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The *cobea* module [1] is a Python implementation of Closed-Orbit Bilinear-Exponential Analysis [2], an algorithm for studying closed-orbit response matrices of storage rings (particle accelerators).

If you publish material using this software, please cite one or more of the references [1-2].

For more information, visit https://bitbucket.org/b-riemann/cobea.

(References)

- [1] B. Riemann et al., "COBEA Optical Parameters From Response Matrices Without Knowledge of Magnet Strengths", in Proc. IPAC17, paper MOPIK066, 2017.
- [2] B. Riemann, ''[The Bilinear-Exponential Closed-Orbit Model and its Application to Storage Ring Beam Diagnostics](http://dx.doi.org/10.17877/DE290R-17221)', Ph.D. Dissertation, TU Dortmund University, 2016. DOI [10.17877/DE290R-17221](http://dx.doi.org/10.17877/DE290R-17221).

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# **QUICK START TUTORIAL**

This is a brief introduction on how to use the cobea module.

# 1.1 Reading in data

COBEAs input consists of

- A set of corrector names corresponding to rows of your matrix
- A set of monitor names corresponding to columns of your matrix
- The response matrix itself
- The ordering information, given as a list of monitor and corrector names, ordered along the beampath (downstream)

You need to convert your response data into a standardized input for COBEA. This is handled by the *Response* class:

```
class cobea.model.Response (matrix, corr_names, mon_names, line, include_dispersion=True, unit='')
```

Representation of COBEA input, used as such for the function cobea.cobea()

During creation of the this object, py:data:matrix rows and columns, as well as the corresponding py:data:corr\_names and py:data:mon\_names, are resorted to their respective order in py:data:line.

# **Parameters**

- **matrix** (array) input response matrix of shape (correctors, monitors, directions). If only one direction is considered, the last dimension can be omitted.
- corr\_names (list) a list of corrector labels corresponding to each row of the matrix
- mon\_names (list) a list of monitor labels corresponding to each column of the matrix
- line (list) a list of element names in ascending s order
- **include\_dispersion** (bool) whether to use a model with or without dispersion for fitting. default: True
- unit (str) unit for the input values of the matrix (optional)

#### topology

*object* – A Topology object holding the re-ordered py:data:'corr\_names', py:data:'mon\_names', and py:data:'line' as attributes.

# matrix

array – re-ordered input response matrix.

# 1.2 Running the algorithm

The COBEA algorithm is then applied using the function cobea.cobea() (click link, return back to 1.3 afterwards)

# 1.3 Obtaining and plotting results

```
The cobea function returns a Result object. This object contains all computed information.
class cobea.model.Result (response, additional={}, **kwargs)
     COBEA Result.
     Besides the attributes and methods contained in BEModel, the following information is included.
     matrix
           array – Original input response matrix
           object - computed BE model errors, represented as ErrorModel object
      additional
           dict – may contain the following keywords
           coretime [float] time used for computation in the start and optimization layer.
           err [dict] dictionary with additional model parameter error estimates.
           conv [dict] dictionary with L-BFGS convergence information (if convergence info was True)
          invariants [array] computed during normalization of monitor vectors if drift space is given. These
               are just returned for completeness and do not contain information about beam physics.
           pca_singvals [array] custom info from MCS algorithm
           pca_orbits [array] custom info from MCS algorithm
           version [str] version of the object
      cbeta_jmw
           Ripken-Mais beta parameters * constant. If self.R_jmw is normalized, constant = 1.
           const*beta at correctors assuming decoupled optics and thin correctors
      delphi_jmw
           Ripken-Mais phase advances per element
      delphi km
           Betatron phase advances per corrector assuming decoupled optics and thin correctors
           switch the sign of mu_m for given m, simultaneously changing the conjugation of R_jmw and A_km
           so that the response matrix remains unchanged
     phase_integral(m)
           integrated phase from first to last BPM (not one turn!), used for tune () computation
     phi_jmw
           Compute Ripken-Mais betatron phases in units of degrees
      response_matrix()
           generate a 'simulated' response matrix from the present model parameters
               Returns rsim_kjw – response array of shape (K, J, M)
```

Return type array

# ${\tt save}\,(filename)$

save the Result object as a pickle file with the given filename. The object can be reloaded using <code>cobea.load\_result()</code> (which simply uses pickle)

#### tune (m)

compute tune including integer part for a given mode m

## update\_errors()

compute errors in attribute error for given BE-Model parameters and input response, including errors for Ripken-Mais parameters

The module <code>cobea.plotting</code> includes many helper functions to view these results. A summary of results is created by the <code>cobea.plotting.plot\_result()</code> function.

API

This page contains automatic documentation of the complete cobea module.

# 2.1 cobea (main namespace)

Closed-Orbit Bilinear-Exponential Analysis (COBEA)

This is a Python implementation of the COBEA algorithm [1] to be used for studying betatron oscillations in particle accelerators by closed-orbit information.

[1] B. Riemann. 'The Bilinear-Exponential Model and its Application to Storage Ring Beam Diagnostics', PhD Dissertation (TU Dortmund University, 2016), DOI Link: (https://dx.doi.org/10.17877/DE290R-17221)

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cobea.cobea (response, drift\_space=None, convergence\_info=False)
Main COBEA function with pre- and postprocessing.

### **Parameters**

- response (object) A valid cobea. model. Response object representing the input.
- **drift\_space** (*iterable*) if not None, a tuple or list with 3 elements (monitor name 1, monitor name 2, drift space length / m)
- **convergence\_info** (bool) if True, convergence information from L-BFGS is added to the result dictionary (before saving).

Returns result - A cobea.model.Result object.

Return type object

cobea.load\_result (savefile)

Load (un-pickle) a Result object (or any other object)

```
cobea.optimization_layer(result, iprint=-1)
```

Implementation of the Optimization layer. It uses L-BFGS [1] as special case of L-BFGS-B [2] in scipy.optimize. The result object is modified to yield the optimal BEModel. A sub-dictionary with additional information is added under the key result.additional['Opt'].

- [1] D.C. Liu and J. Nocedal, "On the Limited Memory Method for Large Scale Optimization", Math. Prog. B 45 (3), pp.~503–528, 1989. DOI 10.1007/BF01589116
- [2] C. Zhu, R.H. Byrd and J. Nocedal, "Algorithm 778: L-BFGS-B: Fortran subroutines for large-scale bound-constrained optimization", ACM Trans. Math. Software 23 (4), pp.~550–560, 1997. DOI 10.1145/279232.279236

**Parameters result** (object) – A valid cobea.model.Result object. The object is modified during processing; the model variables are set to their optimal values.

**Returns** result – Identical to input object.

Return type object

```
cobea.read_elemnames (finame)
```

A helper function to read element names from text files into a list of strings. Standard input is a text file with linebreaks between elements.

# 2.2 cobea.model: COBEA classes and objects

This COBEA submodule defines all classes used by *cobea*. Besides input (*Response*) and output (*Result*) containers, this also includes gradient-based optimization procedures in BE\_Model.

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Bilinear-Exponential model with topology information and optimization routines. Besides the attributes and methods contained in Bare Model, the following information is included.

#### **Parameters**

- **K**, **J**, **M** (*int*) dimensions of the model, with K being the number of correctors, J being the number of monitors, and M the number of modes respectively directions.
- init\_fun (function) a (possibly self-defined) initialization function like zeros() or empty() from numpy.

#### topology

object - input topology, represented as Topology object

#### cbeta jmw

Ripken-Mais beta parameters \* constant. If self.R\_jmw is normalized, constant = 1.

#### cbeta km

const\*beta at correctors assuming decoupled optics and thin correctors

### delphi jmw

Ripken-Mais phase advances per element

## delphi km

Betatron phase advances per corrector assuming decoupled optics and thin correctors

```
\mathtt{flip}\_\mathtt{mu}\,(m)
```

switch the sign of mu\_m for given m, simultaneously changing the conjugation of R\_jmw and A\_km so that the response matrix remains unchanged

### phase\_integral(m)

integrated phase from first to last BPM (not one turn!), used for tune () computation

#### phi jmw

Compute Ripken-Mais betatron phases in units of degrees

# response\_matrix()

generate a 'simulated' response matrix from the present model parameters

Returns rsim\_kjw - response array of shape (K, J, M)

Return type array

# tune(m)

compute tune including integer part for a given mode m

```
class cobea.model.BasicModel(K, J, M, init_fun=<built-in function empty>)
```

 $simple\ representation\ of\ the\ Bilinear-Exponential\ model\ (without\ topology\ or\ optimization\ attributes).$ 

#### **Parameters**

- **K**, **J**, **M** (*int*) dimensions of the model, with K being the number of correctors, J being the number of monitors, and M the number of modes respectively directions.
- init\_fun (function) a (possibly self-defined) initialization function like zeros() or empty() from numpy.

K

int – total number of correctors. defines limit of corrector index k.

J

*int* – total number of monitors. defines limit of monitor index j.

M

int – number of directions respectively modes. defines limits of mode index m and direction index w.

R\_jmw

array – monitor vectors in format [monitor, mode, direction]

A km

array - corrector parameters, format [corrector, mode]

d\_jw

array – unnormalized dispersion function at monitors, format [monitor, direction]

b k

array – unnormalized dispersion coefficients at correctors, format [corrector]

mu m

array – fractional phase advances per turn (in rad)

A reduced model class without topology or gradient computation

Representation of COBEA input, used as such for the function cobea.cobea()

During creation of the this object, py:data:matrix rows and columns, as well as the corresponding py:data:corr\_names and py:data:mon\_names, are resorted to their respective order in py:data:line.

# **Parameters**

- **matrix** (array) input response matrix of shape (correctors, monitors, directions). If only one direction is considered, the last dimension can be omitted.
- corr\_names (list) a list of corrector labels corresponding to each row of the matrix
- mon\_names (list) a list of monitor labels corresponding to each column of the matrix
- line (list) a list of element names in ascending s order
- **include\_dispersion** (bool) whether to use a model with or without dispersion for fitting. default: True
- unit (str) unit for the input values of the matrix (optional)

## topology

*object* – A *Topology* object holding the re-ordered py:data:'corr\_names', py:data:'mon\_names', and py:data:'line' as attributes.

#### matrix

array – re-ordered input response matrix.

class cobea.model.Result (response, additional={}, \*\*kwargs)

Bases: cobea.model.BEModel

COBEA Result.

Besides the attributes and methods contained in BEModel, the following information is included.

#### matrix

array - Original input response matrix

#### error

object - computed BE model errors, represented as ErrorModel object

#### additional

dict - may contain the following keywords

**coretime** [float] time used for computation in the start and optimization layer.

**err** [dict] dictionary with additional model parameter error estimates.

**conv** [dict] dictionary with L-BFGS convergence information (if convergence\_info was True)

**invariants** [array] computed during normalization of monitor vectors if drift space is given. These are just returned for completeness and do not contain information about beam physics.

pca\_singvals [array] custom info from MCS algorithm

pca\_orbits [array] custom info from MCS algorithm

version [str] version of the object

# save (filename)

save the Result object as a pickle file with the given filename. The object can be reloaded using cobea.load\_result() (which simply uses pickle)

## update\_errors()

compute errors in attribute *error* for given BE-Model parameters and input response, including errors for Ripken-Mais parameters

## class cobea.model.Topology (corr\_names, mon\_names, line)

Representation of corrector/monitor labels and the order between them along the ring. During creation, all columns and rows of the input matrix, together with their labels in corr\_names, mon\_names, are re-ordered in ascending s-position according to the line list.

#### **Parameters**

- **corr\_names** (*list*) corrector labels (strings), e.g. ['HK01', 'VCM1', 'special\_Hcorr', ...]. The list index should correspond to the monitor\_index, e.g. matrix[1,:,:] holds all information for the corrector named 'VCM1' in the above example.
- mon\_names (list) monitor labels (strings), e.g. ['BPM1','BPM2a','buggy\_BPM',..,'important-bpm42']. the list index should correspond to the monitor\_index, e.g. matrix[:,0,:] holds all information for the monitor named 'BPM1' in the above example.
- line (list) corrector and monitor labels in ascending s position, downstream of the storage ring.

# 2.3 cobea.mcs: Monitor-Corrector Subspace algorithm

Monitor-Corrector Subset (MCS) algorithm submodule

MCS can be used as start-value layer of COBEA.

```
cobea.mcs.complexsolv(realvec, mat)
```

solve the half-complex equation system realvec = real(compmat\*conj(compsol)) for compsol. :returns: compsol, res (from lstsq),

realvec\_rc: reconstructed realvec from compsol, s: singular values of compmat (from lstsq)

```
cobea.mcs.composite_vectors(pcaDev)
```

make two-orbit vectors (similar to phase space vectors) at beginning and end of partial orbits

```
cobea.mcs.corrector_matrix_k(R, cE)
     output the complex corrector equation system matrix corrmat for a given corrector. corrmat.shape = [in-
     put_bpm*Directions+direction,mode] R: full input monitor array, R.shape = [input_bpm,mode,direction]
     cE: conj(E[:,k,:]) of Ejkm
cobea.mcs.corrector_systems(Dev, monvec, bpm_s, corr_s, mus, printmsg=True, E=[])
     set up and solve the corrector equation systems. Dev[k,f,d]: Deviations at all correctors for fast BPMs.
     monvec: all input monitor vectors. returns: D[k,m]: corrector parameters complexsolv parameters as arrays
cobea.mcs.dice_splitpoints (n, monidx, splitidx)
     numpy arrays are passed by reference, so splitidx can be overwritten without return
cobea.mcs.find indices (x, y)
     find all indices i for which x[n] = y[i[n]] (j arbitrary). len(x) < len(y). (This function could be re-moved to
      __init__ later on)
cobea.mcs.flatten_Dev(Dev)
     Index transform of Deviation matrix (k,j,w) to PCA processing matrix (k,j*w)
cobea.mcs.layer(response, trials=-1)
     implementation of the Monitor-Corrector Subspace algorithm
          Parameters
                 • response (object) - A valid cobea. model. Response object.
                 • trials (int) – Number of different monitor subsets tried for MCS. If set to -1, value
                  is set automatically.
cobea.mcs.local_optimization(Dev, monidx, corridx, Nelems, include_dispersion, runs)
     solve CES and MES systems compute residual Res error and find optimal splitidx
cobea.mcs.monitor matrix j(Y, E)
     output the complex monitor equation system matrix monmat for a given monitor AND direction. mon-
     mat.shape = [corrector,mode] Y: corrector parameters, Y.shape = [corrector,mode] E: E[j,:,:] of Ejkm
cobea.mcs.monitor_systems(Dev, D, all_bpm_s, corr_s, mus, printmsg=True, E=[])
```

cobea.mcs.pca\_core (Dev, principal\_orbits=True)

Principal Component Analysis of a Deviation matrix.

```
cobea.mcs.topo_indices (strilist, elto)
```

construct indices from stringlists. holds up to level.2 lists. strilist: list of elements elto: larger list of elements in which strilist elements are looked for.

set up and solve the monitor equation systems, return R[j,m,d], the full monitor vector set for all monitors.

```
\verb"cobea.mcs.unflatten_Dev" (pcaproc, Devshp")
```

Index transform of PCA processing matrix (k,j\*w) to Deviation matrix (k,j,w)

# 2.4 cobea.pproc: Standalone postprocessing functions

Dev[k,j,d]: Deviations at all correctors for all BPMs. D[k,m]: all corrector parameters.

Small postprocessing and helper functions for COBEA results.

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```
cobea.pproc.guess\_mu\_sign(rslt)
```

for weakly coupled setups, guess the sign of mu (quadrant) based on monitor phase advance

```
cobea.pproc.invariants_from_eigenvectors (Q)
```

Compute invariant of motion from a phase space eigenvector

**Parameters Q** (array) – phase space eigenvector with shape (1,2\*M)

Returns invariant – invariants of motion

# Return type float

```
cobea.pproc.invariants_of_motion(R_drift, length)
```

Compute invariant of motion from the eigenorbits around a known drift space

#### **Parameters**

- **R\_drift** (array) An array of two spatial vectors **R\_drift**[0] and **R\_drift**[1]
- length (float) length of the drift space

**Returns** invariant – invariants of motion

Return type float

```
\verb"cobea.pproc.l_bfgs_iterate" (alloc_items=10000)
```

convert the iterate.dat file produced by L-BFGS-B

**Parameters alloc\_items** (*int*) – the number of maximum iterations for which memory is allocated.

#### Returns

iter –

a dictionary with the following fields. The field names and descriptions have been copied from a demo output

```
'it' [array] iteration number
```

'nf' [array] number of function evaluations

'nseg' [array] number of segments explored during the Cauchy search

'nact' [array] number of active bounds at the generalized Cauchy point

'sub' [str]

manner in which the subspace minimization terminated con = converged, bnd = a bound was reached

'itls' [int] number of iterations performed in the line search

'stepl' [float] step length used

**'tstep'** [float] norm of the displacement (total step)

'projg' [float] norm of the projected gradient

'f' [float] function value

# Return type dict

```
cobea.pproc.normalize_using_drift (model, di, drift_length)
```

Invariant postprocessing algorithm. The Result object is modified by information from a drift space. monitor vectors, corrector parameters and the sign of mu\_m is changed accordingly.

# **Parameters**

- model (object) A valid cobea.model.BEModel object or descendant. The object is modified.
- di (list) j indices of the used drift space
- **drift\_length** (float) length of the use drift space

# cobea.pproc.phasor\_eigenvectors(R\_drift, length)

Compute phase space vector from the spatial vectors around a drif t space

#### **Parameters**

- **R\_drift** (array) An array of two spatial vectors **R\_drift**[0] and **R\_drift**[1]
- length (float) length of the drift space

```
Return type array
cobea.pproc.symplectic_form (D=2)
     Compute the symplectic form.
          Parameters D(int) – number of spatial dimensions of the phase space vectors considered.
          Returns Omega – a matrix that can be used to compute invariants I from phase space eigenvec-
              tors Q via (* matrix product) I = Q.T * Omega * Q
          Return type array
2.5 cobea.plotting: Routines for plotting results
routines for plotting cobea results
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cobea.plotting.A_km (result, m, ax=<matplotlib.axes._subplots.AxesSubplot object>)
     plot real and imaginary parts of corrector parameters (incl. errors) into an axis for a given mode m
cobea.plotting.R_jmw (result, m, w=None, direction='xy', ax=<matplotlib.axes._subplots.AxesSubplot
                            object>)
     plot real and imaginary parts of monitor vectors (incl. errors) into an axis for a given mode m
cobea.plotting.cbeta_jmw(result,
                                                            comparison_data={},
                                          m,
                                                w=None,
                                                                                   direction='xy',
                                  ax=<matplotlib.axes._subplots.AxesSubplot object>)
     plot beta resp. const*beta (incl. errors) into an axis for a given mode m
cobea.plotting.cbeta_km(result, m, comparison_data={}, ax=<matplotlib.axes._subplots.AxesSubplot
                                object>)
     plot const*beta at correctors assuming decoupled optics and thin correctors ToDo: errors for this quantity
cobea.plotting.coleur (n=-1)
     a colorset compiled of: - 0-5: colorbrewer2 2-class paired - 6-11: inverse of 0-5
cobea.plotting.corrector_label(corr_labels=[],
                                                                                         dir='v',
                                                                    spacing=0,
                                          ax=<matplotlib.axes._subplots.AxesSubplot object>)
     apply corrector labels to an axis
cobea.plotting.corrector_results (result, m=0, comparison_data={}, direction='xy')
     create a figure with corrector results for a given mode m
cobea.plotting.d_jw (result,
                                                        comparison_data,
                                                                                   direction='xy',
                                           w.
                           ax=<matplotlib.axes._subplots.AxesSubplot object>)
     plot const*dispersion (incl. errors) into an axis for a given direction w (0: x, 1: y)
cobea.plotting.delphi_jmw(result, m, w=None, comparison_data={}, yl=-1, direction='xy',
                                   ax=<matplotlib.axes._subplots.AxesSubplot object>)
     plot phase-advance per monitor (incl. errors) into an axis for a given mode m
cobea.plotting.monitor_label (mon_labels=0, spacing=0, ax=<matplotlib.axes._subplots.AxesSubplot
                                       object>)
     apply monitor labels to an axis
cobea.plotting.monitor_results(result, m=0, w=None,
                                                                     comparison\_data=\{\},
                                          tion='xy'
     plot monitor results for mode m, optionally in comparison with comparison_data.
          Parameters
                • result (object) - A cobea.model.Result object.
                • m (int) - mode index to plot results for
```

• **w** (*int*) – direction index to plot results for

**Returns Q** – Phase space vector

• comparison\_data (dict) – a dictionary containing optional data from alternative decoupled storage ring models, which may contain the following keys: 'name': name of the algorithm or model used 'beta': an array of shape (result.M,result.J) that contains Courant-Snyder beta values for each direction and monitor 'phi': an array of the same shape as 'beta', containing Courant-Snyder betatron phases 'dispersion': an array of the same shape, containing dispersion values

```
cobea.plotting.plot_Dev_err(result, w=0)
     create a figure that shows response matrix and residual error for a given direction w (0: x, 1: y)
cobea.plotting.plot_matrix(Devdr,
                                                    devlbl.
                                                                  cmap=('PRGn',
                                                                                         'Greens'),
                                     ax=<matplotlib.axes._subplots.AxesSubplot object>)
     plot an arbitrary matrix with divergent or sequential colormap (helper function)
cobea.plotting.plot_residual(result,
                                                                                   label='residual',
                                                              w=0.
                                        ax=<matplotlib.axes._subplots.AxesSubplot object>)
     plot fit residual into an axis for a given direction w (0: x, 1: y)
cobea.plotting.plot_response(response,
                                                               w=0.
                                                                                  label='deviation',
                                        ax=<matplotlib.axes._subplots.AxesSubplot object>)
     Plot response matrix into an axis for a given direction w(0: x, 1: y)
cobea.plotting.plot_result (result, print_figures=True, prefix='', comparison_data={}, direc-
                                     tion='xy', plot_flags='mcdtv')
     plot cobea results.
```

## **Parameters**

- result (object) A cobea.model.Result object.
- **print\_figures** (bool) whether to print figures into separate pdf files instead of showing them. Default: True
- **prefix** (str) if print\_figures=True, prefix contains the relative path to the current folder where results are printed.
- comparison\_data (dict) a dictionary containing optional data from alternative decoupled storage ring models, which may contain the following keys: 'name': name of the algorithm or model used 'beta': an array of shape (result.M,result.J) that contains Courant-Snyder beta values for each direction and monitor 'phi': an array of the same shape as 'beta', containing Courant-Snyder betatron phases 'dispersion': an array of the same shape, containing dispersion values
- **direction** (str) direction characters for the result object. can be 'x','y', or 'xy'.
- plot\_flags (str) which plots are to be created. Each character represents a different result plot: 'm': monitor\_results -> monitor\_m\*.pdf 'c': corrector\_results -> corrector\_m\*.pdf 'd': plot\_Dev\_err, hist -> Dev\_err\_w\*.pdf, hist\_w\*.pdf 't': plot\_topology -> topology.pdf 'v': convergence information -> convergence.pdf. Only works if convergence information is available.

```
cobea.plotting.plot_size (plot_type=0)
    plot sizes for all plot types

cobea.plotting.plot_topology (topology)
    create a figure that shows the accelerator topology. Input: Topology object

cobea.plotting.prepare_figure (plot_type=0)
    set fonts, tex packages, and figure size. returns figure
```

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