

2)  $r(x,y) = \ln(x+y)$

$r_x = \frac{1}{x+y}$        $r_y = \frac{1}{x+y}$

~~רש~~  $r_x = r_y \Rightarrow \begin{cases} r_{xx} = r_{xy} \\ r_{xy} = r_{yy} \end{cases} \Rightarrow r_{xx} = r_{xy} = r_{yx} = r_{yy} = \frac{-1}{(x+y)^2}$  זהו

4)  $f(x,y) = 1-x+y-3x^2y$

~~$\frac{\partial f}{\partial x}(1,2) = \lim_{x \rightarrow 2} \frac{f(x,2) - f(1,2)}{x-2} = \lim_{x \rightarrow 2} \frac{1-x+2-6x^2 - (1-1+2-6)}{x-2} = \lim_{x \rightarrow 2} \frac{-6x^2 - x + 3}{x-2}$~~

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$= \lim_{x \rightarrow 1} \frac{-6x^2 - x + 7}{x-1} = \lim_{x \rightarrow 1} \frac{(-6x-7)(x-1)}{x-1} = \lim_{x \rightarrow 1} (-6x-7) = -13$

$\Rightarrow \boxed{\frac{\partial f}{\partial x} = -13}$

$\frac{\partial f}{\partial y} = \lim_{y \rightarrow 2} \frac{f(1,y) - f(1,2)}{y-2} = \lim_{y \rightarrow 2} \frac{1-1+y-3y - (1-1+2-6)}{y-2} = \lim_{y \rightarrow 2} \frac{-2y+4}{y-2} = \lim_{y \rightarrow 2} \frac{-2(y-2)}{y-2} = -2$

$\Rightarrow \boxed{\frac{\partial f}{\partial y} = -2}$