

Statistical Analysis of Proteomics data

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1 Required packages and other preparations

```
library(BiocStyle)
library(knitr)
library(Biobase)
library(geneplotter)
library(ggplot2)
library(reshape2)
library(plyr)
library(dplyr)
library(gplots)
library(RColorBrewer)
library(arrayQualityMetrics)
library(stringr)
library(matrixStats)
library(genefilter)
library(limma)
library(openxlsx)
library(smoothmest)
library(tidyr)
library(vsn)
library(MSnbbase)
library(pheatmap)
library(fdrtool)
library(purrr)
library(tidyverse)
library(Hmisc)
library(gridExtra)
library(Peptides)
library("genefilter")

glog2 <- function(x) ((asinh(x)-log(2))/log(2))

# function to retrieve annotation data from Uniprot

getUniprotGoodies <- function(query) # columns
{
  ## query and columns start as character vectors
  qstring <- paste(query, collapse="+or+")
  cstring <- paste(columns, collapse=",")
  uri <- 'http://www.uniprot.org/uniprot/?query='
  fullUri <- paste0(uri,qstring,'&format=tab')#&columns=',cstring)
  dat <- read.delim(fullUri, stringsAsFactors=FALSE)
  ## now remove things that were not in the specific original query...
  dat <- dat[dat[,1] %in% query,]
  dat
}

plotProtein <- function(Acc){
```

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```
tmp <- exprs(time_data_vsn)[Acc, ]  
pl <- (qplot(time, tmp, color = time, main = Acc)  
       + ylab("protein_exp_log2"))  
pl + scale_color_brewer(type="qual", palette=2)  
}  
  
  
# function to compute a robust mean  
robustMean <- function(x){  
  if(length(x) == 1){return(x)}  
  else{  
    return(smhuber(x)$mu)  
  }  
}
```

2 Overview of a typical proteomics experiment

A typical proteomics experiment follows the steps depicted in the Figure below.

Full proteome analysis - experimental workflow

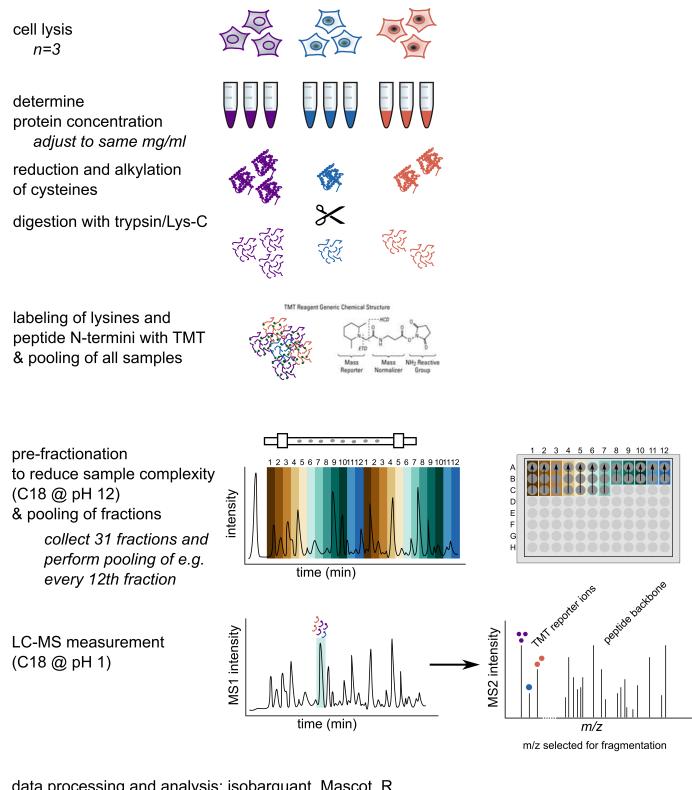


Figure 1: Workflow of a proteomics experiment

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This is an example of a full proteome analysis of three different cell lines. The first cell line is the wildtype of HEK 293T (wt), the second cell line is a CRISPR knock-out (ko) of Sphingosine-1-phosphate lyase 1 (SPGL1 - single_ko) and the third cell line is a double CRISPR knock-out of Ceramide glucosyltransferase (UGCG) and SPGL1 (double_ko). For each biological conditions, three independent replicates were generated and analyzed as shown in the figure above.

In our case, the raw output files of the mass spectrometer were processed with IsobarQuant ([Franken et. al., 2015](#)), a software that was developed at Cellzome.

3 Processing strategy

3.1 Raw data

IsobarQuant gives three text files as an output, a summary.txt file, a peptides.txt file and a protein.txt file. The peptides.txt and proteins.txt files contain the intensities that were quantified for the different tmt channels. The peptides.txt file contain the raw intensities for each identified peptide ("sig") whereas the proteins.txt file contains already summarized values for each protein for which the individual peptide tmt signals belonging to a particular protein were summed up ("signal_sum").

3.2 Use of intensities instead of ratios

We use the intensities directly here using the following steps:

- 1.) We first perform a glog transformation on the raw protein-intensities. The glog is very similar to a standard log transform, but performs a less severe shrinkage for low intensities. The figure below illustrates this point:
- 2.) Following this, we apply the vsn algorithm to all the summarized values on the protein level on the raw intensity scale (We exponentiate the summarized values again). vsn essentially centers and scales the values within a channel and then performs a glog transformation.
- 3.) We finally run *limma* on the *vsn* normalized data.

This is very similar to the strategy followed in [Hughes et. al., 2014](#), although there *vsn* is applied on the peptide level data and the protein group summarization is performed later on.

3.3 Some reasons why it is better to not work with ratios

Although ratios are widely used in proteomics, from a statistical point of view, it is better to use raw intensities values as their computing a ratio beforehand changes the distribution and especially the variance of your data dramatically: by dividing by a large intensity, small intensity values will be compressed, dividing by a small intensity will boost the values.

Also, once ratios have been formed, it is not easy to go back, thus essentially throwing data away.

► the “glog” transformation

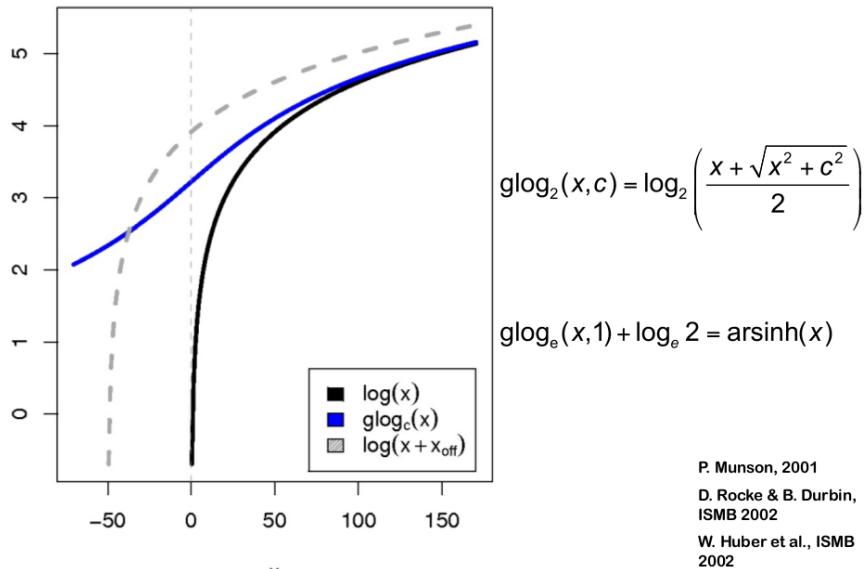


Figure 2: [glog2](#)

On top of that, if your experimental design becomes more complex, you can use full featured linear models (such as we do here) more easily instead of just simple two-group comparisons. Furthermore, one can find batch effects and the like more readily in the data.

4 Experimental design

In the data set at hand, we have single run with 10 TMT labels. This labels cover 3 conditions with 3 replicates in each condition.

We first import the table holding the experimental design.

```

expDesign <- as.data.frame(read_csv("metadata.csv"))
Parsed with column specification:
cols(
  tmt.label = col_character(),
  rep = col_character(),
  condition = col_character()
)
rownames(expDesign) <- expDesign$tmt.label

expDesign
      tmt.label   rep condition
126       126  rep1        wt
127L     127L  rep1  single_ko
127H     127H  rep1 double_ko
128L     128L  rep2        wt
128H     128H  rep2  single_ko
129L     129L  rep2 double_ko
129H     129H  rep3        wt
130L     130L  rep3  single_ko
130H     130H  rep3 double_ko
131L     131L <NA>      <NA>

```

In the analysis below, we will only use the `wt` and `single_ko` conditions in order to keep it simple.

5 Import of the raw data

We first import the raw data, the protein quantifications saved as tab-separated file, with one column per label as well as the peptide level data. We extract the samples fraction from the column `source_file` in the peptide table.

```
load("peptide_data.RData")  
  
peptide_data  
# A tibble: 348,352 x 38  
  protein_group_no protein_id sequence modifications      mw precursor_mz  
            <int>     <chr>    <chr>        <chr>      <dbl>      <dbl>  
1              1 P30613   SQRDLAK  TMT10plex K7; 1046.      524.  
2              1 P30613   EMIKAGM~ TMT10plex N-~ 1691.      424.  
3              1 P30613   GPEIR    TMT10plex N-~  799.      401.  
4              1 P30613   GDLGIEI~ TMT10plex N-- 1599.      800.  
5              1 P30613   GDLGIEI~ TMT10plex N-~ 1599.      800.  
6              1 P30613   GDLGIEI~ TMT10plex N-~ 1599.      800.
```

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```

7          1 P30613    GDLGIEI~ TMT10plex N~- 1599.      800.
8          1 P30613    GDLGIEI~ TMT10plex K1~ 1370.      686.
9          1 P30613    GDLGIEI~ TMT10plex N~- 1599.      534.
10         1 P30613    GDLGIEI~ TMT10plex N~- 1599.      800.
# ... with 348,342 more rows, and 32 more variables: charge_state <int>,
#   ppm_error <dbl>, score <int>, fdr_at_score <dbl>, `delta mod` <dbl>,
#   rank <int>, msms_id <int>, source_file <chr>, `retention time` <dbl>,
#   peak_intensity <dbl>, s2i <dbl>, p2t <dbl>, is_unique <int>,
#   in_quantification_of_protein <int>, in_protein_inference <dbl>,
#   in_top3 <int>, seq_start <int>, seq_end <int>, is_decoy <int>, `prior ion
#   ratio` <dbl>, `least squares` <dbl>, `ms1 source` <chr>, sig_126 <dbl>,
#   sig_127L <dbl>, sig_127H <dbl>, sig_128L <dbl>, sig_128H <dbl>,
#   sig_129L <dbl>, sig_129H <dbl>, sig_130L <dbl>, sig_130H <dbl>,
#   sig_131L <dbl>

peptide_data$fraction <- gsub("(.+R1_)|(.\$raw$)", "", peptide_data$source_file)
peptide_data$fraction <- factor(peptide_data$fraction,
                                 ordered = TRUE,
                                 levels = c("F01", "F02", "F03", "F04", "F05",
                                           "F06", "F07", "F08", "F09", "F10",
                                           "F11", "F12"))

protein_data <- read_tsv("H0027_student_PEP_merged_results_20180202_1618_proteins.txt")
Parsed with column specification:
cols(
  .default = col_double(),
  protein_group_no = col_integer(),
  protein_id = col_character(),
  description = col_character(),
  gene_name = col_character(),
  mw = col_character(),
  max_score = col_integer(),
  total_score = col_integer(),
  ssm = col_integer(),
  upm = col_integer(),
  fqssm = col_integer(),
  qssm = col_integer(),
  qupm = col_integer(),
  reference_label = col_integer()
)
See spec(...) for full column specifications.

protein_data
# A tibble: 9,586 x 45
  protein_group_no protein_id description gene_name mw      top3 protein_fdr
              <int>     <chr>      <chr>      <chr> <dbl>      <dbl>
1             1 P30613 Pyruvate k~ PKLR    6677~  5.40      0
2             2 P23919 Thymidylat~ DTYMK   2764~  8.21      0
3             3 P40425 Pre-B-cell~ PBX2    5117~  6.08      0
4             4 P40429 60S riboso~ RPL13A  3003~  9.01      0
5             5 F5GZF0|01~ Cyclin-dep~ CDK2AP1 8136~  6.56      0

```

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```
6          6 A0A087WT5~ Transthyre~ TTR      2219~  6.80   0.00640
7          7 P35251|P3~ Replicatio~ RFC1     1651~  7.67   0
8          8 C9JBG0|Q9~ Ras-relate~ RAB34    2766~  7.04   0.000678
9          9 I3L1H5|K7~ Diphthamid~ DPH1     5117~  7.28   0
10        10 P53701   Cytochrome~ HCCS      3510~  8.14   0
# ... with 9,576 more rows, and 38 more variables: max_score <int>,
#   total_score <int>, ssm <int>, upm <int>, fqssm <int>, qssm <int>,
#   qupm <int>, reference_label <int>, signal_sum_126 <dbl>,
#   signal_sum_127L <dbl>, signal_sum_127H <dbl>, signal_sum_128L <dbl>,
#   signal_sum_128H <dbl>, signal_sum_129L <dbl>, signal_sum_129H <dbl>,
#   signal_sum_130L <dbl>, signal_sum_130H <dbl>, signal_sum_131L <dbl>,
#   rel_fc_126 <dbl>, rel_fc_127L <dbl>, rel_fc_127H <dbl>, rel_fc_128L <dbl>,
#   rel_fc_128H <dbl>, rel_fc_129L <dbl>, rel_fc_129H <dbl>, rel_fc_130L <dbl>,
#   rel_fc_130H <dbl>, rel_fc_131L <dbl>, delta_conf_126 <dbl>,
#   delta_conf_127L <dbl>, delta_conf_127H <dbl>, delta_conf_128L <dbl>,
#   delta_conf_128H <dbl>, delta_conf_129L <dbl>, delta_conf_129H <dbl>,
#   delta_conf_130L <dbl>, delta_conf_130H <dbl>, delta_conf_131L <dbl>
```

6 Quality control analysis of workflow steps

In the following analysis we will analyze the `peptides.txt` file and the `protein.txt` file in various ways in order to assess the results of each individual step of the experimental workflow.

6.1 Protein counts

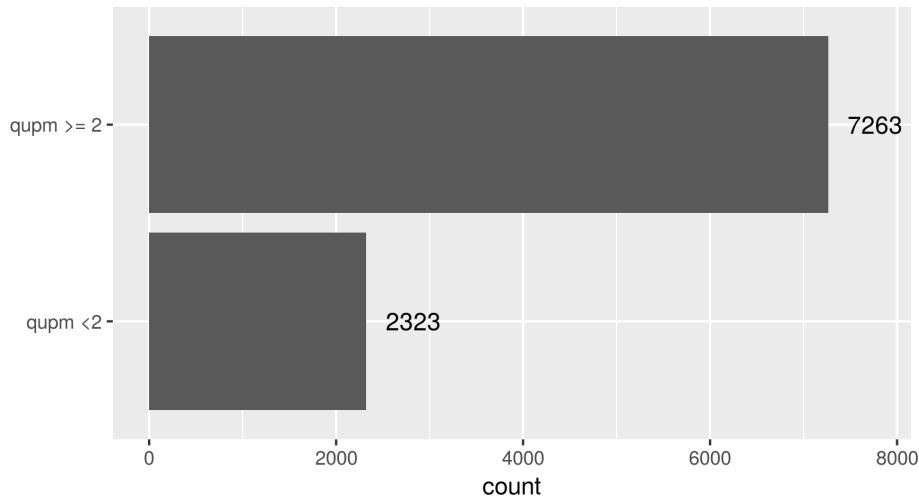
The total number of identified proteins is useful to judge the overall quality of the experiment. This includes both the success of the cell lysis as well as the performance of the mass spectrometer.

The variable `qupm` indicates the number of peptides quantified per protein. We inspect how many proteins have at least 2 uniquely quantified peptides.

```
ggplot(data = protein_data, aes(ifelse(qupm >= 2, "qupm >= 2", "qupm <2"))) +
  geom_bar() +
  xlab("") +
  geom_text(stat='count', aes(label = ..count..), nudge_y = 500) +
  ggtitle(paste("total number of identified proteins:", nrow(protein_data))) +
  coord_flip()
```

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total number of identified proteins: 9586

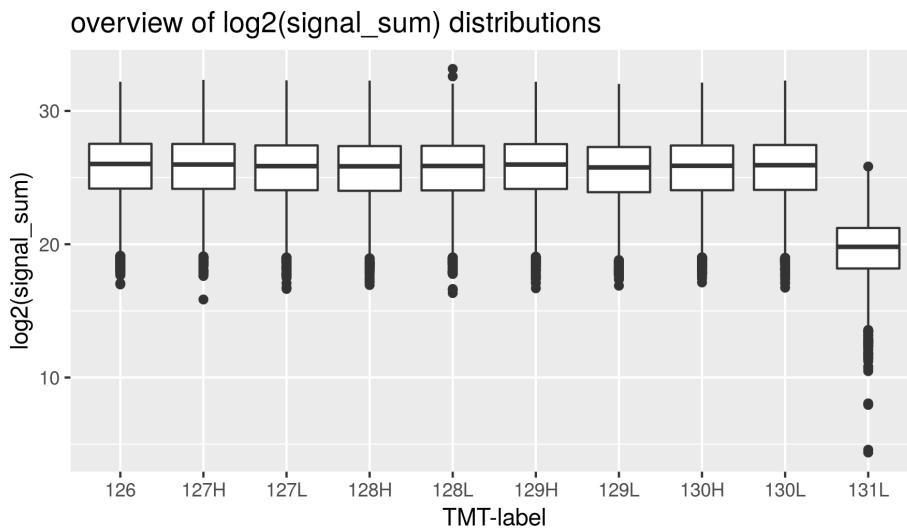


6.2 Measurement of protein concentration

Prior to TMT labeling, the protein concentration of each sample is measured and the protein amount for the proteomics experiment might be adapted if needed. The distribution of the signal sums of all proteins for each TMT channel is a good estimate of the protein concentration in each sample.

```
sub <- protein_data %>%
  dplyr::select(starts_with("signal_sum")) %>%
  gather()

ggplot(data = sub,aes(gsub("signal_sum_","",key), log2(value))) +
  geom_boxplot() +
  xlab("TMT-label") + ylab("log2(signal_sum)") +
  ggtitle("overview of log2(signal_sum) distributions")
```



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```
rm(sub)
```

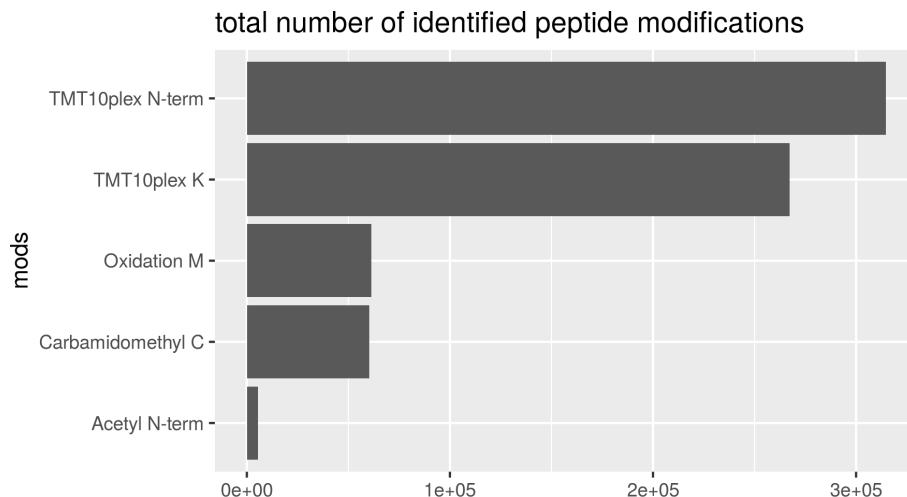
We can see that label 131L has a very low signal intensity compared to the rest of the channels. This is expected, as this label was not used in the experiment.

6.3 Reduction and alkylation of cysteines

The 'modifications' column of the peptides.txt output file of IsobarQuant contains an overview of the identified modifications for each peptide. The count statistic of the various modifications enables us to judge both the reduction and alkylation step of Cysteines, as well as the labeling with the TMT reagents.

```
mods <- peptide_data$modifications
mods <- gsub("[0-9]+; ;", "", mods)
mods <- gsub(";$", "", mods)
mods <- unlist(strsplit(mods, split = "; "))
mods <- na.omit(mods)

qplot(mods, geom = "bar") +
  coord_flip() +
  ggtitle("total number of identified peptide modifications")
```



Cysteines are first reduced with Dithiothreitol (DTT) and then alkylated with Iodoacetamide (IAA) in order to destroy disulfide bridges between them. They would otherwise link peptides together.

The reduction and alkylation results in a carbamidomethyl group attached to the sulphur of the cysteine side chains. This is a peptide modification that is included into the mascot search. Therefore, this modification can be found in the 'modifications' column. Missing carbamidomethyl modification could indicate problems with the reduction and alkylation step of the protocol.

Furthermore, TMT labels are identified on the N-terminus as well as on lysine side-chains. This is because they are attached via an succinimidylester which is reactive to amino groups. Those are present on the N-terminus of peptides as well as on the lysine side chains.

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6.4 Tryptic digest

Trypsine is used to digest the proteins into smaller peptides. The enzyme cleaves after an arginine (R) or a lysine (K).

From the identified sequences in the peptides table, we can count how often an arginine or a lysine appears inside the sequence.

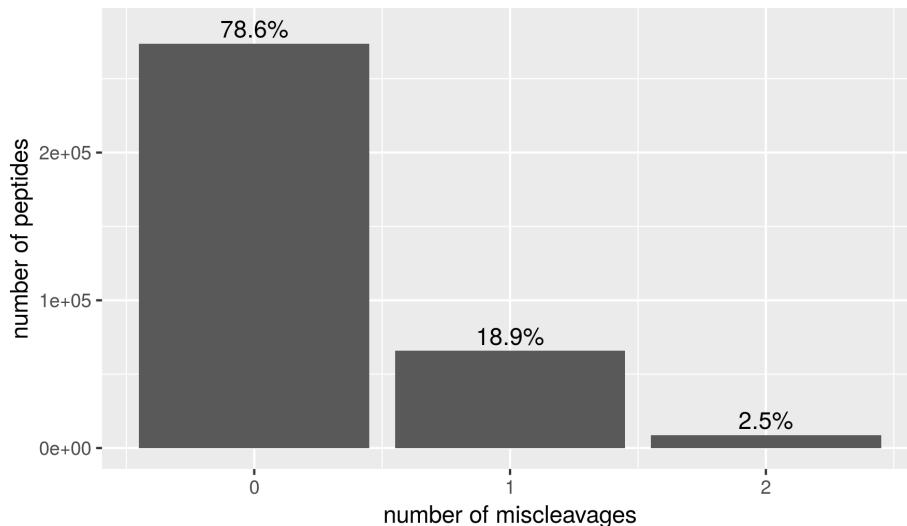
We interpret this the number of miscleavages as a performance measure for the tryptic digest.

```
peptide_data <- peptide_data %>%
  mutate(sequence = toupper(sequence)) %>%
  mutate(no.of.misceavages = gsub("[K,R]$", "", sequence)) %>%
  mutate(no.of.misceavages = gsub("[^KR]", "", no.of.misceavages)) %>%
  mutate(no.of.misceavages = nchar(no.of.misceavages))

bar_pl <- ggplot(data = peptide_data, aes(x = no.of.misceavages)) +
  stat_count()

bar_data <- layer_data(bar_pl, 1) %>%
  mutate(prop_rounded = paste0(round(prop, 3)*100, "%"))

ggplot(data = bar_data, aes(x = x, y = y)) +
  geom_bar(stat = "identity") +
  geom_text(mapping = aes(x = x, y = y, label = prop_rounded),
            nudge_y = 10000) +
  xlab("number of miscleavages") +
  ylab("number of peptides")
```

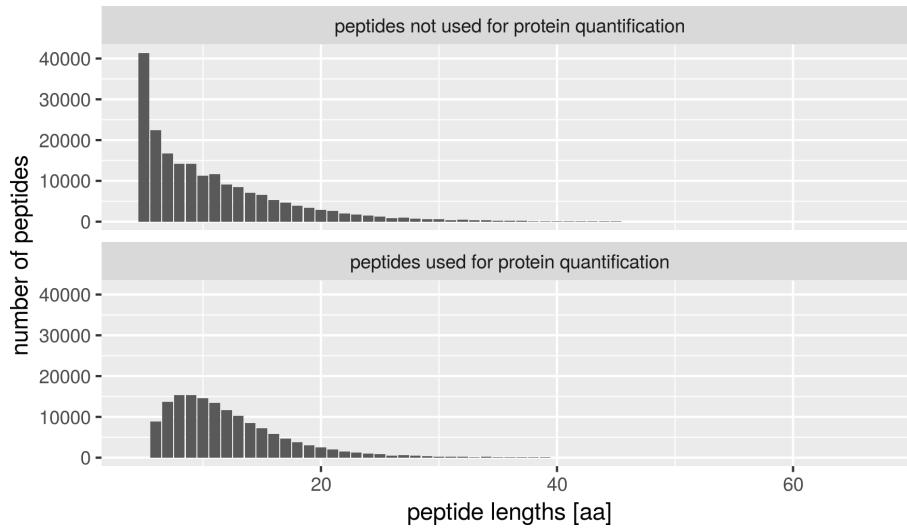


Furthermore, the distribution of peptide lengths is another way to judge the quality of the tryptic digest. The minimum peptide length required for quantification is 5, so peptides used in the quantification step should typically be longer.

```
ggplot(data = peptide_data, aes(nchar(sequence))) +
  geom_bar() +
  xlab("peptide lengths [aa]") +
```

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```
ylab("number of peptides") +  
  facet_wrap(~ifelse(in_quantification_of_protein == 1,  
                     "peptides used for protein quantification",  
                     "peptides not used for protein quantification"),  
            ncol = 1)
```



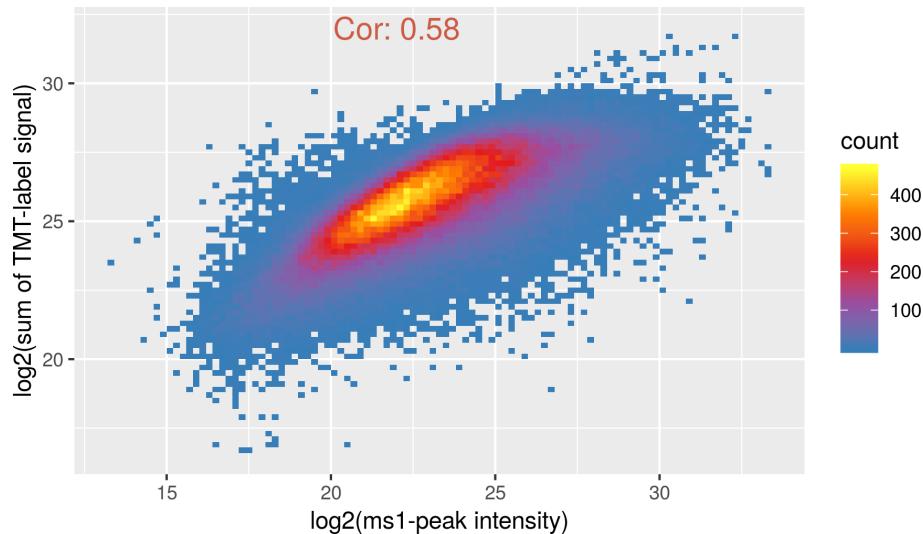
6.5 TMT based quantification vs MS 1 peak

In order to judge the TMT labeling efficiency, one can correlate the ms1 peak intensities with the sum of all tmt signals for each identified peptide.

Those two values should correlate. We first compute the sum the TMT labels and then create a scatterplot of this and the MS1 peak.

```
peptide_data$sig_sum <- peptide_data %>%  
  dplyr::select(starts_with("sig")) %>%  
  apply(1, sum, na.rm = TRUE)  
  
scp <- ggplot(data = subset(peptide_data,in_quantification_of_protein == 1),  
               mapping = aes(log2(peak_intensity), log2(sig_sum))) +  
  stat_bin2d(binwidth = 0.2) +  
  scale_fill_gradient(colours = c("#377eb8", "#984ea3", "#e41alc",  
                                "#ff7f00", "#ffff33")) +  
  xlab("log2(ms1-peak intensity)") +  
  ylab("log2(sum of TMT-label signal)")  
  
scp +  
  annotate("text", label = paste0("Cor: ",  
                                 round(cor(layer_data(scp)$x,  
                                             layer_data(scp)$y,  
                                             method = "spearman"), 2)),  
          x = 22, y = 32, size = 5, colour = "coral3")
```

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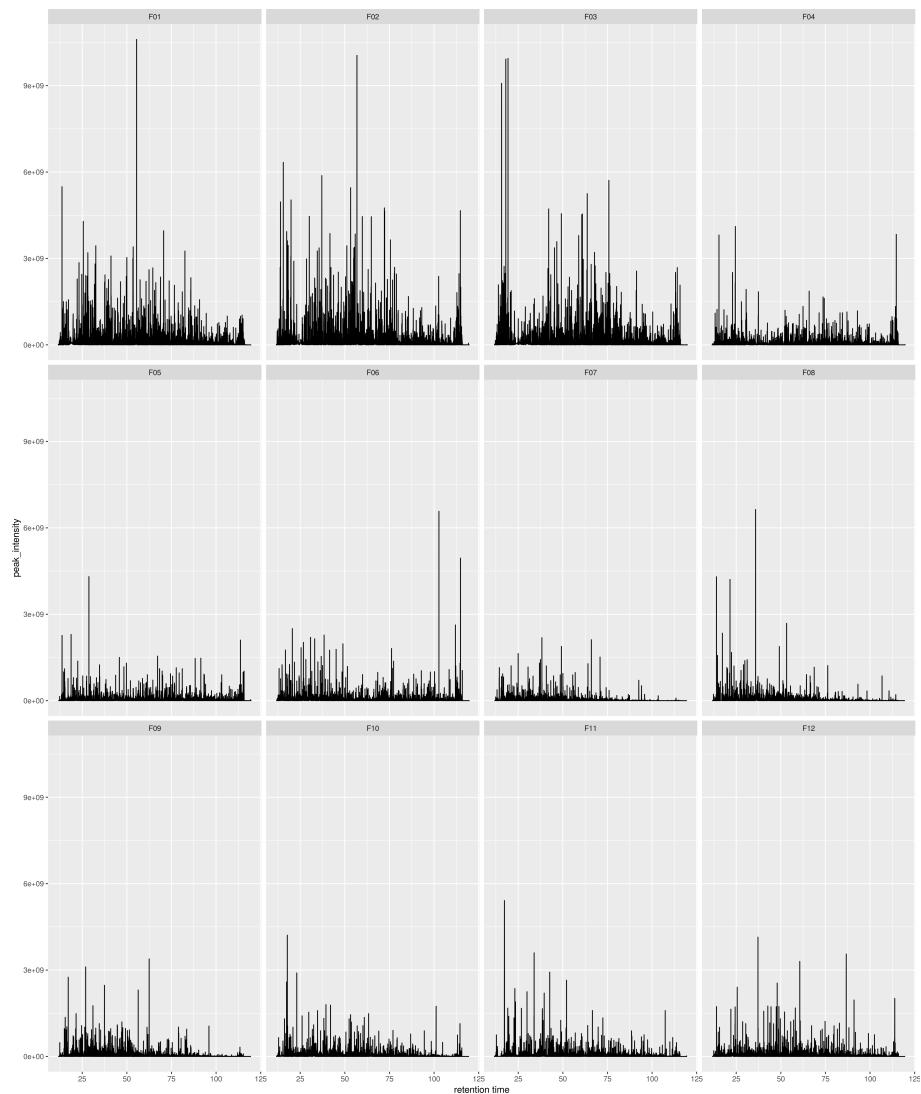
We can see that these values are reasonably correlated to each other. Otherwise, this could indicate problems with the TMT labeling.

6.6 Prefractionation and chromatography

Prefractionation of the input samples, results in 12 different fractions. Each of them was injected into the mass spectrometer separately producing a ms1 spectrum, which we plot now:

```
ggplot(data = subset(peptide_data, in_quantification_of_protein == 1),
       aes(`retention time`, peak_intensity)) +
  geom_line() +
  facet_wrap(~fraction)
```

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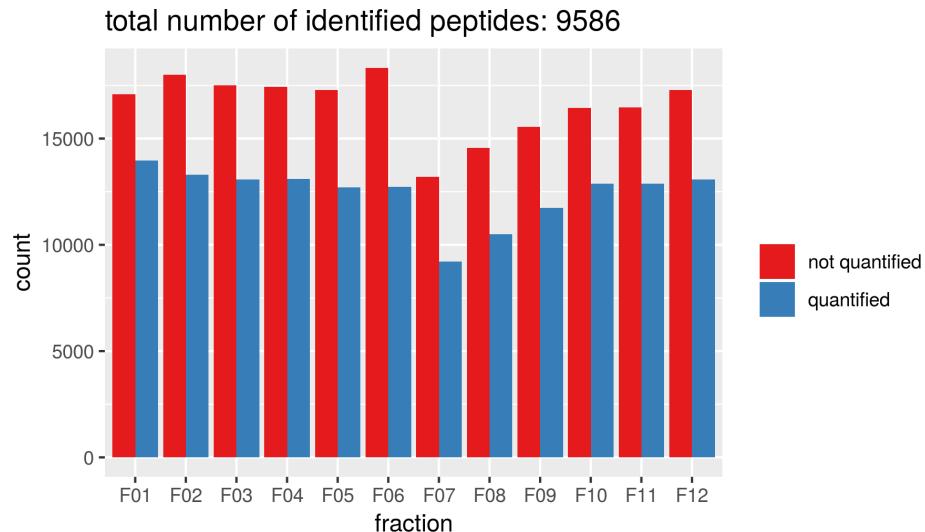


In order to judge the performance of the instrument, we plot the number of peptide identifications in the different fractions.

We also distinguish between peptides used / not used for the final quantification.

```
ggplot(data = peptide_data,
        aes(fraction, fill = ifelse(in_quantification_of_protein == 1,
                                    "quantified", "not quantified")) +
        geom_bar(position = position_dodge()) +
        xlab("fraction") +
        ggtitle(paste("total number of identified peptides:",
                     nrow(protein_data))) +
        scale_fill_brewer(palette = "Set1", name = "")
```

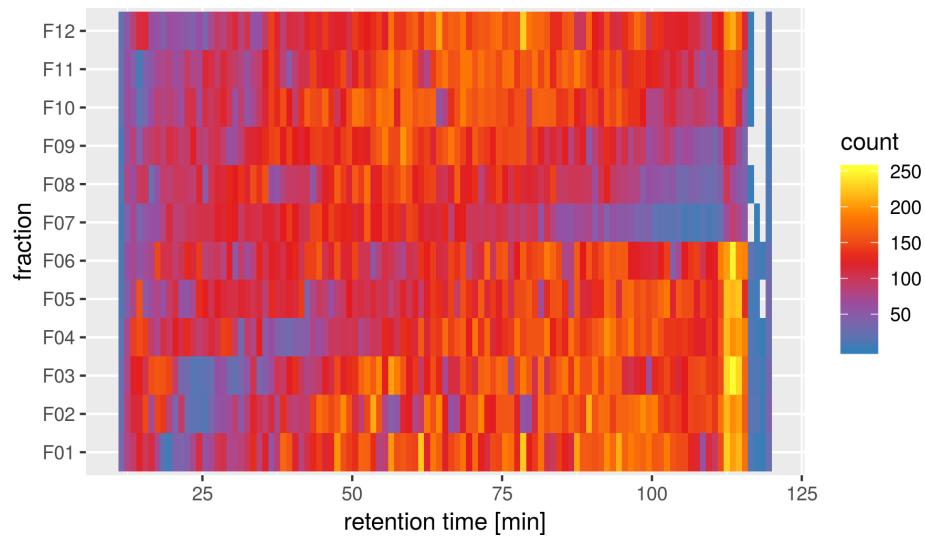
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Fractions 7, 8 and 9 show smaller numbers of identified peptides. Here, the fractionation could possibly be optimized.

For each mass spec run, the peptides are separated with a C18 column. The next plot shows the frequency of which the peptides are eluted from the column in each fraction.

```
ggplot(data = subset(peptide_data,in_quantification_of_protein == 1),  
       aes(`retention time`, fraction)) +  
  stat_bin2d(binwidth = 1) +  
  scale_fill_gradientn(colors = c("#377eb8", "#984ea3", "#e41a1c",  
                         "#ff7f00", "#ffff33")) +  
  xlab("retention time [min]")
```

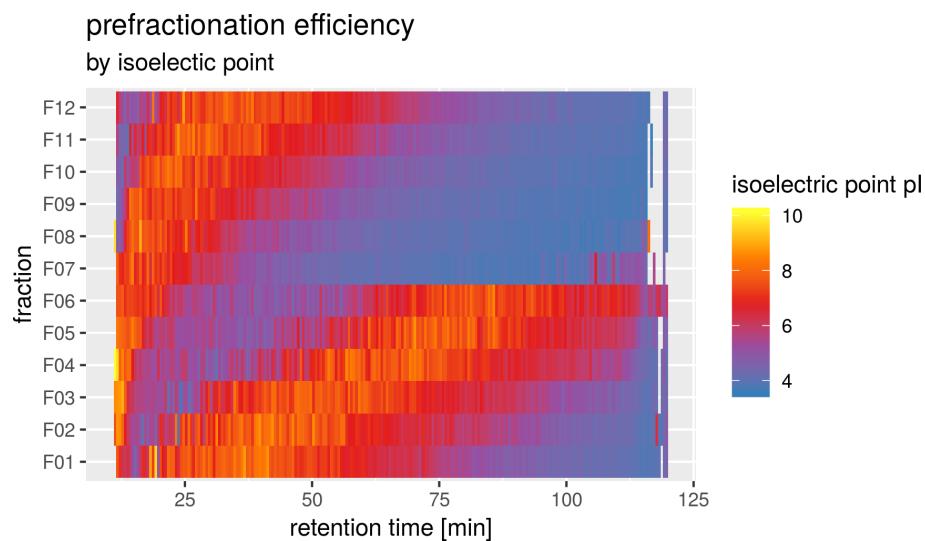


The prefractionation took place at a much higher pH, resulting in the deprotonation of certain peptide residues. Therefore, the peptides were separated based on their isoelectric point (pI). The isoelectric point indicates the pH on which the peptide has a neutral net charge. Changing

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the pH changes the total charge of the peptide and thereby the interaction with the C18 column. This can be visualized by computing the pI for each peptide and summarizing the average pI per retention time for each fraction.

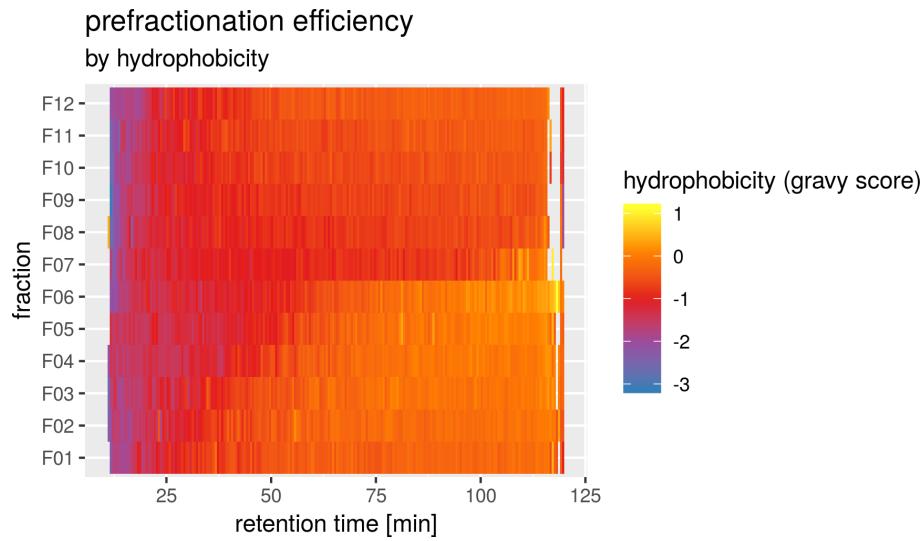
```
peptide_data$pI <- Peptides::pI(peptide_data$sequence)
ggplot(data = subset(peptide_data,in_quantification_of_protein == 1),
       aes(`retention time`,fraction)) +
  stat_summary_2d(aes(z = pI),binwidth = 0.5) +
  scale_fill_gradient(colours = c("#377eb8","#984ea3","#e41a1c",
                                  "#ff7f00","#ffff33"),
                      name = "isoelectric point pI") +
  xlab("retention time [min]") +
  ggtitle("prefractionation efficiency",
          subtitle = "by isoelectric point")
```



A C18 column also separates peptides based on their hydrophobicity. To visualize this, one can calculate a hydrophobicity score for each peptide and show again the average for a specific retention time.

```
peptide_data$gravy <- Peptides::hydrophobicity(peptide_data$sequence)
ggplot(data = subset(peptide_data, in_quantification_of_protein == 1),
       aes(`retention time`,fraction)) +
  stat_summary_2d(aes(z = gravy), binwidth = 0.5) +
  scale_fill_gradient(colours = c("#377eb8","#984ea3","#e41a1c",
                                  "#ff7f00","#ffff33"),
                      name = "hydrophobicity (gravy score)") +
  xlab("retention time [min]") +
  ggtitle("prefractionation efficiency",
          subtitle = "by hydrophobicity")
```

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The cumulative sum of unique protein ids over the different fractions is helpful to judge the gain of depth for the various fractions.

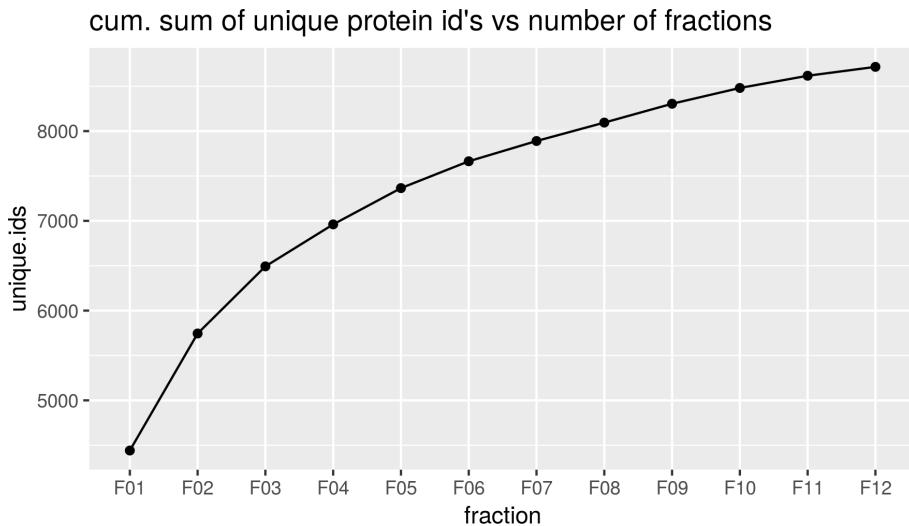
This gain will be decreasing with an increasing number of fractions.

```
id_data <- NULL

pfractions <- levels(peptide_data$fraction)
for (i in seq_along(pfractions)) {
  sub <- subset(peptide_data,fraction %in% pfractions[1:i]&
    in_quantification_of_protein==1)
  if (nrow(sub) > 0) {
    id_sub <- data.frame(fraction = pfractions[i],
      unique.ids = length(unique(sub$protein_id)))
    id_data <- rbind(id_data,id_sub)
    rm(id_sub)
  }
}

id_data$fraction <- factor(id_data$fraction,
  ordered = TRUE, levels = pfractions)
id_data$file <- "file"
ggplot(data = id_data, aes(fraction,unique.ids)) +
  geom_line(aes(group = file)) +
  geom_point() +
  ggtitle(label = "cum. sum of unique protein id's vs number of fractions")
```

Statistical Analysis of Proteomics data

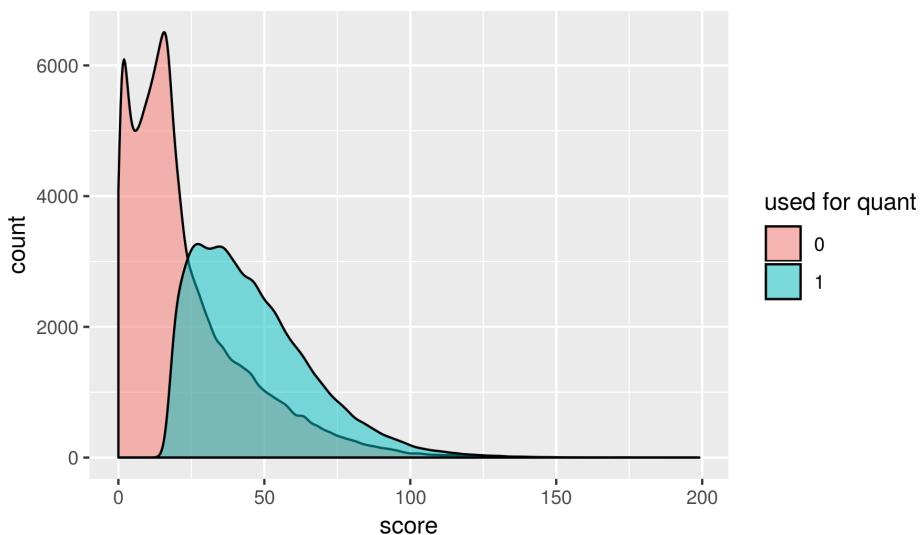


6.7 Peptide identification

6.7.1 Mascot score

Each identified ms₂ spectrum is annotated to a specific peptide sequence. The quality of the annotation is quantified by a mascot score, a probability- based scoring system. The better the quality of the identification, the higher the score. Peptides which were used for the protein quantification have a higher mascot score than the ones not used. Their scores have a lower bound of 20, our quality cut-off.

```
ggplot(data = peptide_data,aes(score,  
fill = factor(in_quantification_of_protein))) +  
  geom_density(aes(y = ..count..), alpha = 0.5) +  
  scale_fill_discrete(guide = guide_legend(title = "used for quant"))
```

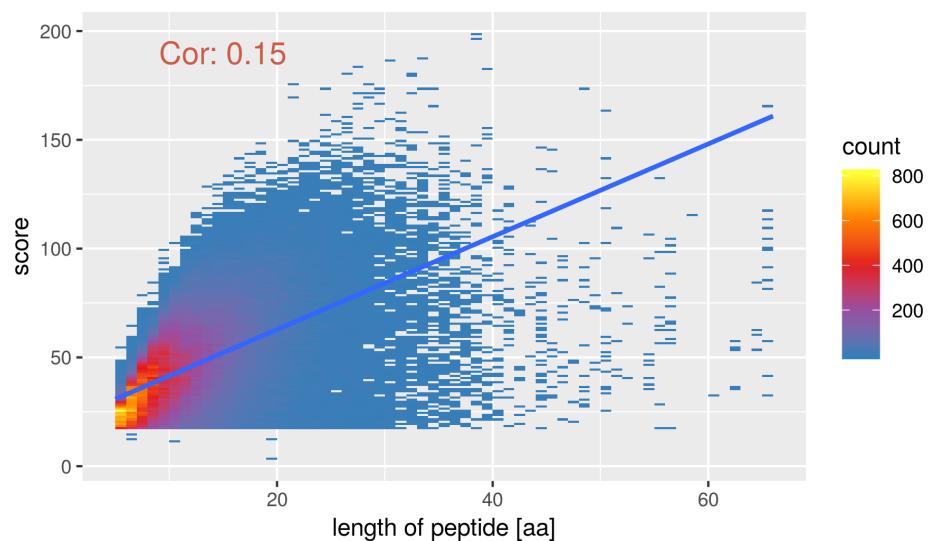


Statistical Analysis of Proteomics data

One determining factor to the mascot score is the peptide length. Longer peptides tend to have a better identification quality since they result in more ion fragments.

```
scp_mascot <- ggplot(data = subset(peptide_data,
                                         in_quantification_of_protein == 1),
                       aes(nchar(sequence), score)) +
  stat_bin2d(binwidth = 1) +
  geom_smooth(method = "lm") +
  scale_fill_gradient(colours =
    c("#377eb8", "#984ea3",
      "#e41a1c", "#ff7f00", "#ffff33")) +
  xlab("length of peptide [aa]")

scp_mascot +
  annotate("text", label = paste0("Cor: ", round(cor(layer_data(scp_mascot)$x,
                                                       layer_data(scp_mascot)$y,
                                                       method = "spearman"), 2)),
          x = 15, y = 190, size = 5, colour = "coral3")
```

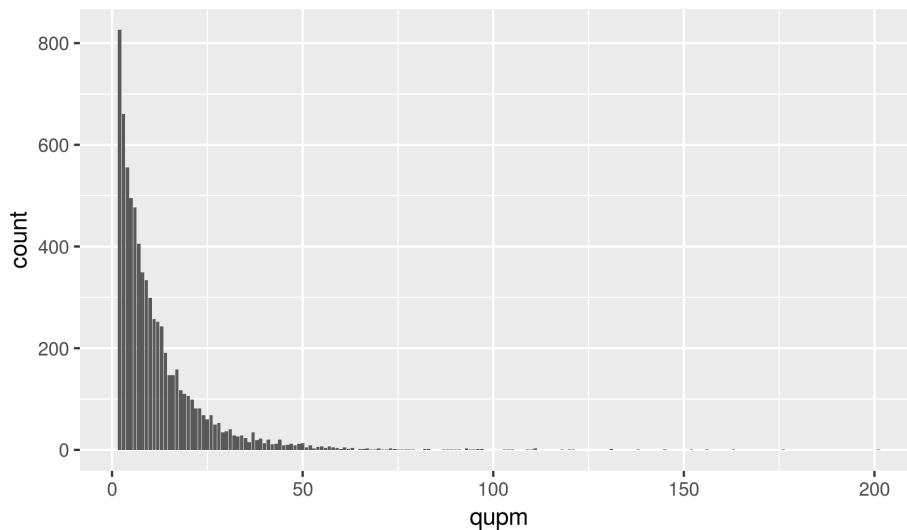


6.7.2 Number of unique peptides per protein

There is a different number of unique peptides identified for each protein.

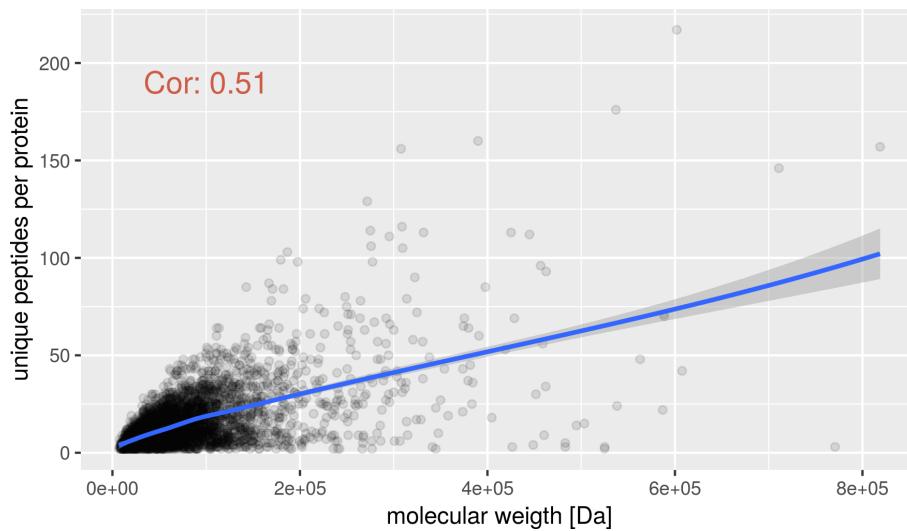
```
ggplot(data = subset(protein_data, qupm >= 2), aes(qupm)) +
  geom_bar()
```

Statistical Analysis of Proteomics data



This depends on two things: The length of the protein and its molecular weight:

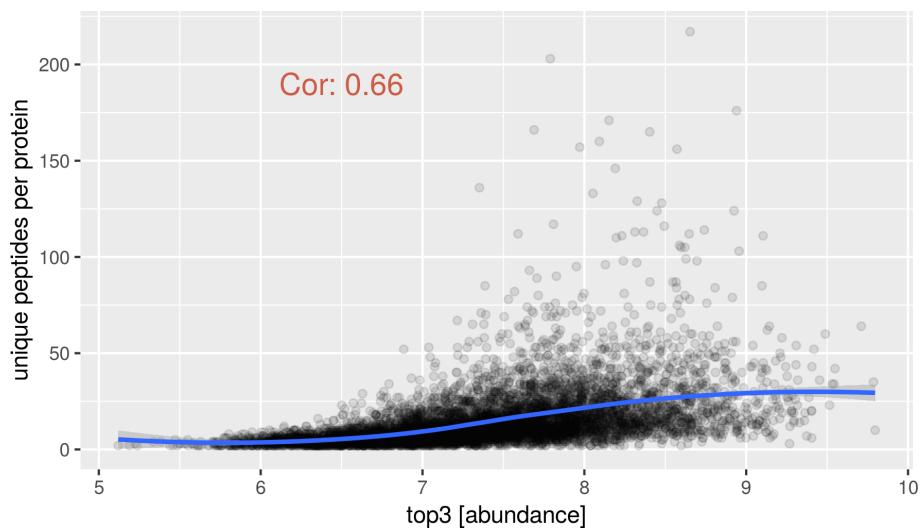
```
scp_mw <- ggplot(data = subset(protein_data, qupm >= 2),
  aes(as.numeric(as.character(mw)), upm)) +
  geom_point(alpha = I(0.1)) +
  geom_smooth(method = "loess") +
  scale_fill_gradientn(colours = c("#377eb8", "#984ea3",
  "#e41a1c", "#ff7f00", "#ffff33")) +
  xlab("molecular weight [Da]") +
  ylab("unique peptides per protein")
scp_mw +
  annotate("text", label = paste0("Cor: ", round(cor(layer_data(scp_mw)$x,
  layer_data(scp_mw)$y,
  use = "pairwise.complete.obs",
  method = "spearman"), 2))),
  x = 1e5, y = 190, size = 5, colour = "coral3")
```



Statistical Analysis of Proteomics data

As well as the abundance of the protein in the sample.

```
scp_top3 <- ggplot(data = subset(protein_data,qupm >= 2),aes(top3,upm)) +  
  geom_point(alpha = I(0.1) ) +  
  geom_smooth(method = "loess") +  
  scale_fill_gradientn(colours = c("#377eb8","#984ea3","#e41a1c",  
 "#ff7f00","#ffff33")) +  
  xlab("top3 [abundance]") +  
  ylab("unique peptides per protein")  
scp_top3 +  
  annotate("text", label = paste0("Cor: ",  
                                round(cor(layer_data(scp_top3)$x,  
                                         layer_data(scp_top3)$y,  
                                         use = "pairwise.complete.obs",  
                                         method = "spearman"), 2)),  
          x = 6.5, y = 190, size = 5, colour = "coral3")
```



7 Statistical analysis

7.1 Filter protein data

Identified proteins which are known to be a contaminant as well as proteins for which the TMT quantification is based on less than two unique peptides (qupm) are removed.

```
protein_data <- protein_data %>%  
  filter(!grepl("###",gene_name), qupm >= 2)
```

Statistical Analysis of Proteomics data

7.2 Extract intensity data as matrix

We gather the protein intensity data in a data matrix. The columns interesting to us start with `signal_sum` and then the respective TMT label. We discard the label `131L` as this does not correspond to a sample in our data.

We remove the `signal_sum` part from the sample labels in order to match the `tmt.label` column in the experimental Design table.

```
prot_matrix <- dplyr::select(protein_data,
                               signal_sum_126:signal_sum_130H) %>%
  as.matrix()

colnames(prot_matrix) <- str_remove(colnames(prot_matrix), "signal_sum_")
rownames(prot_matrix) <- protein_data$protein_id

stopifnot(colnames(prot_matrix) == expDesign$tmt.label[-length(expDesign$tmt.label)])

to_exclude <- apply(prot_matrix, 1, function(x){any(!is.finite(x))})
table(to_exclude)
  to_exclude
  FALSE
  7212

prot_matrix <- prot_matrix[!to_exclude, ]

head(prot_matrix)
      126     127L     127H     128L     128H
P23919 3.51e+08 3.57e+08 3.47e+08 3.08e+08 3.88e+08
P40425 1.06e+07 8.46e+06 8.68e+06 9.06e+06 8.30e+06
P40429 7.40e+08 7.31e+08 7.28e+08 6.80e+08 6.48e+08
F5GZF0|014519|014519-2 2.35e+07 1.97e+07 2.31e+07 2.09e+07 2.10e+07
A0A087WT59|A0A087WV45|P02766 7.33e+07 8.89e+07 3.76e+07 4.01e+07 8.90e+07
P35251|P35251-2 3.63e+08 3.87e+08 3.96e+08 3.48e+08 3.50e+08
      129L     129H     130L     130H
P23919 2.76e+08 3.34e+08 3.99e+08 3.07e+08
P40425 7.91e+06 9.50e+06 9.03e+06 9.22e+06
P40429 6.36e+08 7.65e+08 7.40e+08 6.51e+08
F5GZF0|014519|014519-2 1.82e+07 2.15e+07 2.13e+07 2.17e+07
A0A087WT59|A0A087WV45|P02766 2.34e+07 4.37e+07 8.52e+07 3.17e+07
P35251|P35251-2 3.43e+08 3.76e+08 3.71e+08 3.50e+08
```

7.3 Prepare a feature annotation

We now create another matrix holding the protein annotation.

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```
feature_anno <- as.matrix(dplyr::select(protein_data, protein_id, gene_name,
                                         top3, qupm, description))

rownames(feature_anno) <- protein_data$protein_id

feature_anno <- as.data.frame(feature_anno)[!to_exclude, ]
```

7.4 Create an expressionSet

We now join the replicates and add annotation data. We then turn the data into an **expressionSet**.

7.4.1 About Bioconductor ExpressionSets

Genomic and proteomic data can be very complex, usually consisting of a number of different bits and pieces, e.g. information on the experimental samples, annotation of genomic features measured as well as the experimental data itself. In Bioconductor the approach is taken that these pieces should be stored in a single structure to easily manage the data.

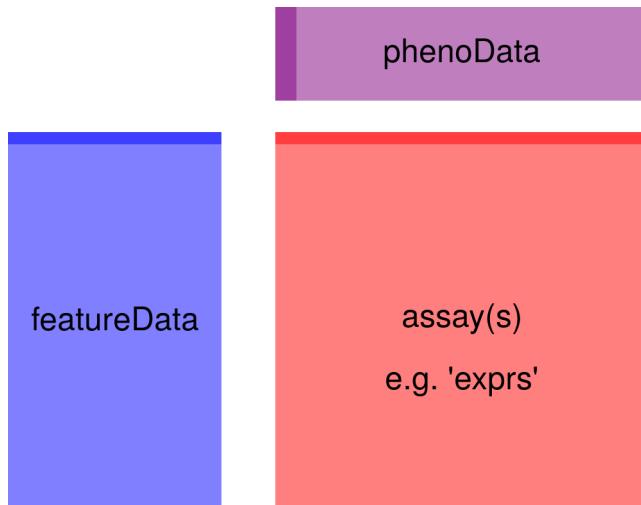
The package *Biobase* contains standardized data structures to represent genomic data. The **ExpressionSet** class is designed to combine several different sources of information into a single convenient structure. An **ExpressionSet** can be manipulated (e.g., subsetted, copied), and is the input to or output of many Bioconductor functions.

The data in an **ExpressionSet** consist of

- **assayData**: Expression data.
- **metaData**: A description of the samples in the experiment (**phenoData**), metadata about the features/proteins (**featureData**), and further annotations for the proteins, for example gene annotations from biomedical databases (**annotation**).
- **experimentData**: A flexible structure to describe the experiment.

The **ExpressionSet** class coordinates all of these data, so that one does not have to worry about the details. However, some constraints have to be met. In particular, the rownames of the **phenoData** have to match the column names of the assay data (as they represent the sample identifiers), while the row names of the expression data have to match the row names of the **featureData** (as they represent the feature identifiers). This is illustrated in the figure.

Statistical Analysis of Proteomics data



7.4.2 Creating the ExpressionSet

You can use the functions `pData` and `fData` to extract the sample and feature annotation respectively from an `ExpressionSet`. The function `exprs` will return the expression data itself as a matrix.

We can now combine the data into an `ExpressionSet` object.

```
eset_raw <- ExpressionSet(prot_matrix,
                           phenoData = AnnotatedDataFrame(expDesign[-nrow(expDesign),]),
                           featureData = AnnotatedDataFrame(feature_anno))

validObject(eset_raw)
[1] TRUE
pData(eset_raw)
  tmt.label rep condition
126       126 rep1      wt
127L     127L rep1 single_ko
127H     127H rep1 double_ko
128L     128L rep2      wt
128H     128H rep2 single_ko
129L     129L rep2 double_ko
129H     129H rep3      wt
130L     130L rep3 single_ko
130H     130H rep3 double_ko

# prots with very low expression / zero expression
strange_prots <- apply(exprs(eset_raw), 1, function(x){min(x) < 1})
eset_raw <- eset_raw[!strange_prots, ]
save(eset_raw, file = "eset_raw.RData")
```

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7.5 Quality control of the raw data

7.6 Array quality metrics report of the raw data

The package `arrayQualityMetrics` produces an html report, containing lots of quality control plots together with a description of their aims. We check our raw data using this reporting tool.

```
try(arrayQualityMetrics(expressionset = eset_raw,
                        outdir = "Report_for_eset_raw",
                        force = TRUE,
                        do.logtransform = TRUE,
                        intgroup = c("condition", "rep")
))
```

We can see a clear clustering by replicate, rep3 of WT seems to be an outlier on the PCA plot.

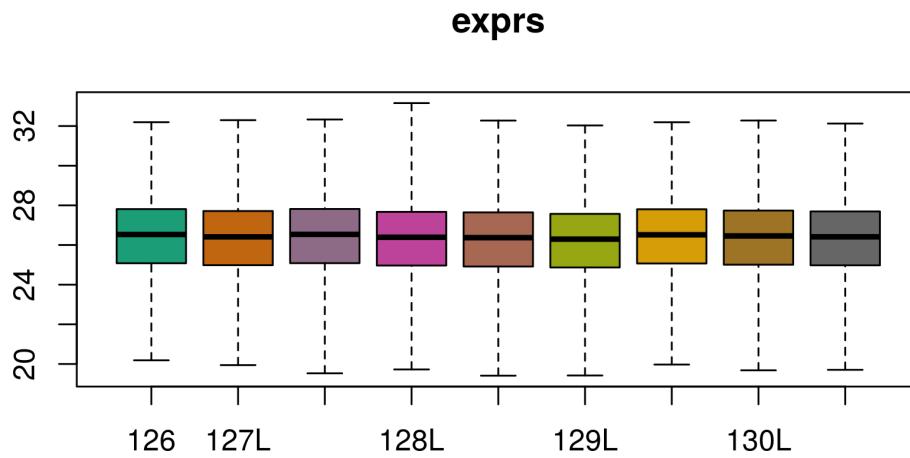
7.7 vsn normalization and feature annotation

vsn (variance stabilization transformation, `vsn`) is a Microarray normalization algorithm that performs background correction and normalization by robustly shifting and scaling intensity values within a sample before glog-transforming them. This is less “severe” than quantile normalization. vsn does perform a robust within-sample centering and scaling.

It is useful in general for intensity based data, e.g. also proteomics, see [Hughes et. al., 2014](#) for an example usage in proteomics .

We first create boxplots for the raw data.

```
oligo:::boxplot(eset_raw, transfo = log2, range = 0)
```



We can see that there only very minor differences between the different samples in the tags in the raw data are quite minimal in our example data.

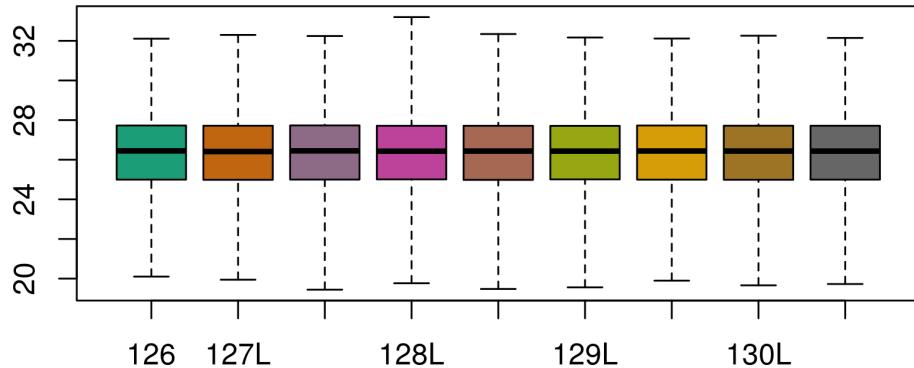
Nonetheless, we use vsn to normalize the data and create another set of boxplots.

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```
vsn_fit <- vsn2(eset_raw)
vsn2: 7211 x 9 matrix (1 stratum).
Please use 'meanSdPlot' to verify the fit.
eset_vsn <- predict(vsn_fit, newdata = eset_raw)

oligo:::boxplot(eset_vsn, transfo = identity)
```

exprs



```
save(eset_vsn, file = "eset_vsn.RData")
```

As expected both boxplots are quite similar to each other.

7.7.1 check array quality metrics again

We now check the normalized data again.

```
try(arrayQualityMetrics(expressionset = eset_vsn,
  outdir = "Report_for_eset_after_vsn",
  force = TRUE,
  do.logtransform = FALSE,
  intgroup = c("condition", "rep")
))
```

7.8 PCA plots of the normalized data

7.8.1 PCA using the most variable proteins

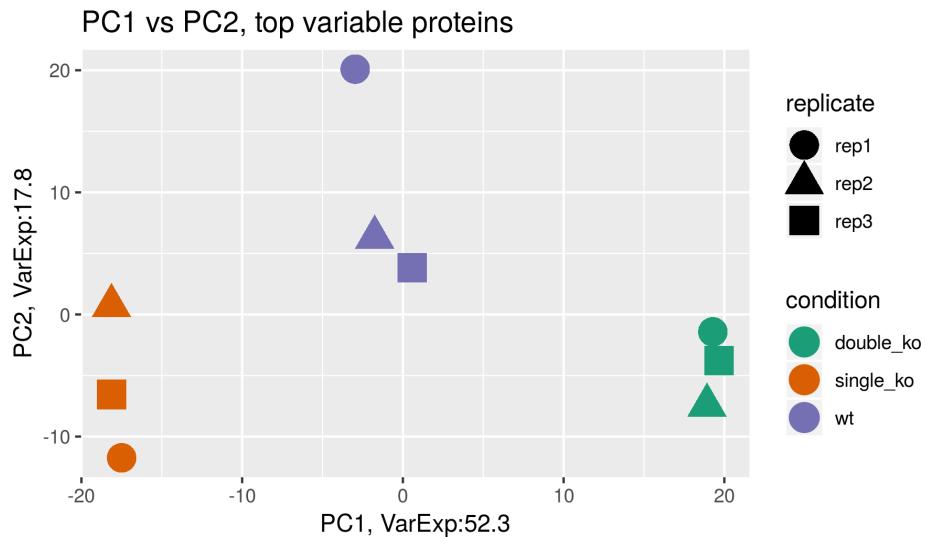
We now look at a PCA plot. First, we perform a simple variable selection and use only the top variable proteins for the computation of the principal components.

```
ntop <- 500

Pvars <- rowVars(exprs(eset_vsn))
select <- order(Pvars, decreasing = TRUE)[seq_len(min(ntop,
```

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```
length(Pvars)))]  
PCA <- prcomp(t(exprs(eset_vsn)[select, ]), scale = TRUE)  
percentVar <- round(100*PCA$sdev^2/sum(PCA$sdev^2),1)  
  
dataGG = data.frame(PC1 = PCA$x[,1], PC2 = PCA$x[,2],  
                     PC3 = PCA$x[,3], PC4 = PCA$x[,4],  
                     replicate = pData(eset_vsn)$rep,  
                     condition = pData(eset_vsn)$condition)  
  
(qplot(PC1, PC2, data = dataGG, color = condition,  
       main = "PC1 vs PC2, top variable proteins", size = I(6),  
       shape = replicate)  
+ labs(x = paste0("PC1, VarExp:", round(percentVar[1],4)),  
      y = paste0("PC2, VarExp:", round(percentVar[2],4)))  
+ scale_colour_brewer(type = "qual", palette = 2)  
)
```



The PCA plot shows a very separation between the experimental conditions.

7.9 Limma analysis

We now perform a differential analysis using *limma*. We first create a design matrix that then allows us to compare between the different conditions. Here, the intercept represent the WT baseline, and the other coefficients represent the fold changes. See the limma user guide, chapter 9 for further details on typical designs.

<http://bioconductor.org/packages/release/bioc/vignettes/limma/inst/doc/usersguide.pdf>

```
condition <- as_factor(pData(eset_vsn)$condition )  
des <- model.matrix(~ condition)  
colnames(des) <- str_remove(colnames(des), "condition")  
des
```

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```
(Intercept) single_ko double_ko
1          1         0         0
2          1         1         0
3          1         0         1
4          1         0         0
5          1         1         0
6          1         0         1
7          1         0         0
8          1         1         0
9          1         0         1
attr(),"assign")
[1] 0 1 1
attr(),"contrasts")
attr(),"contrasts")$condition
[1] "contr.treatment"
```

7.9.1 Comparison of WT vs single KO

As we have a coefficient, "single_ko" that encodes the fold change between WT the single knockout.

The result we get is a big table, with all significant proteins and a short description of what they are doing.

```
lm_fit <- eBayes(lmFit(eset_vsn, design = des))

limma_table <- topTable(lm_fit, sort.by = "t", coef = "single_ko",
                        number = Inf)

as.tibble(limma_table)
# A tibble: 7,211 x 11
  protein_id gene_name top3  uppm description logFC AveExpr      t  P.Value
* <fct>      <fct>   <fct> <fct> <dbl>    <dbl> <dbl> <dbl>
  1 095470     SGPL1    6.71  " 2" Sphingosin~ -2.25    23.9 -45.9 6.59e-12
  2 Q9HBL8     NMRAL1    7.01  " 7" NmrA-like ~ -1.48    25.7 -31.2 2.04e-10
  3 P47712     PLA2G4A   7.25  " 5" Cytosolic ~ -2.00    25.5 -28.3 4.82e-10
  4 P10620     MGST1     6.98  " 2" Microsomal~ -1.53    25.1 -24.3 1.85e- 9
  5 C9JYQ9|H0~  RPL22L1  7.88  " 4" 60S riboso~ -2.34    26.1 -23.0 2.94e- 9
  6 Q9NZU0     FLRT3     6.67  " 9" Leucine-ri~ -0.627   25.4 -21.4 5.72e- 9
  7 F2Z2X0|00~  NME4     7.18  " 5" Nucleoside~ -0.764   25.2 -20.8 7.13e- 9
  8 P55809     OXCT1     7.79  " 12" Succinyl-C~ -0.874   27.6 -20.4 8.47e- 9
  9 P00918     CA2       8.10  " 11" Carbonic a~ -2.04    27.5 -18.9 1.69e- 8
 10 Q9ULP9|Q9~  TBC1D24  6.83  " 10" TBC1 domai~ -0.671   26.0 -18.0 2.57e- 8
# ... with 7,201 more rows, and 2 more variables: adj.P.Val <dbl>, B <dbl>

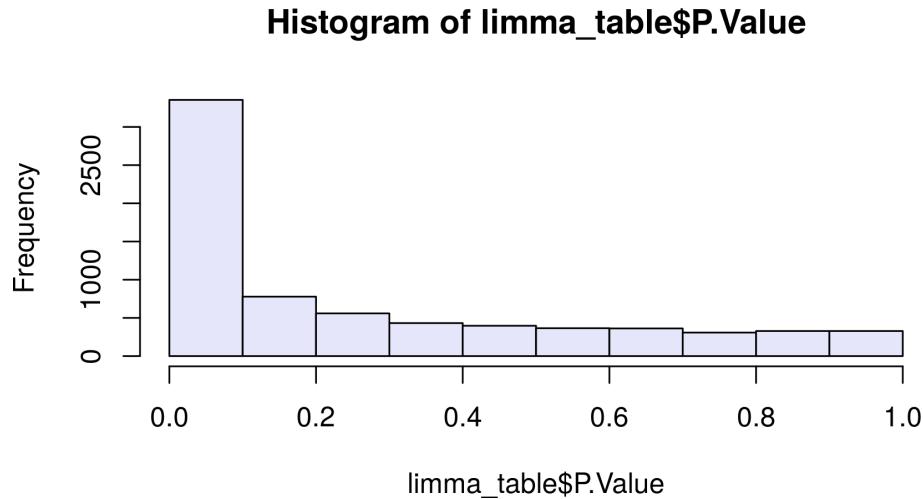
table(limma_table$adj.P.Val < 0.0001)

FALSE  TRUE
7174    37
```

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Here, we use a very stringent FDR cutoff of 0.0001 (represented by the “adjusted” p-value). The FDR is proportion of false positives in our hit list, this means we have $0.0001 * 37 = 0.004$, so almost zero false positives in this list.

```
hist(limma_table$P.Value, col = "lavender")
```



Another very important diagnostic is the p-value histogram: if everything worked well, we should have a uniform background of p-values (non-differentially abundant proteins) and a peak near zero representing the differentially abundant proteins.

Unusual p-value histogram can point to batch effects and variance estimation issues.

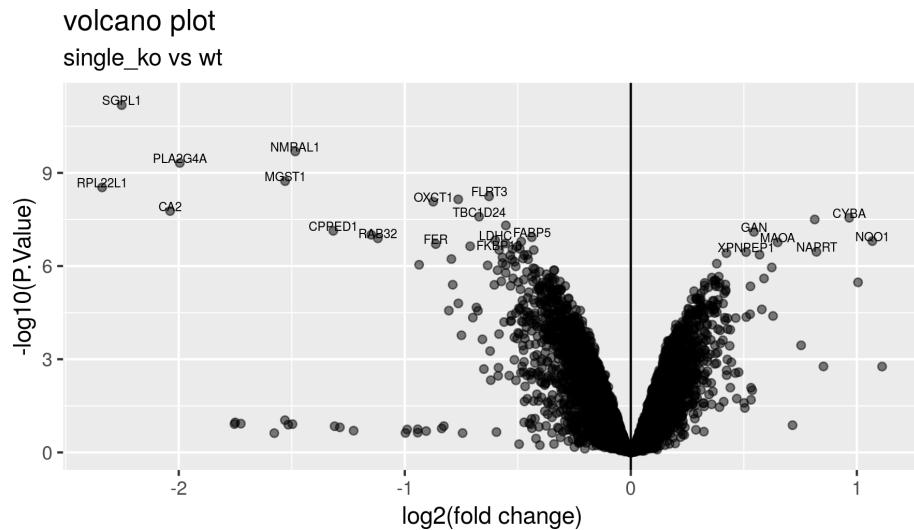
7.9.2 Volcano plot

We now visualize the results of the differential expression analysis in a Volcano plot, where we plot the log₂ fold change vs the -log₁₀ p-value. This allows us to assess statistical significance and effect size simultaneously.

The p-values should relate to the fold changes, but not directly correlated, as the p-values are (apart from the fold change) also based on the protein variance and sample size.

```
ggplot(data = limma_table,aes(logFC,-log10(P.Value))) +  
  geom_point(alpha = I(0.5)) +  
  geom_vline(xintercept = 0) +  
  xlab("log2(fold change)") +  
  geom_text(data = subset(limma_table, adj.P.Val <= 0.0001),  
            aes(label = gene_name),  
            size = 2,nudge_y = 0.15,check_overlap = TRUE) +  
  ggtitle("volcano plot", subtitle = "single_ko vs wt")
```

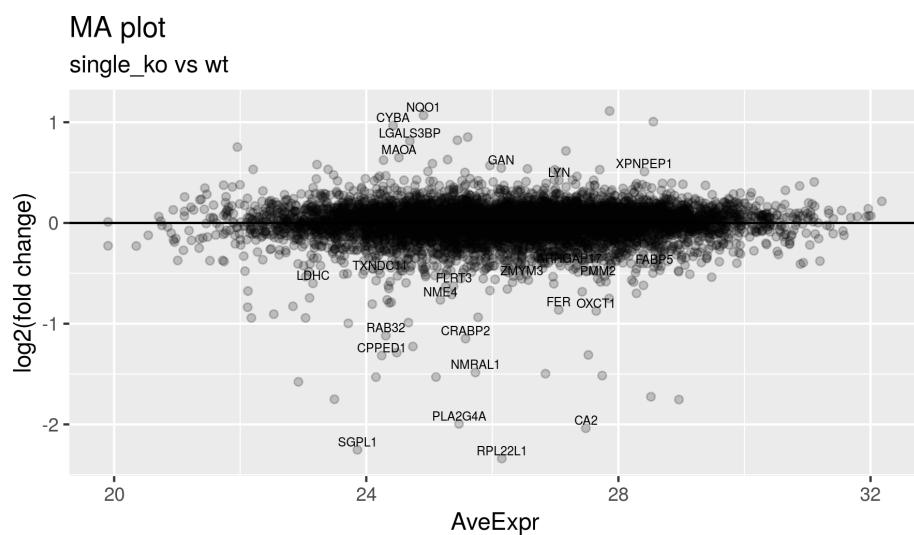
Statistical Analysis of Proteomics data



7.9.3 MA-plot

We can also visualize the results in an MA plot. It plots the average protein abundance (log₂ scale) vs. the log₂ fold change. This allows us to see whether our differences between the conditions depend on the protein abundance.

```
ggplot(data = limma_table,aes(AveExpr, logFC)) +
  geom_point(alpha = I(0.2)) +
  geom_hline(yintercept = 0) +
  ylab("log2(fold change)") +
  geom_text(data = subset(limma_table,adj.P.Val <= 0.0001),
            aes(label = gene_name),
            size = 2, nudge_y = 0.08,check_overlap = TRUE) +
  ggtitle("MA plot",subtitle = "single_ko vs wt")
```



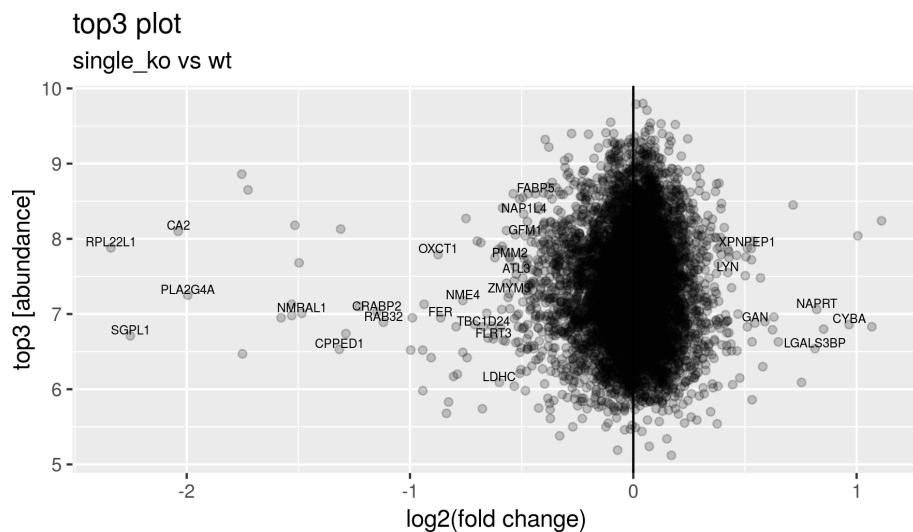
From the plot, we can see that our differentially abundant proteins are also abundant, and that there are no systematic biases between the experimental conditions.

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7.9.4 Top3 vs logFC

Here, we plot the top3 value as reported by IsobarQuant against the fold change. The top3 value is a measure of abundance computed from the top3 MS1 peptide-peaks for a protein (mean of \log_{10} intensities; the top3 peptides can be found in the peptides file). Again, we see that our hits are not in the low abundance range.

```
ggplot(data = limma_table,
        aes(logFC, as.numeric(as.character(top3))) +
        geom_point(alpha = I(0.2)) +
        geom_vline(xintercept = 0) +
        xlab("log2(fold change)") +
        ylab("top3 [abundance]") +
        geom_text(data = subset(limma_table, adj.P.Val <= 0.0001),
                  aes(label = gene_name),
                  size = 2, nudge_y = 0.08, check_overlap = TRUE) +
        ggtitle("top3 plot", subtitle = "single_ko vs wt")
```



Note that both this and the previous plot would not be possible if we were working with ratios.

7.10 Testing relative to a fold-change threshold

Very often, you want to test relative to a specific fold-change threshold, e.g. you want to identify proteins which have a \log_2 fold-change of greater than 2.

This is often implemented via a “post-hoc” strategy: one thresholds the FDR and the fold change after testing using the null hypothesis that the fold change is zero.

7.10.1 The naive post-hoc strategy is biased

This naive strategy might lead to a loss of FDR control. We illustrate this in the following: We first simulate data with 10000 proteins, 1000 of which are differentially abundant with a FC that scatters around 2, and 20 samples, with 10 in each group.

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We now perform a t-test for each protein.

```
n <- 20
p <- 10000

true_fcs <- numeric(10000)
idx_ab <- sample(x = p, 1000)
true_fcs[idx_ab] <- rnorm(length(idx_ab), mean = 2, sd = 0.5)

x <- matrix(rnorm(n*p), nrow = p, ncol = n)
fac <- factor(c(rep(0, 10), rep(1, 10)))
x[idx_ab, fac == 1] <- x[idx_ab, fac == 1] + true_fcs[idx_ab]
rt <- rowttests(x, fac)
```

We now compute the proportion of false positives among all positives, the false discovery proportion (FDP) which the Benjamini-Hochberg method controls at a pre-specified level. Indeed, this is controlled for our t-test:

```
FDR <- p.adjust(rt$p.value, method = "BH")

P <- which(FDR < 0.1)
TP <- intersect(idx_ab, P)
FP <- setdiff(P, idx_ab)

FDP <- length(FP) / length(P)

FDP
[1] 0.0928
```

The actual level is 0.093 less than the 10% we set. If we now do a post-hoc thresholding, we can again compute the FDP:

7.11 Thresholding approach

```
fcs <- rt$dm

thresh_hits <- which(abs(fcs) > 2 & FDR < 0.1)

P_thresh <- thresh_hits

true_fcs_2 <- intersect(idx_ab, which(abs(true_fcs) > 2))

FP_thresh <- setdiff(P_thresh, true_fcs_2)

FDP_thresh <- length(FP_thresh) / length(P_thresh)

FDP_thresh
[1] 0.212
```

Of 481 proteins we identify this way, 0.212 are actually false positives, much higher than the target value of 10%.

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Therefore, post-hoc thresholding does not work.

7.11.1 Using limma treat

limma implements a strategy to specifically test relative to a fold change threshold, for details see the paper by McCarthy and Smyth:

Testing significance relative to a fold-change threshold is a TREAT

Running it, we get an FDP lower than the threshold:

```
treat_res <- topTreat(treat(lmFit(x, design = model.matrix(~ fac)), lfc = 2),
                      coef = 2, number = Inf, sort.by = "none")

P_treat <- which(treat_res$adj.P.Val < 0.1)

FP_treat <- setdiff(P_treat, true_fcs_2)

FDP_treat <- length(FP_treat) / length(P_treat)

FDP_treat
[1] 0
```

However, here we only identify a handful of proteins, therefore, we might want to lower the threshold in practice.

8 Session Info

```
sessionInfo()
R version 3.5.1 (2018-07-02)
Platform: x86_64-pc-linux-gnu (64-bit)
Running under: Ubuntu 16.04.5 LTS

Matrix products: default
BLAS: /usr/lib/openblas-base/libblas.so.3
LAPACK: /usr/lib/libopenblas-r0.2.18.so

locale:
[1] LC_CTYPE=en_US.UTF-8      LC_NUMERIC=C
[3] LC_TIME=de_DE.UTF-8       LC_COLLATE=en_US.UTF-8
[5] LC_MONETARY=de_DE.UTF-8    LC_MESSAGES=en_US.UTF-8
[7] LC_PAPER=de_DE.UTF-8      LC_NAME=C
[9] LC_ADDRESS=C              LC_TELEPHONE=C
[11] LC_MEASUREMENT=de_DE.UTF-8 LC_IDENTIFICATION=C

attached base packages:
[1] stats4     parallel   stats      graphics   grDevices  utils      datasets 
[8] methods    base
```

Statistical Analysis of Proteomics data

```
other attached packages:
[1] bindrcpp_0.2.2          Peptides_2.4
[3] gridExtra_2.3           Hmisc_4.1-1
[5] Formula_1.2-3          survival_2.42-6
[7]forcats_0.3.0            readr_1.1.1
[9] tibble_1.4.2             tidyverse_1.2.1
[11] purrr_0.2.5             fdrtool_1.2.15
[13] pheatmap_1.0.10          MSnbase_2.6.2
[15] ProtGenerics_1.12.0       BiocParallel_1.14.2
[17] mzR_2.14.0                Rcpp_0.12.18
[19] vsn_3.48.1               tidyR_0.8.1
[21] smoothmest_0.1-2          MASS_7.3-50
[23] openxlsx_4.1.0             limma_3.36.2
[25] genefilter_1.62.0          matrixStats_0.54.0
[27] stringr_1.3.1             arrayQualityMetrics_3.36.0
[29] RColorBrewer_1.1-2         gplots_3.0.1
[31] dplyr_0.7.6                plyr_1.8.4
[33] reshape2_1.4.3              ggplot2_3.0.0
[35] geneplotter_1.58.0          annotate_1.58.0
[37] XML_3.98-1.16              AnnotationDbi_1.42.1
[39] IRanges_2.14.10             S4Vectors_0.18.3
[41] lattice_0.20-35             Biobase_2.40.0
[43] BiocGenerics_0.26.0          knitr_1.20
[45] BiocStyle_2.8.2

loaded via a namespace (and not attached):
[1] readxl_1.1.0                backports_1.1.2
[3] lazyeval_0.2.1               oligo_1.44.0
[5] splines_3.5.1                GenomeInfoDb_1.16.0
[7] digest_0.6.15                 foreach_1.4.4
[9] BiocInstaller_1.30.0          htmltools_0.3.6
[11] fansi_0.3.0                  gdata_2.18.0
[13] magrittr_1.5                  checkmate_1.8.5
[15] memoise_1.1.0                 affyPLM_1.56.0
[17] cluster_2.0.7-1              doParallel_1.0.11
[19] gcrma_2.52.0                  Biostrings_2.48.0
[21] modelr_0.1.2                  beadarray_2.30.0
[23] colorspace_1.3-2              rvest_0.3.2
[25] blob_1.1.1                   haven_1.1.2
[27] xfun_0.3                     crayon_1.3.4
[29] RCurl_1.95-4.11              jsonlite_1.5
[31] bindr_0.1.1                   impute_1.54.0
[33] iterators_1.0.10              glue_1.3.0
[35] gtable_0.2.0                  zlibbioc_1.26.0
[37] XVector_0.20.0                 DelayedArray_0.6.5
[39] BeadDataPackR_1.32.0          scales_1.0.0
[41] setRNG_2013.9-1              DBI_1.0.0
[43] xtable_1.8-2                  htmlTable_1.12
[45] foreign_0.8-71                bit_1.1-14
[47] preprocessCore_1.42.0          httr_1.3.1
[49] htmlwidgets_1.2                acepack_1.4.1
```

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```
[51] ff_2.2-14                  pkgconfig_2.0.2
[53] nnet_7.3-12                utf8_1.1.4
[55] labeling_0.3               tidyselect_0.2.4
[57] rlang_0.2.2                cellranger_1.1.0
[59] munsell_0.5.0              tools_3.5.1
[61] cli_1.0.0                  RSQLite_2.1.1
[63] broom_0.5.0                evaluate_0.11
[65] mzID_1.18.0                yaml_2.2.0
[67] bit64_0.9-7               oligoClasses_1.42.0
[69] zip_1.0.0                  caTools_1.17.1.1
[71] nlme_3.1-137              xml2_1.2.0
[73] compiler_3.5.1             rstudioapi_0.7
[75] affyio_1.50.0              stringi_1.2.4
[77] Matrix_1.2-14              pillar_1.3.0
[79] MALDIquant_1.18            data.table_1.11.4
[81] bitops_1.0-6               GenomicRanges_1.32.6
[83] R6_2.2.2                   latticeExtra_0.6-28
[85] pcaMethods_1.72.0           affy_1.58.0
[87] hwriter_1.3.2               bookdown_0.7
[89] affxparser_1.52.0            KernSmooth_2.23-15
[91] gridSVG_1.6-0               codetools_0.2-15
[93] gtools_3.8.1                assertthat_0.2.0
[95] SummarizedExperiment_1.10.1 openssl_1.0.2
[97] rprojroot_1.3-2              withr_2.1.2
[99] GenomeInfoDbData_1.1.0      hms_0.4.2
[101] grid_3.5.1                 rpart_4.1-13
[103] base64_2.0                  rmarkdown_1.10
[105] illuminaio_0.22.0            Cairo_1.5-9
[107] lubridate_1.7.4              base64enc_0.1-3
```