

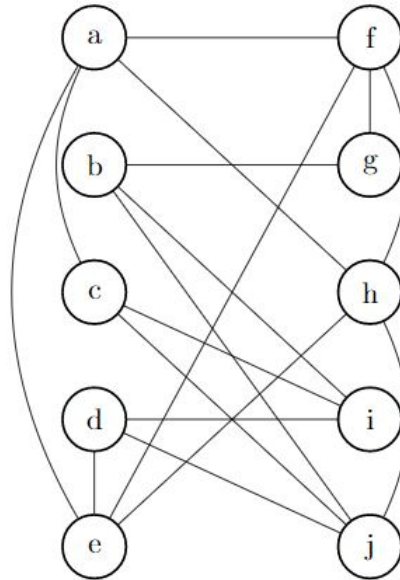
### Kuratowski's Theorem

A graph  $G$  is not planar  $\iff$  it has a subgraph that is a subdivision of either  $K_5$  (the pentagram) or  $K_{3,3}$

We'll be looking at problem set 7.6 in the course notes:

### Problem 1(d)

Prove whether or not this graph is planar: There is no algorithm to determine this efficiently. We just have



to play around with it. To prove that it's planar, we must show a planar embedding. If it's not planar, show that there exists a subdivision of either  $K_5$  or  $K_{3,3}$ .

In this case, this graph is *not* planar.

### Problem 8

Consider the prime graph  $B_n$ , where the vertices of  $B_n$  are  $\{1, \dots, n\}$ , and there is an edge  $uv$  if and only if  $u + v$  is prime.

- a) Prove that  $B_8$  is planar