## **Contents**

## 1 Basic

#### 1.1 .vimrc

```
syntax on
set nu ai bs=2 sw=2 et ve=all cb=unnamed mouse=a ruler
incsearch
```

## 2 Combinatorics

### 2.1 FFT

```
typedef complex<double> cpx;
const double PI = acos(-1);
vector<cpx> FFT(vector<cpx> &P, bool inv = 0) {
  assert(__builtin_popcount(P.size()) == 1);
  int lg = 31 - __builtin_clz(P.size()), n = 1 << lg;
// == P.size();</pre>
  for (int j = 1, i = 0; j < n - 1; ++j) {
  for (int k = n >> 1; k > (i ^= k); k >>= 1);
    if (j < i) swap(P[i], P[j]);</pre>
  } //bit reverse
  auto w1 = \exp((2 - 4 * inv) * PI / n * cpx(0, 1)); //
        order is 1<<lg
  for (int i = 1; i \le lg; ++i) {
    auto wn = pow(w1, 1<<(lg - i)); // order is 1<<i</pre>
    for (int k = 0; k < (1 << lg); k += 1 << i) {
      cpx base = 1;
      for (int j = 0; j < (1 << i - 1); ++j, base = base * wn) {
         auto t = base * P[k + j + (1 << i - 1)];
         auto u = P[k + j];
         P[k + j] = u + t;
         P[k + j + (1 \ll i - 1)] = u - t;
    }
  if(inv)
    for (int i = 0; i < n; ++i) P[i] /= n;
  return P;
} //faster performance with calling by reference
```

## 2.2 FWT

```
vector<int> fast_OR_transform(vector<int> f, bool
     inverse) {
   for (int i = 0; (2 << i) <= f.size(); ++i)
     for (int j = 0; j < f.size(); j += 2 << i)
  for (int k = 0; k < (1 << i); ++k)
    f[j + k + (1 << i)] += f[j + k] * (inverse? -1</pre>
                : 1);
  return f;
vector<int> rev(vector<int> A) {
  for (int i = 0; i < A.size(); i += 2) swap(A[i], A[i])</pre>
       ^ (A.size() - 1)]);
   return A;
vector<int> fast_AND_transform(vector<int> f, bool
      inverse) {
   return rev(fast_OR_transform(rev(f), inverse));
vector<int> fast_XOR_transform(vector<int> f, bool
     inverse) {
   for (int i = 0; (2 << i) <= f.size(); ++i)
     for (int j = 0; j < f.size(); j += 2 << i)
for (int k = 0; k < (1 << i); ++k) {</pre>
          int u = f[j + k], v = f[j + k + (1 << i)];

f[j + k + (1 << i)] = u - v, f[j + k] = u + v;
  if (inverse) for (auto &a : f) a /= f.size();
   return f;
```

#### 2.3 NTT

```
/* p == (a << n) + 1
         1 \ll n
                                          root
   n
                       97
   5
         32
                                    3
                       193
   6
         64
         128
                       257
                                          3
   8
         256
                       257
                                    1
                                          3
   9
         512
                       7681
                                    15
                                          17
   10
                       12289
                                    12
         1024
                                          11
   11
         2048
                       12289
                                          11
   12
         4096
                       12289
                                          11
   13
         8192
                       40961
                                          3
                       65537
   14
         16384
   15
         32768
                       65537
                                          3
   16
         65536
                       65537
                                    1
                                          3
   17
         131072
                       786433
                                    6
                                          10
                                          10 (605028353,
   18
         262144
                       786433
                                    3
        2308, 3)
   19
         524288
                       5767169
                                    11
                                          3
   20
         1048576
                       7340033
                                          3
         2097152
   21
                       23068673
                       104857601
   22
         4194304
                                          3
                                    25
                                          3
   23
         8388608
                       167772161
                                    20
   24
         16777216
                       167772161
                                    10
   25
         33554432
                       167772161
                                          3 (1107296257, 33,
        10)
   26
         67108864
                       469762049 7
                                          31 */
   27
         134217728
                       2013265921 15
LL root = 10, p = 786433, a = 3;
LL powM(LL x, LL b) {
  LL s = 1, m = x \% p;
  for (; b; m = m * m % p, b >>= 1)
    if (b\&1) s = s * m % p;
  return s;
vector<LL> NTT(vector<LL> P, bool inv = 0) {
  assert(__builtin_popcount(P.size()) == 1);
  int lg = 31 - __builtin_clz(P.size()), n = 1 << lg;</pre>
       // == P.size();
  for (int j = 1, i = 0; j < n - 1; ++j) {
  for (int k = n >> 1; k > (i ^= k); k >>= 1);
     if (j < i) swap(P[i], P[j]);</pre>
  } //bit reverse
  LL w1 = powM(root, a * (inv? p - 2: 1)); // order is
       1<<lg
  for (LL i = 1; i \le lg; ++i)
    LL wn = powM(w1, 1 << (lg - i)); // order is 1 << i
    for (int k = 0; k < (1 << lg); k += 1 << i) {
       LL base = 1;
       for (int j = 0; j < (1 << i - 1); ++j, base = base * wn % p) {
LL t = base * P[k + j + (1 << i - 1)] % p;
         LL u = P[k + j] \% p;
         P[k + j] = (u + t) \% p
         P[k + j + (1 \ll i - 1)] = (u - t + p) \% p;
       }
    }
  if(inv){
    LL invN = powM(n, p - 2);
    transform(P.begin(), P.end(), P.begin(), [&](LL a)
         {return a * invN % p;});
  return P:
} //faster performance with calling by reference
```

## 2.4 permanent

```
typedef vector<vector<LL> > mat;
LL permanent(mat A) {
   LL n = A.size(), ans = 0, *tmp = new LL[n], add;
   for (int pgray = 0, s = 1, gray, i; s < 1 << n; ++s)
      {
       gray = s ^ s >> 1, add = 1;
       i = __builtin_ctz(pgray ^ gray);
       for (int j = 0; j < n; ++j)
            add *= tmp[j] += A[i][j] * (gray>>i&1 ? 1 : -1);
       ans += add * (s&1^n&1? -1 : 1), pgray = gray;
```

## 3 Data Structure

## 3.1 Heavy Light Decomposition

```
struct HLD {
  using Tree = vector<vector<int>>>;
   vector<int> par, head, vid, len, inv;
  HLD(const Tree &g) : par(g.size()), head(g.size()),
    vid(g.size()), len(g.size()), inv(g.size()) {
     int k = 0;
     vector<int> size(g.size(), 1);
     function<void(int, int)> dfs_size = [&](int u, int
       for (int v : g[u]) {
         if (v != p) {
           dfs_size(v, u);
            size[u] += size[v];
       }
     };
     function<void(int, int, int)> dfs_dcmp = [&](int u,
           int p, int h) {
       par[u] = p;
       head[u] = h;
       vid[u] = k++;
       inv[vid[u]] = u;
       for (int v : g[u]) {
         if (v != p && size[u] < size[v] * 2) {</pre>
            dfs_dcmp(v, u, h);
         }
       for (int v : g[u]) {
         if (v != p && size[u] >= size[v] * 2) {
           dfs_dcmp(v, u, v);
       }
     dfs_size(0, -1);
     dfs_dcmp(0, -1, 0);
for (int i = 0; i < g.size(); ++i) {</pre>
       ++len[head[i]];
   template<typename T>
   void foreach(int u, int v, T f) {
     while (true) {
       if (vid[u] > vid[v])
         if (head[u] == head[v])
            f(vid[v] + 1, vid[u], 0);
           break
            f(vid[head[u]], vid[u], 1);
            u = par[head[u]];
       } else {
         if (head[u] == head[v]) +
            f(vid[u] + 1, vid[v], 0);
           break;
         } else
            f(vid[head[v]], vid[v], 0);
            v = par[head[v]];
       }
    }
  }
|};
```

## 4 Flow

## 4.1 CostFlow

```
template <class TF, class TC>
struct CostFlow {
   static const int MAXV = 205;
   static const TC INF = 0x3f3f3f3f3f;
   struct Edge {
     int v, r;
     TF f;
     TC c;
     Edge(int _v, int _r, TF _f, TC _c) : v(_v), r(_r), f(_f), c(_c) {}
  int n, s, t, pre[MAXV], pre_E[MAXV], inq[MAXV];
  TF fl;
  TC dis[MAXV], cost;
  vector<Edge> E[MAXV];
  CostFlow(int _n, int _s, int _t) : n(_n), s(_s), t(_t
     ), fl(0), cost(0) {}
  void add_edge(int u, int v, TF f, TC c) {
    E[u].emplace_back(v, E[v].size(), f, c);
    E[v].emplace_back(u, E[u].size() - 1, 0, -c);
  pair<TF, TC> flow() {
  while (true) {
    for (int i = 0; i < n; ++i) {</pre>
          dis[i] = INF;
          inq[i] = 0;
       dis[s] = 0;
       queue<int> que;
       que.emplace(s);
       while (not que.empty()) {
          int u = que.front();
          que.pop();
          inq[u] = 0;
          for (int i = 0; i < E[u].size(); ++i) {
  int v = E[u][i].v;</pre>
             TC w = E[\bar{u}][\bar{i}].c;
             if (E[u][i].f > 0 and dis[v] > dis[u] + w) {
               pre[v] = u;
               pre_E[v] = i;
               dis[v] = dis[u] + w;
if (not inq[v]) {
                  inq[v] = 1;
                  que.emplace(v);
            }
          }
        if (dis[t] == INF) break;
       TF tf = INF;
        for (int v = t, u, l; v != s; v = u) {
          u = pre[v];
          l = pre_E[v];
          tf = min(tf, E[u][l].f);
        for (int v = t, u, l; v != s; v = u) {
          u = pre[v];
          l = pre_E[v];
          E[u][l].f -= tf;
          E[v][E[u][l].r].f += tf;
        cost += tf * dis[t];
       fl += tf;
     return {fl, cost};
};
```

### 4.2 Dinic

```
template <class T>
struct Dinic {
  static const int MAXV = 10000;
  static const T INF = 0x3f3f3f3f3f;
```

```
struct Edge {
     int v;
     Tf;
     int re;
     Edge(int _v, T _f, int _re) : v(_v), f(_f), re(_re)
   int n, s, t, level[MAXV];
   vector<Edge> E[MAXV];
   int now[MAXV];
   Dinic(int _n, int _s, int _t) : n(_n), s(_s), t(_t)
       {}
   void add_edge(int u, int v, T f, bool bidirectional =
        false) {
     E[u].emplace_back(v, f, E[v].size());
     E[v].emplace_back(u, 0, E[u].size() - 1);
     if (bidirectional) {
       E[v].emplace_back(u, f, E[u].size() - 1);
   bool BFS() {
     memset(level, -1, sizeof(level));
     queue<int> que;
     que.emplace(s);
     level[s] = 0;
     while (not que.empty()) {
       int u = que.front();
       que.pop();
       for (auto it : E[u]) {
   if (it.f > 0 and level[it.v] == -1) {
     level[it.v] = level[u] + 1;
           que.emplace(it.v);
       }
     return level[t] != -1;
   T DFS(int u, T nf) {
     if (u == t) return nf;
     T res = 0;
     while (now[u] < E[u].size()) {</pre>
       Edge &it = E[u][now[u]];
if (it.f > 0 and level[it.v] == level[u] + 1) {
         T tf = DFS(it.v, min(nf, it.f));
         res += tf;
         nf -= tf;
         it.f -= tf;
         E[it.v][it.re].f += tf;
         if (nf == 0) return res;
       } else
         ++now[u];
     if (not res) level[u] = -1;
     return res;
   T flow(T res = 0) {
     while (BFS()) {
       T temp;
       memset(now, 0, sizeof(now))
       while (temp = DFS(s, INF)) {
         res += temp;
         res = min(res, INF);
       }
     }
     return res;
|};
      Geometry
```

## 5.1 Line and points

```
namespace kika {
  using cod = complex<double>;
  const double EPS = 1e-9;
  const double PI = acos(-1);
```

```
int dcmp(double x) {
  if (abs(x) < EPS) return 0;
  return x > 0 ? 1 : -1;
bool less(cod a, cod b) {
  return real(a) < real(b) || real(a) == real(b) &&</pre>
      imag(a) < imag(b);
bool more(cod a, cod b) {
  return real(a) > real(b) || real(a) == real(b) &&
      imag(a) > imag(b);
double dot(cod a, cod b) {
  return real(conj(a) * b);
double cross(cod a, cod b) {
  return imag(conj(a) * b);
int ori(cod b, cod a, cod c) {
  return dcmp(cross(a - b, c - b));
double angle(cod a, cod b) {
  return acos(dot(a, b) / abs(a) / abs(b));
double sarea(cod a, cod b, cod c) {
  return cross(b - a, c - a);
cod rotate(cod a, double rad) {
  return a * cod(cos(rad), sin(rad));
cod normal(cod a) {
  return cod(-imag(a) / abs(a), real(a) / abs(a));
cod get_line_intersection(cod p, cod v, cod q, cod w)
      { // p and v are two points that decides a line
  cod u(p - q);
  double t = cross(w, u) / cross(v, w);
  return p + v * t;
double distance_to_line(cod p, cod a, cod b) {
  return abs(cross(b - a, p - a) / abs(b - a));
double distance_to_segment(cod p, cod a, cod b) {
  if (a == b) return abs(p - a);
  cod v1(b - a), v2(p - a), v3(p - b);
  if (dcmp(dot(v1, v2)) < 0) return abs(v2);</pre>
  else if (dcmp(dot(v1, v3)) > 0) return abs(v3);
  return abs(cross(v1, v2)) / abs(v1);
cod get_line_projection(cod p, cod a, cod b) {
  cod v(b - a);
  return a + dot(v, p - a) / dot(v, v) * v;
bool segment_proper_intersection(cod a1, cod a2, cod
    b1, cod b2) {
  double c1 = cross(a2 - a1, b1 - a1), c2 = cross(a2)
       - a1, b2 - a1)
  double c3 = cross(b2 - b1, a1 - b1), c4 = cross(b2)
       - b1, a2 - b1);
  return dcmp(c1) * dcmp(c2) < 0 && dcmp(c3) * dcmp(</pre>
      c4) < 0;
}
double polygon_area(vector<cod> p) {
  double area = 0;
  for (int i = 1; i < int(p.size()) - 1; ++i) {
    area += cross(p[i] - p[0], p[i + 1] - p[0]);
```

```
return area / 2:
   bool is_point_on_segment(cod p, cod a1, cod a2) {
     return dcmp(cross(a1 - p, a2 - p)) == 0 \&\& dcmp(dot
         (a1 - p, a2 - p)) < 0;
   int is_point_in_polygon(cod p, vector<cod> gon) {
     int wn = 0;
     int n = gon.size();
     for (int i = 0; i < n; ++i) {
       if (is_point_on_segment(p, gon[i], gon[(i + 1) %
           n])) return -1;
       int k = dcmp(cross(gon[(i + 1) % n] - gon[i], p -
            gon[i]))
       int d1 = dcmp(imag(gon[i]) - imag(p));
       int d2 = dcmp(imag(gon[(i + 1) % n] - imag(p)));
       wn += k > 0 \&\& d1 <= 0 \&\& d2 > 0;
       wn -= k < 0 \&\& d2 <= 0 \&\& d1 > 0;
     return wn != 0;
   vector<cod> convex_hull(vector<cod> p) {
     sort(p.begin(), p.end(), less);
p.erase(unique(p.begin(), p.end()), p.end());
     int n = p.size(), m = 0;
     vector<cod> ch(n + 1);
     for (int i = 0; i < n; ++i) { // note that border
         is cleared
       while (m > 1 \&\& dcmp(cross(ch[m - 1] - ch[m - 2],
            p[i] - ch[m - 2])) <= 0) {
         --m;
       ch[m++] = p[i];
     for (int i = n - 2, k = m; i >= 0; --i) {
       while (m > k \&\& dcmp(cross(ch[m - 1] - ch[m - 2],
            p[i] - ch[m - 2])) <= 0) {
       ch[m++] = p[i];
     ch.erase(ch.begin() + m - (n > 1), ch.end());
     return ch;
};
```

# 6 Graph

#### 6.1 2-SAT

```
#include <cstdio>
#include <vector>
#include <stack>
#include <cstring>
using namespace std;
const int N = 2010;
struct two_SAT {
  int n;
  vector<int> G[N], revG[N];
  stack<int> finish;
bool sol[N], visit[N];
  int cmp[N];
  void init(int _n) {
    n = _n;
    for (int i = 0; i < N; i++) {
       G[i].clear();
       revG[i].clear();
    }
  void add_edge(int u, int v) {
    // 2 * i -> i is True, 2 * i + 1 -> i is False
    G[u].push_back(v);
    G[v^1].push_back(u^1);
    revG[v].push_back(u);
```

```
revG[u^1].push_back(v^1);
   void dfs(int v) {
     visit[v] = true
     for ( auto i:G[v] ) {
       if ( !visit[i] ) dfs(i);
     finish.push(v);
  void revdfs(int v, int id) {
     visit[v] = true;
     for ( auto i:revG[v] ) {
       if ( !visit[i] ) revdfs(i,id);
     cmp[v] = id;
  if ( !visit[i] ) dfs(i);
     int id = 0;
     memset( visit, 0, sizeof(visit) );
while ( !finish.empty() ) {
  int v = finish.top(); finish.pop();
       if ( visit[v] ) continue;
       revdfs(v,++id);
     return id;
  bool solve() {
     scc();
     for (int i = 0; i < n; i++) {
  if ( cmp[2*i] == cmp[2*i+1] ) return 0;</pre>
       sol[i] = (cmp[2*i] > cmp[2*i+1]);
     return 1;
} sat;
int main() {
  // ( a or not b ) and ( b or c ) and ( not c or not a
  sat.init(3);
  sat.add_edge( 2*0+1, 2*1+1 );
sat.add_edge( 2*1+1, 2*2+0 );
sat.add_edge( 2*2+0, 2*0+1 );
printf("%d\n", sat.solve() );
  return 0;
}
```

### 6.2 maximal cliques

```
#include <bits/stdc++.h>
using namespace std;
const int N = 60;
typedef long long LL;
struct Bron_Kerbosch {
  int n, res;
  LL edge[N];
  void init(int _n) {
   n = _n;
    for (int i = 0; i <= n; i++) edge[i] = 0;
  void add_edge(int u, int v) {
    if ( u == v ) return;
    edge[u] l = 1LL \ll v;
    edge[v] l= 1LL \ll u;
  void go(LL R, LL P, LL X) {
    if ( P == 0 && X == 0 ) {
      res = max( res, __builtin_popcountll(R) ); //
          notice LL
      return;
           _builtin_popcountll(R) + __builtin_popcountll
    (P) <= res ) return;
for (int i = 0; i <= n; i++) {
```

```
LL v = 1LL << i;
if ( P & v ) {
         go( R | v, P & edge[i], X & edge[i] );
         P &= ~v;
         X \mid = v;
      }
    }
  int solve() {
    res = 0;
    go( 0LL, ( 1LL << (n+1) ) - 1, 0LL );
    return res;
   BronKerbosch1(R, P, X):
      if P and X are both empty:
         report R as a maximal clique
       for each vertex v in P:
         BronKerbosch1(R \square {v}, P \square N(v), X \square N(v))
         P := P \setminus \{v\}
         X := X \square \{v\}
} MaxClique;
int main() {
  MaxClique.init(6);
  MaxClique.add_edge(1,2);
  MaxClique.add_edge(1,5);
  MaxClique.add_edge(2,5);
  MaxClique.add_edge(4,5);
  MaxClique.add_edge(3,2);
  MaxClique.add_edge(4,6);
  MaxClique.add\_edge(3,4);
  cout << MaxClique.solve() << "\n";</pre>
  return 0;
```

## 6.3 Tarjan SCC

```
#include <cstdio>
#include <vector>
#include <stack>
#include <cstring>
using namespace std;
const int N = 10010;
struct Tarjan {
  int n:
  vector<int> G[N], revG[N];
  stack<int> finish;
  bool visit[N];
  int cmp[N];
  void init(int _n) {
    n = _n;
for (int i = 0; i <= n; i++) {</pre>
      G[i].clear();
      revG[i].clear();
    }
  }
  void add_edge(int u, int v) {
    G[u].push_back(v)
    revG[v].push_back(u);
  void dfs(int v) {
    visit[v] = true
    for ( auto i:G[v] ) {
      if ( !visit[i] ) dfs(i);
    finish.push(v);
  }
  void revdfs(int v, int id) {
    visit[v] = true;
    for ( auto i:revG[v] ) {
      if ( !visit[i] ) revdfs(i,id);
    cmp[v] = id;
  int solve() {
    memset( visit, 0, sizeof(visit) );
    for (int i = 0; i < n; i++) {
  if (!visit[i]) dfs(i);</pre>
```

```
}
int id = 0;
memset( visit, 0, sizeof(visit) );
while ( !finish.empty() ) {
    int v = finish.top(); finish.pop();
    if ( visit[v] ) continue;
    revdfs(v,++id);
}
return id;
}
} scc;
int main() {
    int V, E;
    scanf("%d %d", &V, &E);
    scc.init(V);
    for (int i = 0; i < E; i++) {
        int u, v;
        scanf("%d %d", &u, &v);
        scc.add_edge(u-1,v-1);
}
printf("%d\n", scc.solve() );
return 0;
}</pre>
```

## 7 Number Theory

## 7.1 basic

```
PLL exd_gcd(LL a, LL b) {
  if (a \% b == 0) return \{0, 1\};
  PLL T = exd_gcd(b, a % b);
return {T.second, T.first - a / b * T.second};
LL mul(LL x, LL y, LL mod) {
  LL ans = 0, m = x, s = 0, sgn = (x > 0) xor (y > 0)?
       -1: 1;
  for (x = abs(x), y = abs(y); y; y >>= 1, m <<= 1, m =
        m \ge mod? m - mod: m
  if (y&1) s += m, s = s >= mod? s - mod: s; return s * sgn;
LL dangerous_mul(LL a, LL b, LL mod){ // 10 times
    faster than the above in average, but could be
  prone to wrong answer (extreme low prob?)
return (a * b - (LL)((long double)a * b / mod) * mod)
        % mod;
LL powmod(LL x, LL p, LL mod) {
  LL s = 1, m = x \% \text{ mod};
  for (; p; m = mul(m, m, mod), p >>= 1)
    if (p&1) s = mul(s, m, mod);
  return s;
```

## 7.2 Chinese Remainder Theorem

# 7.3 Discrete Log

### 7.4 Lucas

### 7.5 Meissel-Lehmer PI

```
LL PI(LL m)
const int MAXM = 1000, MAXN = 650, UPBD = 10000000;
// 650 ~ PI(cbrt(1e11))
LL pi[UPBD] = {0}, phi[MAXM][MAXN];
vector<LL> primes;
void init() {
  fill(pi + 2, pi + UPBD, 1);
for (LL p = 2; p < UPBD; ++p)
    if (pi[p]) {
      for (LL N = p * p; N < UPBD; N += p)
        pi[N] = 0;
      primes.push_back(p);
  for (int i = 1; i < UPBD; ++i) pi[i] += pi[i - 1];
  for (int i = 0; i < MAXM; ++i)
    phi[i][0] = i;
  for (int i = 1; i < MAXM; ++i)
    for (int j = 1; j < MAXN; ++j)
      phi[i][j] = phi[i][j - 1] - phi[i / primes[j -
           1]][j - 1];
LL P_2(LL m, LL n) {
  LL ans = 0;
  for (LL i = n; primes[i] * primes[i] <= m and i <</pre>
      primes.size(); ++i)
    ans += PI(m / primes[i]) - i;
  return ans;
LL PHI(LL m, LL n) {
  if (m < MAXM and n < MAXN) return phi[m][n];</pre>
  if (n == 0) return m;
  LL p = primes[n - 1];
  if (m < UPBD) {
    if (m <= p) return 1;</pre>
    if (m <= p * p * p) return pi[m] - n + 1 + P_2(m, n</pre>
  return PHI(m, n - 1) - PHI(m / p, n - 1);
LL PI(LL m) {
  if (m < UPBD) return pi[m];</pre>
  LL y = cbrt(m) + 10, n = pi[y];
return PHI(m, n) + n - 1 - P_2(m, n);
```

|}

### 7.6 Miller Rabin with Pollard rho

```
// Miller_Rabin
LL abs(LL a) {return a > 0? a: -a;}
bool witness(LL a, LL n, LL u, int t) {
  LL x = modpow(a, u, n), nx;
  for (int i = 0; i < t; ++i, x = nx){
    nx = mul(x, x, n);
if (nx == 1 and x != 1 and x != n - 1) return 1;
  }
  return x != 1;
const LL wits[7] = {2, 325, 9375, 28178, 450775,
    9780504, 1795265022};
bool miller_rabin(LL n, int s = 7) {
  if (n < 2) return 0;
  if (n&1^1) return n == 2;
  LL u = n - 1, t = 0, a; // n == (u << t) + 1
  while (u&1^1) u >>= 1, ++t;
  while (s--)
    if (a = wits[s] % n and witness(a, n, u, t)) return
          0;
  return 1;
// Pollard_rho
LL f(LL x, LL n) {
  return mul(x, x, n) + 1;
LL pollard_rho(LL n) {
  if (n&1^1) return 2;
  while (true) {
    LL x = rand() % (n - 1) + 1, y = 2, d = 1;
    for (int sz = 2; d == 1; y = x, sz <<= 1)
for (int i = 0; i < sz and d <= 1; ++i)
    x = f(x, n), d = \_gcd(abs(x - y), n);
if (d and n - d) return d;
  }
```

## 7.7 Primitive Root

```
vector<LL> factor(LL N) {
  vector<LL> ans;
  for (LL p = 2, n = N; p * p <= n; ++p)
if (N % p == 0) {
      ans.push_back(p);
      while (N % p == 0) N /= p;
  if (N != 1) ans.push_back(N);
  return ans;
LL find_root(LL p) {
  LL ans = 1;
  for (auto q: factor(p - 1)) {
    LL a = rand() \% (p - 1) + 1, b = (p - 1) / q;
    while (powmod(a, b, p) == 1) a = rand() \% (p - 1) +
    while (b % q == 0) b /= q;
    ans = mul(ans, powmod(a, b, p), p);
  }
  return ans;
bool is_root(LL a, LL p) {
  for (auto q: factor(p - 1))
if (powmod(a, (p - 1) / q, p) == 1)
      return false;
  return true;
```