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1 Basic

1.1 .vimrc

```
syntax on
set nu ai bs=2 sw=2 ts=2 et ve=all cb=unnamed mouse=a
ruler incsearch hlsearch
```

2 Math

2.1 FFT

```
typedef complex<double> cpx;
const double PI = acos(-1);
vector<cpx> FFT(vector<cpx> &P, bool inv = 0) {
    assert(__builtin_popcount(P.size()) == 1);
    int lg = 31 - __builtin_clz(P.size()), n = 1 << lg;
    // == P.size();
    for (int j = 1, i = 0; j < n - 1; ++j) {
        for (int k = n >> 1; k > (i ^= k); k >= 1);
        if (j < i) swap(P[i], P[j]);
    } //bit reverse
    auto w1 = exp((2 - 4 * inv) * PI / n * cpx(0, 1)); //
    order is 1<<lg
    for (int i = 1; i <= lg; ++i) {
        auto wn = pow(w1, 1<<(lg - i)); // order is 1<<i
        for (int k = 0; k < (1<<lg); k += 1 << i) {
            cpx base = 1;
            for (int j = 0; j < (1 << i - 1); ++j, base =
                base * wn) {
                auto t = base * P[k + j + (1 << i - 1)];
                auto u = P[k + j];
                P[k + j] = u + t;
                P[k + j + (1 << i - 1)] = u - t;
            }
        }
    }
    if(inv)
        for (int i = 0; i < n; ++i) P[i] /= n;
    return P;
} //faster performance with calling by reference
```

2.2 FWT

```
vector<LL> fast_OR_transform(vector<LL> f, bool inverse
) {
    for (int i = 0; (2 << i) <= f.size(); ++i)
        for (int j = 0; j < f.size(); j += 2 << i)
            for (int k = 0; k < (1 << i); ++k)
                f[j + k + (1 << i)] += f[j + k] * (inverse? -1
                    : 1);
    return f;
}
vector<LL> rev(vector<LL> A) {
    for (int i = 0; i < A.size(); i += 2) swap(A[i], A[i
        ^ (A.size() - 1)]);
    return A;
}
vector<LL> fast_AND_transform(vector<LL> f, bool
    inverse) {
    return rev(fast_OR_transform(rev(f), inverse));
}
vector<LL> fast_XOR_transform(vector<LL> f, bool
    inverse) {
    for (int i = 0; (2 << i) <= f.size(); ++i)
        for (int j = 0; j < f.size(); j += 2 << i)
            for (int k = 0; k < (1 << i); ++k) {
                int u = f[j + k], v = f[j + k + (1 << i)];
                f[j + k + (1 << i)] = u - v, f[j + k] = u + v;
            }
    if (inverse) for (auto &a : f) a /= f.size();
    return f;
}
```

2.3 NTT

```

/* p == (a << n) + 1
n   1 << n   p       a       root
5   32       97       3       5
6   64       193      3       5
7   128      257      2       3
8   256      257      1       3
9   512      7681     15      17
10  1024     12289     12      11
11  2048     12289     6       11
12  4096     12289     3       11
13  8192     40961     5       3
14  16384    65537     4       3
15  32768    65537     2       3
16  65536    65537     1       3
17  131072   786433    6      10
18  262144   786433    3      10 (605028353,
    2308, 3)
19  524288   5767169   11      3
20  1048576  7340033    7       3
21  2097152  23068673   11      3
22  4194304  104857601  25      3
23  8388608  167772161  20      3
24  16777216 167772161  10      3
25  33554432 167772161  5       3 (1107296257, 33,
    10)
26  67108864 469762049  7       3
27  134217728 2013265921 15      31 */
LL root = 10, p = 786433, a = 3;
LL powM(LL x, LL b) {
    LL s = 1, m = x % p;
    for (; b; m = m * m % p, b >>= 1)
        if (b&1) s = s * m % p;
    return s;
}
vector<LL> NTT(vector<LL> P, bool inv = 0) {
    assert(__builtin_popcount(P.size()) == 1);
    int lg = 31 - __builtin_clz(P.size()), n = 1 << lg;
    // == P.size();
    for (int j = 1, i = 0; j < n - 1; ++j) {
        for (int k = n >> 1; k > (i ^ k); k >>= 1);
        if (j < i) swap(P[i], P[j]);
    } //bit reverse
    LL w1 = powM(root, a * (inv ? p - 2 : 1)); // order is
    1<<lg
    for (LL i = 1; i <= lg; ++i) {
        LL wn = powM(w1, 1<<(lg - i)); // order is 1<<i
        for (int k = 0; k < (1<<lg); k += 1 << i) {
            LL base = 1;
            for (int j = 0; j < (1 << i - 1); ++j, base =
                base * wn % p) {
                LL t = base * P[k + j + (1 << i - 1)] % p;
                LL u = P[k + j] % p;
                P[k + j] = (u + t) % p;
                P[k + j + (1 << i - 1)] = (u - t + p) % p;
            }
        }
    }
    if (inv) {
        LL invN = powM(n, p - 2);
        transform(P.begin(), P.end(), P.begin(), [&](LL a)
            {return a * invN % p;});
    }
    return P;
} //faster performance with calling by reference

```

2.4 Polynomail root

```

const double eps = 1e-12;
const double inf = 1e+12;
double a[10], x[10];
int n;
int sign(double x){return (x < -eps)?(-1):(x>eps);}
double f(double a[], int n, double x){
    double tmp=1,sum=0;
    for(int i=0;i<=n;i++){
        sum=sum+a[i]*tmp; tmp=tmp*x; }
    return sum;
}

```

```

}
double binary(double l,double r,double a[],int n){
    int sl=sign(f(a,n,l)),sr=sign(f(a,n,r));
    if(sl==0) return l; if(sr==0) return r;
    if(sl*sr>0) return inf;
    while(r-l>eps){
        double mid=(l+r)/2;
        int ss=sign(f(a,n,mid));
        if(ss==0) return mid;
        if(ss*sl>0) l=mid; else r=mid;
    }
    return l;
}
void solve(int n,double a[],double x[],int &nx){
    if(n==1){ x[1]=-a[0]/a[1]; nx=1; return; }
    double da[10], dx[10]; int ndx;
    for(int i=n;i>=1;i--) da[i-1]=a[i]*i;
    solve(n-1,da,dx,ndx);
    nx=0;
    if(ndx==0){
        double tmp=binary(-inf,inf,a,n);
        if (tmp<inf) x[++nx]=tmp;
        return;
    }
    double tmp;
    tmp=binary(-inf,dx[1],a,n);
    if(tmp<inf) x[++nx]=tmp;
    for(int i=1;i<=ndx-1;i++){
        tmp=binary(dx[i],dx[i+1],a,n);
        if(tmp<inf) x[++nx]=tmp;
    }
    tmp=binary(dx[ndx],inf,a,n);
    if(tmp<inf) x[++nx]=tmp;
}
int main() {
    scanf("%d",&n);
    for(int i=n;i>=0;i--) scanf("%lf",&a[i]);
    int nx;
    solve(n,a,x,nx);
    for(int i=1;i<=nx;i++) printf("%.6f\n",x[i]);
}

```

3 Number Theory

3.1 basic

```

PLL exd_gcd(LL a, LL b) {
    if (a % b == 0) return {0, 1};
    PLL T = exd_gcd(b, a % b);
    return {T.second, T.first - a / b * T.second};
}
LL powmod(LL x, LL p, LL mod) {
    LL s = 1, m = x % mod;
    for (; p; m = m * m % mod, p >>= 1)
        if (p&1) s = s * m % mod; // or consider int128
    return s;
}
LL LLMul(LL x, LL y, LL mod) {
    LL ans = 0, m = abs(x), s = 0, sgn = (x > 0) xor (y >
        0)? -1: 1;
    for (x = abs(x), y = abs(y); y; y >>= 1, m <= 1, m =
        m >= mod? m - mod: m)
        if (y&1) s += m, s = s >= mod? s - mod: s;
    return (s * sgn % mod + mod) % mod;
}
LL dangerous_mul(LL a, LL b, LL mod){ // 10 times
    faster than the above in average, but could be
    prone to wrong answer (extreme low prob?)
    return (a * b - (LL)((long double)a * b / mod) * mod)
        % mod;
}
vector<LL> linear_inv(LL p, int k) { // take k
    vector<LL> inv(min(p, 1ll + k));
    inv[1] = 1;
    for (int i = 2; i < inv.size(); ++i)
        inv[i] = (p - p / i) * inv[p % i] % p;
    return inv;
}

```

```

inline LL add(LL _x, LL _y, LL _mod = 1e9 + 7) {
    ll _ = _x + _y;
    if (_ >= _mod) _ -= _mod;
    if (_ < 0) _ += _mod;
    return _;
}
inline LL mul(LL _x, LL _y, LL _mod = 1e9 + 7) {
    ll _ = _x * _y;
    if (_ >= _mod) _ %= _mod;
    return _;
}

```

3.2 Chinese Remainder Theorem

```

PLL CRT(PLL eq1, PLL eq2) {
    LL m1, m2, x1, x2;
    tie(x1, m1) = eq1, tie(x2, m2) = eq2;
    LL g = __gcd(m1, m2);
    if ((x1 - x2) % g) return {-1, 0}; // NO SOLUTION
    m1 /= g, m2 /= g;
    auto p = exd_gcd(m1, m2);
    LL lcm = m1 * m2 * g, res = mul(mul(p.first, (x2 - x1
    ), lcm), m1, lcm) + x1;
    return {(res % lcm + lcm) % lcm, lcm};
}

```

3.3 Discrete Log

```

LL discrete_log(LL b, LL p, LL n) {
    map<LL, LL> att;
    LL m = sqrt((double)p) + 1, M = powmod(b, m * (p - 2)
    , p);
    for (LL cur = 1, i = 0; i < m; ++i, cur = cur * b % p)
        if (not att.count(cur)) att[cur] = i;
    for (LL cur = 1, i = 0; i * m < p - 1; ++i, cur = cur
    * M % p)
        if (att.count(n * cur % p))
            return (att[cur * n % p] + i * m) % (p - 1);
    return -1;
}
// find x s.t. b**x % p == n with complexity O(sqrt(N))
// return the smallest
// return -1 if ans doesn't exist

```

3.4 Lucas

```

LL fac[100000] = {1};
LL C(LL a, LL b, LL p) {
    for (int i = 1; i <= p; ++i) fac[i] = fac[i - 1] * i
    % p;
    LL ans = 1;
    for (; a; a /= p, b /= p) {
        LL A = a % p, B = b % p;
        if (A < B) return 0;
        (ans *= fac[A] * powmod(fac[B] * fac[A - B] % p, p
        - 2, p) % p) %= p;
    }
    return ans;
}

```

3.5 Meissel-Lehmer PI

```

LL PI(LL m);
const int MAXM = 1000, MAXN = 650, UPBD = 1000000;
// 650 ~ PI(cbrt(1e11))
LL pi[UPBD] = {0}, phi[MAXN][MAXN];
vector<LL> primes;
void init() {
    fill(pi + 2, pi + UPBD, 1);
    for (LL p = 2; p < UPBD; ++p)
        if (pi[p]) {
            for (LL N = p * p; N < UPBD; N += p)

```

```

                pi[N] = 0;
                primes.push_back(p);
            }
        }
        for (int i = 1; i < UPBD; ++i) pi[i] += pi[i - 1];
        for (int i = 0; i < MAXM; ++i)
            phi[i][0] = i;
        for (int i = 1; i < MAXM; ++i)
            for (int j = 1; j < MAXN; ++j)
                phi[i][j] = phi[i][j - 1] - phi[i / primes[j -
                1]][j - 1];
    }
    LL P_2(LL m, LL n) {
        LL ans = 0;
        for (LL i = n; primes[i] * primes[i] <= m and i <
        primes.size(); ++i)
            ans += PI(m / primes[i]) - i;
        return ans;
    }
    LL PHI(LL m, LL n) {
        if (m < MAXM and n < MAXN) return phi[m][n];
        if (n == 0) return m;
        LL p = primes[n - 1];
        if (m < UPBD) {
            if (m <= p) return 1;
            if (m <= p * p * p) return pi[m] - n + 1 + P_2(m, n
            );
        }
        return PHI(m, n - 1) - PHI(m / p, n - 1);
    }
    LL PI(LL m) {
        if (m < UPBD) return pi[m];
        LL y = cbrt(m) + 10, n = pi[y];
        return PHI(m, n) + n - 1 - P_2(m, n);
    }
}

```

3.6 Miller Rabin with Pollard rho

```

// Miller_Rabin
LL abs(LL a) {return a > 0? a: -a;}
bool witness(LL a, LL n, LL u, int t) {
    LL x = modpow(a, u, n), nx;
    for (int i = 0; i < t; ++i, x = nx){
        nx = mul(x, x, n);
        if (nx == 1 and x != 1 and x != n - 1) return 1;
    }
    return x != 1;
}
const LL wits[7] = {2, 325, 9375, 28178, 450775,
    9780504, 1795265022};
bool miller_rabin(LL n, int s = 7) {
    if (n < 2) return 0;
    if (n & 1) return n == 2;
    LL u = n - 1, t = 0, a; // n == (u << t) + 1
    while (u & 1) u >>= 1, ++t;
    while (s--)
        if (a = wits[s] % n and witness(a, n, u, t)) return
        0;
    return 1;
}
// Pollard_rho
LL f(LL x, LL n) {
    return mul(x, x, n) + 1;
}
LL pollard_rho(LL n) {
    if (n & 1) return 2;
    while (true) {
        LL x = rand() % (n - 1) + 1, y = 2, d = 1;
        for (int sz = 2; d == 1; y = x, sz <= 1)
            for (int i = 0; i < sz and d == 1; ++i)
                x = f(x, n), d = __gcd(abs(x - y), n);
        if (d and n - d) return d;
    }
}

```

3.7 Primitive Root

```

vector<LL> factor(LL N) {
    vector<LL> ans;

```

```

for (LL p = 2, n = N; p * p <= n; ++p)
    if (N % p == 0) {
        ans.push_back(p);
        while (N % p == 0) N /= p;
    }
if (N != 1) ans.push_back(N);
return ans;
}
LL find_root(LL p) {
    LL ans = 1;
    for (auto q: factor(p - 1)) {
        LL a = rand() % (p - 1) + 1, b = (p - 1) / q;
        while (powmod(a, b, p) == 1) a = rand() % (p - 1) + 1;
        while (b % q == 0) b /= q;
        ans = mul(ans, powmod(a, b, p), p);
    }
    return ans;
}
bool is_root(LL a, LL p) {
    for (auto q: factor(p - 1))
        if (powmod(a, (p - 1) / q, p) == 1)
            return false;
    return true;
}
}

```

4 Data Structure

4.1 Disjoint Set

```

struct DisjointSet{
    // save() is like recursive
    // undo() is like return
    int n, compo;
    vector<int> fa, sz;
    vector<pair<int*,int>> h;
    vector<int> sp;
    void init(int tn) {
        compo = n = tn, sz.assign(n, 1), fa.resize(n);
        for (int i = 0; i < n; ++i)
            fa[i] = i, sz[i] = 1;
        sp.clear(); h.clear();
    }
    void assign(int *k, int v) {
        h.push_back({k, *k});
        *k = v;
    }
    void save() { sp.push_back(h.size()); }
    void undo() {
        assert(!sp.empty());
        int last = sp.back(); sp.pop_back();
        while (h.size() != last) {
            auto x = h.back(); h.pop_back();
            *x.first = x.second;
        }
    }
    int f(int x) {
        while (fa[x] != x) x = fa[x];
        return x;
    }
    bool uni(int x, int y) {
        x = f(x), y = f(y);
        if (x == y) return false;
        if (sz[x] < sz[y]) swap(x, y);
        assign(&sz[x], sz[x] + sz[y]);
        assign(&fa[y], x);
        --compo;
        return true;
    }
}
}djs;

```

4.2 KDTree

```

#include <bits/stdc++.h>
using namespace std;

```

```

struct KNode {
    vector<int> v;
    KNode *lc, *rc;
    KNode(const vector<int> &_v) : v(_v), lc(nullptr),
        rc(nullptr) {}
    static KNode *buildKDTree(vector<vector<int>> &pnts,
        int lb, int rb, int dpt) {
        if (rb - lb < 1) return nullptr;
        int axis = dpt % pnts[0].size();
        int mb = lb + rb >> 1;
        nth_element(pnts.begin() + lb, pnts.begin() + mb,
            pnts.begin() + rb, [&](const vector<int> &a,
                const vector<int> &b) {
                    return a[axis] < b[axis];
                });
        KNode *t = new KNode(pnts[mb]);
        t->lc = buildKDTree(pnts, lb, mb, dpt + 1);
        t->rc = buildKDTree(pnts, mb + 1, rb, dpt + 1);
        return t;
    }
    static void release(KNode *t) {
        if (t->lc) release(t->lc);
        if (t->rc) release(t->rc);
        delete t;
    }
    static void searchNearestNode(KNode *t, KNode *q,
        KNode *&c, int dpt) {
        int axis = dpt % t->v.size();
        if (t->v != q->v && (c == nullptr || dis(q, t) <
            dis(q, c))) c = t;
        if (t->lc && (!t->rc || q->v[axis] < t->v[axis])) {
            searchNearestNode(t->lc, q, c, dpt + 1);
            if (t->rc && (c == nullptr || 1LL * (t->v[axis] -
                q->v[axis]) * (t->v[axis] - q->v[axis]) <
                    dis(q, c))) {
                searchNearestNode(t->rc, q, c, dpt + 1);
            }
        } else if (t->rc) {
            searchNearestNode(t->rc, q, c, dpt + 1);
            if (t->lc && (c == nullptr || 1LL * (t->v[axis] -
                q->v[axis]) * (t->v[axis] - q->v[axis]) <
                    dis(q, c))) {
                searchNearestNode(t->lc, q, c, dpt + 1);
            }
        }
    }
    static int64_t dis(KNode *a, KNode *b) {
        int64_t r = 0;
        for (int i = 0; i < a->v.size(); ++i) {
            r += 1LL * (a->v[i] - b->v[i]) * (a->v[i] - b->v[
                i]);
        }
        return r;
    }
};

signed main() {
    ios::sync_with_stdio(false);
    int T;
    cin >> T;
    for (int ti = 0; ti < T; ++ti) {
        int N;
        cin >> N;
        vector<vector<int>> pnts(N, vector<int>(2));
        for (int i = 0; i < N; ++i) {
            for (int j = 0; j < 2; ++j) {
                cin >> pnts[i][j];
            }
        }
        vector<vector<int>> _pnts = pnts;
        KNode *root = KNode::buildKDTree(_pnts, 0, pnts.
            size(), 0);
        for (int i = 0; i < N; ++i) {
            KNode *q = new KNode(pnts[i]);
            KNode *c = nullptr;
            KNode::searchNearestNode(root, q, c, 0);
            cout << KNode::dis(c, q) << endl;
            delete q;
        }
        KNode::release(root);
    }
    return 0;
}

```

|}

4.3 BIT

4.4 RMQ

5 Flow

5.1 CostFlow

```

template <class TF, class TC>
struct CostFlow {
    static const int MAXV = 205;
    static const TC INF = 0x3f3f3f3f;
    struct Edge {
        int v, r;
        TF f;
        TC c;
        Edge(int _v, int _r, TF _f, TC _c) : v(_v), r(_r),
            f(_f), c(_c) {}
    };
    int n, s, t, pre[MAXV], pre_E[MAXV], inq[MAXV];
    TF fl;
    TC dis[MAXV], cost;
    vector<Edge> E[MAXV];
    CostFlow(int _n, int _s, int _t) : n(_n), s(_s), t(_t)
        , fl(0), cost(0) {}
    void add_edge(int u, int v, TF f, TC c) {
        E[u].emplace_back(v, E[v].size(), f, c);
        E[v].emplace_back(u, E[u].size() - 1, 0, -c);
    }
    pair<TF, TC> flow() {
        while (true) {
            for (int i = 0; i < n; ++i) {
                dis[i] = INF;
                inq[i] = 0;
            }
            dis[s] = 0;
            queue<int> que;
            que.emplace(s);
            while (not que.empty()) {
                int u = que.front();
                que.pop();
                inq[u] = 0;
                for (int i = 0; i < E[u].size(); ++i) {
                    int v = E[u][i].v;
                    TC w = E[u][i].c;
                    if (E[u][i].f > 0 and dis[v] > dis[u] + w) {
                        pre[v] = u;
                        pre_E[v] = i;
                        dis[v] = dis[u] + w;
                        if (not inq[v]) {
                            inq[v] = 1;
                            que.emplace(v);
                        }
                    }
                }
            }
            if (dis[t] == INF) break;
            TF tf = INF;
            for (int v = t, u, l; v != s; v = u) {
                u = pre[v];
                l = pre_E[v];
                tf = min(tf, E[u][l].f);
            }
            for (int v = t, u, l; v != s; v = u) {
                u = pre[v];
                l = pre_E[v];
                E[u][l].f -= tf;
                E[v][E[u][l].r].f += tf;
            }
            cost += tf * dis[t];
            fl += tf;
        }
        return {fl, cost};
    }
};

```

5.2 MaxFlow

```

template <class T>
struct Dinic {
    static const int MAXV = 10000;
    static const T INF = 0x3f3f3f3f;
    struct Edge {
        int v;
        T f;
        int re;
        Edge(int _v, T _f, int _re) : v(_v), f(_f), re(_re)
            {}
    };
    int n, s, t, level[MAXV];
    vector<Edge> E[MAXV];
    int now[MAXV];
    Dinic(int _n, int _s, int _t) : n(_n), s(_s), t(_t)
        {}
    void add_edge(int u, int v, T f, bool bidirectional =
        false) {
        E[u].emplace_back(v, f, E[v].size());
        E[v].emplace_back(u, 0, E[u].size() - 1);
        if (bidirectional) {
            E[v].emplace_back(u, f, E[u].size() - 1);
        }
    }
    bool BFS() {
        memset(level, -1, sizeof(level));
        queue<int> que;
        que.emplace(s);
        level[s] = 0;
        while (not que.empty()) {
            int u = que.front();
            que.pop();
            for (auto it : E[u]) {
                if (it.f > 0 and level[it.v] == -1) {
                    level[it.v] = level[u] + 1;
                    que.emplace(it.v);
                }
            }
        }
        return level[t] != -1;
    }
    T DFS(int u, T nf) {
        if (u == t) return nf;
        T res = 0;
        while (now[u] < E[u].size()) {
            Edge &it = E[u][now[u]];
            if (it.f > 0 and level[it.v] == level[u] + 1) {
                T tf = DFS(it.v, min(nf, it.f));
                res += tf;
                nf -= tf;
                it.f -= tf;
                E[it.v][it.re].f += tf;
                if (nf == 0) return res;
            }
            ++now[u];
        }
        if (not res) level[u] = -1;
        return res;
    }
    T flow(T res = 0) {
        while (BFS()) {
            T temp;
            memset(now, 0, sizeof(now));
            while (temp = DFS(s, INF)) {
                res += temp;
            }
        }
        return res;
    }
};

```

5.3 KM matching

```

const int MAXN = 1000;
template <class TC>
struct KM_matching { // if there's no edge, the weight
    is 0

```

```
// complexity: O(n^3), support for negative edge
int n, matchy[MAXN];
bool visx[MAXN], visy[MAXN];
TC adj[MAXN][MAXN], coverx[MAXN], covery[MAXN], slack
    [MAXN];
KM_matching(int _n) : n(_n) {
    memset(matchy, -1, sizeof(matchy));
    memset(coverx, 0, sizeof(coverx));
    memset(adj, 0, sizeof(adj));
}
void add_edge(int x, int y, TC w) { adj[x][y] = w; }
bool aug(int u) {
    visx[u] = true;
    for (int v = 0; v < n; ++v)
        if (not visy[v]) {
            TC t = coverx[u] + covery[v] - adj[u][v];
            if (t == 0) { // The edge is in Equality
                subgraph
                visy[v] = true;
                if (matchy[v] == -1 or aug(matchy[v]))
                    return matchy[v] = u, true;
            }
            else if (slack[v] > t) slack[v] = t;
        }
    return false;
}
TC solve() {
    for (int u = 0; u < n; ++u)
        coverx[u] = *max_element(adj[u], adj[u] + n);
    for (int u = 0; u < n; ++u) {
        fill(slack, slack + n, INT_MAX);
        while (memset(visx, 0, sizeof(visx)),
                memset(visy, 0, sizeof(visy)),
                not aug(u)) {
            TC d = INT_MAX;
            for (int v = 0; v < n; ++v)
                if (not visy[v]) d = min(d, slack[v]);
            for (int v = 0; v < n; ++v) {
                if (visx[v]) coverx[v] -= d;
                if (visy[v]) covery[v] += d;
            }
        }
    }
    return accumulate(coverx, coverx + n, (TC)0) +
        accumulate(covery, covery + n, (TC)0);
}
};
```

5.4 Matching

```
class matching {
public:
    vector< vector<int> > g;
    vector<int> pa, pb, was;
    int n, m, res, iter;

    matching(int _n, int _m) : n(_n), m(_m) {
        assert(0 <= n && 0 <= m);
        pa = vector<int>(n, -1);
        pb = vector<int>(m, -1);
        was = vector<int>(n, 0);
        g.resize(n);
        res = 0, iter = 0;
    }

    void add_edge(int from, int to) {
        assert(0 <= from && from < n && 0 <= to && to < m);
        g[from].push_back(to);
    }

    bool dfs(int v) {
        was[v] = iter;
        for (int u : g[v])
            if (pb[u] == -1)
                return pa[v] = u, pb[u] = v, true;
        for (int u : g[v])
            if (was[pb[u]] != iter && dfs(pb[u]))
                return pa[v] = u, pb[u] = v, true;
        return false;
    }
};
```

```
int solve() {
    while (true) {
        iter++;
        int add = 0;
        for (int i = 0; i < n; i++)
            if (pa[i] == -1 && dfs(i))
                add++;
        if (add == 0) break;
        res += add;
    }
    return res;
}

int run_one(int v) {
    if (pa[v] != -1) return 0;
    iter++;
    return (int) dfs(v);
}

pair<vector<bool>, vector<bool>> vertex_cover() {
    solve();
    vector<bool> a_cover(n, true), b_cover(m, false);
    function<void(int)> dfs_aug = [&](int v) {
        a_cover[v] = false;
        for (int u : g[v])
            if (not b_cover[u])
                b_cover[u] = true, dfs_aug(pb[u]);
    };
    for (int v = 0; v < n; ++v)
        if (a_cover[v] and pa[v] == -1)
            dfs_aug(v);
    return {a_cover, b_cover};
}
};
```

6 Geometry

6.1 2D Geometry

```
namespace geo {
    using pt = complex<double>;
    using cir = pair<pt, double>;
    using poly = vector<pt>;
    using line = pair<pt, pt>; // point to point
    using plane = pair<pt, pt>;
    pt get_pt() { static double a, b; cin >> a >> b;
        return geo::pt(a, b); };
    const double EPS = 1e-10;
    const double PI = acos(-1);
    pt cent(cir C) { return C.first; }
    double radi(cir C) { return C.second; }
    pt st(line H) { return H.first; }
    pt ed(line H) { return H.second; }
    pt vec(line H) { return ed(H) - st(H); }
    int dcmp(double x) { return abs(x) < EPS ? 0 : x > 0
        ? 1 : -1; }
    bool less(pt a, pt b) { return real(a) < real(b) ||
        real(a) == real(b) && imag(a) < imag(b); }
    bool more(pt a, pt b) { return real(a) > real(b) ||
        real(a) == real(b) && imag(a) > imag(b); }
    double dot(pt a, pt b) { return real(conj(a) * b); }
    double cross(pt a, pt b) { return imag(conj(a) * b); }
    double sarea(pt a, pt b, pt c) { return cross(b - a,
        c - a); }
    double area(cir c) { return radi(c) * radi(c) * PI; }
    int ori(pt a, pt b, pt c) { return dcmp(sarea(a, b, c)); }
    double angle(pt a, pt b) { return acos(dot(a, b) /
        abs(a) / abs(b)); }
    pt rotate(pt a, double rad) { return a * pt(cos(rad),
        sin(rad)); }
    pt normal(pt a) { return pt(-imag(a), real(a)) / abs(a); }
    pt normalized(pt a) { return a / abs(a); }

    pt get_line_intersection(line A, line B) {
        pt p = st(A), v = vec(A), q = st(B), w = vec(B);
```



```

    return p + v * cross(w, p - q) / cross(v, w);
}
double distance_to_line(pt p, line B) {
    return abs(cross(vec(B), p - st(B)) / abs(vec(B)));
}
double distance_to_segment(pt p, line B) {
    pt a = st(B), b = ed(B), v1(vec(B)), v2(p - a), v3(
        p - b);
    // similar to previous function
    if (a == b) return abs(p - a);
    if (dcmp(dot(v1, v2)) < 0) return abs(v2);
    else if (dcmp(dot(v1, v3)) > 0) return abs(v3);
    return abs(cross(v1, v2)) / abs(v1);
}
pt get_line_projection(pt p, line(B)) {
    pt v = vec(B);
    return st(B) + dot(v, p - st(B)) / dot(v, v) * v;
}
bool is_segment_proper_intersection(line A, line B) {
    pt a1 = st(A), a2 = ed(A), b1 = st(B), b2 = ed(B);
    double det1 = ori(a1, a2, b1) * ori(a1, a2, b2);
    double det2 = ori(b1, b2, a1) * ori(b1, b2, a2);
    return det1 < 0 && det2 < 0;
}
double area(poly p) {
    if (p.size() < 3) return 0;
    double area = 0;
    for (int i = 1; i < p.size() - 1; ++i)
        area += sarea(p[0], p[i], p[i + 1]);
    return area / 2;
}
bool is_point_on_segment(pt p, line B) {
    pt a = st(B), b = ed(B);
    return dcmp(sarea(p, a, b)) == 0 && dcmp(dot(a - p,
        b - p)) < 0;
}
bool is_point_in_plane(pt p, line H) {
    return ori(st(H), ed(H), p) > 0;
}
bool is_point_in_polygon(pt p, poly gon) {
    int wn = 0;
    int n = gon.size();
    for (int i = 0; i < n; ++i) {
        if (is_point_on_segment(p, {gon[i], gon[(i + 1) %
            n]})) return true;
        if (not is_point_in_plane(p, {gon[i], gon[(i + 1)
            % n]})) return false;
    }
    return true;
}
poly convex_hull(vector<pt> p) {
    sort(p.begin(), p.end(), less);
    p.erase(unique(p.begin(), p.end()), p.end());
    int n = p.size(), m = 0;
    poly ch(n + 1);
    for (int i = 0; i < n; ++i) { // note that border
        is cleared
        while (m > 1 && ori(ch[m - 2], ch[m - 1], p[i])
            <= 0) --m;
        ch[m++] = p[i];
    }
    for (int i = n - 2, k = m; i >= 0; --i) {
        while (m > k && ori(ch[m - 2], ch[m - 1], p[i])
            <= 0) --m;
        ch[m++] = p[i];
    }
    ch.erase(ch.begin() + m - (n > 1), ch.end());
    return ch;
}
cir circumscribed_circle(poly tri) {
    pt B = tri[1] - tri[0];
    pt C = tri[2] - tri[0];
    double det = 2 * cross(B, C);
    pt r = pt(imag(C) * norm(B) - imag(B) * norm(C),
        real(B) * norm(C) - real(C) * norm(B)) /
        det;
    return {r + tri[0], abs(r)};
}
cir inscribed_circle(poly tri) {
    assert(tri.size() == 3);
    pt ans = 0;
    double div = 0;

```

```

    for (int i = 0; i < 3; ++i) {
        double l = abs(tri[(i + 1) % 3] - tri[(i + 2) %
            3]);
        ans += l * tri[i], div += l;
    }
    ans /= div;
    return {ans, distance_to_line(ans, {tri[0], tri
        [1]})};
}
poly tangent_line_through_point(cir c, pt p) {
    if (dcmp(abs(cent(c) - p) - radi(c)) < 0) return
        {};
    else if (dcmp(abs(cent(c) - p) - radi(c)) == 0)
        return {p};
    double theta = acos(radi(c) / abs(cent(c) - p));
    pt norm_v = normalized(p - cent(c));
    return {cent(c) + radi(c) * rotate(norm_v, +theta),
        cent(c) + radi(c) * rotate(norm_v, -theta)
        };
}
vector<pt> get_line_circle_intersection(cir d, line B
    ) {
    pt v = vec(B), p = st(B) - cent(d);
    double r = radi(d), a = norm(v), b = 2 * dot(p, v),
        c = norm(p) - r * r;
    double det = b * b - 4 * a * c;
    // t^2 * norm(v) + 2 * t * dot(p, v) + norm(p) - r
        * r = 0
    auto get_point = [=](double t) { return st(B) + t *
        v; };
    if (dcmp(det) < 0) return {};
    if (dcmp(det) == 0) return {get_point(-b / 2 / a)};
    return {get_point((-b + sqrt(det)) / 2 / a),
        get_point((-b - sqrt(det)) / 2 / a)};
}
vector<pt> get_circle_circle_intersection(cir c, cir
    d) {
    pt a = cent(c), b = cent(d);
    double r = radi(c), s = radi(d), g = abs(a - b);
    if (dcmp(g) == 0) return {}; // may be C == D
    if (dcmp(r + s - g) < 0 or dcmp(abs(r - s) - g) >
        0) return {};
    pt C_to_D = normalized(b - a);
    double theta = acos((r * r + g * g - s * s) / (2 *
        r * g));
    if (dcmp(theta) == 0) return {a + r * C_to_D};
    else return {a + rotate(r * C_to_D, theta), a +
        rotate(r * C_to_D, -theta)};
}
cir min_circle_cover(vector<pt> A) {
    random_shuffle(A.begin(), A.end());
    cir ans = {0, 0};
    auto is_incir = [&](pt a) { return dcmp(abs(cent(
        ans) - a) - radi(ans)) < 0; };
    for (int i = 0; i < A.size(); ++i) if (not is_incir
        (A[i])) {
        ans = {A[i], 0};
        for (int j = 0; j < i; ++j) if (not is_incir(A[j]
            )) {
            ans = {(A[i] + A[j]) / 2., abs(A[i] - A[j]) /
                2};
            for (int k = 0; k < j; ++k) if (not is_incir(A[
                k]))
                ans = circumscribed_circle({A[i], A[j], A[k]
                    });
        }
    }
    return ans;
}
poly half_plane_intersection(vector<plane> A) {
    const double INF = 1e19;
    sort(A.begin(), A.end(), [=](plane a, plane b) {
        int res = dcmp(arg(vec(a)) - arg(vec(b)));
        return res == 0 ? is_point_in_plane(st(a), b) :
            res < 0;
    });
    deque<pt> ans;
    deque<plane> q;
    q.push_back(A[0]);
    for (int i = 1; i < A.size(); ++i) {
        if (dcmp(cross(vec(A[i]), vec(A[i - 1]))) == 0)
            continue;
    }

```

```

while (ans.size() and not is_point_in_plane(ans.
    back(), A[i]))
    q.pop_back(), ans.pop_back();
while (ans.size() and not is_point_in_plane(ans.
    front(), A[i]))
    q.pop_front(), ans.pop_front();
ans.push_back(get_line_intersection(A[i], q.back()
    ));
q.push_back(A[i]);
}
while (ans.size() and not is_point_in_plane(ans.
    back(), q.front()))
    ans.pop_back(), q.pop_back();
while (ans.size() and not is_point_in_plane(ans.
    front(), q.back()))
    ans.pop_front(), q.pop_front();
if (q.size() < 3) return {};
ans.push_back(get_line_intersection(q.back(), q.
    front()));
return poly(ans.begin(), ans.end());
}
pair<pt, pt> closest_pair(vector<pt> &V, int l, int r
    ) { // l = 0, r = V.size()
    pair<pt, pt> ret = {pt(-1e18), pt(1e18)};
    const auto upd = [&](pair<pt, pt> a) {
        if (abs(a.first - a.second) < abs(ret.first - ret
            .second)) ret = a;
    };
    if (r - l < 40) { // GOD's number! It performs well
        !
        for (int i = l; i < r; ++i) for (int j = l; j < i
            ; ++j)
            upd({V[i], V[j]});
        return ret;
    }
    int m = l + r >> 1;
    const auto cmpy = [](pt a, pt b) { return imag(a) <
        imag(b); };
    const auto cmpx = [](pt a, pt b) { return real(a) <
        real(b); };
    nth_element(V.begin() + l, V.begin() + m, V.begin()
        + r, cmpx);
    pt mid = V[m];
    upd(closest_pair(V, l, m));
    upd(closest_pair(V, m, r));
    double delta = abs(ret.first - ret.second);
    vector<pt> spine;
    for (int k = l; k < r; ++k)
        if (abs(real(V[k]) - real(V[m])) < delta) spine.
            push_back(V[k]);
    sort(spine.begin(), spine.end(), cmpy);
    for (int i = 0; i < spine.size(); ++i)
        for (int j = i + 1; j - i < 8 and j < spine.size
            (); ++j) {
            upd({spine[i], spine[j]});
        }
    return ret;
}
};

```

6.2 3DConvexHull

```

#define SIZE(X) (int(X.size()))
#define PI 3.14159265358979323846264338327950288
struct Pt {
    Pt cross(const Pt &p) const
    { return Pt(y * p.z - z * p.y, z * p.x - x * p.z, x *
        p.y - y * p.x); }
} info[N];
int mark[N][N], n, cnt;
double mix(const Pt &a, const Pt &b, const Pt &c)
{ return a * (b ^ c); }
double area(int a, int b, int c)
{ return norm((info[b] - info[a]) ^ (info[c] - info[a])
    ); }
double volume(int a, int b, int c, int d)
{ return mix(info[b] - info[a], info[c] - info[a], info
    [d] - info[a]); }
struct Face {
    int a, b, c; Face() {}

```

```

Face(int a, int b, int c): a(a), b(b), c(c) {}
int &operator [](int k)
{ if (k == 0) return a; if (k == 1) return b; return
    c; }
};
vector<Face> face;
void insert(int a, int b, int c)
{ face.push_back(Face(a, b, c)); }
void add(int v) {
    vector<Face> tmp; int a, b, c; cnt++;
    for (int i = 0; i < SIZE(face); i++) {
        a = face[i][0]; b = face[i][1]; c = face[i][2];
        if (Sign(volume(v, a, b, c)) < 0)
            mark[a][b] = mark[b][a] = mark[b][c] = mark[c][b] =
                mark[c][a] = mark[a][c] = cnt;
        else tmp.push_back(face[i]);
    } face = tmp;
    for (int i = 0; i < SIZE(tmp); i++) {
        a = face[i][0]; b = face[i][1]; c = face[i][2];
        if (mark[a][b] == cnt) insert(b, a, v);
        if (mark[b][c] == cnt) insert(c, b, v);
        if (mark[c][a] == cnt) insert(a, c, v);
    }
}
int Find() {
    for (int i = 2; i < n; i++) {
        Pt ndir = (info[0] - info[i]) ^ (info[1] - info[i])
            ;
        if (ndir == Pt()) continue; swap(info[i], info[2]);
        for (int j = i + 1; j < n; j++) if (Sign(volume(0,
            1, 2, j)) != 0) {
            swap(info[j], info[3]); insert(0, 1, 2); insert
                (0, 2, 1); return 1;
        }
    } return 0; }
int main() {
    for (; scanf("%d", &n) == 1; ) {
        for (int i = 0; i < n; i++) info[i].Input();
        sort(info, info + n); n = unique(info, info + n) -
            info;
        face.clear(); random_shuffle(info, info + n);
        if (Find()) { memset(mark, 0, sizeof(mark)); cnt =
            0;
            for (int i = 3; i < n; i++) add(i); vector<Pt>
                Ndir;
            for (int i = 0; i < SIZE(face); ++i) {
                Pt p = (info[face[i][0]] - info[face[i][1]]) ^
                    (info[face[i][2]] - info[face[i][1]]);
                p = p / norm(p); Ndir.push_back(p);
            } sort(Ndir.begin(), Ndir.end());
            int ans = unique(Ndir.begin(), Ndir.end()) - Ndir
                .begin();
            printf("%d\n", ans);
        } else printf("1\n");
    }
}
double calcDist(const Pt &p, int a, int b, int c)
{ return fabs(mix(info[a] - p, info[b] - p, info[c] - p
    ) / area(a, b, c)); }
//compute the minimal distance of center of any faces
double findDist() { //compute center of mass
    double totalWeight = 0; Pt center(.0, .0, .0);
    Pt first = info[face[0][0]];
    for (int i = 0; i < SIZE(face); ++i) {
        Pt p = (info[face[i][0]] + info[face[i][1]] + info[face
            [i][2]] + first) * .25;
        double weight = mix(info[face[i][0]] - first, info[
            face[i][1]]
            - first, info[face[i][2]] - first);
        totalWeight += weight; center = center + p * weight
            ;
    } center = center / totalWeight;
    double res = 1e100; //compute distance
    for (int i = 0; i < SIZE(face); ++i)
        res = min(res, calcDist(center, face[i][0], face[i
            ][1], face[i][2]));
    return res; }

```

6.3 Half plane intersection

```

Pt interPnt( Line l1, Line l2, bool &res ) {
    Pt p1, p2, q1, q2;
    tie(p1, p2) = l1; tie(q1, q2) = l2;

```



```

double f1 = (p2 - p1) ^ (q1 - p1);
double f2 = (p2 - p1) ^ (p1 - q2);
double f = (f1 + f2);
if( fabs(f) < eps){ res=0; return {0, 0}; }
res = true;
return q1 * (f2 / f) + q2 * (f1 / f);
}
bool isin( Line l0, Line l1, Line l2 ){
    // Check inter(l1, l2) in l0
    bool res; Pt p = interPnt(l1, l2, res);
    return ( (l0.SE - l0.FI) ^ (p - l0.FI) ) > eps;
}
/* If no solution, check: 1. ret.size() < 3
 * Or more precisely, 2. interPnt(ret[0], ret[1])
 * in all the lines. (use (1.5 - 1.F) ^ (p - 1.F) > 0
 */
/* --- Line.FI --- Line.SE --- */
vector<Line> halfPlaneInter( vector<Line> lines ){
    int sz = lines.size();
    vector<double> ata(sz), ord(sz);
    for( int i=0; i<sz; i++) {
        ord[i] = i;
        Pt d = lines[i].SE - lines[i].FI;
        ata[i] = atan2(d.Y, d.X);
    }
    sort( ord.begin(), ord.end(), [&](int i, int j) {
        if( fabs(ata[i] - ata[j]) < eps )
            return ( (lines[i].SE - lines[i].FI) ^
                    (lines[j].SE - lines[j].FI) ) < 0;
        return ata[i] < ata[j];
    });
    vector<Line> fin;
    for( int i=0; i<sz; i++)
        if (!i or fabs(ata[ord[i]] - ata[ord[i-1]]) > eps)
            fin.PB(lines[ord[i]]);
    deque<Line> dq;
    for( int i=0; i<(int)(fin.size()); i++) {
        while((int)(dq.size()) >= 2 and
            not isin(fin[i], dq[(int)(dq.size())-2],
                    dq[(int)(dq.size())-1]))
            dq.pop_back();
        while((int)(dq.size()) >= 2 and
            not isin(fin[i], dq[0], dq[1]))
            dq.pop_front();
        dq.push_back(fin[i]);
    }
    while( (int)(dq.size()) >= 3 and
        not isin(dq[0], dq[(int)(dq.size())-2],
                dq[(int)(dq.size())-1]))
        dq.pop_back();
    while( (int)(dq.size()) >= 3 and
        not isin(dq[(int)(dq.size())-1], dq[0], dq[1]))
        dq.pop_front();
    vector<Line> res(dq.begin(), dq.end());
    return res;
}

```

6.4 polyUnion

```

#define eps 1e-8
class PY{ public:
    int n;
    Pt pt[5];
    Pt& operator[](const int x){ return pt[x]; }
    void input(){
        int i; n=4;
        for(i=0; i<n; i++) scanf("%lf%lf", &pt[i].x, &pt[i].y);
    }
    double getArea(){
        int i; double s=pt[n-1]^pt[0];
        for(i=0; i<n-1; i++) s+=pt[i]^pt[i+1];
        return s/2;
    }
};
PY py[500];
pair<double, int> c[5000];
inline double segP(Pt &p, Pt &p1, Pt &p2){
    if(SG(p1.x-p2.x)==0) return (p.y-p1.y)/(p2.y-p1.y);
    return (p.x-p1.x)/(p2.x-p1.x);
}

```

```

double polyUnion(int n){
    int i, j, ii, jj, ta, tb, r, d;
    double z, w, s, sum, tc, td;
    for(i=0; i<n; i++) py[i][py[i].n]=py[i][0];
    sum=0;
    for(i=0; i<n; i++){
        for(ii=0; ii<py[i].n; ii++){
            r=0;
            c[r++]=make_pair(0.0, 0);
            c[r++]=make_pair(1.0, 0);
            for(j=0; j<n; j++){
                if(i==j) continue;
                for(jj=0; jj<py[j].n; jj++){
                    ta=SG(tri(py[i][ii], py[i][ii+1], py[j][jj]));
                    tb=SG(tri(py[i][ii], py[i][ii+1], py[j][jj+1]));
                    if(ta==0 && tb==0){
                        if((py[j][jj+1]-py[j][jj])*(py[i][ii+1]-py[i][ii])>0 && j<i){
                            c[r++]=make_pair(segP(py[j][jj], py[i][ii],
                                py[i][ii+1]), 1);
                            c[r++]=make_pair(segP(py[j][jj+1], py[i][ii+1],
                                py[i][ii+1]), -1);
                        }
                    }
                    else if(ta>0 && tb<0){
                        tc=tri(py[j][jj], py[j][jj+1], py[i][ii]);
                        td=tri(py[j][jj], py[j][jj+1], py[i][ii+1]);
                        c[r++]=make_pair(tc/(tc-td), 1);
                    }
                    else if(ta<0 && tb>0){
                        tc=tri(py[j][jj], py[j][jj+1], py[i][ii]);
                        td=tri(py[j][jj], py[j][jj+1], py[i][ii+1]);
                        c[r++]=make_pair(tc/(tc-td), -1);
                    }
                }
            }
            sort(c, c+r);
            z=min(max(c[0].first, 0.0), 1.0);
            d=c[0].second; s=0;
            for(j=1; j<r; j++){
                w=min(max(c[j].first, 0.0), 1.0);
                if(!d) s+=w-z;
                d+=c[j].second; z=w;
            }
            sum+=(py[i][ii]^py[i][ii+1])*s;
        }
    }
    return sum/2;
}
int main(){
    int n, i, j, k;
    double sum, ds;
    scanf("%d", &n); sum=0;
    for(i=0; i<n; i++){
        py[i].input();
        ds=py[i].getArea();
        if(ds<0){
            for(j=0, k=py[i].n-1; j<k; j++, k--) swap(py[i][j],
                py[i][k]);
            ds=-ds;
        }
        sum+=ds;
    }
    printf("%.9f\n", sum/polyUnion(n));
}

```

7 Graph

7.1 2-SAT

```

#include <cstdio>
#include <vector>
#include <stack>
#include <cstring>
using namespace std;

const int N = 2010;
struct two_SAT {
    int n;
    vector<int> G[N], revG[N];
    stack<int> finish;
}

```

```

bool sol[N], visit[N];
int cmp[N];
void init(int _n) {
    n = _n;
    for (int i = 0; i < N; i++) {
        G[i].clear();
        revG[i].clear();
    }
}
void add_edge(int u, int v) {
    // 2 * i -> i is True, 2 * i + 1 -> i is False
    G[u].push_back(v);
    G[v^1].push_back(u^1);
    revG[v].push_back(u);
    revG[u^1].push_back(v^1);
}
void dfs(int v) {
    visit[v] = true;
    for (auto i:G[v]) {
        if (!visit[i]) dfs(i);
    }
    finish.push(v);
}
void revdfs(int v, int id) {
    visit[v] = true;
    for (auto i:revG[v]) {
        if (!visit[i]) revdfs(i, id);
    }
    cmp[v] = id;
}
int scc() {
    memset(visit, 0, sizeof(visit));
    for (int i = 0; i < 2 * n; i++) {
        if (!visit[i]) dfs(i);
    }
    int id = 0;
    memset(visit, 0, sizeof(visit));
    while (!finish.empty()) {
        int v = finish.top(); finish.pop();
        if (visit[v]) continue;
        revdfs(v, ++id);
    }
    return id;
}
bool solve() {
    scc();
    for (int i = 0; i < n; i++) {
        if (cmp[2*i] == cmp[2*i+1]) return 0;
        sol[i] = (cmp[2*i] > cmp[2*i+1]);
    }
    return 1;
}
} sat;

int main() {
    // ( a or not b ) and ( b or c ) and ( not c or not a )
    sat.init(3);
    sat.add_edge( 2*0+1, 2*1+1 );
    sat.add_edge( 2*1+1, 2*2+0 );
    sat.add_edge( 2*2+0, 2*0+1 );
    printf("%d\n", sat.solve());
    return 0;
}

```

7.2 General Matching

```

#define MAXN 505
struct Blossom {
    vector<int> g[MAXN];
    int pa[MAXN] = {0}, match[MAXN] = {0}, st[MAXN] = {0}, S[MAXN] = {0}, v[MAXN] = {0};
    int t, n;
    Blossom(int _n) : n(_n) {}
    void add_edge(int v, int u) { // 1-index
        g[u].push_back(v), g[v].push_back(u);
    }
    inline int lca(int x, int y) {
        ++t;
        while (v[x] != t) {

```

```

            v[x] = t;
            x = st[pa[match[x]]];
            swap(x, y);
            if (x == 0) swap(x, y);
        }
        return x;
    }
    inline void flower(int x, int y, int l, queue<int> &q) {
        while (st[x] != l) {
            pa[x] = y;
            if (S[y = match[x]] == 1) q.push(y), S[y] = 0;
            st[x] = st[y] = l, x = pa[y];
        }
    }
    inline bool bfs(int x) {
        for (int i = 1; i <= n; ++i) st[i] = i;
        memset(S + 1, -1, sizeof(int) * n);
        queue<int> q;
        q.push(x), S[x] = 0;
        while (q.size()) {
            x = q.front(), q.pop();
            for (size_t i = 0; i < g[x].size(); ++i) {
                int y = g[x][i];
                if (S[y] == -1) {
                    pa[y] = x, S[y] = 1;
                    if (not match[y]) {
                        for (int lst; x; y = lst, x = pa[y])
                            lst = match[x], match[x] = y, match[y] = x;
                        return 1;
                    }
                    q.push(match[y]), S[match[y]] = 0;
                } else if (not S[y] and st[y] != st[x]) {
                    int l = lca(y, x);
                    flower(y, x, l, q), flower(x, y, l, q);
                }
            }
        }
        return 0;
    }
    inline int blossom() {
        int ans = 0;
        for (int i = 1; i <= n; ++i)
            if (not match[i] and bfs(i)) ++ans;
        return ans;
    }
};

```

7.3 maximal cliques

```

#include <bits/stdc++.h>
using namespace std;

const int N = 60;
typedef long long LL;

struct Bron_Kerbosch {
    int n, res;
    LL edge[N];
    void init(int _n) {
        n = _n;
        for (int i = 0; i <= n; i++) edge[i] = 0;
    }
    void add_edge(int u, int v) {
        if (u == v) return;
        edge[u] |= 1LL << v;
        edge[v] |= 1LL << u;
    }
    void go(LL R, LL P, LL X) {
        if (P == 0 && X == 0) {
            res = max(res, __builtin_popcountll(R)); // notice LL
            return;
        }
        if (__builtin_popcountll(R) + __builtin_popcountll(P) <= res) return;
        for (int i = 0; i <= n; i++) {
            LL v = 1LL << i;
            if (P & v) {

```

```

        go( R | v, P & edge[i], X & edge[i] );
        P &= ~v;
        X |= v;
    }
}
int solve() {
    res = 0;
    go( 0LL, ( 1LL << (n+1) ) - 1, 0LL );
    return res;
}
/* BronKerbosch1(R, P, X):
   if P and X are both empty:
       report R as a maximal clique
   for each vertex v in P:
       BronKerbosch1(R ∪ {v}, P ∩ N(v), X ∪ N(v))
   P := P \ {v}
   X := X ∪ {v}
*/
} MaxClique;

int main() {
    MaxClique.init(6);
    MaxClique.add_edge(1,2);
    MaxClique.add_edge(1,5);
    MaxClique.add_edge(2,5);
    MaxClique.add_edge(4,5);
    MaxClique.add_edge(3,2);
    MaxClique.add_edge(4,6);
    MaxClique.add_edge(3,4);
    cout << MaxClique.solve() << "\n";
    return 0;
}

```

7.4 Tarjan SCC

```

#include <cstdio>
#include <vector>
#include <stack>
#include <cstring>
using namespace std;

const int N = 10010;
struct Tarjan {
    int n;
    vector<int> G[N], revG[N];
    stack<int> finish;
    bool visit[N];
    int cmp[N];
    void init(int _n) {
        n = _n;
        for (int i = 0; i <= n; i++) {
            G[i].clear();
            revG[i].clear();
        }
    }
    void add_edge(int u, int v) {
        G[u].push_back(v);
        revG[v].push_back(u);
    }
    void dfs(int v) {
        visit[v] = true;
        for (auto i:G[v]) {
            if (!visit[i]) dfs(i);
        }
        finish.push(v);
    }
    void revdfs(int v, int id) {
        visit[v] = true;
        for (auto i:revG[v]) {
            if (!visit[i]) revdfs(i,id);
        }
        cmp[v] = id;
    }
    int solve() {
        memset( visit, 0, sizeof(visit) );
        for (int i = 0; i < n; i++) {
            if (!visit[i]) dfs(i);
        }
        int id = 0;

```

```

        memset( visit, 0, sizeof(visit) );
        while ( !finish.empty() ) {
            int v = finish.top(); finish.pop();
            if ( visit[v] ) continue;
            revdfs(v,++id);
        }
        return id;
    }
} scc;

int main() {
    int V, E;
    scanf("%d %d", &V, &E);
    scc.init(V);
    for (int i = 0; i < E; i++) {
        int u, v;
        scanf("%d %d", &u, &v);
        scc.add_edge(u-1,v-1);
    }
    printf("%d\n", scc.solve() );
    return 0;
}

```

7.5 CentroidDecomposition

```

vector<int> adj[N];
int p[N], vis[N];
int sz[N], M[N]; // subtree size of u and M(u)

inline void maxify(int &x, int y) { x = max(x, y); }
int centroidDecomp(int x) {
    vector<int> q;
    { // bfs
        size_t pt = 0;
        q.push_back(x);
        p[x] = -1;
        while (pt < q.size()) {
            int now = q[pt++];
            sz[now] = 1;
            M[now] = 0;
            for (auto &nxt : adj[now])
                if (!vis[nxt] && nxt != p[now])
                    q.push_back(nxt), p[nxt] = now;
        }
    }

    // calculate subtree size in reverse order
    reverse(q.begin(), q.end());
    for (int &nd : q)
        if (p[nd] != -1) {
            sz[p[nd]] += sz[nd];
            maxify(M[p[nd]], sz[nd]);
        }
    for (int &nd : q)
        maxify(M[nd], (int)q.size() - sz[nd]);

    // find centroid
    int centroid = *min_element(q.begin(), q.end(),
                                [&](int x, int y) {
                                    return M[x] < M[y];
                                });

    vis[centroid] = 1;
    for (auto &nxt : adj[centroid]) if (!vis[nxt])
        centroidDecomp(nxt);
    return centroid;
}

```

7.6 MinMeanCycle

```

/* minimum mean cycle O(VE) */
struct MMC{
#define E 101010
#define V 1021
#define inf 1e9
#define eps 1e-6
    struct Edge { int v,u; double c; };
    int n, m, prv[V][V], prve[V][V], vst[V];

```

```

Edge e[E];
vector<int> edgeID, cycle, rho;
double d[V][V];
void init( int _n )
{ n = _n; m = 0; }
// WARNING: TYPE matters
void addEdge( int vi , int ui , double ci )
{ e[ m ++ ] = { vi , ui , ci }; }
void bellman_ford() {
    for(int i=0; i<n; i++) d[0][i]=0;
    for(int i=0; i<n; i++) {
        fill(d[i+1], d[i+1]+n, inf);
        for(int j=0; j<m; j++) {
            int v = e[j].v, u = e[j].u;
            if(d[i][v]<inf && d[i+1][u]>d[i][v]+e[j].c) {
                d[i+1][u] = d[i][v]+e[j].c;
                prv[i+1][u] = v;
                prve[i+1][u] = j;
            }
        }
    }
}
double solve(){
    // returns inf if no cycle, mmc otherwise
    double mmc=inf;
    int st = -1;
    bellman_ford();
    for(int i=0; i<n; i++) {
        double avg=-inf;
        for(int k=0; k<n; k++) {
            if(d[n][i]<inf-eps) avg=max(avg,(d[n][i]-d[k][i])/(n-k));
            else avg=max(avg,inf);
        }
        if (avg < mmc) tie(mmc, st) = tie(avg, i);
    }
    FZ(vst); edgeID.clear(); cycle.clear(); rho.clear()
    for (int i=n; !vst[st]; st=prv[i--][st]) {
        vst[st]++;
        edgeID.PB(prve[i][st]);
        rho.PB(st);
    }
    while (vst[st] != 2) {
        int v = rho.back(); rho.pop_back();
        cycle.PB(v);
        vst[v]++;
    }
    reverse(ALL(edgeID));
    edgeID.resize(SZ(cycle));
    return mmc;
}
} mmc;

```

7.7 BCC

7.8 DirectedGraphMinCycle

```

// works in O(N M)
#define INF 1000000000000000LL
#define N 5010
#define M 200010
struct edge{
    int to; LL w;
    edge(int a=0, LL b=0): to(a), w(b){}
};
struct node{
    LL d; int u, next;
    node(LL a=0, int b=0, int c=0): d(a), u(b), next(c){}
}b[M];
struct DirectedGraphMinCycle{
    vector<edge> g[N], grev[N];
    LL dp[N][N], p[N], d[N], mu;
    bool inq[N];
    int n, bn, bsz, hd[N];
    void b_insert(LL d, int u){
        int i = d/mu;
        if(i >= bn) return;
        b[++bsz] = node(d, u, hd[i]);
        hd[i] = bsz;
    }

```

```

}
void init( int _n ){
    n = _n;
    for( int i = 1 ; i <= n ; i ++ )
        g[ i ].clear();
}
void addEdge( int ai , int bi , LL ci )
{ g[ai].push_back(edge(bi,ci)); }
LL solve(){
    fill(dp[0], dp[0]+n+1, 0);
    for(int i=1; i<=n; i++){
        fill(dp[i]+1, dp[i]+n+1, INF);
        for(int j=1; j<=n; j++) if(dp[i-1][j] < INF){
            for(int k=0; k<(int)g[j].size(); k++){
                dp[i][g[j][k].to] =min(dp[i][g[j][k].to],
                    dp[i-1][j]+g[j][k].w);
            }
        }
    }
    mu=INF; LL bunbo=1;
    for(int i=1; i<=n; i++) if(dp[n][i] < INF){
        LL a=-INF, b=1;
        for(int j=0; j<=n-1; j++) if(dp[j][i] < INF){
            if(a*(n-j) < b*(dp[n][i]-dp[j][i])){
                a = dp[n][i]-dp[j][i];
                b = n-j;
            }
        }
        if(mu*b > bunbo*a)
            mu = a, bunbo = b;
    }
    if(mu < 0) return -1; // negative cycle
    if(mu == INF) return INF; // no cycle
    if(mu == 0) return 0;
    for(int i=1; i<=n; i++)
        for(int j=0; j<(int)g[i].size(); j++)
            g[i][j].w *= bunbo;
    memset(p, 0, sizeof(p));
    queue<int> q;
    for(int i=1; i<=n; i++){
        q.push(i);
        inq[i] = true;
    }
    while(!q.empty()){
        int i=q.front(); q.pop(); inq[i]=false;
        for(int j=0; j<(int)g[i].size(); j++){
            if(p[g[i][j].to] > p[i]+g[i][j].w-mu){
                p[g[i][j].to] = p[i]+g[i][j].w-mu;
                if(!inq[g[i][j].to]){
                    q.push(g[i][j].to);
                    inq[g[i][j].to] = true;
                }
            }
        }
    }
    for(int i=1; i<=n; i++) grev[i].clear();
    for(int i=1; i<=n; i++){
        for(int j=0; j<(int)g[i].size(); j++){
            g[i][j].w += p[i]-p[g[i][j].to];
            grev[g[i][j].to].push_back(edge(i, g[i][j].w));
        }
    }
    LL mldc = n*mu;
    for(int i=1; i<=n; i++){
        bn=mldc/mu, bsz=0;
        memset(hd, 0, sizeof(hd));
        fill(d+i+1, d+n+1, INF);
        b_insert(d[i]=0, i);
        for(int j=0; j<=bn-1; j++) for(int k=hd[j]; k=
            b[k].next){
            int u = b[k].u;
            LL du = b[k].d;
            if(du > d[u]) continue;
            for(int l=0; l<(int)g[u].size(); l++) if(g[u][l]
                .to > i){
                if(d[g[u][l].to] > du + g[u][l].w){
                    d[g[u][l].to] = du + g[u][l].w;
                    b_insert(d[g[u][l].to], g[u][l].to);
                }
            }
        }
    }
    for(int j=0; j<(int)grev[i].size(); j++) if(grev[
        i][j].to > i)
        mldc=min(mldc,d[grev[i][j].to] + grev[i][j].w);
}

```

```

    }
    return mldc / bunbo;
}
} graph;

```

7.9 GeneralWeightedMatching

```

struct WeightGraph {
    static const int INF = INT_MAX;
    static const int N = 514;
    struct edge {
        int u, v, w;
        edge() {}
        edge(int ui, int vi, int wi) : u(ui), v(vi), w(wi) {}
    };
    int n, n_x;
    edge g[N * 2][N * 2];
    int lab[N * 2];
    int match[N * 2], slack[N * 2], st[N * 2], pa[N * 2];
    int flo_from[N * 2][N + 1], S[N * 2], vis[N * 2];
    vector<int> flo[N * 2];
    queue<int> q;
    int e_delta(const edge& e) { return lab[e.u] + lab[e.v] - g[e.u][e.v].w * 2; }
    void update_slack(int u, int x) {
        if (not slack[x] or e_delta(g[u][x]) < e_delta(g[slack[x]][x]))
            slack[x] = u;
    }
    void set_slack(int x) {
        slack[x] = 0;
        for (int u = 1; u <= n; ++u)
            if (g[u][x].w > 0 and st[u] != x and S[st[u]] == 0) update_slack(u, x);
    }
    void q_push(int x) {
        if (x <= n)
            q.push(x);
        else
            for (size_t i = 0; i < flo[x].size(); ++i) q_push(flo[x][i]);
    }
    void set_st(int x, int b) {
        st[x] = b;
        if (x > n)
            for (size_t i = 0; i < flo[x].size(); ++i) set_st(flo[x][i], b);
    }
    int get_pr(int b, int xr) {
        int pr = find(flo[b].begin(), flo[b].end(), xr) - flo[b].begin();
        if (pr % 2 == 1) {
            reverse(flo[b].begin() + 1, flo[b].end());
            return (int)flo[b].size() - pr;
        } else
            return pr;
    }
    void set_match(int u, int v) {
        match[u] = g[u][v].v;
        if (u <= n) return;
        edge e = g[u][v];
        int xr = flo_from[u][e.u], pr = get_pr(u, xr);
        for (int i = 0; i < pr; ++i) set_match(flo[u][i], flo[u][i ^ 1]);
        set_match(xr, v);
        rotate(flo[u].begin(), flo[u].begin() + pr, flo[u].end());
    }
    void augment(int u, int v) {
        for (;;) {
            int xnv = st[match[u]];
            set_match(u, v);
            if (not xnv) return;
            set_match(xnv, st[pa[xnv]]);
            u = st[pa[xnv]], v = xnv;
        }
    }
    int get_lca(int u, int v) {
        static int t = 0;

```

```

        for (++t; u or v; swap(u, v)) {
            if (u == 0) continue;
            if (vis[u] == t) return u;
            vis[u] = t;
            u = st[match[u]];
            if (u) u = st[pa[u]];
        }
        return 0;
    }
    void add_blossom(int u, int lca, int v) {
        int b = n + 1;
        while (b <= n_x and st[b]) ++b;
        if (b > n_x) ++n_x;
        lab[b] = 0, S[b] = 0;
        match[b] = match[lca];
        flo[b].clear();
        flo[b].push_back(lca);
        for (int x = u, y; x != lca; x = st[pa[y]])
            flo[b].push_back(x), flo[b].push_back(y = st[match[x]]), q_push(y);
        reverse(flo[b].begin() + 1, flo[b].end());
        for (int x = v, y; x != lca; x = st[pa[y]])
            flo[b].push_back(x), flo[b].push_back(y = st[match[x]]), q_push(y);
        set_st(b, b);
        for (int x = 1; x <= n_x; ++x) g[b][x].w = g[x][b].w = 0;
        for (int x = 1; x <= n; ++x) flo_from[b][x] = 0;
        for (size_t i = 0; i < flo[b].size(); ++i) {
            int xs = flo[b][i];
            for (int x = 1; x <= n_x; ++x)
                if (g[b][x].w == 0 or e_delta(g[xs][x]) < e_delta(g[b][x]))
                    g[b][x] = g[xs][x], g[x][b] = g[x][xs];
            for (int x = 1; x <= n; ++x)
                if (flo_from[xs][x]) flo_from[b][x] = xs;
        }
        set_slack(b);
    }
    void expand_blossom(int b) {
        for (size_t i = 0; i < flo[b].size(); ++i) set_st(flo[b][i], flo[b][i]);
        int xr = flo_from[b][g[b][pa[b]].u], pr = get_pr(b, xr);
        for (int i = 0; i < pr; i += 2) {
            int xs = flo[b][i], xns = flo[b][i + 1];
            pa[xs] = g[xns][xs].u;
            S[xs] = 1, S[xns] = 0;
            slack[xs] = 0, set_slack(xns);
            q_push(xns);
        }
        S[xr] = 1, pa[xr] = pa[b];
        for (size_t i = pr + 1; i < flo[b].size(); ++i) {
            int xs = flo[b][i];
            S[xs] = -1, set_slack(xs);
        }
        st[b] = 0;
    }
    bool on_found_edge(const edge& e) {
        int u = st[e.u], v = st[e.v];
        if (S[v] == -1) {
            pa[v] = e.u, S[v] = 1;
            int nu = st[match[v]];
            slack[v] = slack[nu] = 0;
            S[nu] = 0, q_push(nu);
        } else if (S[v] == 0) {
            int lca = get_lca(u, v);
            if (not lca)
                return augment(u, v), augment(v, u), true;
            else
                add_blossom(u, lca, v);
        }
        return false;
    }
    bool matching() {
        memset(S + 1, -1, sizeof(int) * n_x);
        memset(slack + 1, 0, sizeof(int) * n_x);
        q = queue<int>();
        for (int x = 1; x <= n_x; ++x)
            if (st[x] == x and not match[x]) pa[x] = 0, S[x] = 0, q_push(x);
        if (q.empty()) return false;

```



```

for (;;) {
    while (q.size()) {
        int u = q.front();
        q.pop();
        if (S[st[u]] == 1) continue;
        for (int v = 1; v <= n; ++v)
            if (g[u][v].w > 0 and st[u] != st[v]) {
                if (e_delta(g[u][v]) == 0) {
                    if (on_found_edge(g[u][v])) return true;
                } else
                    update_slack(u, st[v]);
            }
    }
    int d = INF;
    for (int b = n + 1; b <= n_x; ++b)
        if (st[b] == b and S[b] == 1) d = min(d, lab[b] / 2);
    for (int x = 1; x <= n_x; ++x)
        if (st[x] == x and slack[x]) {
            if (S[x] == -1)
                d = min(d, e_delta(g[slack[x]][x]));
            else if (S[x] == 0)
                d = min(d, e_delta(g[slack[x]][x]) / 2);
        }
    for (int u = 1; u <= n; ++u) {
        if (S[st[u]] == 0) {
            if (lab[u] <= d) return 0;
            lab[u] -= d;
        } else if (S[st[u]] == 1)
            lab[u] += d;
    }
    for (int b = n + 1; b <= n_x; ++b)
        if (st[b] == b) {
            if (S[st[b]] == 0)
                lab[b] += d * 2;
            else if (S[st[b]] == 1)
                lab[b] -= d * 2;
        }
    q = queue<int>();
    for (int x = 1; x <= n_x; ++x)
        if (st[x] == x and slack[x] and st[slack[x]] !=
            x and
            e_delta(g[slack[x]][x]) == 0)
            if (on_found_edge(g[slack[x]][x])) return
                true;
    for (int b = n + 1; b <= n_x; ++b)
        if (st[b] == b and S[b] == 1 and lab[b] == 0)
            expand_blossom(b);
}
return false;
}
pair<long long, int> solve() {
    memset(match + 1, 0, sizeof(int) * n);
    n_x = n;
    int n_matches = 0;
    long long tot_weight = 0;
    for (int u = 0; u <= n; ++u) st[u] = u, flo[u].
        clear();
    int w_max = 0;
    for (int u = 1; u <= n; ++u)
        for (int v = 1; v <= n; ++v) {
            flo_from[u][v] = (u == v ? u : 0);
            w_max = max(w_max, g[u][v].w);
        }
    for (int u = 1; u <= n; ++u) lab[u] = w_max;
    while (matching()) ++n_matches;
    for (int u = 1; u <= n; ++u)
        if (match[u] and match[u] < u) tot_weight += g[u]
            [match[u]].w;
    return {tot_weight, n_matches};
}
void add_edge(int ui, int vi, int wi) { g[ui][vi].w =
    g[vi][ui].w = wi; }
void init(int _n) { // 1-index, zero indicates
    unsaturated
    n = _n;
    for (int u = 1; u <= n; ++u)
        for (int v = 1; v <= n; ++v) g[u][v] = edge(u, v,
            0);
}
} graph;

```

7.10 Euler Tour

7.11 Diameter

7.12 Topological Sort

7.13 SPFA

7.14 is_deg_sequence

8 String

8.1 AC automaton

```

// SIGMA[0] will not be considered
const string SIGMA = "
    _0123456789ABCDEFGHIJKLMNOPQRSTUVWXYZabcdefghijklmnopqrstuvwxyz";
vector<int> INV_SIGMA;
const int SGSZ = 63;

struct PMA {
    PMA *next[SGSZ]; // next[0] is for fail
    vector<int> ac;
    PMA *last; // state of longest accepted string that
                // is pre of this
    PMA() : last(nullptr) { fill(next, next + SGSZ,
        nullptr); }
};

template<typename T>
PMA *buildPMA(const vector<T> &p) {
    PMA *root = new PMA;
    for (int i = 0; i < p.size(); ++i) { // make trie
        PMA *t = root;
        for (int j = 0; j < p[i].size(); ++j) {
            int c = INV_SIGMA[p[i][j]];
            if (t->next[c] == nullptr) t->next[c] = new PMA;
            t = t->next[c];
        }
        t->ac.push_back(i);
    }
    queue<PMA *> que; // make failure link using bfs
    for (int c = 1; c < SGSZ; ++c) {
        if (root->next[c]) {
            root->next[c]->next[0] = root;
            que.push(root->next[c]);
        } else root->next[c] = root;
    }
    while (!que.empty()) {
        PMA *t = que.front();
        que.pop();
        for (int c = 1; c < SGSZ; ++c) {
            if (t->next[c]) {
                que.push(t->next[c]);
                PMA *r = t->next[0];
                while (!r->next[c]) r = r->next[0];
                t->next[c]->next[0] = r->next[c];
                t->next[c]->last = r->next[c]->ac.size() ? r->
                    next[c] : r->next[c]->last;
            }
        }
    }
    return root;
}

void destructPMA(PMA *root) {
    queue<PMA *> que;
    que.emplace(root);
    while (!que.empty()) {
        PMA *t = que.front();
        que.pop();
        for (int c = 1; c < SGSZ; ++c) {
            if (t->next[c] && t->next[c] != root) que.emplace
                (t->next[c]);
        }
        delete t;
    }
}

```

```

template<typename T>
map<int, int> match(const T &t, PMA *v) {
    map<int, int> res;
    for (int i = 0; i < t.size(); ++i) {
        int c = INV_SIGMA[t[i]];
        while (!v->next[c]) v = v->next[0];
        v = v->next[c];
        for (int j = 0; j < v->ac.size(); ++j) ++res[v->ac[j]];
        for (PMA *q = v->last; q; q = q->last) {
            for (int j = 0; j < q->ac.size(); ++j) ++res[q->ac[j]];
        }
    }
    return res;
}

signed main() {
    INV_SIGMA.assign(256, -1);
    for (int i = 0; i < SIGMA.size(); ++i) {
        INV_SIGMA[SIGMA[i]] = i;
    }
}

```

8.2 Gusfield(Z-algorithm)

```

template<typename T>
vector<int> gusfield(const T &s) {
    vector<int> z(s.size(), s.size()); // z[i] := max k
    for z[0, k) = z[i, i + k)
    for (int i = 1, L = 0, R = 0; i < s.size(); ++i) {
        if (R < i) {
            L = R = i;
            while (R < s.size() && s[R] == s[R - L]) ++R;
            z[i] = R - L;
            --R;
        } else {
            int k = i - L;
            if (z[k] < R - i + 1) {
                z[i] = z[k];
            } else {
                L = i;
                while (R < s.size() && s[R] == s[R - L]) ++R;
                z[i] = R - L;
                --R;
            }
        }
    }
    return z;
}

```

8.3 KMP

```

template<typename T>
vector<int> build_kmp(const T &s) {
    vector<int> f(s.size());
    int fp = f[0] = -1;
    for (int i = 1; i < s.size(); ++i) {
        while (~fp && s[fp + 1] != s[i]) fp = f[fp];
        if (s[fp + 1] == s[i]) ++fp;
        f[i] = fp;
    }
    return f;
}

template<typename S>
vector<int> kmp_match(vector<int> fail, const S &P,
    const S &T) {
    vector<int> res; // start from these points
    const int n = P.size();
    for (int j = 0, i = -1; j < T.size(); ++j) {
        while (~i and T[j] != P[i + 1]) i = fail[i];
        if (P[i + 1] == T[j]) ++i;
        if (i == n - 1) res.push_back(j - n + 1), i = fail[i];
    }
    return res;
}

```

```

}

```

8.4 Manacher

```

template<typename T, int INF>
vector<int> manacher(const T &s) { // p = "INF" + s.
    join("INF") + "INF", returns radius on p
    vector<int> p(s.size() * 2 + 1, INF);
    for (int i = 0; i < s.size(); ++i) {
        p[i << 1 | 1] = s[i];
    }
    vector<int> w(p.size());
    for (int i = 1, j = 0, r = 0; i < p.size(); ++i) {
        int t = min(r >= i ? w[2 * j - i] : 0, r - i + 1);
        for (; i - t >= 0 && i + t < p.size(); ++t) {
            if (p[i - t] != p[i + t]) break;
        }
        w[i] = --t;
        if (i + t > r) r = i + t, j = i;
    }
    return w;
}

```

8.5 Suffix Array

```

// -----O(NlgNlgN)-----
pair<vector<int>, vector<int>> sa_db(const string s) {
    int n = s.size();
    vector<int> sa(n), ra(n), t(n);
    for (int i = 0; i < n; ++i) ra[sa[i] = i] = s[i];
    for (int h = 1; t[n - 1] != n - 1; h *= 2) {
        auto cmp = [&](int i, int j) {
            if (ra[i] != ra[j]) return ra[i] < ra[j];
            return i + h < n && j + h < n ? ra[i + h] < ra[j + h] : i > j;
        };
        sort(sa.begin(), sa.end(), cmp);
        for (int i = 0; i + 1 < n; ++i) t[i + 1] = t[i] + cmp(sa[i], sa[i + 1]);
        for (int i = 0; i < n; ++i) ra[sa[i]] = t[i];
    }
    return {sa, ra};
}

// O(N) -- CF: 1e6->31ms,18MB;1e7->296ms;158MB;3e7->856ms,471MB
bool is_lms(const string &t, int i) {
    return i > 0 && t[i - 1] == 'L' && t[i] == 'S';
}

template<typename T>
vector<int> induced_sort(const T &s, const string &t,
    const vector<int> &lmss, int sigma = 256) {
    vector<int> sa(s.size(), -1);

    vector<int> bin(sigma + 1);
    for (auto it = lmss.rbegin(); it != lmss.rend(); ++it) {
        ++bin[*it + 1];
    }

    int sum = 0;
    for (int i = 0; i < bin.size(); ++i) {
        sum += bin[i];
        bin[i] = sum;
    }

    vector<int> cnt(sigma);
    for (auto it = lmss.rbegin(); it != lmss.rend(); ++it) {
        int ch = s[*it];
        sa[bin[ch] - 1] = *it;
        ++cnt[ch];
    }

    cnt = vector<int>(sigma);
    for (auto it = sa.begin(); it != sa.end(); ++it) {
        if (*it <= 0 || t[*it - 1] == 'S') continue;
        int ch = s[*it - 1];
    }
}

```

```

    sa[bin[ch] + cnt[ch]] = *it - 1;
    ++cnt[ch];
}

cnt = vector<int>(sigma);
for (auto it = sa.rbegin(); it != sa.rend(); ++it) {
    if (*it <= 0 || t[*it - 1] == 'L') continue;
    int ch = s[*it - 1];
    sa[bin[ch + 1] - 1 - cnt[ch]] = *it - 1;
    ++cnt[ch];
}

return sa;
}

template<typename T>
vector<int> sa_is(const T &s, int sigma = 256) {
    string t(s.size(), 0);
    t[s.size() - 1] = 'S';
    for (int i = int(s.size()) - 2; i >= 0; --i) {
        if (s[i] < s[i + 1]) t[i] = 'S';
        else if (s[i] > s[i + 1]) t[i] = 'L';
        else t[i] = t[i + 1];
    }

    vector<int> lmss;
    for (int i = 0; i < s.size(); ++i) {
        if (is_lms(t, i)) {
            lmss.emplace_back(i);
        }
    }

    vector<int> sa = induced_sort(s, t, lmss, sigma);
    vector<int> sa_lms;
    for (int i = 0; i < sa.size(); ++i) {
        if (is_lms(t, sa[i])) {
            sa_lms.emplace_back(sa[i]);
        }
    }

    int lmp_ctr = 0;
    vector<int> lmp(s.size(), -1);
    lmp[sa_lms[0]] = lmp_ctr;
    for (int i = 0; i + 1 < sa_lms.size(); ++i) {
        int diff = 0;
        for (int d = 0; d < sa.size(); ++d) {
            if (s[sa_lms[i] + d] != s[sa_lms[i + 1] + d] ||
                is_lms(t, sa_lms[i] + d) != is_lms(t, sa_lms[i + 1] + d)) {
                diff = 1; // something different in range of lms
                break;
            } else if (d > 0 && is_lms(t, sa_lms[i] + d) &&
                is_lms(t, sa_lms[i + 1] + d)) {
                break; // exactly the same
            }
        }
        if (diff) ++lmp_ctr;
        lmp[sa_lms[i + 1]] = lmp_ctr;
    }

    vector<int> lmp_compact;
    for (int i = 0; i < lmp.size(); ++i) {
        if (~lmp[i]) {
            lmp_compact.emplace_back(lmp[i]);
        }
    }

    if (lmp_ctr + 1 < lmp_compact.size()) {
        sa_lms = sa_is(lmp_compact, lmp_ctr + 1);
    } else {
        for (int i = 0; i < lmp_compact.size(); ++i) {
            sa_lms[lmp_compact[i]] = i;
        }
    }

    vector<int> seed;
    for (int i = 0; i < sa_lms.size(); ++i) {
        seed.emplace_back(lmss[sa_lms[i]]);
    }

    return induced_sort(s, t, seed, sigma);
}

// s must end in char(0)
// O(N) lcp, note that s must end in '\0'
vector<int> build_lcp(string &s, vector<int> &sa,
    vector<int> &ra) {
    int n = s.size();
    vector<int> lcp(n);
    for (int i = 0, h = 0; i < n; ++i) {
        if (ra[i] == 0) continue;
        if (h > 0) --h;
        for (int j = sa[ra[i] - 1]; max(j, i) + h < n; ++h) {
            if (s[j + h] != s[i + h]) break;
        }
        lcp[ra[i] - 1] = h;
    }
    return lcp; // lcp[i] := LCP(s[sa[i]], s[sa[i + 1]])
}

// O(N) build segment tree for lcp
vector<int> build_lcp_rmq(const vector<int> &lcp) {
    vector<int> sgt(lcp.size() << 2);
    function<void(int, int, int)> build = [&](int t, int
        lb, int rb) {
        if (rb - lb == 1) return sgt[t] = lcp[lb], void();
        int mb = lb + rb >> 1;
        build(t << 1, lb, mb);
        build(t << 1 | 1, mb, rb);
        sgt[t] = min(sgt[t << 1], sgt[t << 1 | 1]);
    };
    build(1, 0, lcp.size());
    return sgt;
}

// O(|P| + lg |T|) pattern searching, returns last
// index in sa
int match(const string &p, const string &s, const
    vector<int> &sa, const vector<int> &rmq) { // rmq
    // is segtree on lcp
    int t = 1, lb = 0, rb = s.size(); // answer in [lb,
        rb)
    int lcplp = 0; // lcp(char(0), p) = 0
    while (rb - lb > 1) {
        int mb = lb + rb >> 1;
        int lcplm = rmq[t << 1];
        if (lcplp < lcplm) t = t << 1 | 1, lb = mb;
        else if (lcplp > lcplm) t = t << 1, rb = mb;
        else {
            int lcpmp = lcplp;
            while (lcpmp < p.size() && p[lcpmp] == s[sa[mb] +
                lcpmp]) ++lcpmp;
            if (lcpmp == p.size() || p[lcpmp] > s[sa[mb] +
                lcpmp]) t = t << 1 | 1, lb = mb, lcplp =
                lcpmp;
            else t = t << 1, rb = mb;
        }
    }
    if (lcplp < p.size()) return -1;
    return sa[lb];
}

int LCA(int i, int j, const vector<int> &ra, const
    vector<int> &lcp_seg) {
    // lca of ith and jth suffix
    if (ra[i] > ra[j]) swap(i, j);
    function<int(int, int, int, int, int)> query = [&](
        int L, int R, int l, int r, int v) {
        if (L <= l and r <= R) return lcp_seg[v];
        int m = l + r >> 1, ans = 1e9;
        if (L < m) ans = min(ans, query(L, R, l, m, v << 1));
        if (m < R) ans = min(ans, query(L, R, m, r, v <<
            1 | 1));
        return ans;
    };
    return query(ra[i], ra[j], 0, ra.size(), 1);
}

vector<vector<int>> build_lcp_sparse_table(const vector
    <int> &lcp) {
    int n = lcp.size(), lg = 31 - __builtin_clz(n);
    vector<vector<int>> st(lg + 1, vector<int>(n));
    for (int i = 0; i < n; ++i) st[0][i] = lcp[i];
}

```

```

for (int j = 1; (1<<j) <= n; ++j)
    for (int i = 0; i + (1<<j) <= n; ++i)
        st[j][i] = min(st[j - 1][i], st[j - 1][i + (1<<(j - 1))]);
return st;
}
int sparse_rmq(int i, int j, const vector<int> &ra,
    const vector<vector<int>> &st) {
    int n = st[0].size();
    if (ra[i] > ra[j]) swap(i, j);
    int k = 31 - __builtin_clz(ra[j] - ra[i]);
    return min(st[k][ra[i]], st[k][ra[j] - (1<<k)]);
} // sparse_rmq(sa[i], sa[j], ra, st) is the lcp of sa(i), sa(j)

```

8.6 Suffix Automaton

8.7 Trie

8.8 minimum_rotation

9 Formulas

9.1 Pick's theorem

Pick's theorem provides a simple formula for calculating the area A of this polygon in terms of the number i of lattice points in the interior located in the polygon and the number b of lattice points on the boundary placed on the polygon's perimeter:

$$A = i + \frac{b}{2} - 1$$

9.2 Graph Properties

1. Euler's Formula $V - E + F = 2$
2. For a planar graph, $F = E - V + n + 1$, n is the numbers of components
3. For a planar graph, $E \leq 3V - 6$ For a connected graph G , let $I(G)$ be the size of maximum independent set, $M(G)$ be the size of maximum matching, $Cv(G)$ be the size of minimum vertex cover, $Ce(G)$ be the size of minimum edge cover.
4. For any connected graph:

- (a) $I(G) + Cv(G) = |V|$
- (b) $M(G) + Ce(G) = |V|$

5. For any bipartite:

- (a) $I(G) = Cv(G)$
- (b) $M(G) = Ce(G)$

```

double l=0, r=m, stop=1.0/n/n;
while(r-l>=stop){
    double mid;
    if((n*m-sol.maxFlow(s,t))/2>eps)l=mid;
    else r=mid;
}
build(l);
sol.maxFlow(s,t);
vector<int> ans;
for(int i=1;i<=n;++i)
    if(sol.vis[i])ans.push_back(i);

```

9.3 Number Theory

1. $g(m) = \sum_{d|m} f(d) \Leftrightarrow f(m) = \sum_{d|m} \mu(d) \times g(m/d)$
2. $\phi(x)$, $\mu(x)$ are Möbius inverse
3. $\sum_{i=1}^n \sum_{j=1}^m [\gcd(i, j) = 1] = \sum \mu(d) \lfloor \frac{n}{d} \rfloor \lfloor \frac{m}{d} \rfloor$
4. $\sum_{i=1}^n \sum_{j=1}^m lcm(i, j) = n \sum_{d|n} d \times \phi(d)$

9.4 Combinatorics

1. Harmonic series $H_n = \ln(n) + \gamma + 1/(2n) - 1/(12n^2) + 1/(120n^4)$
2. $\gamma = 0.57721566490153286060651209008240243104215$
3. Gray Code: $= n \oplus (n >> 1)$
4. Catalan Number: $\frac{C_n^n}{n(k-1)+1}$, $C_m^n = \frac{n!}{m!(n-m)!}$
5. $\gamma(n+1) = n!$
6. $H(n, m) \cong x_1 + x_2 + \dots + x_n = k$, $num = C_k^{n+k-1}$
7. $n! \approx \sqrt{2\pi n} \left(\frac{n}{e}\right)^n$
8. Stirling number of 2^{nd} kind: n 人分 k 組方法數目

- (a) $S(0, 0) = S(n, n) = 1$
- (b) $S(n, 0) = 0$
- (c) $S(n, k) = kS(n-1, k) + S(n-1, k-1)$

9. Bell number, n 人分任意多組方法數目

- (a) $B_0 = 1$
- (b) $B_n = \sum_{i=0}^n S(n, i)$
- (c) $B_{n+1} = \sum_{k=0}^n C_n^k B_k$
- (d) $B_{p+n} \equiv B_n + B_{n+1} \pmod{p}$, p is prime
- (e) $B_{p^m+n} \equiv mB_n + B_{n+1} \pmod{p}$, p is prime
- (f) From $B_0 : 1, 1, 2, 5, 15, 52, 203, 877, 4140, 21147, 115975$

10. Derangement, 錯排, 國人在自己位置上

- (a) $D_n = n!(1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} \dots + (-1)^n \frac{1}{n!})$
- (b) $D_n = (n-1)(D_{n-1} + D_{n-2})$, $D_0 = 1, D_1 = 0$
- (c) From $D_0 : 1, 0, 1, 2, 9, 44, 265, 1854, 14833, 133496$

11. Binomial Equality

- (a) $\sum_k \binom{r}{m+k} \binom{s}{n-k} = \binom{r+s}{m+n}$
- (b) $\sum_k \binom{l}{m+k} \binom{s}{n+k} = \binom{l+s}{l-m+n}$
- (c) $\sum_k \binom{l}{m+k} \binom{s+k}{n} (-1)^k = (-1)^{l+m} \binom{s-m}{n-l}$
- (d) $\sum_{k \leq l} \binom{l-k}{m} \binom{s}{n-k} (-1)^k = (-1)^{l+m} \binom{s-m-1}{l-n-m}$
- (e) $\sum_{0 \leq k \leq l} \binom{l-k}{m} \binom{q+k}{n} = \binom{l+q+1}{m+n+1}$
- (f) $\binom{r}{k} = (-1)^k \binom{k-r-1}{k}$
- (g) $\binom{r}{m} \binom{m}{k} = \binom{r}{k} \binom{r-k}{m-k}$
- (h) $\sum_{k \leq n} \binom{r+k}{k} = \binom{r+n+1}{n}$
- (i) $\sum_{0 \leq k \leq n} \binom{k}{m} = \binom{n+1}{m+1}$
- (j) $\sum_{k \leq m} \binom{m+r}{k} x^k y^{m-k} = \sum_{k \leq m} \binom{-r}{k} (-x)^k (x+y)^{m-k}$

9.5 國次, 國次和

1. $a^b \% P = a^{b \% \varphi(P) + \varphi(P)}$, $b \geq \varphi(P)$
2. $1^3 + 2^3 + 3^3 + \dots + n^3 = \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4}$
3. $1^4 + 2^4 + 3^4 + \dots + n^4 = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} - \frac{n}{30}$
4. $1^5 + 2^5 + 3^5 + \dots + n^5 = \frac{n^6}{6} + \frac{n^5}{2} + \frac{5n^4}{12} - \frac{n^2}{12}$
5. $0^k + 1^k + 2^k + \dots + n^k = P(k)$, $P(k) = \frac{(n+1)^{k+1} - \sum_{i=0}^{k-1} C_i^{k+1} P(i)}{k+1}$, $P(0) = n+1$
6. $\sum_{k=0}^{m-1} k^n = \frac{1}{n+1} \sum_{k=0}^n C_k^{n+1} B_k m^{n+1-k}$
7. $\sum_{j=0}^m C_j^{m+1} B_j = 0$, $B_0 = 1$
8. 除了 $B_1 = -1/2$, 剩下的奇數項都是 0
9. $B_2 = 1/6$, $B_4 = -1/30$, $B_6 = 1/42$, $B_8 = -1/30$, $B_{10} = 5/66$, $B_{12} = -691/2730$, $B_{14} = 7/6$, $B_{16} = -3617/510$, $B_{18} = 43867/798$, $B_{20} = -174611/330$,

9.6 Burnside's lemma

1. $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$
2. $X^g = t^{c(g)}$
3. G 表示有幾種轉法, X^g 表示在那種轉法下, 有幾種是會保持對稱的, t 是國色數, $c(g)$ 是循環節不動的面數。
4. 正立方體塗三國色, 轉 0 有 3^6 個元素不變, 轉 90 有 6 種, 每種有 3^3 不變, 180 有 3×3^4 , 120(角) 有 8×3^2 , 180(邊) 有 6×3^3 , 全部 $\frac{1}{24} (3^6 + 6 \times 3^3 + 3 \times 3^4 + 8 \times 3^2 + 6 \times 3^3) = 57$

9.7 Count on a tree

1. Rooted tree: $s_{n+1} = \frac{1}{n} \sum_{i=1}^n (i \times a_i \times \sum_{j=1}^{\lfloor n/i \rfloor} a_{n+1-i \times j})$
2. Unrooted tree:

- (a) Odd: $a_n - \sum_{i=1}^{n/2} a_i a_{n-i}$
- (b) Even: $Odd + \frac{1}{2} a_{n/2} (a_{n/2} + 1)$

3. Spanning Tree

- (a) 完全圖 $n^n - 2$
- (b) 一般圖 (Kirchhoff's theorem) $M[i][i] = \text{degree}(V_i)$, $M[i][j] = -1$, if have $E(i, j)$, 0 if no edge. delete any one row and col in A , $ans = \det(A)$