P What's C The Story?

# Principles of Complex Systems, Vols. 1 & 2, CSYS/MATH 300 and 303 University of Vermont, Fall 2021

Assignment 04 • code name: Beebo the God of War ✓

Due: Friday, September 24, by 11:59 pm, 2021.

Relevant clips, episodes, and slides are listed on the assignment's page:

https://pdodds.w3.uvm.edu//teaching/courses/2021-2022principles-of-complex-systems//assignments/04/

Some useful reminders:

**Deliverator:** Prof. Peter Sheridan Dodds (contact through Teams) **Assistant Deliverator:** Michael Arnold (contact through Teams)

Office: The Ether
Office hours: TBD
Course website:

https://pdodds.w3.uvm.edu//teaching/courses/2021-2022principles-of-complex-systems

All parts are worth 3 points unless marked otherwise. Please show all your workingses clearly and list the names of others with whom you collaborated.

For coding, we recommend you improve your skills with Python, R, and/or Julia. The Deliverator uses Matlab.

Graduate students are requested to use  $\prescript{ETEX}$  (or related TEX variant). If you are new to  $\prescript{ETEX}$ , please endeavor to submit at least n questions per assignment in  $\prescript{ETEX}$ , where n is the assignment number.

Assignment submission: Via Blackboard.

For Q1–5, you'll further explore the Google data set you examined earlier.

For Q6–8, you'll explore random walks, touching the Central Limit Theorem and the first return problem. There and back again.

- 1. Plot the complementary cumulative distribution function (CCDF).
- 2. Using standard linear regression, measure the exponent  $\gamma-1$  where  $\gamma$  is the exponent of the underlying distribution function. Identify and use a range of frequencies for which scaling appears consistent. Report the 95% confidence interval for your estimate.

You will find two scaling regimes—please examine them both.

3. Using the alternate data set providing the raw word frequencies, plot word frequency as a function of rank in the manner of Zipf.

**Hint:** you will not be able to plot all points (there are close to 14 million) so think about how to plot a subsample that still shows the full form.

4. Using standard linear regression, measure  $\alpha$ , Zipf's exponent. Report the 95% confidence interval for your estimate.

Again, you will find two regimes.

- 5. For each scaling regime, write down how  $\gamma$  and  $\alpha$  are related (per lectures) and check how this expression works for your estimates here.
- 6. (3 + 3) Baby name frequencies in the US:
  - (a) Plot the Complementary Cumulative Frequency Distributions and Zipf's law for the following:
    - i. Baby girl names in 1952.
    - ii. Baby boy names in 1952.
    - iii. Baby girl names in 2002.
    - iv. Baby boy names in 2002.
  - (b) As you did for the Google data set, fit regression lines and report values of  $\gamma$  and the Zipf exponent  $\alpha$ .

We will revisit these distributions in following assignments.

#### Download:

Data for 1880 through 2018:

http://pdodds.w3.uvm.edu/permanent-share/pocs-babynames.zip 🖸 (8.0M)

#### Files:

For each year, Zipf distribution of counts are stored in: names-girlsYYYY.txt and names-boyYYYY.txt.

For normalization to estimate rates, total number of births per year: births\_per\_year.txt. For this question, you do not need to determine rates, and this file is included for completeness.

For privacy, names with less than 5 counts are excluded.

#### Notes:

You should be able to re-use scripts from previous assignments.

Data is based on names registered through Social Security within the US.

### Source:

## Baby name dataset available here:

 $\label{lem:https://catalog.data.gov/dataset?tags=baby-names} \ensuremath{\ensuremath{\sc C}}. Separate dataset for total births available here:$