

SLR

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```
library(tidyverse)

## — Attaching packages — tidyverse
1.3.1 —

## ✓ ggplot2 3.3.5      ✓ purrr  0.3.4
## ✓ tibble  3.1.6      ✓ dplyr  1.0.7
## ✓ tidyr   1.1.4      ✓ stringr 1.4.0
## ✓ readr   2.1.1      ✓ forcats 0.5.1

## — Conflicts —
tidyverse_conflicts() —
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()     masks stats::lag()

getwd()

## [1] "/Users/brookewheeler/Desktop/Regression/Labs"

House <- read.csv("../Data/HOME_SALES.csv")
attach(House)
```

1. Find correlation and covariance between house prices and house sizes. What do these values indicate?

```
cor(SALES_PRICE, FINISHED_AREA)

## [1] 0.8194701

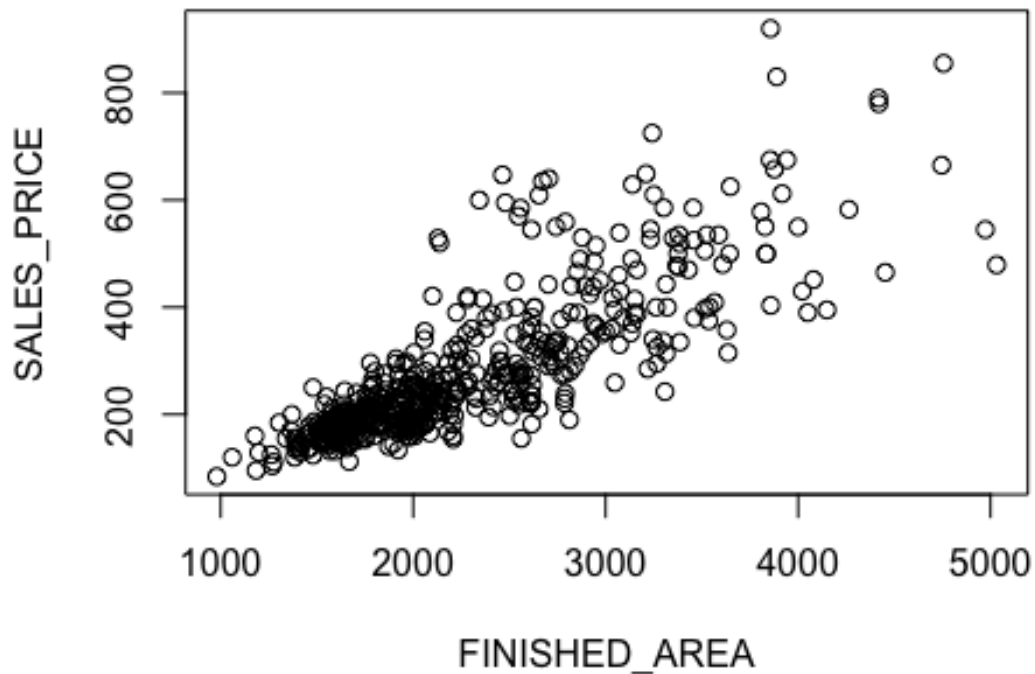
cov(SALES_PRICE, FINISHED_AREA)

## [1] 80367.58

# The correlation value is closer to 1 than 0 meaning that linear
# relationship between sales price and house size is strong. The covariance
# value is positive, showing that as sales price increases so does house size
# and as house size increases so does sales price.
```

2. Scatterplot

```
plot(FINISHED_AREA, SALES_PRICE)
```



3. Find equation of least-squares regression line. Find regression coefficients.

```
#y first
reg <- lm(SALES_PRICE ~ FINISHED_AREA, data = House)
reg

##
## Call:
## lm(formula = SALES_PRICE ~ FINISHED_AREA, data = House)
##
## Coefficients:
## (Intercept)  FINISHED_AREA
##      -81.433         0.159

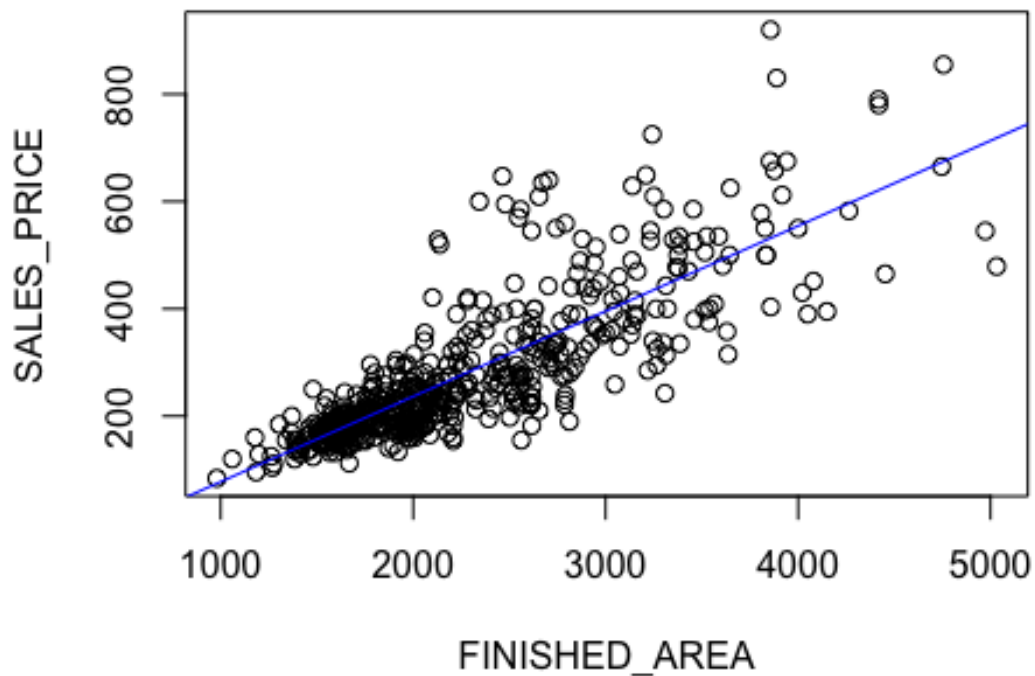
# y (hat)= -81.433 + .159
```

4. Plot regression line

```
reg
```

```
##
## Call:
## lm(formula = SALES_PRICE ~ FINISHED_AREA, data = House)
##
## Coefficients:
## (Intercept)  FINISHED_AREA
##      -81.433         0.159

plot(FINISHED_AREA, SALES_PRICE)
abline(reg, col = "blue")
```



5. Create a new plot that shows all predicted house prices, using new color for points

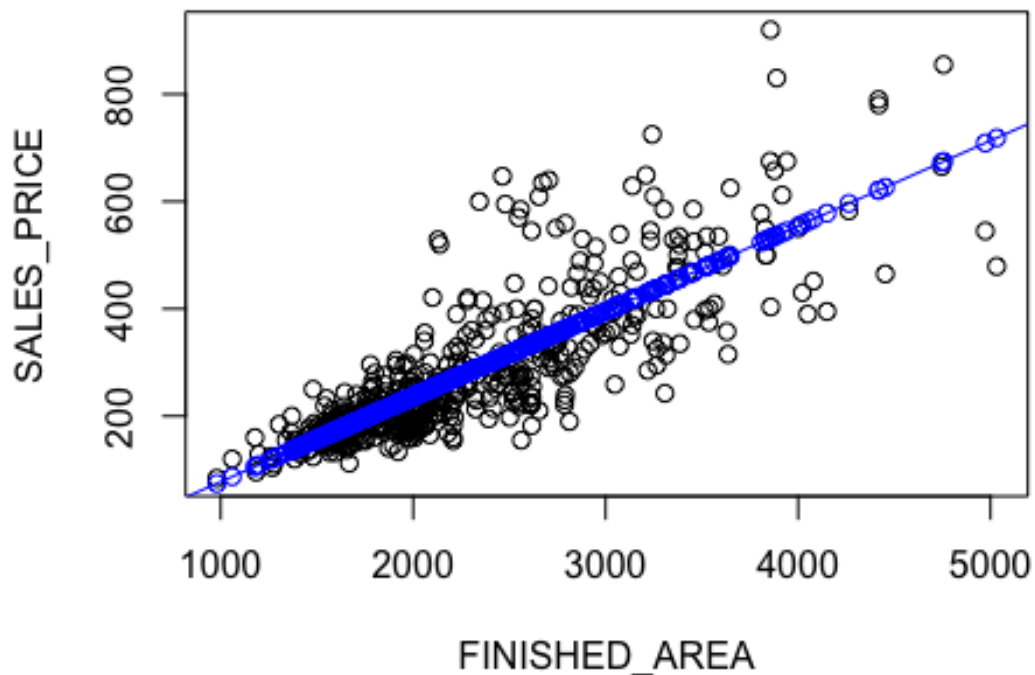
reg

```
##
## Call:
## lm(formula = SALES_PRICE ~ FINISHED_AREA, data = House)
##
## Coefficients:
## (Intercept)  FINISHED_AREA
##      -81.433         0.159
```

```
plot(FINISHED_AREA, SALES_PRICE)
abline(reg, col = "blue")

Yhat <- predict(reg, x= FINISHED_AREA)

points(FINISHED_AREA, Yhat, col="blue")
```



**6. If the size of a house is 2000 square feet, what is the predicted house price?
Also, show predictions for houses that are 1500 and 3500 square feet.**

```
predict(reg, data.frame(FINISHED_AREA = 2000))

##          1
## 236.4675

# predicted house price for 2000 square feet is 236.4675 thousand $

predict(reg, data.frame(FINISHED_AREA = 1500))

##          1
## 156.9924

predict(reg, data.frame(FINISHED_AREA = 3500))
```

```
##          1
## 474.8929
```

7. Find values of all residuals

```
resid(reg)
```

```
##          1          2          3          4          5
## -40.50415343  94.31337139  48.50153555  26.57246833  7.87823953
##          6          7          8          9         10
##  16.93679262 -40.90076508 -22.41057221  18.61567202 -72.65270969
##          11         12         13         14         15
## -175.53510265 196.80285220  79.02221602  56.62409802  49.12696400
##          16         17         18         19         20
##  94.70580041  12.58969972 -19.95333764 -54.03322065 -8.65122484
##          21         22         23         24         25
##  41.60948217  13.20368947 -73.64478456 -75.72188568 -142.69850743
##          26         27         28         29         30
## -68.74651984 -33.53535308 -30.68353369 -109.52916324 -144.04735712
##          31         32         33         34         35
##  13.86560941 -42.30063987 -115.52916324 -53.47964448 -66.16347931
##          36         37         38         39         40
## -75.78851061 -201.87441713 -152.38085741  27.36560941  2.19158171
##          41         42         43         44         45
##  14.86560941  20.14959095 -4.18997397 -1.70222844 -20.20841829
##          46         47         48         49         50
## -30.35647368 -39.02780360 -74.93669122 -64.50762400  9.18041495
##          51         52         53         54         55
## -28.19294368  3.64340110 -71.69603860  9.66172020 -170.79754494
##          56         57         58         59         60
##  75.21161461 -16.11594627 138.54956945 108.99547092 -85.29618531
##          61         62         63         64         65
##  -5.34248392 -8.24664506 -18.75446647 -53.95204062 -0.54476306
##          66         67         68         69         70
## -23.91582106 -7.71205706 -57.08326177 259.83825598 -4.46797685
##          71         72         73         74         75
## 129.85113654 293.27549877 388.36190616 180.46564866 142.07928426
##          76         77         78         79         80
##  62.55278959 169.19082667 -7.94484904 291.11629810 336.77957768
##          81         82         83         84         85
## 159.03187644 122.68290154  54.15046747  44.81696718  98.64926781
##          86         87         88         89         90
## 268.57903382 291.71792967  62.22746487 126.68250440 117.70389894
##          91         92         93         94         95
## -46.54077013  23.57014620 220.20270549  46.11951824 291.47257205
##          96         97         98         99        100
## 308.85360537 -13.83083778 210.77809282 -12.05948637 282.39532421
##          101        102        103        104        105
## 174.68574603 246.58670852 -239.40461505 -164.02655143  6.02345044
##          106        107        108        109        110
## 211.48817188  28.06393486 271.77790500 -15.24493127  77.79072295
```

##	111	112	113	114	115
##	72.96502257	56.13338278	70.82489231	94.44942274	2.21830532
##	116	117	118	119	120
##	132.13783734	113.04685018	41.61617289	-112.69850743	-18.88073219
##	121	122	123	124	125
##	6.23365471	81.50797583	153.97418212	78.17621083	-128.29704408
##	126	127	128	129	130
##	195.59141351	-88.53485221	-28.30013900	-161.37243141	-115.58399532
##	131	132	133	134	135
##	-107.26176551	22.97146285	58.87391019	73.03434528	127.52976550
##	136	137	138	139	140
##	120.99250122	-30.04116727	115.38158489	23.92961879	53.77363827
##	141	142	143	144	145
##	83.03139706	117.76868284	-2.57991641	143.67980662	61.74887889
##	146	147	148	149	150
##	-27.66433807	48.51441611	-17.51665833	22.50203642	-127.86488193
##	151	152	153	154	155
##	19.65801694	16.15318674	-81.25087068	-7.57050643	-183.21051147
##	156	157	158	159	160
##	94.81943601	85.54498968	10.35373059	69.98012153	52.38706873
##	161	162	163	164	165
##	127.42466337	10.66383114	-64.24022628	-26.66483894	-131.82811851
##	166	167	168	169	170
##	56.97393169	63.23488913	-12.87776249	-16.63388972	-37.16270651
##	171	172	173	174	175
##	23.60529954	-29.94238020	30.11914259	-138.05639145	65.84419539
##	176	177	178	179	180
##	49.79480185	-65.84384356	133.70851968	-2.32811851	12.37353454
##	181	182	183	184	185
##	-2.95030533	-78.98570911	16.86004565	45.38442938	61.22993370
##	186	187	188	189	190
##	45.98334167	96.18660479	30.06974906	-47.85287789	-24.18462140
##	191	192	193	194	195
##	-76.38357668	-13.46107495	-26.74183635	-33.98558389	-6.68662861
##	196	197	198	199	200
##	-50.53483072	-47.70172757	-49.52594310	-36.42245103	-20.45488510
##	201	202	203	204	205
##	-80.43606514	-105.81506975	261.59735292	-25.59378095	30.23934369
##	206	207	208	209	210
##	-4.57818112	-108.68610625	18.99547092	-7.77721863	-172.31548839
##	211	212	213	214	215
##	-31.27291078	-76.86216266	30.08361360	-64.11841511	-94.51950282
##	216	217	218	219	220
##	-41.84532841	19.84741553	61.68551709	-181.51009284	72.83800555
##	221	222	223	224	225
##	-29.96357985	-121.77253513	55.53260999	65.30099170	34.67757046
##	226	227	228	229	230
##	-99.53980764	-96.74505648	-36.59202417	5.83060278	46.05711893
##	231	232	233	234	235
##	-29.45662039	-39.27613092	168.47851146	51.74243861	23.98309124

##	236	237	238	239	240
##	37.41983316	-111.74505648	-6.27734385	-60.24505648	-105.07224171
##	241	242	243	244	245
##	18.61765774	-20.44127100	-36.57370507	-10.83462140	-42.90549157
##	246	247	248	249	250
##	77.89668385	94.00688812	-12.22673739	-12.92109140	-93.12163525
##	251	252	253	254	255
##	-85.39323710	5.76397785	-87.52916324	23.00760018	0.13436677
##	256	257	258	259	260
##	-46.72351725	-113.84505648	15.93382291	-63.13698464	27.29183215
##	261	262	263	264	265
##	-40.51774604	-39.68340848	-36.53547830	-8.57518992	-86.82029711
##	266	267	268	269	270
##	-88.59081125	-21.81611448	7.55578079	21.21916409	22.26876694
##	271	272	273	274	275
##	-65.04760755	-34.40883692	-40.63859471	20.45214201	15.17744525
##	276	277	278	279	280
##	-63.93613092	-52.49821401	-13.77303600	-2.85647368	-145.22784659
##	281	282	283	284	285
##	-130.42096618	75.00463047	7.88578901	-140.40239665	53.27623232
##	286	287	288	289	290
##	-84.54129249	-20.24518170	-36.51812169	-80.11665833	64.11876694
##	291	292	293	294	295
##	-5.66508938	-14.90574200	-51.21893747	-2.49227460	9.75159816
##	296	297	298	299	300
##	8.28564230	-53.34074864	-23.78972354	17.44582695	11.18982493
##	301	302	303	304	305
##	-14.26239160	-12.91515199	-18.16199445	-35.01046849	10.09425800
##	306	307	308	309	310
##	-31.33602215	-53.93050138	4.03235956	-33.04154292	4.37204969
##	311	312	313	314	315
##	30.74568847	31.83633287	23.54043140	15.83033085	-12.70829307
##	316	317	318	319	320
##	35.25644986	14.13733647	-110.31820579	-32.49026739	10.10638725
##	321	322	323	324	325
##	29.04473924	27.87987110	19.62508200	-8.92303600	-68.48595954
##	326	327	328	329	330
##	-29.70816785	-21.65122484	-24.44894569	-56.89955216	-27.33480923
##	331	332	333	334	335
##	0.85335494	-52.54894569	32.09722770	-11.04166814	-19.06617709
##	336	337	338	339	340
##	-3.80250037	1.08175309	-29.03844800	50.42280286	37.95214201
##	341	342	343	344	345
##	-49.52594310	24.16506556	-86.17090357	-33.59254653	-16.68353369
##	346	347	348	349	350
##	5.86585984	-37.76362602	-12.19415660	-58.20952749	38.70456786
##	351	352	353	354	355
##	-47.62176047	-3.94139621	11.79492707	-118.76053109	-18.66236029
##	356	357	358	359	360
##	-44.01071892	7.19170693	13.59716509	-48.14342492	-29.48756961

##	361	362	363	364	365
##	-122.64714780	-76.16793386	-11.09415660	-50.34099907	-0.25781182
##	366	367	368	369	370
##	17.51688494	-10.66098883	-1.75277230	10.47623232	-4.85189391
##	371	372	373	374	375
##	-5.08177691	-25.92431153	-6.06320738	-13.85498883	-41.44894569
##	376	377	378	379	380
##	-57.58016684	-61.54530692	-75.12634024	-57.62176047	-61.16347931
##	381	382	383	384	385
##	-29.22807553	-33.47370507	6.95711893	-43.98271791	0.29158171
##	386	387	388	389	390
##	-20.15404783	0.71755402	-0.45835568	-3.98298984	12.10019741
##	391	392	393	394	395
##	-31.13547830	32.94570174	11.64959095	67.96008864	-131.66134688
##	396	397	398	399	400
##	13.45699372	-56.12309861	-59.26214116	9.06949862	-49.08784154
##	401	402	403	404	405
##	7.48148117	-9.85028384	23.13263148	-1.15283491	12.38417894
##	406	407	408	409	410
##	-15.27140444	51.59413278	-14.27019151	-11.10034645	30.92144323
##	411	412	413	414	415
##	31.73290341	34.62483157	55.64959095	13.84097525	11.55396140
##	416	417	418	419	420
##	-52.56630230	-2.87033822	-73.14181485	26.78430416	21.73599833
##	421	422	423	424	425
##	-31.20802114	-39.89160553	-17.61582106	-28.60963121	-14.77746907
##	426	427	428	429	430
##	-15.88742290	17.06008864	18.25948217	-4.88123306	24.00638725
##	431	432	433	434	435
##	-9.33183952	-20.93493444	-0.06764044	-55.20950600	-37.67598421
##	436	437	438	439	440
##	-28.33305245	2.83788033	-9.81582106	-11.21770305	-51.83790415
##	441	442	443	444	445
##	-15.03991136	6.01379002	-25.48311506	6.06506556	13.07422511
##	446	447	448	449	450
##	-42.39769165	-13.00477951	-97.17855677	-4.51824691	5.11257710
##	451	452	453	454	455
##	-10.38754812	23.62186186	-8.31945983	19.60032263	-13.60963121
##	456	457	458	459	460
##	13.58794294	-98.84384356	-8.84085236	-5.80720536	11.88457609
##	461	462	463	464	465
##	-40.25162198	-103.77600571	-40.51205706	-18.65417305	-2.33802937
##	466	467	468	469	470
##	81.67905531	13.29777156	-0.37370507	-50.87491800	1.70207941
##	471	472	473	474	475
##	-16.71609298	-28.22067276	-13.88432798	-1.52322383	-18.41582106
##	476	477	478	479	480
##	-4.06939722	-45.30089030	22.66197063	-18.88123306	-14.04488828
##	481	482	483	484	485
##	18.38417894	-27.67073537	5.71002603	-19.01393906	-42.99685438

##	486	487	488	489	490
##	-70.73911707	8.76506556	0.60948217	13.75147294	-26.06333260
##	491	492	493	494	495
##	-77.83911707	-15.52322383	-67.03077331	-15.39670767	-21.70222844
##	496	497	498	499	500
##	-38.78244598	-12.65592983	-14.12510582	-38.08183952	6.51997987
##	501	502	503	504	505
##	-43.39785799	14.85026002	-47.28851061	-0.56157582	54.18957450
##	506	507	508	509	510
##	5.67880488	63.50824776	58.66184542	23.43963711	-16.37046344
##	511	512	513	514	515
##	2.99522049	20.01056988	0.08781772	63.67113018	-20.44421921
##	516	517	518	519	520
##	-35.64206529	-5.62792882	-44.62968560	-42.56630230	-90.56939722
##	521	522			
##	-29.81339521	-11.26412689			

8. Look at the first house. Calc. the residual value

```
predict(reg, data.frame(FINISHED_AREA = 3032))
```

```
##      1
## 400.5042
```

#8.

$$e_i = Y_i - \hat{Y}_i$$

$$= 360 - 400$$

$$= -40 \text{ is the residual value}$$

9. One property we discussed is that the sum of the residuals is zero. Find the sum of the residuals here and comment on the value that you obtain.

```
sum(resid(reg))
```

```
## [1] -2.375877e-13
```

#The value I obtained is very very close to one which would make sense if the expected value is zero.

10. Show the regression line passes through (\bar{X}, \bar{Y}) . Hint: First find the means and then predict the appropriate value.

```
summary(House)
```

```
##          ID          SALES_PRICE    FINISHED_AREA    BEDROOMS
BATHROOMS
## Min.      : 1.0    Min.      : 84.0    Min.      : 980    Min.      :0.000    Min.
:0.000
## 1st Qu.:131.2    1st Qu.:180.0    1st Qu.:1701    1st Qu.:3.000    1st
Qu.:2.000
## Median :261.5    Median :229.9    Median :2061    Median :3.000    Median
:3.000
## Mean    :261.5    Mean    :277.9    Mean    :2261    Mean    :3.471    Mean
:2.642
## 3rd Qu.:391.8    3rd Qu.:335.0    3rd Qu.:2636    3rd Qu.:4.000    3rd
Qu.:3.000
## Max.    :522.0    Max.    :920.0    Max.    :5032    Max.    :7.000    Max.
:7.000
##  GARAGE_SIZE    YEAR_BUILT          STYLE          LOT_SIZE
## Min.      :0.0    Min.      :1885    Min.      :1.000    Min.      : 4560
## 1st Qu.:2.0    1st Qu.:1956    1st Qu.:1.000    1st Qu.:17205
## Median :2.0    Median :1966    Median :2.000    Median :22200
## Mean    :2.1    Mean    :1967    Mean    :1.925    Mean    :24370
## 3rd Qu.:2.0    3rd Qu.:1981    3rd Qu.:3.000    3rd Qu.:26787
## Max.    :7.0    Max.    :1998    Max.    :3.000    Max.    :86830
##  AIR_CONDITIONER    POOL          QUALITY          HIGHWAY
## Length:522          Length:522          Length:522          Length:522
## Class :character    Class :character    Class :character    Class :character
## Mode  :character    Mode  :character    Mode  :character    Mode  :character
##
##
##
```

```
# mean sales price = 277.9
# mean finished area = 2261
```

```
predict(reg, data.frame(FINISHED_AREA = 2261))
```

```
##          1
## 277.9535
```

```
# at x= 2261 y = 277.9535
```