

**Bernard Riemann** 

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The *cobea* module [1] is a Python implementation of Closed-Orbit Bilinear-Exponential Analysis [2], an algorithm for studying closed-orbit response matrices of storage rings (particle accelerators).

If you publish material using this software, please cite one or more of the references [1-2].

For more information, visit https://bitbucket.org/b-riemann/cobea.

(References)

- [1] B. Riemann et al., "COBEA Optical Parameters From Response Matrices Without Knowledge of Magnet Strengths", in Proc. IPAC17, paper MOPIK066, 2017.
- [2] B. Riemann, ''[The Bilinear-Exponential Closed-Orbit Model and its Application to Storage Ring Beam Diagnostics](http://dx.doi.org/10.17877/DE290R-17221)', Ph.D. Dissertation, TU Dortmund University, 2016. DOI [10.17877/DE290R-17221](http://dx.doi.org/10.17877/DE290R-17221).

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# **QUICK START TUTORIAL**

This is a brief introduction on how to use the cobea module.

# 1.1 Reading in data

COBEAs input consists of

- A set of corrector names corresponding to rows of your matrix
- A set of monitor names corresponding to columns of your matrix
- The response matrix itself
- The ordering information, given as a list of monitor and corrector names, ordered along the beampath (downstream)

You need to convert your response data into a standardized input for COBEA. This is handled by the *Response* class:

```
class cobea.model.Response (matrix, corr_names, mon_names, line, include_dispersion=True, unit='')
```

Representation of COBEA input, used as such for the function cobea.cobea()

During creation of the this object, py:data:matrix rows and columns, as well as the corresponding py:data:corr\_names and py:data:mon\_names, are resorted to their respective order in py:data:line.

#### **Parameters**

- **matrix** (array) input response matrix of shape (correctors, monitors, directions). If only one direction is considered, the last dimension can be omitted.
- corr\_names (list) a list of corrector labels corresponding to each row of the matrix
- mon\_names (list) a list of monitor labels corresponding to each column of the matrix
- line (list) a list of element names in ascending s order
- unit (str) unit for the input values of the matrix (optional)

#### topology

*object* – A Topology object holding the re-ordered py:data:'corr\_names', py:data:'mon\_names', and py:data:'line' as attributes.

#### matrix

array – re-ordered input response matrix.

# 1.2 Running the algorithm

The COBEA algorithm is then applied using the function cobea.cobea() (click link, return back to 1.3 afterwards)

# 1.3 Obtaining and plotting results

```
The cobea function returns a Result object. This object contains all computed information.
class cobea.model.Result (response, additional={}, **kwargs)
     COBEA Result.
     Besides the attributes and methods contained in BEModel, the following information is included.
     matrix
           array - Original input response matrix
           object - computed BE model errors, represented as ErrorModel object
      additional
           dict – may contain the following keywords
           coretime [float] time used for computation in the start and optimization layer.
           err [dict] dictionary with additional model parameter error estimates.
           conv [dict] dictionary with L-BFGS convergence information (if convergence info was True)
           invariants [array] computed during normalization of monitor vectors if drift space is given. These
               are just returned for completeness and do not contain information about beam physics.
           pca_singvals [array] custom info from MCS algorithm
           pca_orbits [array] custom info from MCS algorithm
           version [str] version of the object
      cbeta_jmw
           Ripken-Mais beta parameters * constant. If self.R_jmw is normalized, constant = 1.
           Ripken-Mais phase advances per element
      flip_mu(m)
           switch the sign of mu_m for given m, simultaneously changing the conjugation of R_jmw and A_km
           so that the response matrix remains unchanged
     {\tt phase\_integral}\,(m)
           integrated phase from first to last BPM (not one turn!), used for tune () computation
     phi jmw
           Compute Ripken-Mais betatron phases
      response_matrix(dispersion=True)
           generate a 'simulated' response matrix from the present model parameters
               Returns Dev – response array of shape (K, J, M)
               Return type array
      save (filename)
           save the Result object as a pickle file with the given filename. The object can be reloaded using
```

cobea.load\_result() (which simply uses pickle)

compute tune including integer part for a given mode m

## update\_errors()

compute errors in attribute *error* for given BE-Model parameters and input response, including errors for Ripken-Mais parameters

The module <code>cobea.plotting</code> includes many helper functions to view these results. A summary of results is created by the <code>cobea.plotting.plot\_result()</code> function.

**CHAPTER** 

TWO

**API** 

This page contains automatic documentation of the complete cobea module.

# 2.1 cobea (main namespace)

Closed-Orbit Bilinear-Exponential Analysis (COBEA)

This is a Python implementation of the COBEA algorithm [1] to be used for studying betatron oscillations in particle accelerators by closed-orbit information.

[1] B. Riemann. 'The Bilinear-Exponential Model and its Application to Storage Ring Beam Diagnostics', PhD Dissertation (TU Dortmund University, 2016), DOI Link: (https://dx.doi.org/10.17877/DE290R-17221)

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cobea.cobea (response, drift\_space=nan, convergence\_info=False)

Main COBEA function with pre- and postprocessing.

#### **Parameters**

- response (object) A valid cobea. model. Response object representing the input.
- **drift\_space** (tuple) if not-NaN, a tuple with 3 elements (monitor name 1, monitor name 2, drift space length / m)
- **convergence\_info** (bool) if True, convergence information from L-BFGS is added to the result dictionary (before saving).

Returns result - A cobea.model.Result object.

Return type object

cobea.l\_bfgs\_iterate(alloc\_items=10000)

convert the iterate.dat file produced by L-BFGS-B

**Parameters alloc\_items** (*int*) – the number of maximum iterations for which memory is allocated.

#### **Returns**

iter –

a dictionary with the following fields. The field names and descriptions have been copied from a demo outpu

'it' [array] iteration number

'nf' [array] number of function evaluations

'nseg' [array] number of segments explored during the Cauchy search

'nact' [array] number of active bounds at the generalized Cauchy point

'sub' [str]

manner in which the subspace minimization terminated con = converged, bnd = a bound was reached

'itls' [int] number of iterations performed in the line search

'stepl' [float] step length used

'tstep' [float] norm of the displacement (total step)

'projg' [float] norm of the projected gradient

'f' [float] function value

#### Return type dict

## cobea.load\_result (savefile)

Load (un-pickle) a Result object (or any other object)

## cobea.optimization\_layer(rslt, iprint=-1)

Implementation of the Optimization layer. It uses L-BFGS [1] as special case of L-BFGS-B [2] in scipy.optimize

[1] D.C.~Liu and J.~Nocedal, "On the Limited Memory Method for Large Scale Optimization", Math. Prog. B extbf{45} (3), pp.~503–528, 1989. DOI 10.1007/BF01589116

[2] C.~Zhu, R.H.~Byrd and J.~Nocedal, "Algorithm 778: L-BFGS-B: Fortran subroutines for large-scale bound-constrained optimization", ACM Trans. Math. Software extbf{23} (4), pp.~550–560, 1997. DOI 10.1145/279232.279236

**Parameters** rslt (object) – A valid cobea.model.Result object. The object is modified during processing; the model variables are set to their optimal values.

**Returns additional\_rslt** – Additional information from the obtimization procedure. The function value and optimum are contained directly in the aforementioned rslt object that acted as input.

Return type dict

#### cobea.read\_elemnames (finame)

A helper function to read element names from text files into a list of strings. Standard input is a text file with linebreaks between elements.

# 2.2 cobea.model: COBEA classes and objects

This submodule defines all classes used by <code>cobea</code>. Besides input (<code>Response</code>) and output (<code>Result</code>) containers, this also includes gradient-based optimization procedures in <code>BE\_Model</code>

```
{\bf class} cobea.model.BEModel
```

```
Bases: cobea.model.BasicModel
```

Bilinear-Exponential model with topology information and optimization routines. Besides the attributes and methods contained in Bare\_Model, the following information is included.

### **Parameters**

- **(K, J, M)** (tuple) dimensions of the model, with K being the number of correctors, J being the number of monitors, and M the number of modes respectively directions.
- init\_fun (function) a (possibly self-defined) initialization function like zeros() or empty() from numpy.

#### topology

object – input topology, represented as Topology object

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```
cbeta_jmw
          Ripken-Mais beta parameters * constant. If self.R_jmw is normalized, constant = 1.
      delphi jmw
           Ripken-Mais phase advances per element
      flip mu(m)
           switch the sign of mu_m for given m, simultaneously changing the conjugation of R_jmw and A_km
           so that the response matrix remains unchanged
     phase_integral (m)
          integrated phase from first to last BPM (not one turn!), used for tune () computation
     phi_jmw
          Compute Ripken-Mais betatron phases
      response_matrix (dispersion=True)
           generate a 'simulated' response matrix from the present model parameters
               Returns Dev – response array of shape (K, J, M)
               Return type array
     tune (m)
           compute tune including integer part for a given mode m
class cobea.model.BasicModel
      simple representation of the Bilinear-Exponential model (without topology or optimization attributes).
           Parameters
                 • (K, J, M) (tuple) – dimensions of the model, with K being the number of correctors,
                   J being the number of monitors, and M the number of modes respectively directions.
                 • init_fun (function) - a (possibly self-defined) initialization function like
                   zeros() or empty() from numpy.
     K
          int – total number of correctors. defines limit of corrector index k.
      J
          int – total number of monitors. defines limit of monitor index j.
     М
          int – number of directions respectively modes. defines limits of mode index m and direction index w.
          array – monitor vectors in format [monitor, mode, direction]
     A_km
          array – corrector parameters, format [corrector, mode]
          array – unnormalized dispersion function at monitors, format [monitor, direction]
     b k
          array – unnormalized dispersion coefficients at correctors, format [corrector]
     mu m
          array – fractional phase advances per turn (in rad)
      A reduced model class without topology or gradient computation
class cobea.model.Response(matrix, corr_names, mon_names, line, include_dispersion=True,
      Representation of COBEA input, used as such for the function cobea.cobea()
     During creation of the this object, py:data:matrix rows and columns, as well as the corresponding
```

py:data:corr\_names and py:data:mon\_names, are resorted to their respective order in py:data:line.

2.2. cobea.model: COBEA classes and objects

#### **Parameters**

- matrix (array) input response matrix of shape (correctors, monitors, directions). If only one direction is considered, the last dimension can be omitted.
- corr\_names (list) a list of corrector labels corresponding to each row of the matrix
- mon\_names (list) a list of monitor labels corresponding to each column of the matrix
- line (list) a list of element names in ascending s order
- unit (str) unit for the input values of the matrix (optional)

#### topology

*object* – A *Topology* object holding the re-ordered py:data:'corr\_names', py:data:'mon\_names', and py:data:'line' as attributes.

#### matrix

array – re-ordered input response matrix.

```
class cobea.model.Result (response, additional={}, **kwargs)
```

Bases: cobea.model.BEModel

COBEA Result.

Besides the attributes and methods contained in BEModel, the following information is included.

#### matrix

array – Original input response matrix

#### error

object - computed BE model errors, represented as ErrorModel object

#### additional

dict - may contain the following keywords

**coretime** [float] time used for computation in the start and optimization layer.

err [dict] dictionary with additional model parameter error estimates.

conv [dict] dictionary with L-BFGS convergence information (if convergence\_info was True)

**invariants** [array] computed during normalization of monitor vectors if drift space is given. These are just returned for completeness and do not contain information about beam physics.

pca\_singvals [array] custom info from MCS algorithm

pca\_orbits [array] custom info from MCS algorithm

version [str] version of the object

#### save (filename)

save the Result object as a pickle file with the given filename. The object can be reloaded using <code>cobea.load\_result()</code> (which simply uses pickle)

### update\_errors()

compute errors in attribute *error* for given BE-Model parameters and input response, including errors for Ripken-Mais parameters

```
class cobea.model.Topology (corr_names, mon_names, line)
```

Representation of corrector/monitor labels and the order between them along the ring. During creation, all columns and rows of the input matrix, together with their labels in corr\_names, mon\_names, are re-ordered in ascending s-position according to the line list.

#### **Parameters**

• **corr\_names** (*list*) – corrector labels (strings), e.g. ['HK01', 'VCM1', 'special\_Hcorr', ...]. The list index should correspond to the monitor\_index, e.g. matrix[1,:,:] holds all information for the corrector named 'VCM1' in the above example.

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- mon\_names (list) monitor labels (strings), e.g. ['BPM1','BPM2a','buggy\_BPM',...,'important-bpm42']. the list index should correspond to the monitor\_index, e.g. matrix[:,0,:] holds all information for the monitor named 'BPM1' in the above example.
- line (list) corrector and monitor labels in ascending s position, downstream of the storage ring.

# 2.3 cobea.mcs: Monitor-Corrector Subspace algorithm

Monitor-Corrector Subset (MCS) algorithm submodule

MCS can be used as start-value layer of COBEA.

```
cobea.mcs.complexsolv(realvec, mat)
```

solve the half-complex equation system realvec = real(compmat\*conj(compsol)) for compsol. :returns: compsol, res (from lstsq),

realvec\_rc: reconstructed realvec from compsol, s: singular values of compmat (from lstsq)

cobea.mcs.composite\_vectors(pcaDev)

make two-orbit vectors (similar to phase space vectors) at beginning and end of partial orbits

cobea.mcs.corrector\_matrix\_k (R, cE)

output the complex corrector equation system matrix corrmat for a given corrector. corrmat.shape = [fast\_bpm\*Directions+direction,mode] R: full fast monitor array from TBT data, R.shape = [fast\_bpm,mode,direction] cE: conj(E[:,k,:]) of Ejkm

cobea.mcs.corrector\_systems (*Dev*, *monvec*, *bpm\_s*, *corr\_s*, *mus*, *printmsg=True*, *E=[]*) set up and solve the corrector equation systems. Dev[k,f,d]: Deviations at all correctors for fast BPMs. monvec: all TBT monitor vectors. returns: D[k,m]: corrector parameters complexsolv parameters as arrays

cobea.mcs.dice\_splitpoints (n, monidx, splitidx)

numpy arrays are passed by reference, so splitidx can be overwritten without return

cobea.mcs.find\_indices(x, y)

find all indices i for which x[n] = y[i[n]] (j arbitrary). len(x) < len(y). (This function could be re-moved to \_\_init\_\_ later on)

cobea.mcs.flatten\_Dev(Dev)

Index transform of Deviation matrix (k,j,w) to PCA processing matrix (k,j\*w)

cobea.mcs.layer(rslt, locruns=-1)

implementation of the Monitor-Corrector Subspace algorithm

#### **Parameters**

- rslt (object) A valid cobea.model.Result object. The object is modified during processing.
- **locruns** (*int*) Number of different monitor subsets tried for MCS. If set to -1, value is set automatically.

cobea.mcs.local\_optimization (*Dev*, *monidx*, *corridx*, *Nelems*, *include\_dispersion*, *runs=-1*) solve CES and MES systems compute residual Res error and find optimal splitidx

cobea.mcs.monitor\_matrix\_j(Y, E)

output the complex monitor equation system matrix monmat for a given monitor AND direction. monmat.shape = [corrector,mode] Y: corrector parameters, Y.shape = [corrector,mode] E: E[j,:,:] of Ejkm

cobea.mcs.monitor\_systems (Dev, D,  $all\_bpm\_s$ ,  $corr\_s$ , mus, printmsg=True, E=[])

set up and solve the monitor equation systems, return R[j,m,d], the full monitor vector set for all monitors. Dev[k,j,d]: Deviations at all correctors for all BPMs. D[k,m]: all corrector parameters.

```
Cobea.mcs.pca_core (Dev, principal_orbits=True)
Principal Component Analysis of a Deviation matrix.

Cobea.mcs.topo_indices (strilist, elto)
construct indices from stringlists. holds up to level.2 lists. strilist: list of elements elto: larger list of elements in which strilist elements are looked for.

Cobea.mcs.unflatten_Dev (pcaproc, Devshp)
Index transform of PCA processing matrix (k,j*w) to Deviation matrix (k,j,w)
```

# 2.4 cobea.plotting: Routines for plotting results

```
routines for plotting COBEA results Bernard Riemann, April 2016

cobea.plotting.coleur(n=-1)

a colorset compiled of: -0-5: colorbrewer2 2-class paired -6-11: inverse of 0-5

cobea.plotting.delphi_jmw(rslt, ax, m, comparison_data={}, yl=-1, direction='xy')

phase-advance plot

cobea.plotting.monitor_results(rslt, m=0, comparison_data={}, direction='xy')

plot monitor (and mu) results for mode m, optionally in comparison with comparison_data.
```

#### **Parameters**

- result (object) A cobea.model.Result object.
- m (int) mode index to plot results for
- comparison\_data (dict) a dictionary containing optional data from alternative decoupled storage ring models, which may contain the following keys: 'name': name of the algorithm or model used 'beta': an array of shape (rslt.M,rslt.J) that contains Courant-Snyder beta values for each direction and monitor 'phi': an array of the same shape as 'beta', containing Courant-Snyder betatron phases 'dispersion': an array of the same shape, containing dispersion values

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