

Homework 9 sample solution

Note Title

11/19/2008

2.30 a

Assume that the language is CF.

According to the pumping lemma, there is a pumping length p .

Consider $s = 0^p 1^p 0^p 1^p$. We'll show that it can't be pumped.

Consider any division of s into $uvxyz$ such that $|v| > 0$, and $|vxy| \leq p$. There are only two cases to consider.

case 1. either v or y contains both 0 and 1.
 $uvvxyyz$ does not contain 0 and 1 in the right order. (i.e., not in the form of $0 \dots 0 1 \dots 1 0 \dots 0 1 \dots 1$)

Thus $uvvxyyz$ is not a member of the language.

case 2. both v and y contains at most one kind of symbol.

$uvvxyyz$ contains runs of 0's and 1's of unequal length and cannot be a member of the language

Consequently $uvvxyyz$ is not a member of the language, contradicting that the language is CF.

2.31

Assume that the language is CF.

According to the pumping lemma, there is a pumping length p .

Consider $s = 0^p 1^{2p} 0^p$. We'll show that it can't be pumped.

Consider any division of s into $uvxyz$ such that $|v| > 0$, and $|vxy| \leq p$.

case 1 vxy contains only 0's or 1's.

$uvvxyyz$ contains an unequal # of 0's and 1's, so that it is not a member of the language

case 2. vxy contains both 0's and 1's

subcase 1. either v or y contains both 0 and 1.
 $uvvxyyz$ is not a palindrome.

subcase 2. both v and y contains at most one kind of symbols.

$uvvxyyz$ is not a palindrome

Consequently $uvvxyyz$ is not a member of
the language, contradicting that the language is CF.