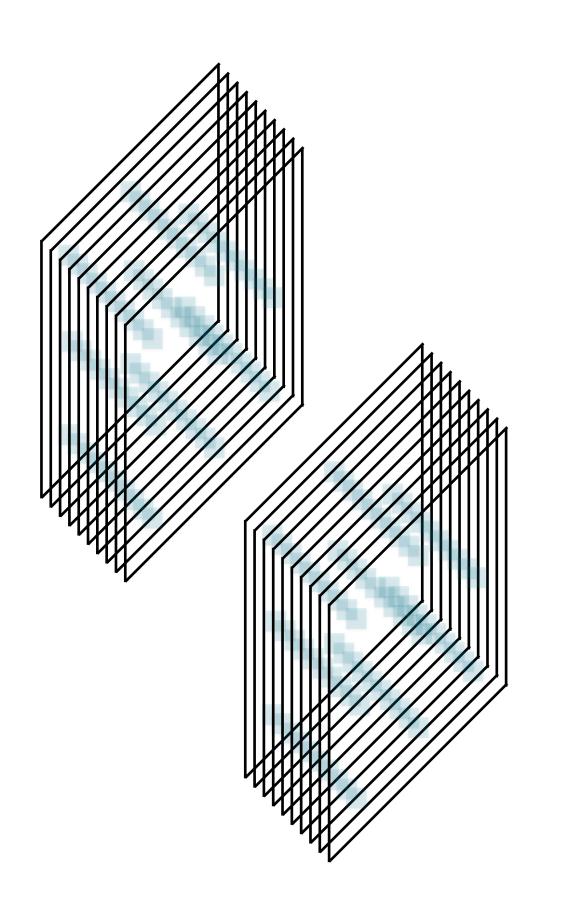




Matrix

Pooling Result

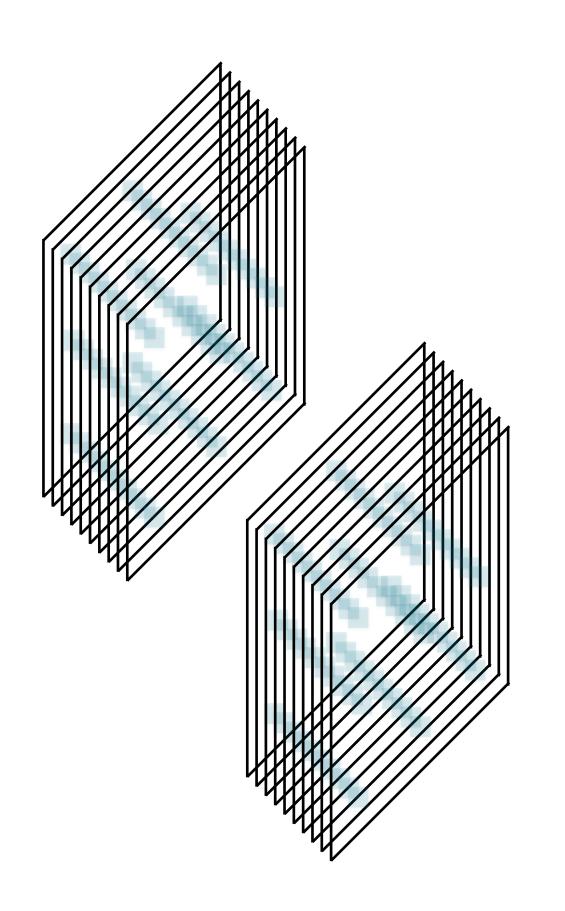




Neurons in a pooling layer have no weights or biases

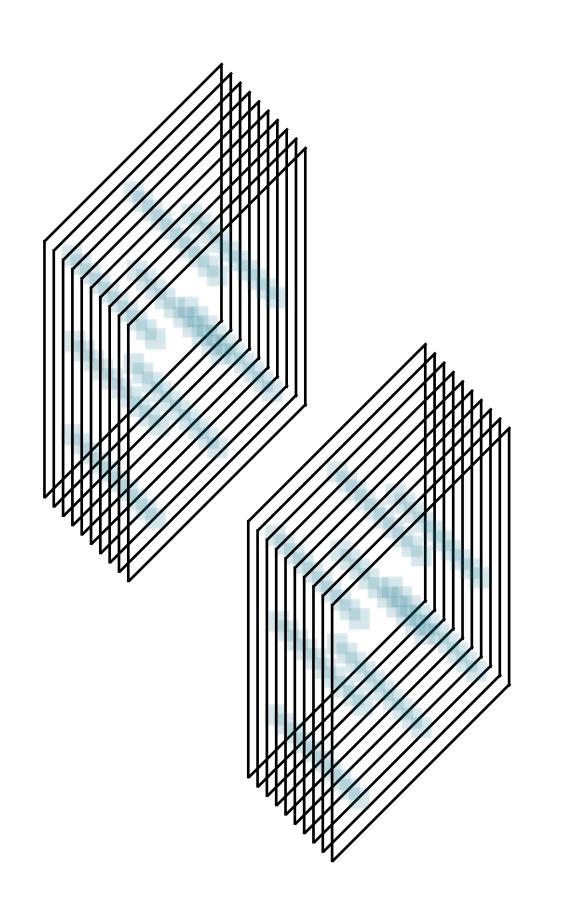
A pooling neuron simply applies some aggregation function to all inputs

Max, sum, average



Why use them?

- Greatly reduce memory usage during training
- Mitigate overfitting (via subsampling)
- Make NN recognize features independent of location (location invariance)

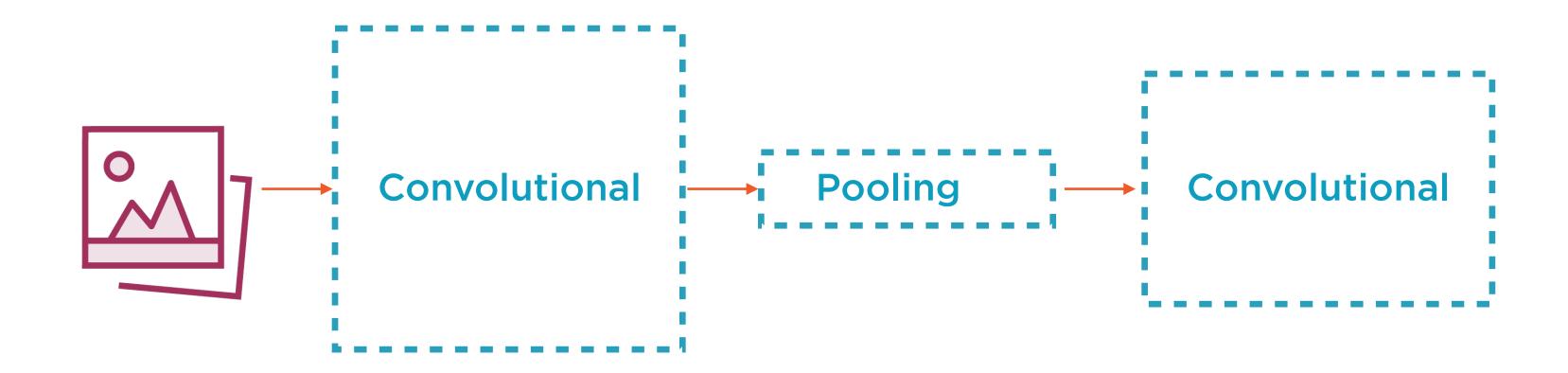


Pooling layers typically act on each channel independently

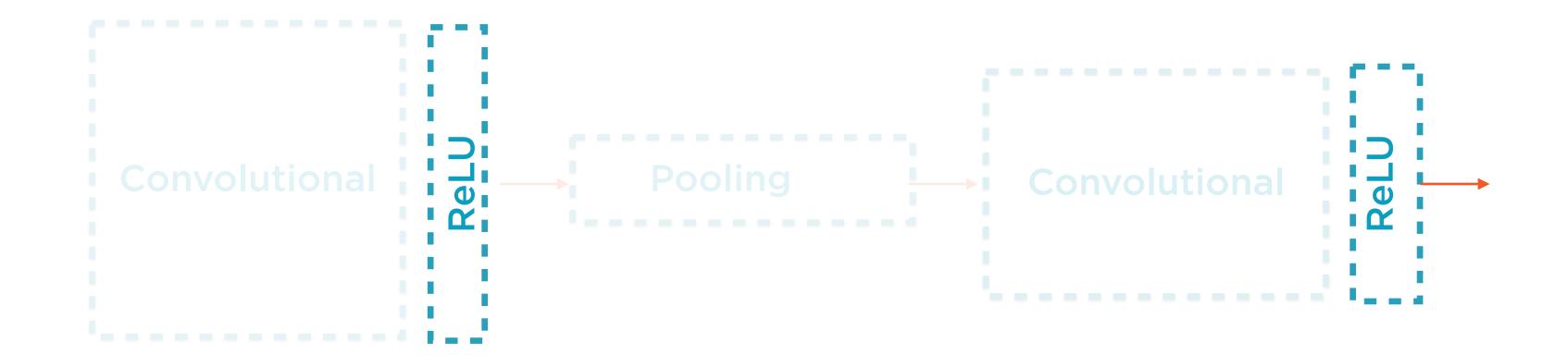
So, usually, output area < input area but

Output depth = Input depth

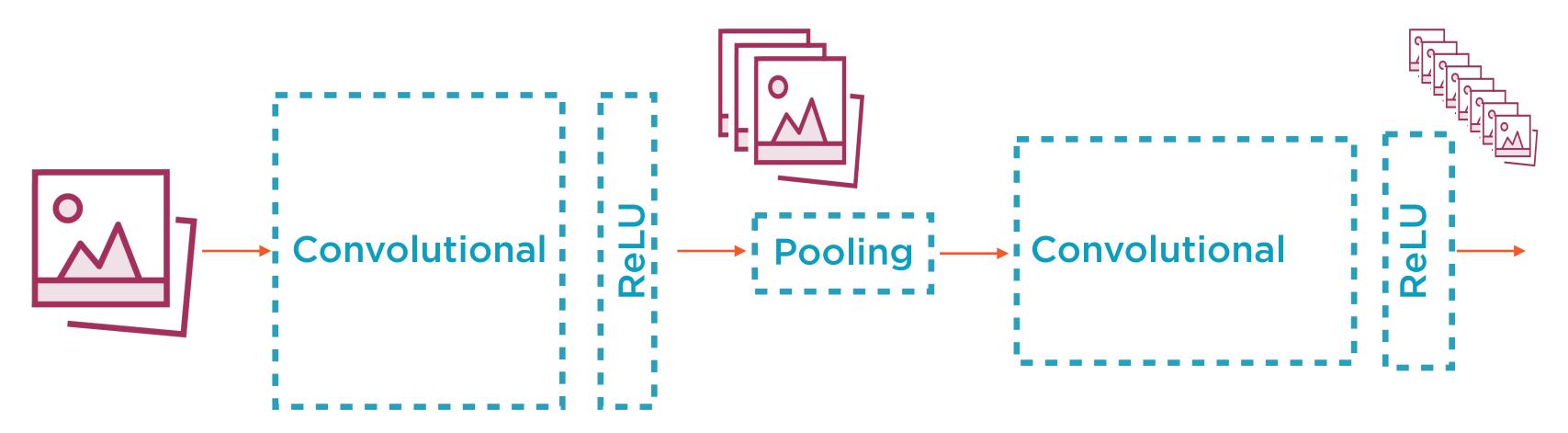
CNN Architectures



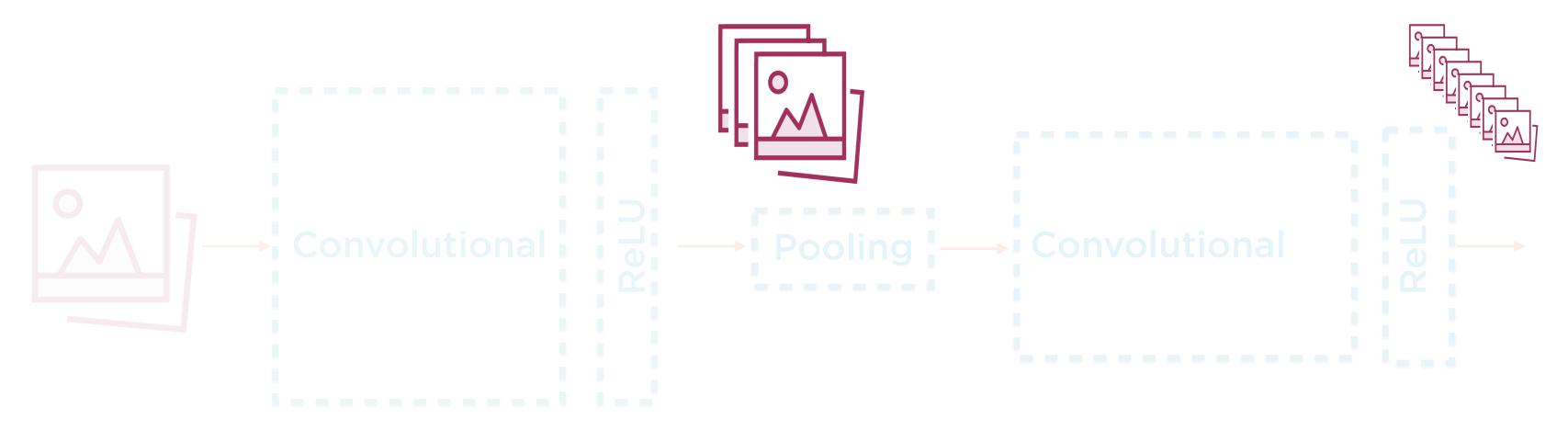
Alternating groups of convolutional and pooling layers



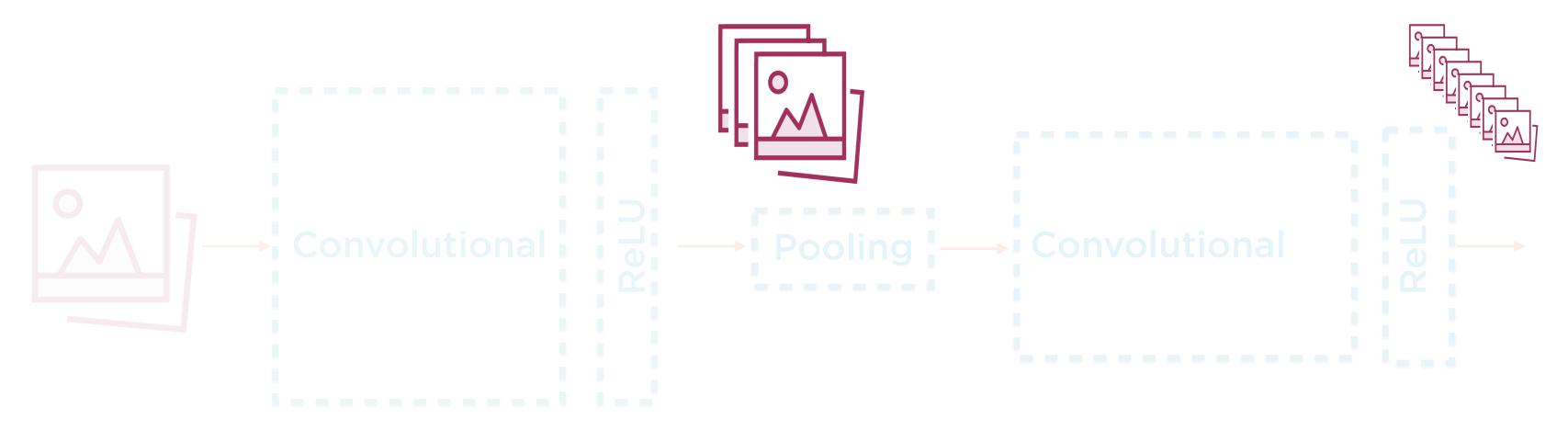
Each group of convolutional layers usually followed by a ReLU layer



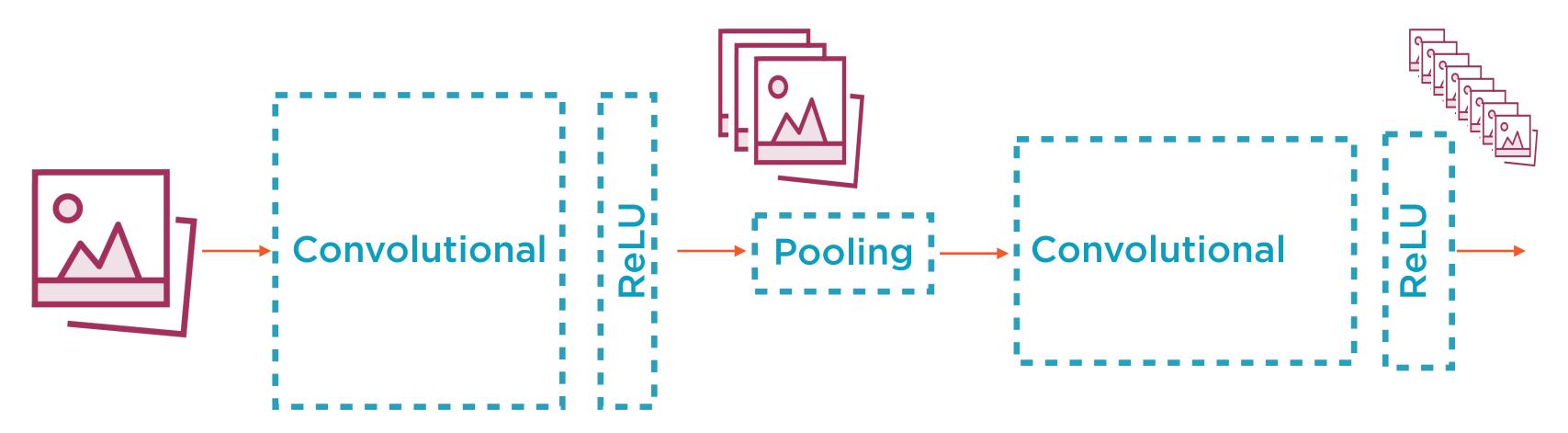
The output of each layer is also an image



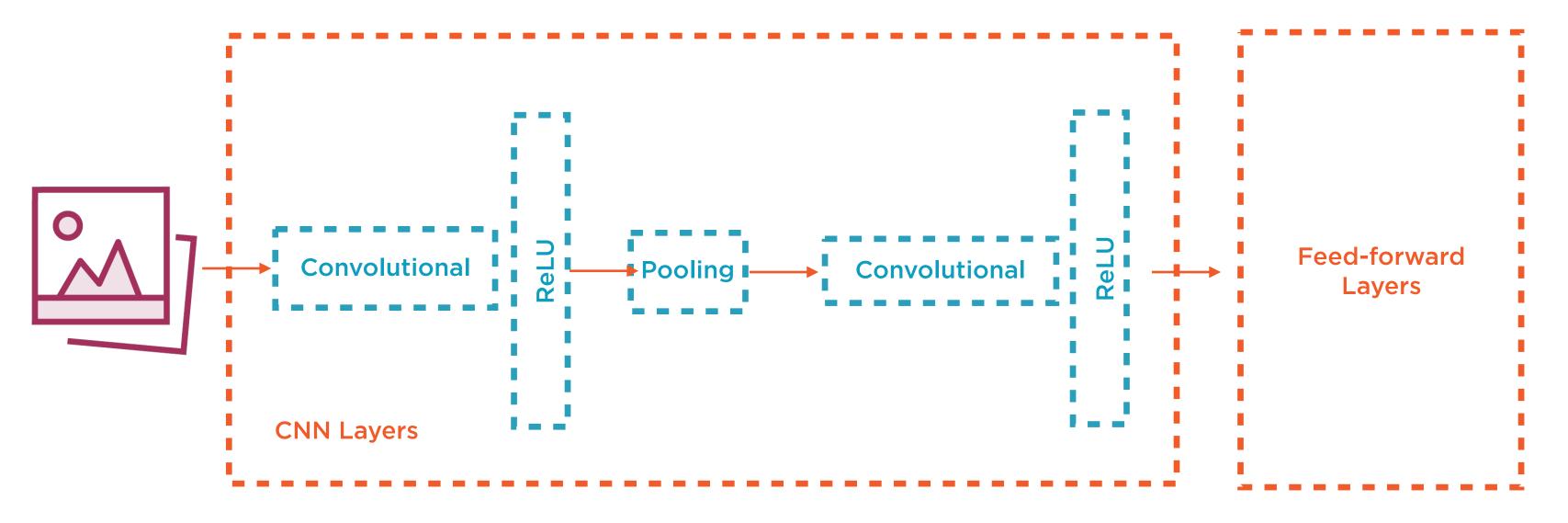
However successive outputs are smaller and smaller (due to pooling layers)



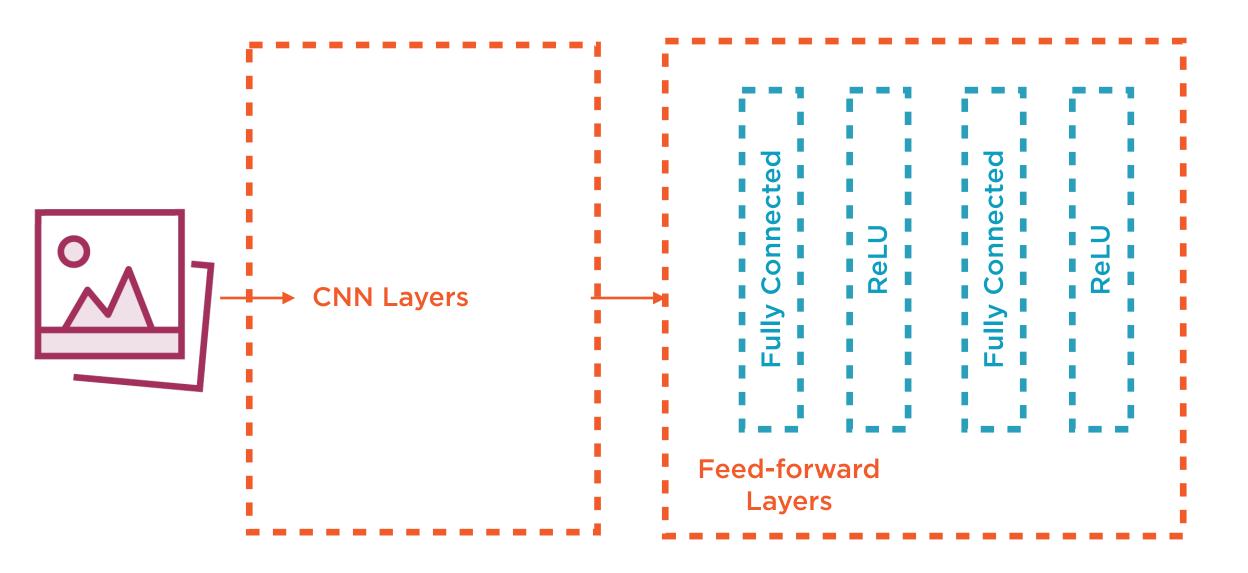
As well as deeper and deeper (due to feature maps in the convolutional layers)



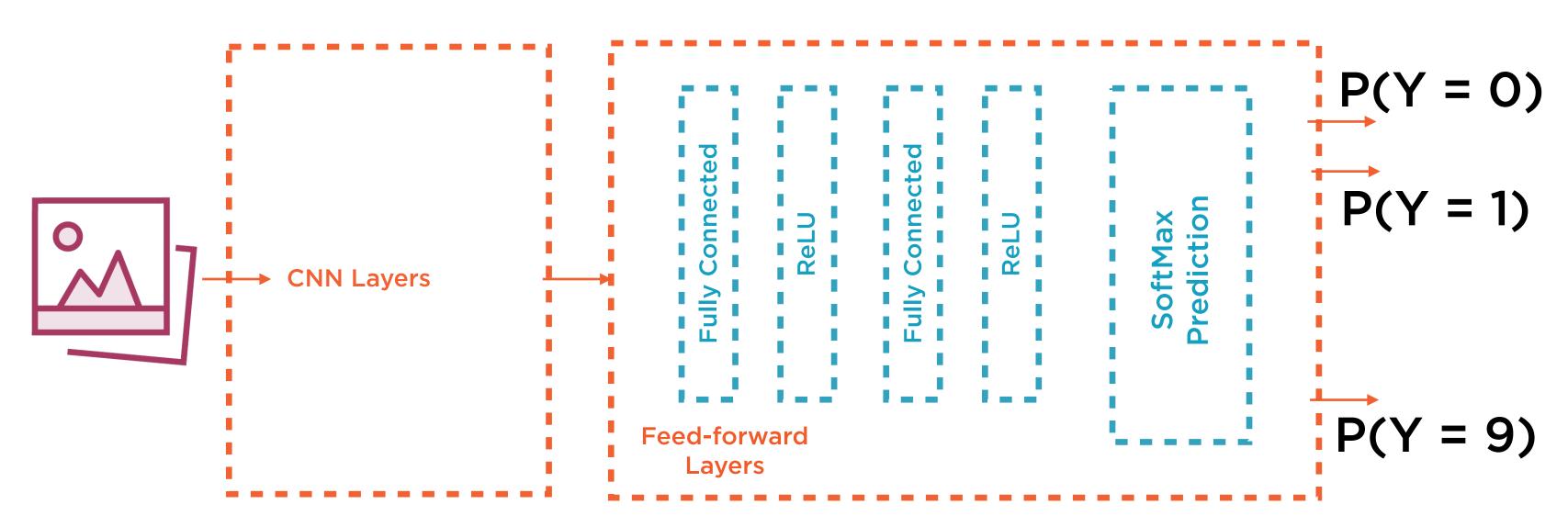
This entire set of layers is then fed into a regular, feed-forward NN



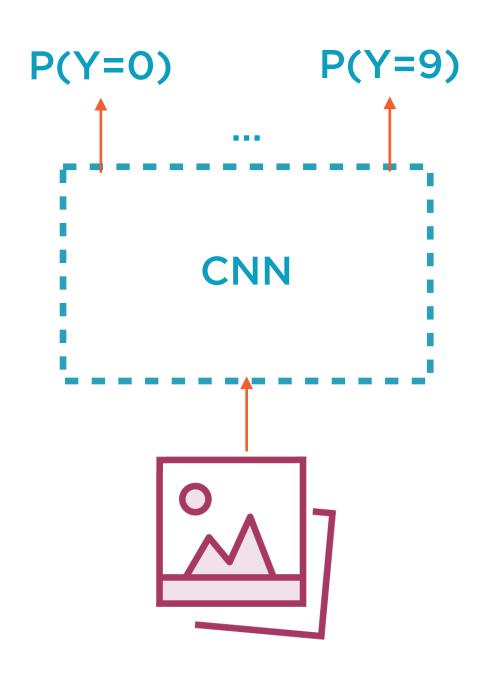
This entire set of layers is then fed into a regular, feed-forward NN



This feed-forward has a few fully connected layers with ReLU activation



This is the output layer, emitting probabilities



Input is an image
Outputs are probabilities

Demo

Apply convolution and pooling filters to images

Summary

Intuition behind Convolutional Neural Networks (CNNs)

Convolution layers and feature maps

Pooling layers to subsample inputs

Typical CNN architecture