

Generals must agree on a decision: attack /retrait

Each general i sends its opinion , $v(i)$, to the other generals

Default value: retrait

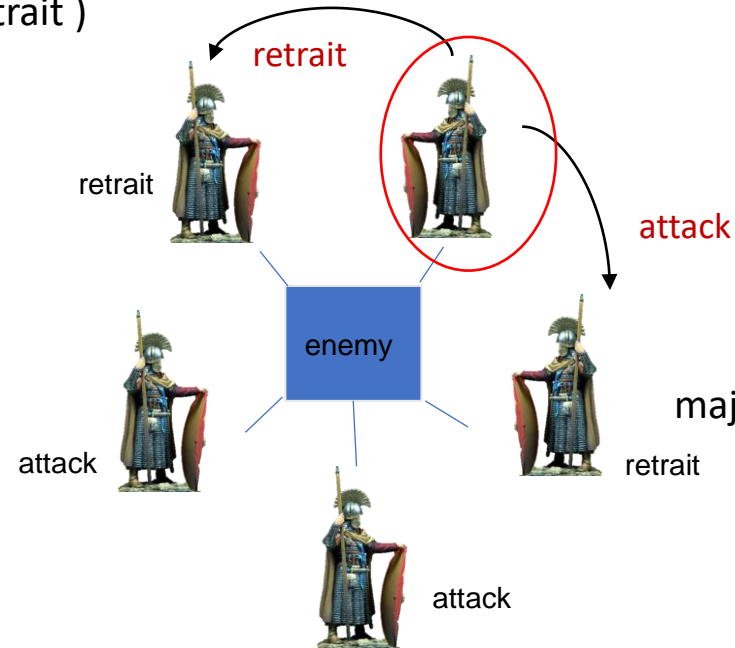
Each general obtains the final decision by majority function:

$\text{majority}(v(1), \dots, v(n))$

If no majority: default value

In case of traitors: a general can lie and sends different opinions

majority(retrait, attack, attack, retrait, retrait)
==> retrait



majority(retrait, attack, attack, retrait, attack)
==> attack

Loyal generals can take different decisions!

Majority vote is applied to different sets of value !!!!!

Generals should agree on the value sent by the traitor before applying majority

Problem: Find the consensus on the value sent by a general

Find the consensus on the value sent by a general

Oral message algorithm

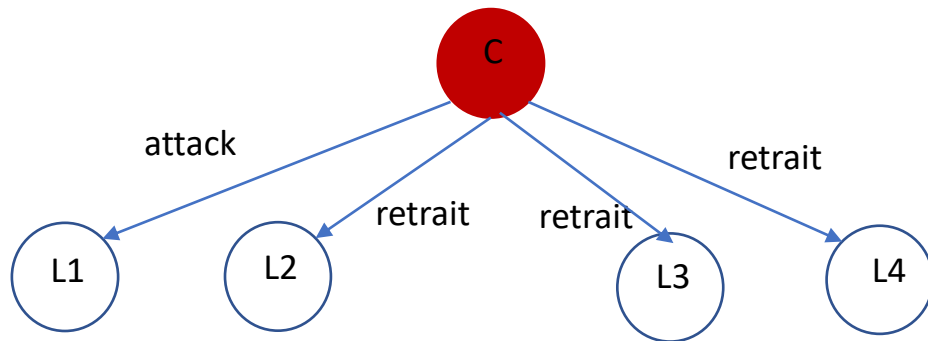
1. Commander sends a message
2. each Lieutenant resends what he has received by the commander
3. Each Lieutenant apply majority function

L_i : $\text{majority}(v_1, v_2, v_3, v_4)$

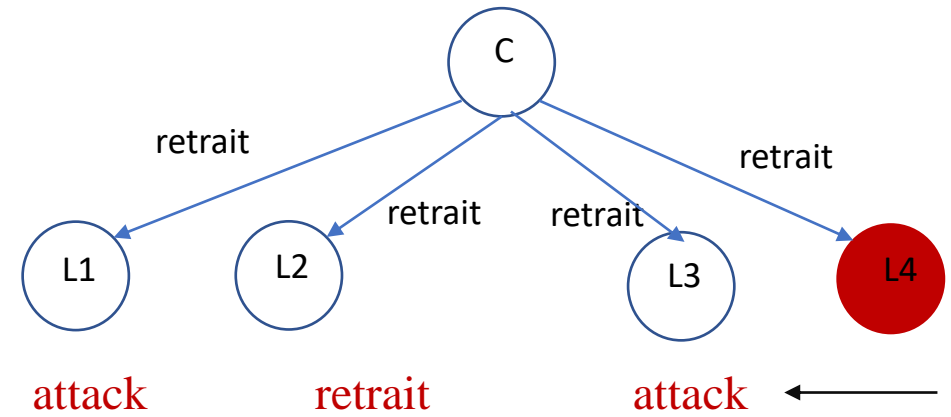
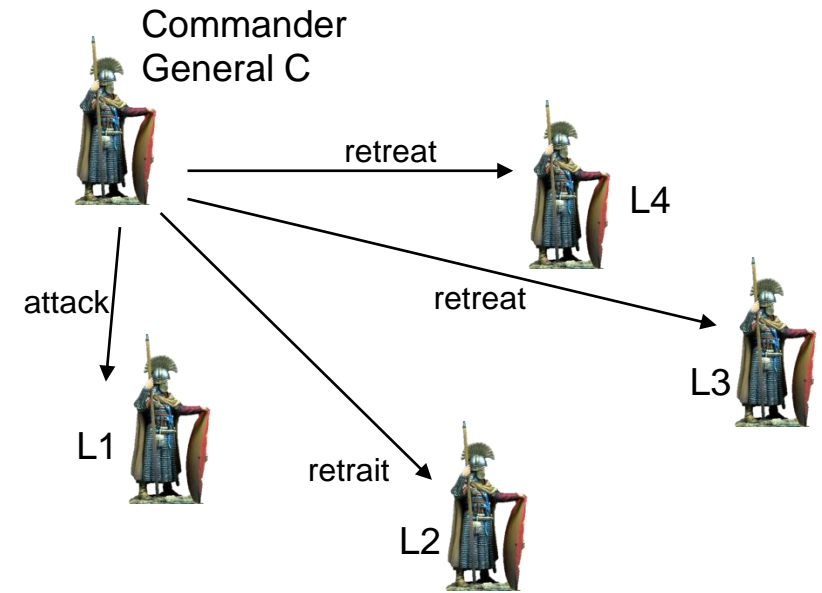
Consensus reached in case of 1 traitor and $n \geq 4$ generals

Traitor: commanding general or lieutenant

Examples



$L1$: $\text{majority}(\text{attack}, \text{retrait}, \text{retrait}, \text{retrait})$

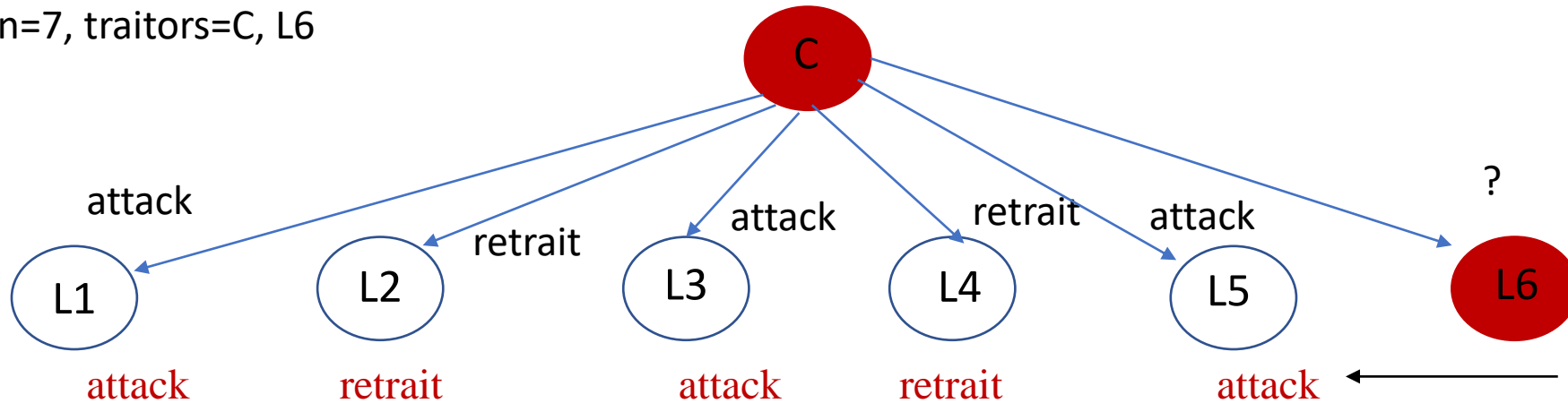


$L1$: $\text{majority}(\text{retrait}, \text{retrait}, \text{retrait}, \text{attack})$

With more traitors?

2 traitors

Scenario: $m=2$, $n=7$, traitors=C, L6



1 round

L1: majority(attack, retrait, attack, retrait, attack, attack) ==> attack

L2: majority(attack, retrait, attack, retrait, attack, retrait) ==> retreat

L3: majority(attack, retrait, attack, retrait, attack, attack) ==> attack

L4: majority(attack, retrait, attack, retrait, attack, retrait) ==> retreat

L5: majority(attack, retrait, attack, retrait, attack, attack) ==> attack

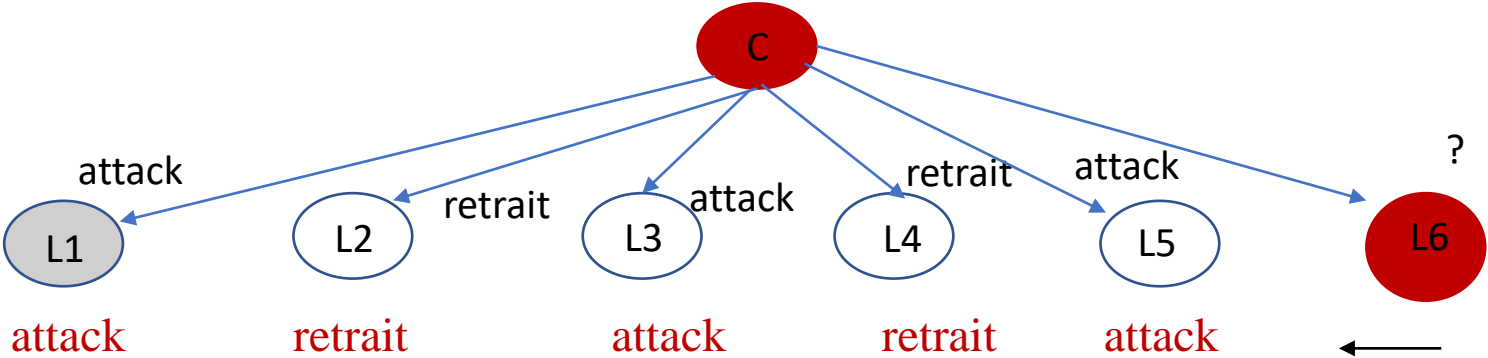
Loyal lieutenants do not choose the same action !!!

Important: what the other tell they have received by L6 !!!

Scenario: m=2, n=7, traitors=C, L6

Additional round:

Majority: what received by Li and what the other tell they have received by Li



Node Li

Round 0: C **attack**

Round 1: L2 retrait , L3 attack, L4 retrait, L5 attack , L6 attack (doesn't know 6 is traitor)

Round 2:

L2 {	L3 attack, L4 retrait, L5 attack ,	L6 retrait}
L3 {L2 retrait,	L4 retrait, L5 attack, L6 attack}	
L4 {L2 retrait, L3 attack,	L5 attack, L6 retrait}	
L5 {L2 retrait, L3 attack, L4 retrait,	L6 attack}	
L6 {L2 ? , L3 ? , L4 ? , L5 ?	}	

all see same messages from
L1, L2, L3, L4, and L5
L1, L2, L3, L4, L5 decide
attack

	majority	majority	majority	majority	majority	
	↓	↓	↓	↓	↓	
majority(attack ,	retrait,	attack,	retrait,	attack,	attack) ==> attack