

Computer Graphics Coursework 1 Report

COMP3811

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1 Implementation

1.1 Drawing Pixels

Within the window the coordinates count from the top left of the window to the bottom right. This means that the pixel (0, 0) is in the top left corner, (w-1, 0) is in the top right corner and (0, h-1) is in the bottom left corner.



Figure 1: Particle field from the project implementation

1.2 Drawing Lines

The line implementation works by starting with two points. The start and end of the line. The program will then take these values and calculate 2 numbers d_x and d_y . Then, the program will find which axis the line moves the most along (Known as the X or Y major). This is done through seeing which value between d_x and d_y is the greatest. Should d_x be greater we step along the X axis. The same is true should d_y be greater. The program then keeps track of this by saving a 'step' variable as the corresponding major.

The final step before moving onto deciding which pixels get drawn is to calculate the increase required each iteration in the x and y directions. This increase is found by dividing d_x and d_y by the step variable that was saved earlier.

In order to draw the line the program now iterates over as many 'steps' needed to draw the line from the start to the end. During each iteration the program will check that the pixel is within the bounds of the surface and should this check return true the pixel will be drawn. This is done to avoid out of bounds errors within the program. The last stage of the loop is to move to the next pixel in the line by adding the x and y increase to our current pixel location. (Kamble and Gawade 2021)

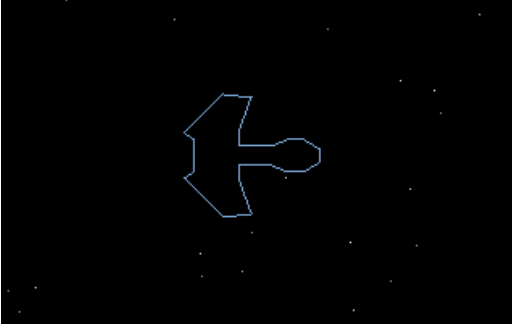


Figure 2: Ship drawn.



Figure 3: Ship rotated

1.3 Drawing Triangles

This algorithm begins by finding the possible bounds of the triangle by iterating through the points given to find the maximum and minimum coordinates. Once the bounds of the triangle are discovered the program will iterate through every pixel within the bounds. Every loop the program will check if the current pixel (X) is within the triangle by performing 3 half-plane tests. These tests are performed using the following algorithm $F(X) = n \cdot (X - P)$. Should $F(X) > 0$ be true for any of the lines the program continues onto the next pixel. Should the pixel pass all the half-plane tests the program will then check the pixel is within the window and if it is the pixel gets drawn.

1.4 Barycentric Interpolation

The algorithm begins exactly the same as the previous triangle algorithm, by finding the bounds of the triangle to be drawn. The algorithm then loops through this rectangle and performs calculations to determine whether or not a pixel is within the triangle to be drawn. The changes from the previous algorithm begin with these checks. These checks involve finding α , β and γ values for a given point. These values are known as Barycentric Coordinates and can be found for any given point (U) on a triangle.

Given a triangle with points A , B and C the program need to find the vectors $u = B - A$ and $v = C - A$. Once these two vectors have been found the program then uses the following formula to find the area of the triangle ABC .

$$area(ABC) = \frac{(u_x \times v_y) - (u_y \times v_x)}{2}$$

The code can then call a function for this formula for each of the three sub triangles. Once each sub area has been calculated the program can then perform the following formulas to find the values of α , β and γ .

$$\alpha = \frac{area(BCU)}{area(ABC)}, \beta = \frac{area(AUC)}{area(ABC)}, \gamma = \frac{area(ABU)}{area(ABC)}$$

Finally, should each of these values be between 0 and 1 the algorithm will draw a pixel at the given point. This pixel shall be a colour interpolated from the three points on the triangle using the following formula for each RGB value.

$$colour = A_{colour} \times \alpha + B_{colour} \times \beta + C_{colour} \times \gamma$$

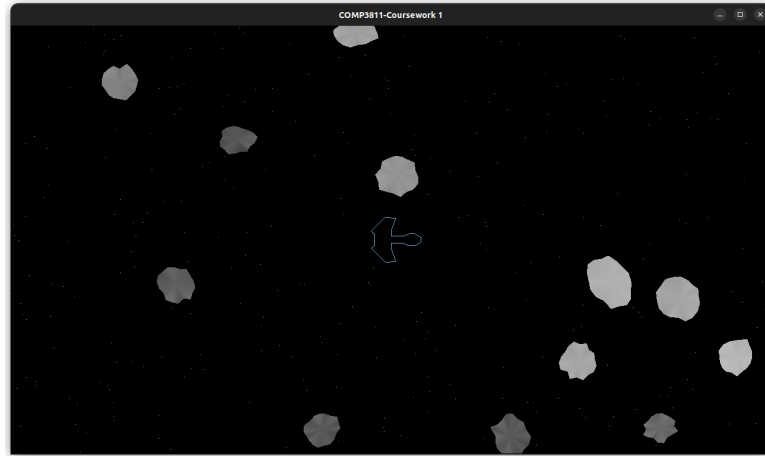


Figure 4: Asteroids drawn using Barycentric Interpolation

1.5 Blitting Images

Helper Algorithms

These helper algorithms differ slightly from the ones used in order to set pixels. This is due to the fact that they use RGBA representation as opposed to RGBx representations. This means that as well as returning the RGB values when getting a pixel the program must also return an A value. This A value is used to indicate the opacity of a pixel which is then later used to check whether a pixel should or should not be drawn on the surface from the image.

Main Blitting Algorithm

The blitting algorithm begins by starting a loop through the image to be rendered. Within this loop the program first finds the current position on the surface by adding the starting position to the x and y values being used to loop through the image. The algorithm then calls the helper algorithm to get a pixel from the image. The program then checks if the current pixel should be masked or not by checking if the A value is greater than 0. The program then makes sure that the current pixel is within the bounds of the surface and if it is the pixel gets drawn onto the surface.

One possible optimisation that could be made is improving the clipping of the image. For example, currently the program will check every pixel outside the bounds of the surface even if no more pixels could possibly be on the surface. This could be further optimised by stopping the current loop if the following pixels will always be outside the borders of the surface.

2 Testing

2.1 Testing: Lines

Test 1 - Drawing multiple directions off screen

This test was implemented as it is important that the program can handle lines being drawn off screen no matter the direction. Currently the tests only check for 1 direction off screen so I decided to expand on that to all directions. Furthermore, if the program cannot handle lines being drawn off screen the program will most likely crash which is unacceptable.

Test 2 - Two connected lines

This test was implemented in order to ensure there's no pixel gaps when two lines are drawn next to each other. This is a desirable effect as when drawing more complex shapes using lines we must ensure the program will not leave any gaps while drawing.

Test 3 - Two lines running parallel next to each other

This test was implemented to ensure no gaps are present when lines are parallel to each other. This is desirable for the same reason as the previous test. That reason being, when drawing more complex shapes with lines we want to ensure no gaps are present.

Test 4 - Two lines overlapping

This test was implemented to ensure that a second line drawn after another line in the same place would overwrite the previous line. This feature is important as some animations will require changes in pixels so it is important pixels drawn later can fully overwrite previous pixels.

Test 5 - Whole screen drawn onto

This test ensures that every pixel within a surface can be drawn onto. This is important as we want to make sure that every pixel can be used. This also ensures that any bug related to drawing to specific pixels can be identified and fixed.

Visualisations

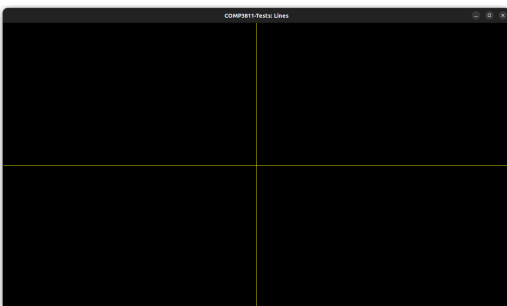


Figure 5: Demonstration of test 1 using lines sandbox.

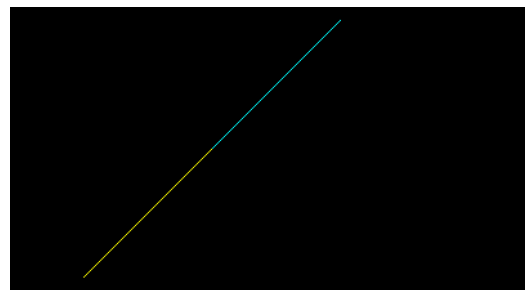


Figure 6: Demonstration of test 2 using lines sandbox

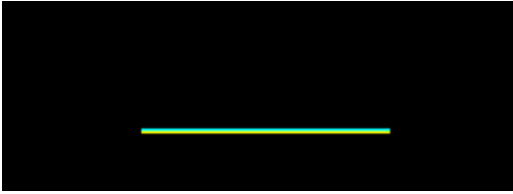


Figure 7: Demonstration of test 3 using lines sandbox



Figure 8: Demonstration of test 4 using lines sandbox

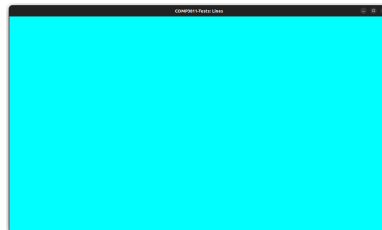


Figure 9: Demonstration of test 5 using lines sandbox

2.2 Testing: Triangles

Test 1 - Flat triangle

For this test we want to ensure that drawing a flat triangle just draws a line on the surface. This could be useful for certain animations that involve a triangle morphing in order to be flatter. This test ensures that the triangle does not disappear early during this animation.

Test 2 - Any point order

This test ensures that no matter what order the points are inputted the triangle is still drawn. This is useful as due to rotation there is no way to know what order the points of the triangle will arrive in. Therefore this test exists to ensure the drawing algorithm accounts for this.

Test 3 - Triangles drawn outside

This test ensures the program does not crash when an entire triangle is drawn outside the bounds of the screen. This is useful as for certain things (such as objects in a video game for example) a user may want to keep track of things even if they are not within the bounds of the screen. This program should be able to handle this.

3 Benchmarks

3.1 Computer Information

All tests were performed using an 11th generation intel core i31115G4. The CPU has 4 caches present: a data cache with 48KiB, an instruction cache with 32KiB, and two unified caches. One unified cache has 1280KiB, the other has 6144KiB. The computer the tests were performed on also has access to 8gb of RAM.

Table 1: Blitting Benchmark Results

Method name	surface size	Time(ns)	CPU(ns)	Iterations
alpha masking	320x240	3,831,941	3,815,423	176
alpha masking	7680x4320	5,756,367	5,729,355	125
no alpha masking	320x240	3,953,626	3,946,029	178
no alpha masking	7680x4320	7,282,696	7,257,732	94
std::memcpy	320x240	226,571	224,768	3,272
std::memcpy	7680x4320	232,251	230,998	3,122

3.2 Blitting

From this data I can see that the fastest algorithm in terms of time taken is clearly blitting through the use of `std::memcpy`. This is most likely due to the algorithm involving `std::memcpy` only containing one `for` loop. This algorithm achieves this through directly copying every row of the image onto the surface from a specified point. Another benefit of this algorithm that can be seen from the data is that it scales well with larger images. This effect is also due to the algorithm only having one `for` loop as opposed to two.

This data also seems to indicate that blitting with alpha masking is faster than blitting with no alpha masking. The most likely reason for this is due to my implementation of clipping. Clipping is performed by checking if a pixel is in bounds right before it is about to be drawn. When alpha masking is performed this (relatively expensive) check is skipped for every pixel that is to be masked. On the other hand, if alpha masking is not performed this check is done for every pixel in the bounds of the image. Should this clipping check be moved to a place in which it's performed no matter whether alpha masking is present or not I expect blitting with no alpha mask to be slightly faster as there is one less check to perform.

3.3 Line drawing

Bresenham's Algorithm

Bresenham's line drawing algorithm begins by calculating $dx = x_2 - x_1$ and $dy = y_2 - y_1$. Following this, the algorithm then finds what is known as the driving axis(DA) by comparing dy and dx . In the case that $|dx| \geq |dy|$ the x-axis is the driving axis. On the other hand, should $|dx| < |dy|$ be true the y-axis is the driving axis. This is where the main differences between Bresenham's algorithm and DDA begin. Bresenham's only uses the driver to increment the driving axis while iterating 1 by 1 over the other axis whereas the DDA algorithm uses a similar value to DA to calculate an increase to both axes. Bresenham's algorithm then keeps track of when to update the current position in the driving axis through the use of an error variable. This variable keeps track of the distance between the line and the current pixel. Should this error value be over 1 the current value on the driving axis is incremented and the error value is returned to where it should be. (Madan, Anand, and Bhushan 2014) Finally, the algorithm checks if the current point to be drawn is within the bounds of the window and if this test passes the pixel is drawn. This check is achieved in the same way in both DDA and Bresenham's algorithm.

Benchmark analysis

The three tests that were performed were chosen as they cover a wide range of use cases. Diagonal and horizontal tests cover the most common uses of line drawing so it is important to cover these within the benchmarks. The fullscreen test covers the most extreme case of drawing every pixel on the surface. This test is interesting as it shows the absolute worst case of each algorithm and highlights how the algorithms scale with size.

Table 2: Line Benchmark Results

Table 3: DDA Results				Table 4: Bresenham Results			
Test	surface size	Time(ns)	Iterations	Test	surface size	Time(ns)	Iterations
Diagonal	320x240	1,667	358,427	Diagonal	320x240	3,173	213,402
Diagonal	7680x4320	53,748	12,640	Diagonal	7680x4320	77,639	8,978
Horizontal	320x240	1,020	628,431	Horizontal	320x240	1,905	354,100
Horizontal	7680x4320	24,398	29,017	Horizontal	7680x4320	45,958	15,184
Fullscreen	320x240	451,847	1,277	Fullscreen	320x240	772,071	817
Fullscreen	7680x4320	170,828,342	4	Fullscreen	7680x4320	335,260,630	2

As can be seen from the data Bresenham's algorithm takes almost twice the amount of time as the DDA algorithm. This may be due to Bresenham's algorithm making more calculations and checks within the main loop of the algorithm whereas the DDA algorithm only increments the current x and y value.

You can also infer from the algorithm that both algorithms are particularly slow at drawing every line on the screen. This could indicate that both algorithms are slow at drawing larger objects (such as triangles) and therefore these algorithms are not ideal for drawing larger shapes. However, should you need a line drawing algorithm in order to draw a shape (such as drawing a triangle with horizontal lines) I would recommend the DDA algorithm.

In conclusion, it is clear that the DDA algorithm is much more effective in terms of time efficiency than Bresenham's algorithm. However, Bresenham's algorithm may still be useful in certain cases as it can be achieved through integer values whereas DDA requires floating point values.

4 My own spaceship

References

- Kamble, A. A. and S. S. Gawade (2021). "DDA Line Drawing Algorithm". In: *International Journal of Advanced Research in Computer and Communication Engineering* 10.12.
- Madan, L, K Anand, and B Bhushan (2014). "BRESENHAM'S LINES ALGORITHM". In: *International Journal of Research in Science And Technology* 4.3.